

Discrete Sliding Mode control of small UAS in tight formation flight under information constraints

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Abstract: This paper is concerned with a new control strategy based on discrete sliding mode control of small Unmanned Aerial Systems (UAS) in tight formation flight under information constraints. It addresses the problem of managing and coordinating several UAS to fly in a tight control formation. Since the formation of n UAS to be controlled is considered to fly in an arbitrary pattern in this work, a high-performance relative position control becomes an important issue. Indeed, a robust control strategy based on the sliding mode approach is proposed to achieve the desired flight performances while assuming realistic information constraints imposed by limited communication bandwidth and availability of relative localization sensors and preserving scalability with respect to formation size.

Also, this paper presents a meaningful study and comparison of the discrete sliding mode control design (DSMC) and time sampling continuous sliding mode control (TSCSMC). Indeed, it is important to study the performance differences between the two approaches that allow to choose the best strategy to be used to solve the considered problem. Here, the comparison focuses on the effect of the sampling on the control error, the mesh stability analytically and the mesh stability in simulation.

Simulation results of a flight scenario with two different sampling frequencies proves the efficiency of the proposed control strategy and shows clearly the effect of the discretization and the sampling on the formation flight behaviour of the UAS obtained by the chosen considered control.

Keywords: Flight formation, Aerospace unmanned vehicle, sliding mode control.

1. INTRODUCTION

The capability of autonomous formation flight has the potential to significantly enhance the utility and efficiency of small low-cost UAS. Formations of small, inexpensive fixed-wing UAS allow for the sharing of remote sensing functionality, mission-level redundancy and range enhancements due to aerodynamic interactions widely exploited by migratory birds. Indeed, aircraft's formation flight can enhance the fuel efficiency thanks to the aerodynamics and the induced airflow by leading aircraft, in the same way that the migratory birds use some formation patterns. Indeed, in Weimerskirch et al. (2001) authors have measured heart rates as an estimate of energy expenditure in imprinted great white pelicans (*Pelecanus onocrotalus*) trained to fly in 'V' formation, and show that

these birds save a significant amount of energy by flying in formation. This advantage is probably a principal reason for the evolution of flight formation in large birds that migrate in groups.

Also, this strategy has a lot of advantages as sharing of remote sensing functionality, mission-level redundancy, range enhancements due to aerodynamic interactions and energy saving. Based on that, the NASA AFF program has demonstrated the feasibility of this approach for manned fighter aircraft in a 2-aircraft configuration. Maximum fuel savings of 14% for the follower are reported. This emphasizes on the importance of the flight formation since no structural changes have to be made to the aircraft to gain considerable fuel savings.

Recently, both academical and industrial communities have been very interested in the flight formation of aircrafts and UAS. In Wolfe et al. (1996), decentralized control is presented to increase the efficiency of flight formation of 5 aircraft in a single line. These controllers are derived from a linear model and tested on a linear simulation incorporating a vortex-lattice aerodynamics routine. Another interesting study in Thien et al. (2008) focuses on the effect of its position and shape on aerodynamics performances of a given V flight formation. Vortices generated the wing tip of the leader moves downstream forming a pair of opposite rotating line vortices. Some interested control solutions for autonomous flight formation were introduced in Giulietti et al. (2000). Moreover, in the last decade, a lot of researchers have focused on improving the control strategies to enhance the formation flight performance behaviour. A suitable control strategy for controlling a team of micro-aerial vehicles moving quickly through a three-dimensional environment while maintaining a tight formation is presented in Turpin et al. (2012). Moreover, an interesting control performance analysis for autonomous close formation flight experiments has been achieved in Rice et al. (2014).

In this paper, a discrete robust sliding mode control strategy is proposed to manage the formation flight of UAS. Indeed, sliding mode control has been proved as a very efficient implementable solution for ground vehicle platooning (see Ferrara et al. (2008) and Zou et al. (2013)). Also, the sliding mode control is very efficient and robust approach regarding environmental disturbances to ensure a good position tracking performances. Here, authors provide a robust discrete sliding mode control solution to manage the tight formation flight of the UAS considering external disturbances. Then, a comparison between the discrete time sliding mode control design and the discretization of a time continuous sliding mode control is achieved. Indeed, it proves that the discretization of the time continuous designed controller decreases the tracking performances and the robustness regarding the environmental disturbances. This paper is structured as follows: section...

