

Homework 1

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ECE 542: Semiconductor Development Fundamentals

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1 A SEMICONDUCTOR HAS A BANDGAP OF 0.5 eV. WHAT IS THE BANDGAP IN JOULES?

0.5 eV = 8.0109×10^{-20} J

2 A SEMICONDUCTOR HAS A BANDGAP OF 2×10^{-19} J. WHAT IS THE BANDGAP IN eV?

2×10^{-19} J = 1.2484 eV

3 FIND THE COST PER TRANSISTOR FOR:

3.1 A SINGLE TRANSISTOR
FQP13N10

\$0.98

3.1.1 Source: Mouser

3.1.2 Part Number:

3.1.2.1 Mouser #: 512-FQP13N10

3.1.2.2 Manufacturer #: FQP13N10

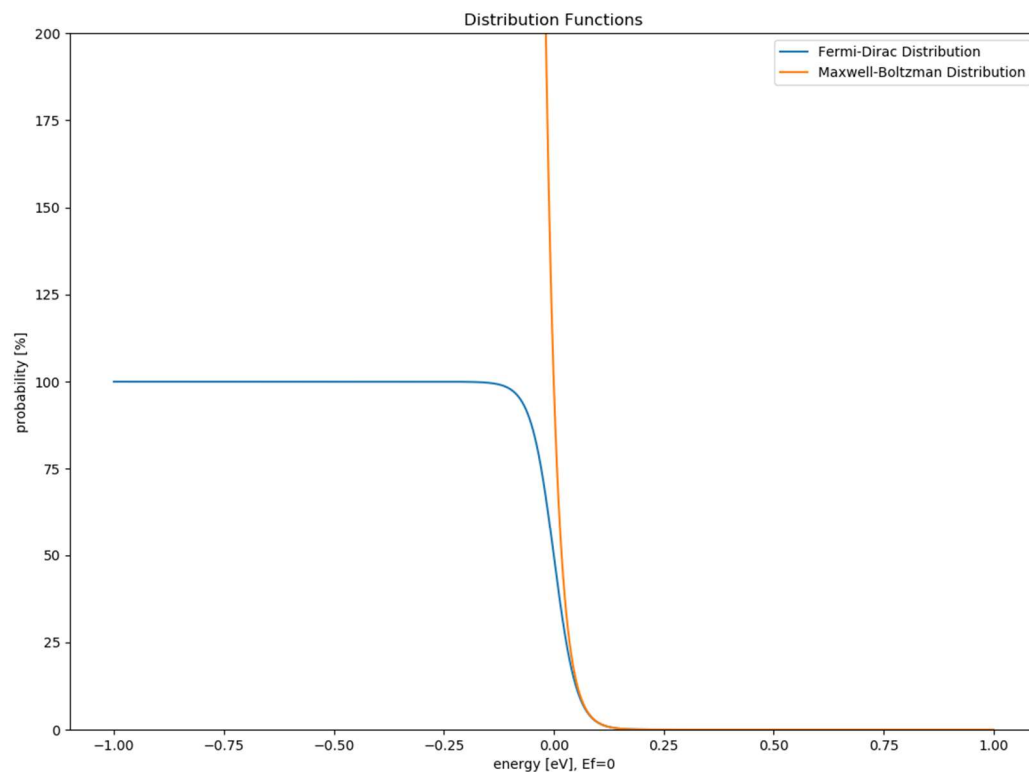
3.2 A REPRESENTATIVE IC
AMD Ryzen™ 9 3900X

\$0.0499e-8

3.2.1 Source: AMD

3.2.2 Part Number: 100-000000023

- 4 USING A COMPUTER AND YOUR FAVORITE MATH PROGRAM, PLOT THE FERMI-DIRAC DISTRIBUTION FUNCTION AS A FUNCTION OF ENERGY. ON THE SAME PLOT, SHOW THE MAXWELL-BOLTZMANN DISTRIBUTION FUNCTION. THE Y-AXIS SHOULD RANGE FROM 0 TO 2. THE X-AXIS SHOULD RANGE FROM $E_F - 1 \text{ eV}$ TO $E_F + 1 \text{ eV}$. DO THIS AT A TEMPERATURE OF 300 K.
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Note: The y-axis range is 0-200 because the entire y-axis is multiplied by 100 to ensure it represents a probability value.

