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# Lecture Notes

## I. Operations Research and Analytics

*(M.S. in Analytics Program)*



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\* Those advanced topics are only for the *doctoral* students.

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