

# HW3-695

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1.

(1) MAP Learning: Maximum a Posteriori.  $H_{MAP} = \arg \max P(h|D)$ ,  $h$  belongs to  $H$

I.e. to find the most probable hypothesis  $h$  for a given data set  $D$ .

(2) Support Vector Machine: to find an optimal decision surface (I.e. a hyperplane) by maximizing the margin to classify instances.

(3) Bias-Variation Trade-offs: choose a proper hypothesis space to get the smallest error by finding a tradeoff between variance and bias.

2.

From the first test, we know

$$P(\text{cancer}) = 0.008 \quad p(\sim\text{cancer}) = 0.992 \quad (\sim \text{ means not })$$

$$P(+|\text{cancer}) = 0.98 \quad p(-|\text{cancer}) = 0.02$$

$$P(+|\sim\text{cancer}) = 0.03 \quad p(-|\sim\text{cancer}) = 0.97$$

For the second test, the result is positive.

$$\begin{aligned} h_{MAP}(\text{cancer}) &= \arg\max p(\text{cancer}|+) = p(+|\text{cancer}) * p(\text{cancer}) = 0.98 * 0.008 \\ &= 0.00784 \end{aligned}$$

$$\begin{aligned} h_{MAP}(\sim\text{cancer}) &= \arg\max p(\sim\text{cancer}|+) = p(+|\sim\text{cancer}) * p(\sim\text{cancer}) = 0.03 * 0.992 = \\ &0.02976 \end{aligned}$$

Thus,  $h_{MAP} = \sim\text{cancer}$

3.

$$(a) P+ = 3/6 = 1/2 \quad p- = 3/6 = 1/2$$

$$\text{Entropy}(s) = -p+ * \log_2 p+ - p- * \log_2 p- = -1/2 * (-1) - 1/2 * (-1) = 1$$

(b) a2: [3+, 3-]

$$E(a2) = 1$$

T: [2+, 2-]      F[1+, 1-]

$$E(T) = 1 \quad E(F) = 1$$

$$\text{Gain}(S, a2) = 1 - (4/6 * 1 + 2/6 * 1) = 0$$

4.

<Outlook = sunny, Temperature = mild, Humidity = normal, wind = strong>

$$V_{nb} = \arg \max p(V_j) * \text{Product}(p(a_i | V_j))$$

$$P(\text{yes}) * p(\text{sunny} | \text{yes}) * p(\text{mild} | \text{yes}) * p(\text{normal} | \text{yes}) * p(\text{strong} | \text{yes}) = 9/14 * 2/9 * 4/9 * 6/9 * 3/9 = 0.014$$

$$P(\text{no}) * p(\text{sunny} | \text{no}) * p(\text{mild} | \text{no}) * p(\text{normal} | \text{no}) * p(\text{strong} | \text{no}) = 5/14 * 3/5 * 2/5 * 1/5 * 3/5 = 0.0103$$

$$V_{nb} = 0.014 \quad \text{output: yes}$$