2. MODEL

2.1 Coordinate frames

The system to be controlled is a formation of n UAS flying in an arbitrary pattern. It is assumed that load factors are controlled in each vehicle's body frame (index b). Therefore separation errors are transformed into the body frame for control purposes, decoupling the three axes. The dynamics of each vehicle are defined in a local inertial North-East-Down frame (index e).

To dispose of a common reference frame for multiple members of the formation, the **Leader Speed Frame** (index ls) is defined. Its x axis is aligned with the formation leader's NED speed projected on the horizontal plane, its z axis is aligned with the NED frame's z axis, and its y axis completes a right-handed Cartesian coordinate system. It is used to define the separation vectors that make up the formation.

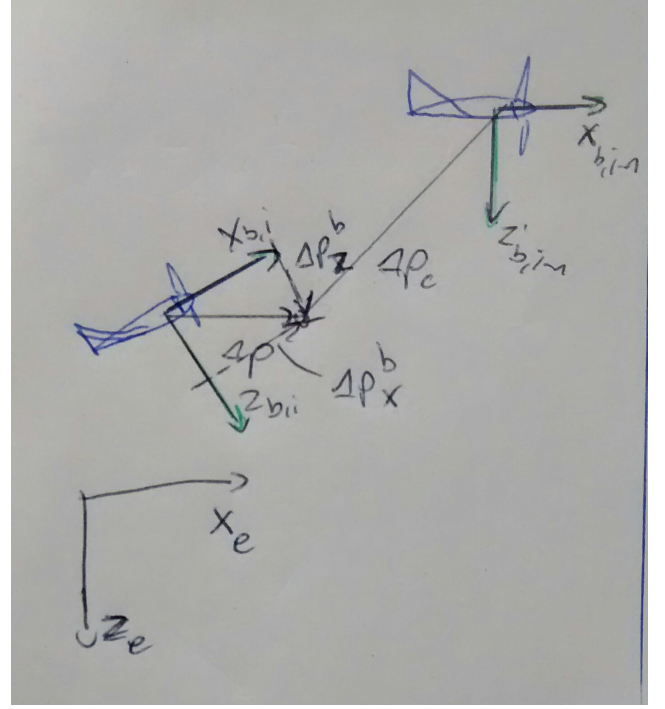


Fig. 1. Predecessor-follower geometry longitudinal

2.2 Vehicle Model

The continuous time vehicle position dynamics w.r.t. the local inertial frame are given by

$$\mathbf{x} = (\mathbf{p} \ \mathbf{v})^T \quad (1)$$

$$\dot{\mathbf{p}} = \mathbf{v} \quad (2)$$

$$\dot{\mathbf{v}} = \mathbf{a}_c + \mathbf{a}_w + \mathbf{g} \quad (3)$$

where $\mathbf{p} \in \mathbb{R}^3$ is the vehicle position, $\mathbf{v} \in \mathbb{R}^3$ is its velocity w.r.t to the local inertial frame, $\mathbf{a}_w \in \mathbb{R}^3$ are accelerations induced by exogenous disturbances such as turbulence and another aircraft's wake, $\mathbf{a}_c \in \mathbb{R}^3$ are commanded accelerations and $\mathbf{g} \in \mathbb{R}^3$ is the gravity vector in the local inertial frame.

It is assumed that load factors \mathbf{n}_c are tracked by fast inner loop controllers in the vehicle body frame.

$$\dot{\mathbf{v}} = \mathbf{R}_{eb}|\mathbf{g}|(\mathbf{n}_c + \mathbf{a}_w + \mathbf{g}) \quad (4)$$

where $\mathbf{R}_{eb} \in \mathbb{R}^{3 \times 3}$ is the rotation matrix from the body frame to the local inertial frame and $\mathbf{n}_c = \frac{1}{|\mathbf{g}|}\mathbf{a}_c$ are commanded load factors. To simplify notation, it is assumed that the vehicle is trimmed, i.e. the nominal gravitational acceleration is compensated for by a trim control input $\mathbf{n}_{c,0} = \mathbf{R}_{be}(0 \ 0 \ -1)^T$ and the control input is redefined as

$$\mathbf{u} = \mathbf{R}_{eb}|\mathbf{g}|(\mathbf{n}_c - \mathbf{n}_{c,0}) \quad (5)$$

leading to

$$\dot{\mathbf{v}} = \mathbf{R}_{eb}|\mathbf{g}|(\frac{1}{|\mathbf{g}|}(\mathbf{R}_{be}\mathbf{u} + \mathbf{n}_{c,0})) + \mathbf{a}_w + \mathbf{g} \quad (6)$$

$$\dot{\mathbf{v}} = \mathbf{u} + \mathbf{a}_w \quad (7)$$

where now \mathbf{a}_w also includes the small effects of imperfect knowledge of local gravitation. ???doubledefinition

