## REDB GPP model report

## 2023-02-01

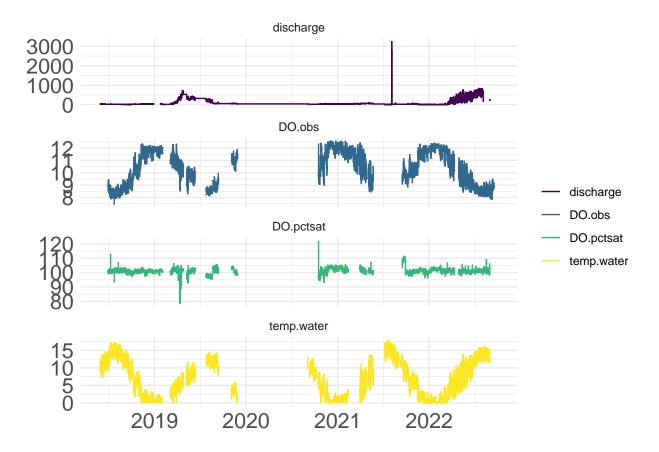


Figure 1: Full metabolism data streams.

The process for building a model suite and selecting a model is iterative. More details for data cleaning will be added here later.

We undergo a process to slim these models down based on a number of criteria. First, we throw out values that have very high estimates of GPP (> 1.5x maximum annual values observed in Berhnardt et al. 2022 Figure 1,  $\sim 5000$  g C m<sup>-2</sup> y<sup>-1</sup>). Next, any models that have especially poor fits are excluded. In this case I automatically exclude any models that are in the upper 30% percentile of RMSE based on the model set, unless this is fewer than 5 models. This slimmed model set is the group I choose from after one final visual assessment.

I do a visual assessment of the slimmed model set to see how they compare and identify any days where the fit is especially poor across dates. To do this, I first chose the 'best' model of the set:

The 'best' model is: mm1

I then compute the model that is most different than the 'best' model and plot the metabolism estimates for each to visually assess.

Table 1: Full model output for all MLE models. 'modelID' represents the model identifier and also information regarding the assumed equations for GPPER. Unmodified models (e.g., 'mm1') represent the default 'mm\_specs' of linear GPPlight relationship. Saturating models (e.g., 'mm1sat') assume a saturating GPPlight relationship. Lastly, Q10 models (e.g., 'mm1satq10') assume a saturating function of GPPlight and an exponential function of GPPlemp. 'modelType' represents how daily K600 values are calculated, whether they are modeled simultaneously with GPP and ER (e.g., 'raw'), modeled as a function of daily discharge with varying relationships (e.g., 'loess', 'lm', 'mean'), modeled from observed night observation (e.g., 'night'), or from empirical gas release estimates (e.g., 'empiricalgam'). The empirical models are further identified by the model used to relate discharge to k, whether GAM or LM. 'RSME' represents the estimated relative root mean square error between observed and modeled dissolved oxygen concentrations standardized to the mean. 'negativeGPP' and 'positiveER' represent the number of days when daily estimates of GPP or ER are negative and positive, respectively. 'meanGPP' is the estimated mean GPP. This value can be scaled to different timeframes or units (i.e., carbon or oxygen) and must be check based on attributes of 'meanGPP'. 'maxK' is the maximum estimated daily k600 value.

modelID	modelType	RMSE	negativeGPP	positiveER	$\max K$	ER.Kcorr	meanGPP
mm1	raw	3.280000e+00	513	606	21348.086	0.759	12.461
mm1_sat	raw	4.110000e+00	174	271	46666.514	0.588	246.190
mm1_satq10	raw	4.160000e+00	140	247	5839.658	0.749	-43.173
mm2	loess	3.270000e+00	592	597	7.055	0.969	-56.398
mm2_sat	loess	4.320000e+00	258	274	-Inf	NA	-70.557
mm2_satq10	loess	4.230000e+00	143	232	4791.713	0.819	-134.409
mm3	lm	3.270000e+00	560	598	58.867	0.053	-61.087
mm3_sat	lm	4.520000e+00	237	238	58.867	0.066	-76.284
mm3_satq10	lm	4.290000e+00	143	227	4791.713	0.819	-149.383
mm4	mean	3.270000e+00	525	594	37.440	NA	-68.968
mm4_sat	mean	4.510000e+00	286	285	1.000	NA	-274.777
mm4_satq10	mean	4.280000e+00	144	230	4791.713	0.819	-146.565
mm5	night	2.493801e+41	555	553	737.714	0.999	9.143
mm5_sat	night	5.795090e + 37	235	228	737.734	1.000	-95.968
mm5_satq10	night	1.326561e+49	228	209	539.134	NA	-257.604
mm6	empirical-gam	1.912000e+01	106	554	144423.279	0.223	105896.680
mm6_sat	empirical-gam	1.622000e+01	67	556	144423.279	0.252	26781.196
mm6_satq10	empirical-gam	1.447000e+01	66	515	144423.279	0.260	29220.672

 $<sup>^{\</sup>rm a}$  GPPmean = g C m-2 y-1

The most distant from best is: mm5

These plots are used to assess any dates that are especially bad (e.g., negative GPP, positive ER, very high GPP, etc.) across all models. This dates identified below for the 'top' model and are excluded from the analysis.

