

交流电

$$V(t) = V_m \cos(\omega t + \varphi)$$

$$= \operatorname{Re}(V_m e^{j(\omega t + \varphi)})$$

$$= V_m \angle \varphi$$

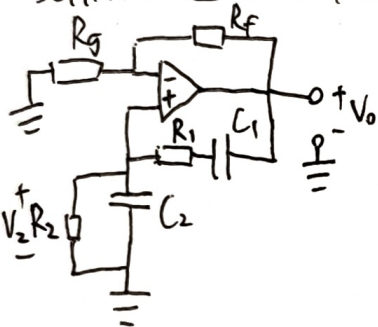
$$= V_m \cos \varphi + j V_m \sin \varphi$$

$$Z_L = j\omega L, Z_C = -j\frac{1}{\omega C}$$

$$Z = \frac{V}{I}$$

遵循全部串并联规律

Oscillator: 通过直流产生交流电



$$\omega_0 = \frac{1}{\sqrt{R_1 R_2 C_1 C_2}}$$

$$\frac{V_0}{V_2} = 1 + \frac{R_f}{R_g}$$

通常 $R_1 = R_2$ $C_1 = C_2$

三相电

$$V_a = V_p \angle 0^\circ, V_b = V_p \angle -120^\circ, V_c = V_p \angle -240^\circ$$

这是 abc sequence, positive sequence

反过来 acb, negative

4线: Y, 3线: Δ

达到相同功率: $Z_\Delta = 3 Z_Y$

Power

$$\text{Avg Power: } P = \frac{1}{2} V_m I_m \cos(\theta_v - \theta_i)$$

$$= \frac{1}{2} \operatorname{Re}(V I^*) \quad (* \text{为共轭})$$

注意, $P = \frac{1}{2} I_m^2 R = \frac{1}{2} \frac{V_m^2}{R}$ 是错误的

若 $Z = R + jX$, 则 $P = \frac{1}{2} I_m^2 R$

$$V_{rms} = \frac{V_m}{\sqrt{2}} \quad I_{rms} = \frac{I_m}{\sqrt{2}}$$

Power angle: $\theta = \theta_v - \theta_i = \angle Z$ leading: $\theta_v < \theta_i$

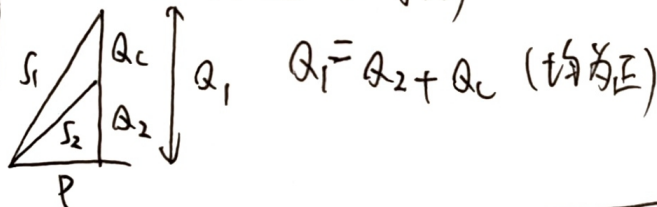
Power factor: $pf = \cos \theta = \frac{P}{|S|}$ lagging: $\theta_v > \theta_i$

Complex power: $S = \frac{1}{2} V I^* = \frac{1}{2} V_m I_m \angle (\theta_v - \theta_i)$
Let $S = P + jQ$ (单位 VA)

P 为平均实际功率 (单位 Watt)

Q 为储存在电路中的电量 (单位 VAR)

$$Q = \frac{1}{2} I_m^2 X \quad (Z = R + jX)$$



4种接线方法: Y-Y, Y-Δ, Δ-Δ, Δ-Y

$$V_L = \sqrt{3} V_p \quad (V_L \text{ line voltage, e.g. (Y-Y)})$$

$$I_L = \sqrt{3} I_p \quad (\Delta-\Delta) \quad (V_{ab})$$

总功率 $P = 3 V_p I_p \cos \theta$ (Y-load)

(V_p, I_p 为 rms, θ 为 Z 的角度)

不准确, 应根据实际情况计算

互感

$$V = N \frac{d\phi}{dt}$$

下标1,2按常识反过来

$$M_{12} = M_{21} = M$$

Dot convention: 主线圈电流从红点流入, 次线圈红点产生正电压

储存能量: $W = \frac{1}{2} L_1 I_1^2 + \frac{1}{2} L_2 I_2^2 - M I_1 I_2$ (要求电流均为正)
(主流入, 次流出 dot)

$$M \leq \sqrt{L_1 L_2}$$

$$k = \frac{M}{\sqrt{L_1 L_2}} \quad \text{coefficient of coupling}$$

$k < 0.5$ loosely coupled, $k > 0.5$ tightly coupled



$$L_a = L_1 - M \quad L_b = L_2 - M \quad L_c = M$$



$$L_A = \frac{L_1 L_2 - M^2}{L_2 - M}$$

$$L_B = \frac{L_1 L_2 - M^2}{L_1 - M}$$

$$L_C = \frac{L_1 L_2 - M^2}{M}$$

变压器

$$\frac{V_1}{V_2} = \frac{n_1}{n_2} \quad \frac{i_1}{i_2} = \frac{n_2}{n_1}, \quad S_1 = S_2$$

$1:n$, 左边的 V 变为 $\frac{1}{n}$, V 变为 $\frac{1}{n}$, I 变为 n 倍

Reflected Impedance

Autotransformers: 滑动变阻器