STAT 650 - Project 2 Data Requirements for Regression Analysis

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Introduction

This guideline outlines the data requirements necessary to perform a comprehensive regression analysis, ensuring the validity and reliability of the results.

1. Data Quality

1.1 Completeness

• No Missing Values: The dataset should have minimal or no missing values. If there are missing values, they should be handled appropriately through imputation or removal.

1.2 Accuracy

- Correct Data Entries: Ensure that the data entries are accurate and free from errors or inconsistencies.
- Validation: Validate the data against reliable sources to ensure its accuracy.

1.3 Consistency

• Uniform Data Format: The data should be in a consistent format, especially categorical variables which should be encoded uniformly.

2. Data Types and Variable Selection

2.1 Types of Variables

• Numerical Variables: These include continuous variables (e.g., age, salary) and discrete variables (e.g., number of children).

• Categorical Variables: These include ordinal variables (e.g., education level) and nominal variables (e.g., gender, marital status).

2.2 Dependent and Independent Variables

- Dependent Variable (Target): The variable that you are trying to predict or explain (e.g., house price, employee salary).
- Independent Variables (Predictors): The variables that are used to predict the dependent variable (e.g., square footage, number of bedrooms).

3. Data Pre-Processing

3.1 Handling Missing Values

- Imputation: Use appropriate imputation methods to fill in missing values (e.g., mean, median, mode for numerical variables; most frequent category for categorical variables).
- **Removal**: If imputation is not feasible, consider removing rows or columns with a high percentage of missing values.

3.2 Encoding Categorical Variables

- Label Encoding: Convert categorical variables into numerical values using label encoding.
- One-Hot Encoding: Use one-hot encoding for nominal variables to avoid ordinal relationships.

3.3 Scaling and Normalization

• Feature Scaling: Apply feature scaling techniques such as standardization (z-score normalization) or min-max scaling to normalize the data.

4. Exploratory Data Analysis (EDA)

4.1 Descriptive Statistics

- Summary Statistics: Calculate mean, median, mode, standard deviation, and other summary statistics for numerical variables.
- **Frequency Distribution**: Analyze the frequency distribution of categorical variables.

4.2 Data Visualization

- Histograms: Plot histograms for numerical variables to understand their distributions.
- Box Plots: Use box plots to detect outliers and understand the spread of numerical data.
- Scatter Plots: Create scatter plots to visualize relationships between pairs of numerical variables.
- Correlation Matrix: Generate a correlation matrix to identify correlations between numerical variables.

5. Checking Assumptions of Regression Models

5.1 Linearity

• Linear Relationship: Ensure that there is a linear relationship between the dependent and independent variables for linear regression models.

5.2 Independence

• **Independent Observations**: The observations should be independent of each other.

5.3 Homoscedasticity

• Constant Variance of Errors: The residuals (errors) should have constant variance across all levels of the independent variables.

5.4 Normality

• Normal Distribution of Errors: The residuals should be approximately normally distributed.

5.5 Multicollinearity

• Low Multicollinearity: The independent variables should not be highly correlated with each other.

6. Advanced Data Requirements for Specific Regression Models

6.1 Polynomial Regression

• Non-Linearity: Ensure that the relationship between the dependent and independent variables is non-linear.

6.2 Logistic Regression

• Binary Outcome: The dependent variable should be binary (0 or 1).

6.3 Regularization Techniques (LASSO, Ridge, Elastic Net)

• Multicollinearity: Regularization techniques are beneficial when multicollinearity is present among the independent variables.

6.4 Quantile Regression

• Quantiles: The dataset should allow for the prediction of conditional quantiles.

6.5 Poisson and Negative Binomial Regression

- Count Data: The dependent variable should be count data (non-negative integers).
- **Overdispersion**: For Negative Binomial Regression, the count data should exhibit overdispersion.

6.6 Cox Regression

• Survival Data: The data should be suitable for survival analysis, with time-to-event and event occurrence information.

6.7 Partial Least Squares Regression and Principal Component Regression

• **High-Dimensional Data**: These techniques are useful for high-dimensional datasets with more predictors than observations.

7. Selected Model Evaluation and Validation

7.1 Train-Test Split

• Data Splitting: Split the dataset into training and testing sets to evaluate model performance.

7.2 Cross-Validation

• **K-Fold Cross-Validation**: Use k-fold cross-validation to assess the model's performance more robustly.

7.3 Performance Metrics

- Regression Metrics: Use metrics such as \mathbb{R}^2 , RMSE (Root Mean Squared Error), MAE (Mean Absolute Error) for regression models.
- Classification Metrics: Use metrics such as accuracy, precision, recall, F1-score, and ROC-AUC for logistic regression.