The most distant of the best models. Days between this model and above that are both bad are likely very difficult days to fit. Depending on how many of them there are we need to remove them or take a look at the QC flags or the timeseries data to decide if they should be thrown out.

The number of dates and proportion of bad dates within the best model are:

From here we assess any data removal and rerun until reasonably clean model outputs are achieved and a final model is chosen based on minimizing 'negativeGPP' and 'postiveER' and assessing the reasonableness of 'maxK'.

Lastly, we then take the top model suite and build an average model based on model fit, RMSE. To do so, we first remove models that have very high correlations between ER and K (i.e.,  $r \ge 0.80$ ) as these models are largely driven by variability in the estimates in K. Then we create a model weight based on relative model fit, dRMSE, the difference in relative root mean squared error from the best fitting model based on RMSE for a set of models, m, is:

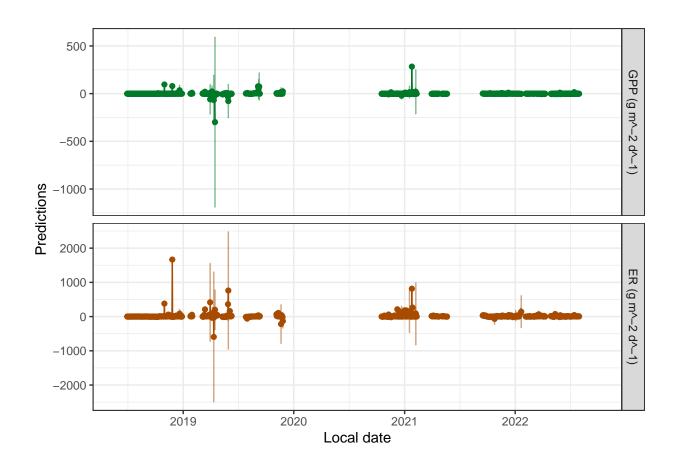


Figure 2: 'Best' model fit.

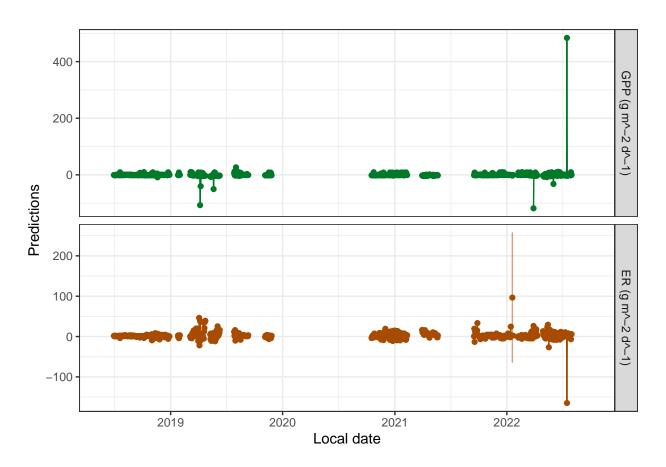


Figure 3: Most distant model.

Table 2: Slimmed model output for all MLE models. 'modelID' represents the model identifier and also information regarding the assumed equations for GPPER. Unmodified models (e.g., 'mm1') represent the default 'mm\_specs' of linear GPPlight relationship. Saturating models (e.g., 'mm1sat') assume a saturating GPPlight relationship. Lastly, Q10 models (e.g., 'mm1satq10') assume a saturating function of GPPlight and an exponential function of GPPTemp. 'modelType' represents how daily K600 values are calculated, whether they are modeled simultaneously with GPP and ER (e.g., 'raw'), modeled as a function of daily discharge with varying relationships (e.g., 'loess', 'lm', 'mean'), modeled from observed night observation (e.g., 'night'), or from empirical gas release estimates (e.g., 'empirical-gam'). The empirical models are further identified by the model used to relate discharge to k, whether GAM or LM. 'RSME' represents the estimated relative root mean square error between observed and modeled dissolved oxygen concentrations standardized to the mean. 'negativeGPP' and 'positiveER' represent the number of days when daily estimates of GPP or ER are negative and positive, respectively. 'meanGPP' is the estimated mean GPP. This value can be scaled to different timeframes or units (i.e., carbon or oxygen) and must be check based on attributes of 'meanGPP'. 'maxK' is the maximum estimated daily k600 value.

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mm1_sat	raw	4.110000e+00	174	271	46666.514	0.588	246.190
$\overline{\mathrm{mm5}}$	night	2.493801e+41	555	553	737.714	0.999	9.143

 $<sup>^{</sup>a}$  GPPmean = g C m-2 y-1

lowGPP	lowGPPperc	highGPP	highGPPperc	NAs
970	67.643	14	0.976	798

$$w_i = exp(\frac{1}{2}dRMSE_i) / \sum_{j=1}^{m} exp(\frac{1}{2}dRMSE_j)$$

From this, we create a weighted average model for GPP estimates, plotted below.

modelID	modelType	RMSE	negativeGPP	positiveER	maxK	ER.Kcorr	meanGPP	dRMSE	RMSEwt
mm1	raw	3.28	513	606	21348.09	0.759	12.461	0.00	0.602
mm1_sat	raw	4.11	174	271	46666.51	0.588	246.190	-0.83	0.398