Considering two UAS i and $i - 1$, this leads to relative position error dynamics

$$\Delta \mathbf{p} = \mathbf{p}_i - \mathbf{p}_{i-1} - \Delta \mathbf{p}_c \quad (8)$$

$$\Delta \dot{\mathbf{p}} = \mathbf{v}_i - \mathbf{v}_{i-1} - \Delta \dot{\mathbf{p}}_c \quad (9)$$

$$\Delta \ddot{\mathbf{p}} = \mathbf{a}_i - \mathbf{a}_{i-1} - \Delta \ddot{\mathbf{p}}_c \quad (10)$$

$$= \mathbf{a}_{c,i} + \mathbf{a}_{w,i} - \mathbf{a}_{i-1} - \Delta \ddot{\mathbf{p}}_c \quad (11)$$

$$= \mathbf{u} + \mathbf{a}_{w,i} - \mathbf{a}_{i-1} - \Delta \ddot{\mathbf{p}}_c \quad (12)$$

where $\Delta \mathbf{p}$ is the relative position error between UAS i and its predecessor $i - 1$, $\Delta \mathbf{v}$ is the corresponding relative velocity error, $\Delta \mathbf{p}_c$ is the desired relative position to the predecessor, \mathbf{a} are accelerations.

The presented model is essentially of the same type as that used in Galzi and Shtessel (2006) and provides the benefit of being vehicle-agnostic, as the specific vehicle dynamics are covered by the inner loop load factor controllers. On the other hand, perturbations \mathbf{a}_w and control input saturations are specific to a given vehicle and mission environment.

3. CONTROL DESIGN

To benefit from significant aerodynamic performance gains, a follower aircraft needs to stay within a narrow spatial window roughly defined by (see e.g. Jake et al. (2003))

$$\begin{aligned} -0.2b < \Delta y' < -0.1b \\ -0.1b < \Delta z' < 0 \end{aligned}$$

while the longitudinal separation $\Delta x'$ is less critical due to slow vortex decay. It is thus the control objective to drive the follower UAS into this window and stay within in.

3.1 Input saturations

For a fixed-wing UAS, the maximum load factors are naturally limited by the maximum thrust of the engine and the aerodynamic parameters of the aircraft, such as the stall angle α_{max} , limiting the maximum vertical load factor n_3 . These limitations are time-varying since, including the engine thrust, they are function of the dynamic pressure $\bar{q}(t) = \frac{1}{2}\rho(t)V_a^2(t)$.

3.2 Information constraints

It is assumed that observations of the relative position and relative velocity vector between each UAS and its predecessor are available.

This limitation allows to use low-cost vision-based relative localization techniques, which is a significant advantage taking into account the price range of GNSS Real Time Kinematics systems which would be required for localization with respect to the formation leader or other members of the formation that are now within the field of view of onboard vision sensors.

