

Activity 9: Statistical reasoning 1: intro to models

Joshua Holt and Jacob Chung

1. Fiddler crabs

```
library(brms) # for statistics
```

Loading required package: Rcpp

Loading 'brms' package (version 2.23.0). Useful instructions can be found by typing `help('brms')`. A more detailed introduction to the package is available through `vignette('brms_overview')`.

Attaching package: 'brms'

The following object is masked from 'package:stats':

ar

```
library(tidyverse)
```

```
-- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
v dplyr     1.1.4     v readr     2.1.5
v forcats   1.0.0     v stringr   1.5.1
v ggplot2   4.0.0     v tibble    3.3.1
v lubridate  1.9.4     v tidyr    1.3.1
v purrr    1.1.0
```

```
-- Conflicts ----- tidyverse_conflicts() --
x dplyr::filter() masks stats::filter()
x dplyr::lag()    masks stats::lag()
i Use the conflicted package (<http://conflicted.r-lib.org/>) to force all conflicts to become non-conflicting
```

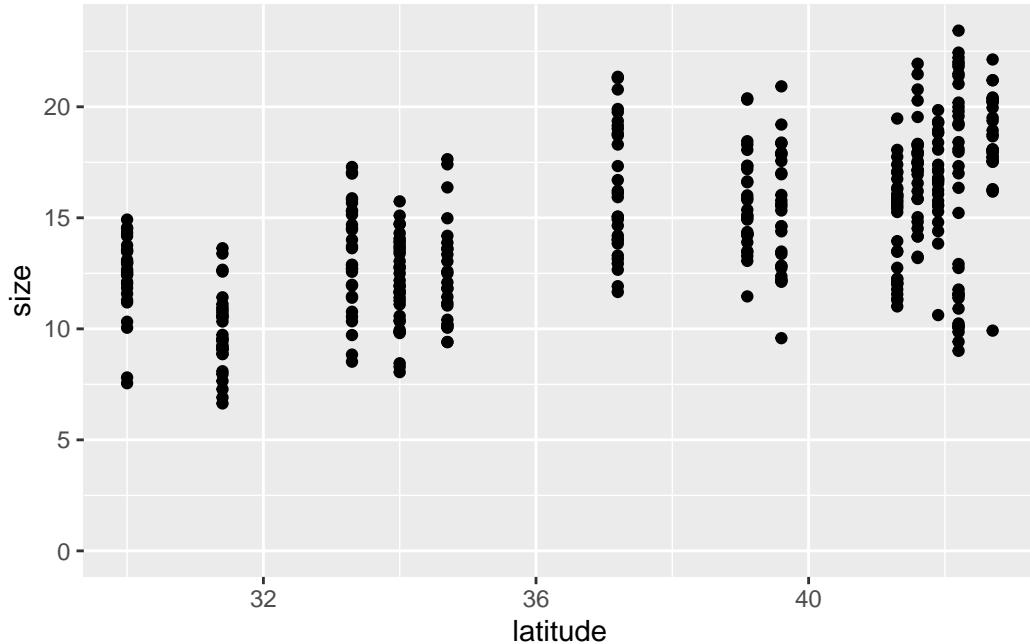
```
library(ggeffects) # for the prediction plot
library(lterdatasampler) # for built-in datasets
```

```
head(pie_crab)
```

```
# A tibble: 6 x 9
  date      latitude site   size air_temp air_temp_sd water_temp water_temp_sd
  <date>     <dbl> <chr> <dbl>    <dbl>    <dbl>    <dbl>    <dbl>
1 2016-07-24      30 GTM    12.4     21.8     6.39     24.5     6.12
2 2016-07-24      30 GTM    14.2     21.8     6.39     24.5     6.12
3 2016-07-24      30 GTM    14.5     21.8     6.39     24.5     6.12
4 2016-07-24      30 GTM    12.9     21.8     6.39     24.5     6.12
5 2016-07-24      30 GTM    12.4     21.8     6.39     24.5     6.12
6 2016-07-24      30 GTM    13.0     21.8     6.39     24.5     6.12
# i 1 more variable: name <chr>
```