4.1 OVER WHAT RANGE DOES THE MAXWELL-BOLTZMANN DISTRIBUTION FUNCTION APPROXIMATE THE FERMI-DIRAC DISTRIBUTION FUNCTION?

Assuming 0.1% error is a sufficient approximation, the energy range if $E - E_F$ where the Maxwell-Boltzmann distribution sufficiently approximates the Fermi-Dirac distribution function is 0.17871787178717868 or greater.

5 APPENDIX

5.1 CALCULATIONS.PY

```
import numpy as np
import matplotlib.pyplot as plt

def convert_ev_to_joules(electron_volts):
    return electron_volts * 1.60218e-19

def convert_joule_to_ev(joules):
    return joules * 6.242e18

def fermi_dirac_distribution(E, Ef=0, T=300, boltzmann_constant = 1.38064852e-23):
    """
        boltzmann_constant units are expected to be m^2*kg*s^-2*K^-1 or J*K^-1
        # E and Ef units are expected to be in eV
    """
    exp_value = convert_ev_to_joules(E - Ef) / (boltzmann_constant * T)
    return 1 / ( 1 + np.exp(exp_value))

def maxwell_boltzmann_distribution(E, Ef=0, T=300, boltzmann_constant = 1.38064852e-23):
    """
        boltzmann_constant units are expected to be m^2*kg*s^-2*K^-1 or J*K^-1
        # E and Ef units are expected to be in eV
    """
    # E and Ef are expected to be in eV
    exp_value = convert_ev_to_joules(E - Ef) / (boltzmann_constant * T)
    return np.exp(-exp_value)

def find_difference_threshold(energies, fermi_dirac_distributions, maxwell_boltzmann_distributions, percentage_threshold):
    percent_error = (np.abs(fermi_dirac_distributions - maxwell_boltzmann_distributions) / fermi_dirac_distributions) * 100
    indices_under_threshold = np.where(percent_error <= percentage_threshold)[0]
    return energies[indices_under_threshold[0]]

if __name__ == "__main__":
    print("A SEMICONDUCTOR HAS A BANDGAP OF 0.5 EV. WHAT IS THE BANDGAP IN JOULES?")
    print("0.5 eV = ", convert_ev_to_joules(0.5), "J")

    print("\nA SEMICONDUCTOR HAS A BANDGAP OF 2e-19 J. WHAT IS THE BANDGAP IN EV?")
    print("2e-19 J = ", convert_joule_to_ev(2e-19), "eV")

    energies = np.linspace(-1, 1, 10000)
    fermi_dirac_distributions = np.array(list(map(fermi_dirac_distribution, energies))) * 100
    maxwell_boltzmann_distributions = np.array(list(map(maxwell_boltzmann_distribution, energies))) * 100

    plt.plot(energies, fermi_dirac_distributions, label="Fermi-Dirac Distribution")
    plt.plot(energies, maxwell_boltzmann_distributions, label="Maxwell-Boltzman Distribution")
    plt.legend()
    plt.title("Distribution Functions")
    plt.xlabel("energy [eV], Ef=0")
    plt.ylabel("probability [%]")
    plt.ylim((0, 200))
    plt.show()

    print("\nOver what range does the maxwell-boltzmann distribution function approximate the Fermi-Dirac Distribution Function.")
    print("Assuming 0.1% error is a sufficient approximation, the energy range is ",
          find_difference_threshold(energies, fermi_dirac_distributions, maxwell_boltzmann_distributions, 0.1),
          "or greater.")
```