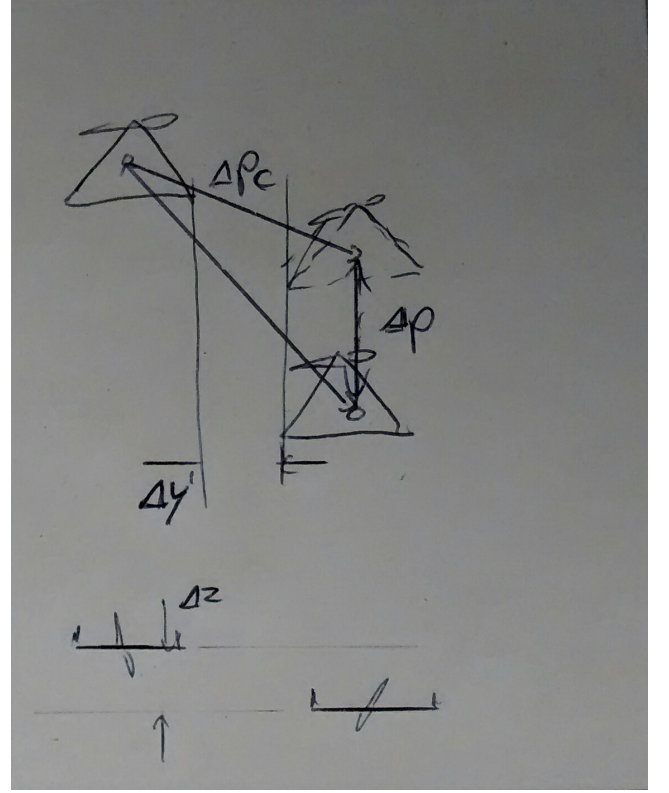


Fig. 2. Predecessor-follower geometry

3.3 CSMC

It is the control objective to drive the system to the sliding surface defined by

$$\sigma(t) = \mathbf{G}\mathbf{x}(t) \quad (13)$$

$$\mathbf{x}(t) = \begin{pmatrix} \Delta \mathbf{p}(t) \\ \Delta \mathbf{v}(t) \end{pmatrix} \quad (14)$$

and, once reached, to keep it on it for all subsequent times $t \geq t^*$. With

$$\mathbf{G} = [\mathbf{G}_1 \mathbf{G}_2] \quad (15)$$

the position error dynamics in sliding mode are

$$\mathbf{0} = [\mathbf{G}_1 \mathbf{G}_2] \begin{pmatrix} \Delta \mathbf{p}(t) \\ \Delta \mathbf{v}(t) \end{pmatrix} \quad (16)$$

$$\Delta \dot{\mathbf{p}} = -\mathbf{G}_2^{-1} \mathbf{G}_1 \Delta \mathbf{p} \quad (17)$$

Selecting $-\mathbf{G}_2^{-1} \mathbf{G}_1$ as Hurwitz ensures that $\Delta \mathbf{p}$ asymptotically converges to zero while in sliding mode.

Mesh stability is a feature of a three-dimensional formation of vehicles that allows separation errors to stay locally contained (see e.g. Pant et al. (2002)). In other words, separation errors between a pair of vehicles are not amplified towards the neighboring vehicle pairs. It is a well known fact (Pant et al. (2002)) that linear controllers with local feedback information are mesh unstable.

While in sliding mode, the position error dynamics are by definition confined to (17), independently of adjacent separation errors, implying mesh stability if the system can be kept in sliding mode.

The open loop sliding variable dynamics are

$$\dot{\sigma} = \mathbf{G} \begin{pmatrix} \Delta \mathbf{v} \\ \mathbf{u} + \mathbf{a}_{w,i} - \mathbf{a}_{i-1} - \Delta \ddot{\mathbf{p}}_c \end{pmatrix} \quad (18)$$

$$= \mathbf{G} \begin{pmatrix} \Delta \mathbf{v} \\ -\Delta \ddot{\mathbf{p}}_c \end{pmatrix} + \mathbf{G} \begin{bmatrix} \mathbf{0} \\ \mathbf{I} \end{bmatrix} (\mathbf{u} + \mathbf{a}_w + \mathbf{a}_{k-1}) \quad (19)$$

$$= \mathbf{G}\Phi_k + \mathbf{G}\mathbf{B}(\mathbf{u} + \Phi_u) \quad (20)$$

$$= \Phi'_k + \Phi'_u + \mathbf{u}' \quad (21)$$

The desired relative position $\Delta \mathbf{p}_c$ and its second derivative are communicated to each follower. Accelerations of the predecessor \mathbf{a}_{i-1} as well as exogenous perturbations \mathbf{a}_w acting on the vehicle i are assumed to be unknown but bounded. For notational convenience they are lumped into the disturbance vector Φ_u

$$\Phi_u = \mathbf{a}_w - \mathbf{a}_{i-1} \quad (22)$$

while the known perturbations $\Delta \ddot{\mathbf{p}}_c$ are redefined as Φ_k

$$\Phi_k = \Delta \ddot{\mathbf{p}}_c \quad (23)$$

further defining

$$\mathbf{u}' = \mathbf{G}\mathbf{B}\mathbf{u} \quad (24)$$

$$\Phi'_k = \mathbf{G}\Phi_k \quad (25)$$

$$\Phi'_u = \mathbf{G}\mathbf{B}\Phi_u \quad (26)$$

Note that all perturbations are assumed to satisfy the matching condition. The three axes are considered decoupled by the inner load factor controllers, allowing for SISO design.