1.1 Plot data, pick the model

```
pie_crab %>%
  ggplot(aes(x = latitude, y = size)) +
  geom_point() +
  # Make the y-axis include 0
  ylim(0, NA)
```

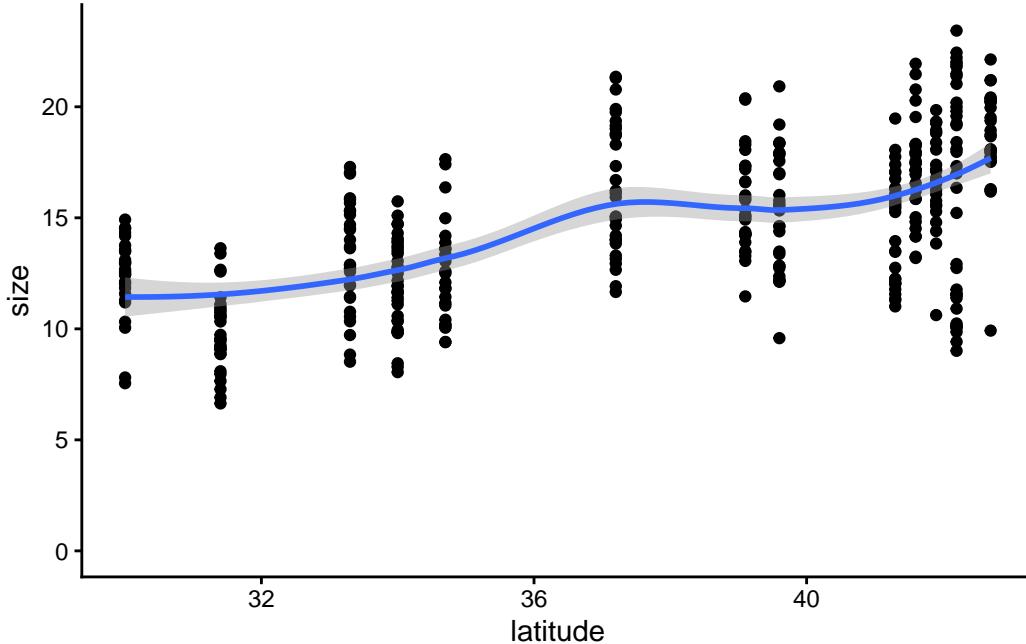


Q1.1) I would say that size does increase with latitude. We are not very confident in this interpretation, due to potential bias in sampling.

Q1.2)

```
pie_crab %>%
  ggplot(aes(x = latitude, y = size)) +
  geom_point() +
  # Make the y-axis include 0
  ylim(0, NA) +
  geom_smooth()+
  theme_classic()

`geom_smooth()` using method = 'loess' and formula = 'y ~ x'
```



1.2 Fit linear regression with brms

```
# latitude model
m.crab.lat <-
  brm(data = pie_crab, # Give the model the pie_crab data
       # Choose a gaussian (normal) distribution
       family = gaussian,
       # Specify the model here.
       size ~ latitude,
       # Here's where you specify parameters for executing the Markov chains
       # We're using similar to the defaults, except we set cores to 4 so the analysis runs faster
       iter = 2000, warmup = 1000, chains = 4, cores = 4,
       # Setting the "seed" determines which random numbers will get sampled.
       # In this case, it makes the randomness of the Markov chain runs reproducible
       # (so that both of us get the exact same results when running the model)
       seed = 4,
       # Save the fitted model object as output - helpful for reloading in the output later
       file = "output/m.crab.lat")
```

Q1.3) The iter tells the computer the number of total iterations per chain (including warmup; defaults to 2000).

