

My research sits at the intersection of computer science, mathematics and physics. I am interested in the building of a bridge between these areas using interactive theorem proving. I have PhD in theoretical physics from the University of Cambridge, have completed a postdoc at Cornell University in which I focused on the application of theorem proving software in Physics. For the academic year 2024-2025 I am undertaking a postdoc in computer science at the University of Reykjavik.

The past

Part of my past research has been the digitalisation of results (meaning theorems, definitions and calculations) from high energy physics into a Lean 4 library called 'HepLean'. Lean 4 is an interactive theorem prover, and will automatically check if proves of theorems etc are correct. Here are the main motivations behind this project:

1. A linear-storage of information: Currently information in high energy physics is stored non-linearly, with material related to the same subject spread across papers indexed only by an arXiv number at best. In HepLean results related to the same area of high energy physics are stored together, making look-up easier.
2. Automated methods to prove new results: In Lean one can write 'tactics' attempt to automatically complete proves to theorems. There has also been work on the use of AI to prove theorems in Lean (which given the nature of Lean are automatically certified as correct). Most notable in this direction is Google Deepmind's use of Lean for the math olympiad.
3. Automatic review of results for mathematical correctness: HepLean provides a way for authors and reviewers to be confident of the mathematical correctness of results. This is because, as mentioned above, Lean automatically checks proves for correctness.
4. New pedagogy methods: HepLean provides a new way to teach both functional programming and physics, whilst also allowing students to engage in active research.

This is the first anything like this has been attempted in high energy physics. However, there is a similar project for mathematics called Mathlib, which forms the mathematical foundation underlying HepLean.

The future

My plan for future research is to continue the development of HepLean, with a focus on the theoretical and computer science foundations, to make it easier for the average physical scientist to adapt to using Lean. In practice this will mean applying techniques from functional programming, AI, category theory etc. to write foundational definitions in the most effective and efficient way.

To achieve this overarching goal, I plan to undertake the following specific research steps:

1. In Lean 4 there is notion of blueprint for a theory. This is an English-written document containing all of the steps that must be taken to turn the prove of an English-written prove into a Lean written prove. This can be thought of as pseudo-code for Lean. To help build the above bridge I would produce such a pseudo-code for a theory in physics.
2. Most work on AI in mathematics has looked at e.g. math Olympiad problems in Lean (e.g. Google Deepmind's work). I would like to see the use of AI to solve problems from the physical science in Lean. To do this I plan to create a data set of Lean 4 written theorems from physics that can be used for AI testing and training.

3. Overlapping a bit with AI, high energy physics use heavily tensors. As part of Lean 4 I would like to develop tactics that help formally verify results related to tensors.

Plan for undergraduate student involvement

Part of the paper ..., discusses how HepLean can be used as a pedagogical tool, and give students the ability to get involved in research. My plan is to develop three list of undergraduate-level projects around HepLean.

The first list will be concerned with functional programming type projects. As an example: the handling of lists in Lean to efficiently undertake computations needed for index notation (a notation used by physicists to deal with tensors). Other examples will involve meta-programming in Lean to make the user-experience easier.

The second list of projects will be concerned with the use of AI for physics and mathematics. Simple example involve auto-formalisation of theorems in physics (turning a human written result into a result written in Lean), as will as the inverse problem, 'auto-informalisation'. These have being heavily explored in mathematics, but not in the physical sciences.

The third list will be at the boundary of physics, computer-science and mathematics. These projects will involve a proving theorems from physics using Lean. There are many such problems that involve very little prerequisites in physics, once the theorem has being written down. Part of my plan above, with the blueprint, will be a first step in this direction. An example of such a project will be to formalisation of properties of the two-Higgs doublet model potential. This is a potential, and physicists are interested in its properties, such as its minima, whether it is bounded or not etc.

Each of these lists of projects will involve 'home-work style projects' which will take no more than a couple of hours to complete, and more detailed thesis level projects. The benefit of having a large project like HepLean is that coming up with such a diversity of projects is relatively easy.

Other research

I have a strong background in the application of category theory outside the ivory towers of the pure mathematicians. Historically, my main use of category theory is as a language to recast problems from the physical sciences and to use this language to derive new previously unknown results. As a specific example, in high energy physics there is a relatively new notion called a "generalised symmetry", in ..., we used special types of categories called higher topoi to define and derive new results about these symmetries. Higher topos theory itself is related to homotopy type theory, which is actually the path that lead me to interactive theorem provers.

Category theory is used heavily in functional programming, for example, the definition a monad is categorical-definition. It turns out that a moad a special case of a more general object in the theory of Higher algebra. This is an area I have expertise, since it overlaps with my use of category theory in physics, as demonstrated in *e.g.* .

In the future I also plan to investigate the role (higher) category theory can play in functional programming and more specifically interactive theorem provers for the physical science. I'm currently making some investigations into area, using the theory of modular operads to develop an efficient method for index notation of tensors.