Since the inner loop load factor controllers cannot track discontinuous reference signals, a continuous control signal is mandatory. The system (20) is of relative degree $\mathbf{r} = (1 \ 1 \ 1)^T$, thus continuous-time Super-Twisting Sliding Mode controllers (CSTSMC, see e.g. Shtessel et al. (2014)) can be applied, providing continuous control signals. We apply the controller presented in Galzi and Shtessel (2006) extending it trivially from 2D to 3D tracking. The CSTSMC controller is then given by

$$u'_i = \alpha_i |\sigma_i|^{1/2} \text{sign}(\sigma_i) + \beta_i \int \text{sign}(\sigma_i) dt \quad (27)$$

where $i = 1...3$ indicates the three decoupled axes. Adding a term that eliminates the known disturbances $\Phi'_{k,i}$ as in Galzi and Shtessel (2006)

$$u'_i = \alpha_i |\sigma_i|^{1/2} \text{sign}(\sigma_i) + \beta_i \int \text{sign}(\sigma_i) dt - \Phi'_{k,i} \quad (28)$$

leads to closed loop σ dynamics of

$$\dot{\sigma}_i = \alpha_i |\sigma_i|^{1/2} \text{sign}(\sigma_i) + \beta_i \int \text{sign}(\sigma_i) dt + \Phi'_{u,i} \quad (29)$$

Provided the disturbances $\Phi_{u,i}$ are bounded by $\Phi_{u,i} \leq L_i$ controller parameters that fulfill

$$\alpha_i = 1.5 \sqrt{L_i} \quad (30)$$

$$\beta_i = 1.1 L_i \quad (31)$$

drive the system into 2-sliding mode, i.e. $\dot{\sigma} = \sigma = 0$ in finite time. The reaching time is bounded by $t^* \leq \frac{7.6\sigma_i(0)}{\beta_i - L_i}$, see Galzi and Shtessel (2006).

The actual control input \mathbf{n}_c is computed from (24, 5) as

$$\mathbf{n}_c = \frac{1}{\|\mathbf{g}\|} \mathbf{R}_{be} (\mathbf{G}\mathbf{B})^{-1} \mathbf{u}' + \mathbf{n}_{c,0} \quad (32)$$

using $\mathbf{R}_{eb}^{-1} = \mathbf{R}_{eb}^T = \mathbf{R}_{be}$

Discretization For implementation, the CSTSMC is sampled with a zero-order hold scheme. There are results for homogeneous sliding controllers such as the CSTSMC (see Shtessel et al. (2014)) stating that the error introduced by discrete sampling is quadratically proportional to the sampling time, i.e.

$$\sigma = O(T^2) \quad (33)$$

3.4 DSMC

Designing a sliding mode controller in the discrete time domain allows to take sampling time effects into account right from the beginning.

The σ dynamics assuming forward Euler discretization are

$$\sigma(k+1) = \sigma(k) + T(\Phi'_k(k) + \Phi'_u(k) + \mathbf{u}'(k)) \quad (34)$$

Since a discrete controller has no control over what happens to the continuous system between sampling instants, ideal sliding mode is not achievable. It is however possible to drive the system into so-called quasi-sliding mode, defined by the control objective

$$|\sigma_i(k)| \leq \epsilon_i \quad (35)$$

for $i = 1...3$, for all $k \geq k^*$ where ϵ is the width of the quasi-sliding mode boundary layer and k^* is the first sample for which eq. 35 is satisfied, i.e. when the system transitions from the reaching phase into quasi-sliding mode. The proposed DSMC is based on ideas presented by the authors of Monsees and Scherpen (2001). The following linear reaching law (proposed e.g. by Spurgeon (1992)) ensures asymptotic convergence to the sliding surface

$$\sigma(k+1) = \Psi \sigma(k) \quad (36)$$

with a diagonal $\Psi \in \mathbb{R}^{3 \times 3}$, $0 < \Psi_{i,i} < 1$ for $i = 1...3$. The choice of Ψ allows to trade off control effort and reaching time. Since (36) is equivalent to

$$|\sigma(k+1)| = \Psi|\sigma(k)| \quad (37)$$

the norm of the sliding variable decreases with every time step, indicating convergence to the sliding surface.