1.3 Assess model

```
summary(m.crab.lat)
```

```
Family: gaussian
Links: mu = identity
Formula: size ~ latitude
Data: pie_crab (Number of observations: 392)
Draws: 4 chains, each with iter = 2000; warmup = 1000; thin = 1;
      total post-warmup draws = 4000
```

Regression Coefficients:

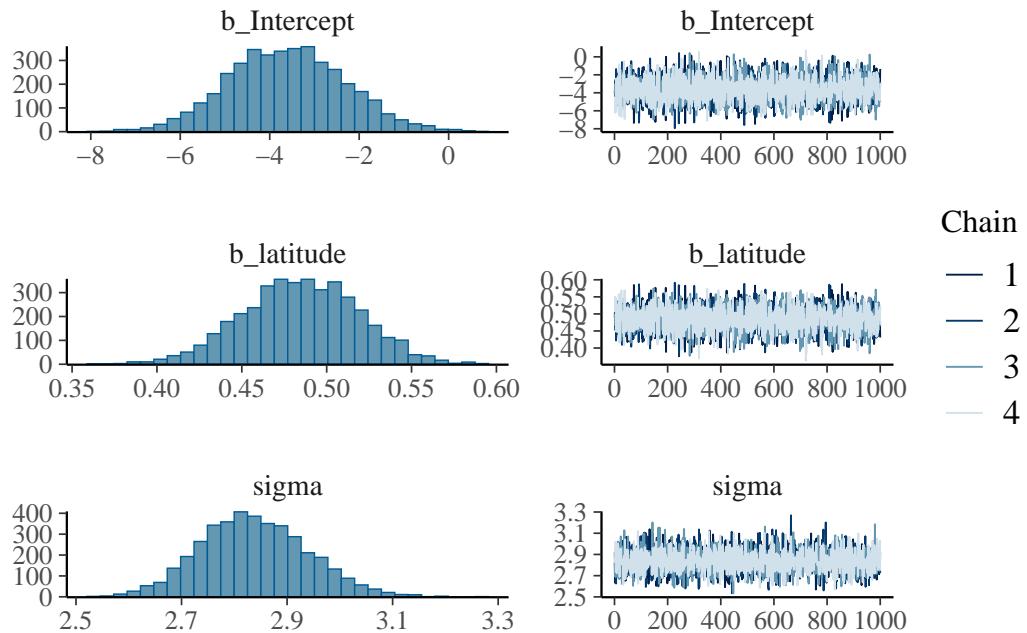
| | Estimate | Est.Error | 1-95% CI | u-95% CI | Rhat | Bulk_ESS | Tail_ESS |
|-----------|----------|-----------|----------|----------|------|----------|----------|
| Intercept | -3.61 | 1.30 | -6.09 | -1.01 | 1.00 | 4116 | 3192 |
| latitude | 0.48 | 0.03 | 0.42 | 0.55 | 1.00 | 4108 | 3140 |

Further Distributional Parameters:

| | Estimate | Est.Error | 1-95% CI | u-95% CI | Rhat | Bulk_ESS | Tail_ESS |
|-------|----------|-----------|----------|----------|------|----------|----------|
| sigma | 2.84 | 0.10 | 2.65 | 3.04 | 1.00 | 3758 | 2852 |

Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS and Tail_ESS are effective sample size measures, and Rhat is the potential scale reduction factor on split chains (at convergence, Rhat = 1).

```
plot(m.crab.lat) # show posteriors and chains
```



1.4 Interpret model

```
summary(m.crab.lat)
```

```

Family: gaussian
Links: mu = identity
Formula: size ~ latitude
Data: pie_crab (Number of observations: 392)
Draws: 4 chains, each with iter = 2000; warmup = 1000; thin = 1;
       total post-warmup draws = 4000

```

Regression Coefficients:

| | Estimate | Est.Error | 1-95% CI | u-95% CI | Rhat | Bulk_ESS | Tail_ESS |
|-----------|----------|-----------|----------|----------|------|----------|----------|
| Intercept | -3.61 | 1.30 | -6.09 | -1.01 | 1.00 | 4116 | 3192 |
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| sigma | 2.84 | 0.10 | 2.65 | 3.04 | 1.00 | 3758 | 2852 |

Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS

and Tail_ESS are effective sample size measures, and Rhat is the potential scale reduction factor on split chains (at convergence, Rhat = 1).

```
as_draws_df(m.crab.lat)  %>% # extract the posterior samples from the model estimate
  select(b_latitude)  %>% # pull out the latitude samples from all 4 chains. we'll get a wa
  summarize(p_slope_lessthanorequalto_zero = sum(b_latitude <= 0)/length(b_latitude))
```

Warning: Dropping 'draws_df' class as required metadata was removed.

