1. Proof of TestAndSet() for meeting 3 requirements

i. Mutual exclusion

As shown in Fig 1., Parameter *lock* is responsible for controlling the usage of critical section for processes. *lock* is a global variable set by multiple processes. Only when *lock* being *False* allow other process to access critical section. If one process has entered the critical section, as shown in Fig 2., *TestAndSet* set *lock* to *True*. This way of controlling critical section can ensure mutual exclusion by locking other processes out when one is in critical section.

ii. Progress

By setting *waiting[j]* to True before entering critical section and to *False* when exiting, letting other process enter critical section. When there exist 2 processes, P0 and P1, P0 wishes to enter the critical section while the other does not. Then *waiting[0]* is *True* and *waiting[1]* is *False*. Even if the key of P1 is *True*, P1 will not enter critical section, eventually P0 can enter. Thus, it achieves the goal of progress, which indicates that processes cannot be postponed indefinitely when entering critical section.

iii. Bounded waiting

The number of the process is n in the algorithm. By j = (i + 1) % n, j = (j + 1) % n, we get the number left divided by n. The number decides which process to be checked next. This mechanism ensures the quality of bounded waiting since the processes can enter critical section in at most n turns.

```
do {
      waiting[i] = TRUE;
      key = TRUE;
      while (waiting[i] && key)
                key = TestAndSet(&lock);
                                                                      boolean TestAndSet (boolean *target)
      waiting[j] = FALSE;
                // critical section
      i = (i + 1) \% n;
                                                                           boolean rv = *target;
      while ((j != i) && !waiting[j])
                                                                           *target = TRUE;
                j = (j + 1) \% n;
                                                                           return rv:
      if (j == i)
                                                                       }
                lock = FALSE; (No one is waiting)
      else
                                                                                          Fig 2.
                waiting[j] = FALSE; (process j enters next)
                // remainder section
} while (TRUE);
```

Fig 1.

- 2. Program to solve 2nd readers-writers program
 - i. By adding a new semaphore: rd to indicate the status of reading, the writer

- can lock the readers out and prevent them from accessing the critical section.
- ii. Also, semaphore *mutex* is changed to *rmutex* and *wmutex* for reader and writer mutex, to ensure mutual exclusion when *counts* are changing.
- iii. The first writer locks readers from accessing critical section by *wait(rd)*.
- iv. The last writer unlocks readers by *signal(rd)*.

Pseudo code:

```
Reader
                                     Writer
do
                                     do
{
                                     {
   wait(rd);
                                         wait(wmutex);
    //a reader is trying to enter
                                         writecount++;
   wait(rmutex);
                                         if (writecount == 1)
    readcount++;
                                         //1st writer
    if (readcount == 1)
                                             wait(rd);
        wait(wrt);
                                             //lock readers out
    signal(rmutex);
                                         signal(wmutex);
    signal(rd);
                                         wait(wrt);
    //done trying to enter
                                             // writing is performed
        // reading is performed
                                         signal(wrt);
    wait(rmutex);
                                         wait(wmutex);
    readcount -;
                                         writecount -;
    if (readcount == 0)
                                         if (writecount == 0)
        signal(wrt);
                                         //last writer
    signal(rmutex);
                                             signal(rd);
}
                                             //unlock readers
                                         signal(wmutex);
```