The control input $\mathbf{u}(k)$ required to drive the system (34) according to the reaching law (36) can be computed from the open-loop σ dynamics to

$$\mathbf{u}'(k) = \frac{1}{T}\sigma(k)(\Psi - \mathbf{I}) - \Phi'_k - \Phi'_u \quad (38)$$

Note that $\mathbf{u}'(k)$ contains the unknown perturbations. Assuming an estimate of the unknown perturbation $\tilde{\Phi}'_u(k) = \Phi'_u(k) + \Delta\Phi'_u(k)$ and closing the loop, one obtains

$$\sigma(k+1) = \Psi\sigma(k) + T(\Delta\Phi'_u(k)) \quad (39)$$

Note that the reaching law (36) can not be followed due to the estimation error $\Delta\Phi'_u(k)$. Instead, assuming that initially the system is outside the quasi-sliding mode band, it will approach the sliding surface at least as long as

$$\Psi\sigma(k) \geq T(\Delta\Phi'_u(k)) \quad (40)$$

This defines the maximum boundary layer thickness as

$$\epsilon = \Psi^{-1}T(\Delta\Phi'_u(k)) \quad (41)$$

A simple way to obtain an estimate of the unknown disturbances is from the previous sample by

$$\Phi'_u(k-1) = \sigma(k) - \sigma(k-1) - T(\Phi'_k(k-1) + \mathbf{u}'(k-1)) \quad (42)$$

assuming that the disturbance rate is bounded by $|\frac{d\Phi'}{dt}| \leq \delta\Phi'$, assuming $\Phi'(k) = \Phi'(k-1)$ and a first-order approximation introduces an error $\Delta\Phi'_u(k)$ that is bounded by $|\Delta\Phi'_u(k)| \leq T\delta\Phi'$.

Note that with (41), the boundary layer thickness depends quadratically on the sampling time.

4. SIMULATIONS

Both controllers have been evaluated in a simulation environment. In all cases, the vehicle dynamics have been simulated at a sampling time of $t_{sim} = 10^{-4}$ s, while the controller sampling time has been varied.

4.1 Controller parameters

For the CSTSMC, the controller gains are computed according to (31). For the DSMC, the entries of the reaching rate matrix Ψ are selected to stay within control input limits for typical initial position errors.

4.2 Disturbance models

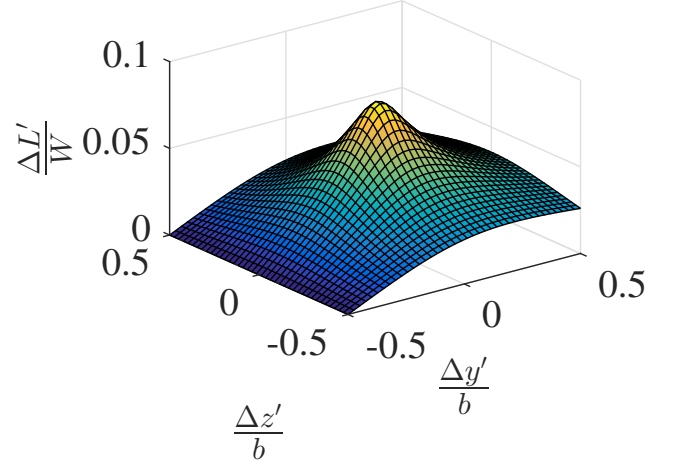
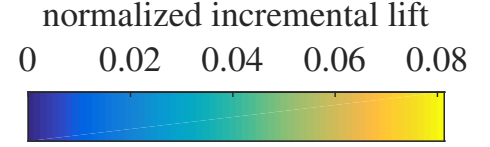


Fig. 3. Normalized incremental lift predicted by modified Horseshoe Vortex Model for $\Delta x' = 2b$. Note that $\Delta x', \Delta y', \Delta z'$ are wingtip to wingtip separations

Wake vortex disturbances A variety of approaches has been proposed to simulate the effects of wake trailing vortices on following UAS, mostly based on modified Horseshoe Vortex Models (HVM) (citethemall) or Vortex Lattice methods (VLM) (citethemall). For the purpose of this work, a HVM with modified core model presented in (Dogan et al. (2005)) is used. It is reported to provide predictions that are in good agreement of both VLM models and wind tunnel measurements while being of great simplicity. In the vertical channel, the model predicts incremental aerodynamic lift perturbations as a function of the separation vector between a UAS and its predecessor, see fig. 3. A variety of approaches has been proposed to simulate the effects of wake trailing vortices on following UAS, mostly based on modified Horseshoe Vortex Models (HVM) (citethemall) or Vortex Lattice methods (VLM) (citethemall). For the purpose of this work, a HVM with modified core model presented in (Dogan et al. (2005)) is used. It is reported to provide predictions that are in good agreement of both VLM models and wind tunnel measurements while being of great simplicity. The model predicts incremental aerodynamic lift perturbations as a function of the separation vector between a UAS and its predecessor, see fig. 3.