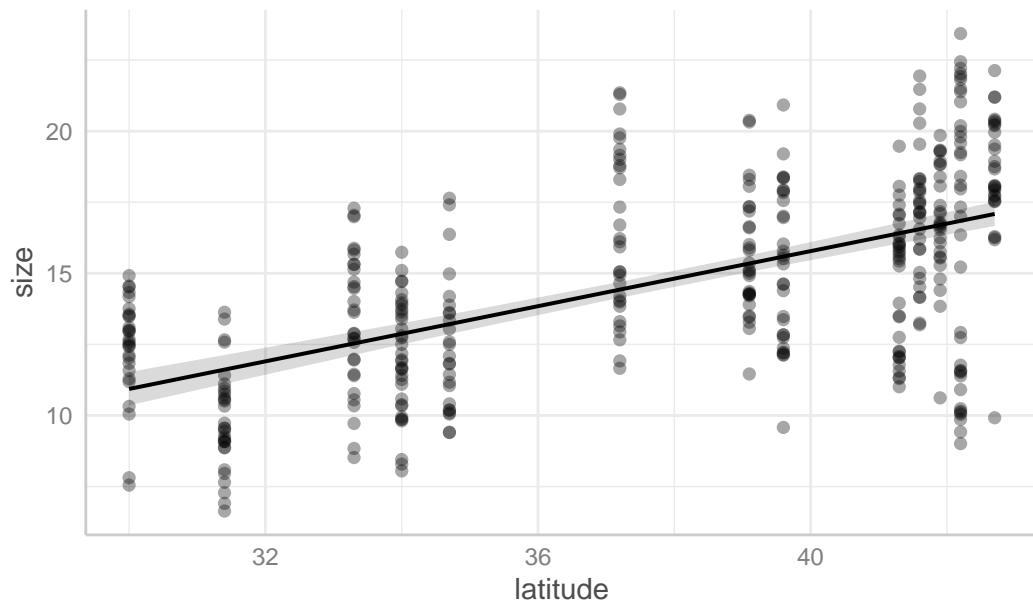
```
# A tibble: 1 x 1
  p_slope_lessthanorequalto_zero
  <dbl>
1 0
```

1.5 Plot model on the data

```
# compatibility interval. the shows uncertainty in the average response.
confm.crab.lat <- predict_response(m.crab.lat)
plot(confm.crab.lat, show_data = TRUE)
```

Data points may overlap. Use the `jitter` argument to add some amount of random variation to the location of data points and avoid overplotting.

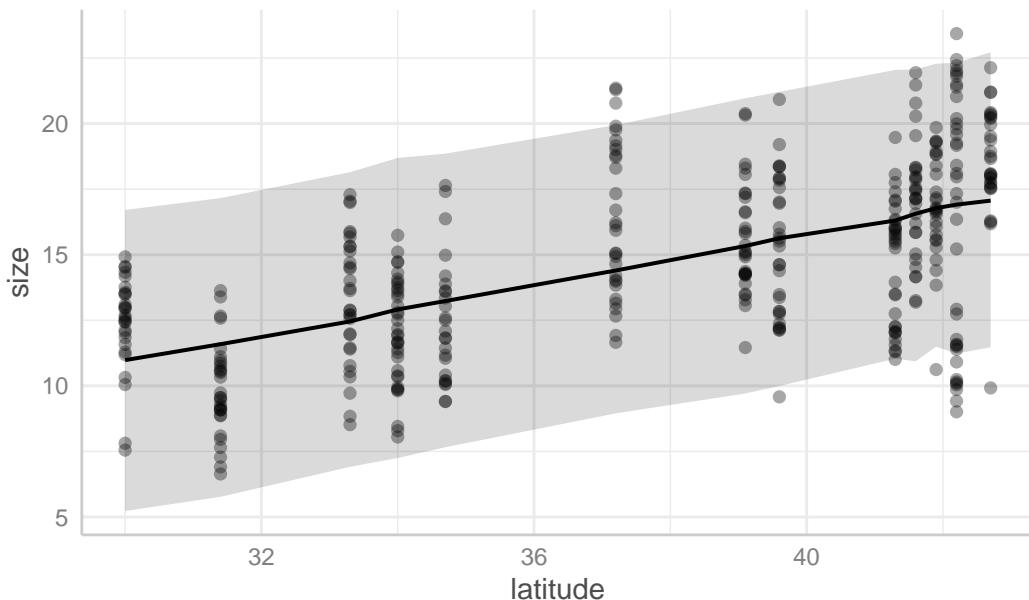
Predicted values of size



```
# prediction interval. this shows uncertainty in the data around the average response.  
confm.crab.lat <- predict_response(m.crab.lat, interval = 'prediction')  
plot(confm.crab.lat, show_data = TRUE)
```