Atmospheric turbulence Atmospheric turbulence time series are generated according to the Dryden turbulence spectrum. The induced velocities are filtered by transfer functions corresponding to LQR load factor controllers designed for a small UAS ($b = 2.6m$).

Maneuver

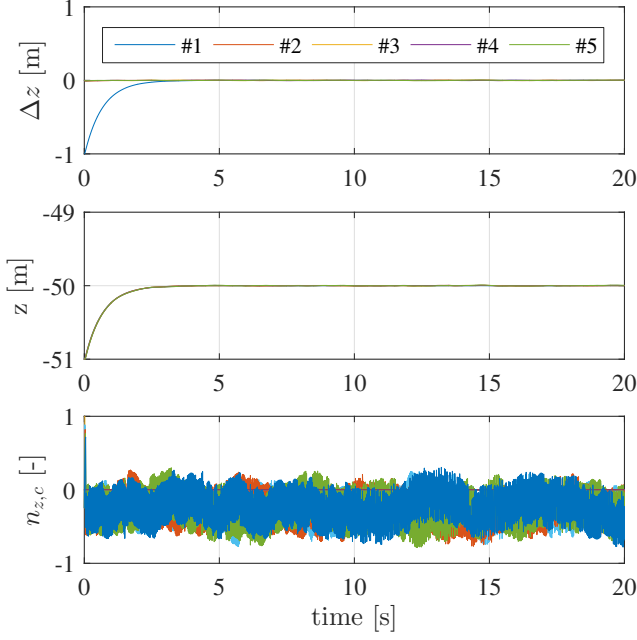


Fig. 4. CSMC controller $10^{-3}s$ sampling time

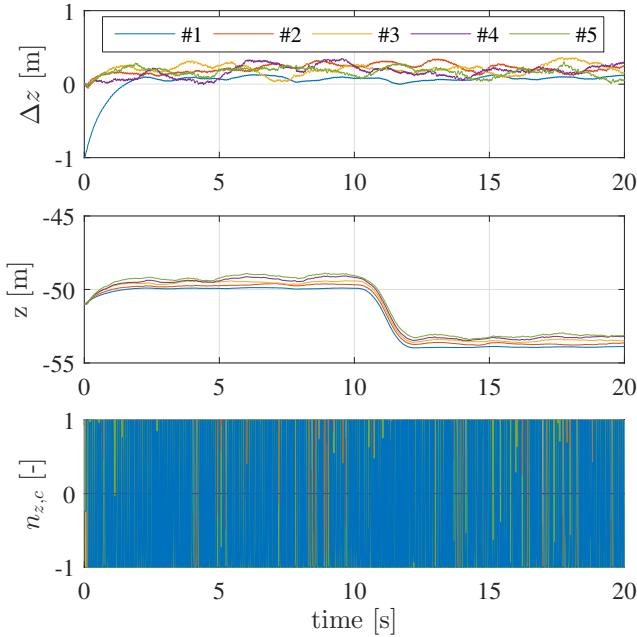


Fig. 5. CSMC controller $10^{-2}s$ sampling time

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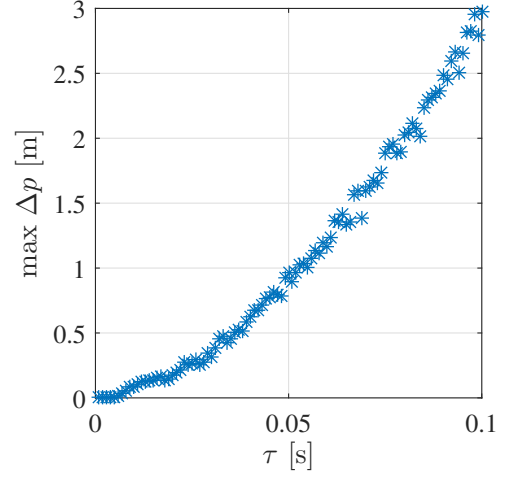


Fig. 6. Maximum vertical position error vs. CSMC controller sampling time

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