Data points may overlap. Use the `jitter` argument to add some amount of random variation to the location of data points and avoid overplotting.

Predicted values of size



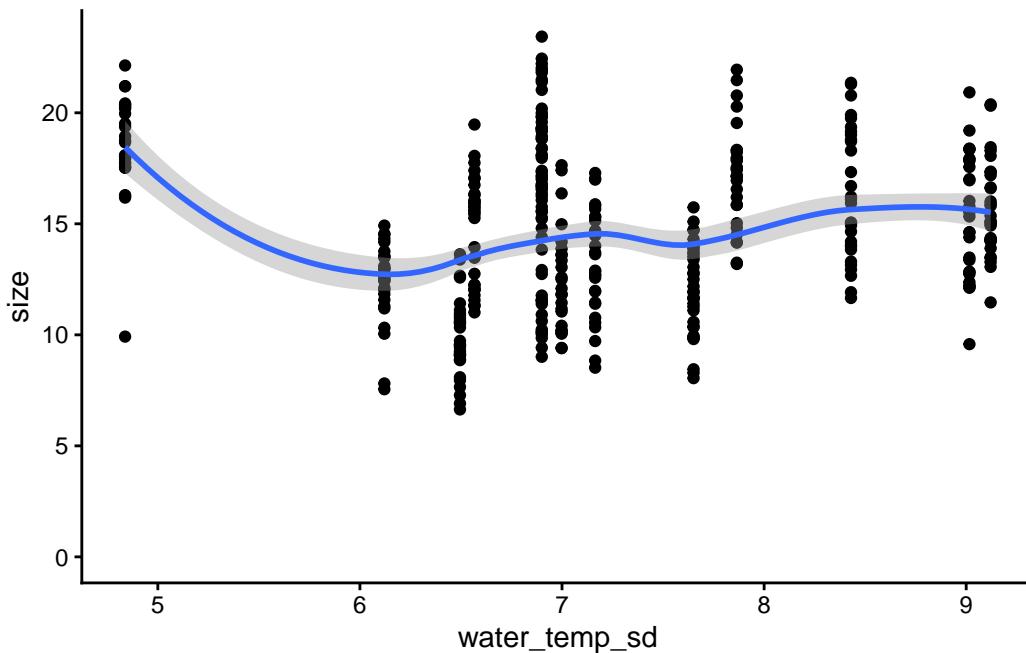
1.6 Repeat with new variable: water temp sd

Q1.4) We predict that higher variability will be observed in smaller crabs, with the larger crabs showing lower variability. This is due to the expectation that larger crabs will handle water temperature variability the best.

Q1.5)

```
pie_crab %>%
  ggplot(aes(x = water_temp_sd, y = size)) +
  geom_point() +
  # Make the y-axis include 0
  ylim(0, NA) +
  geom_smooth()+
  theme_classic()

`geom_smooth()` using method = 'loess' and formula = 'y ~ x'
```



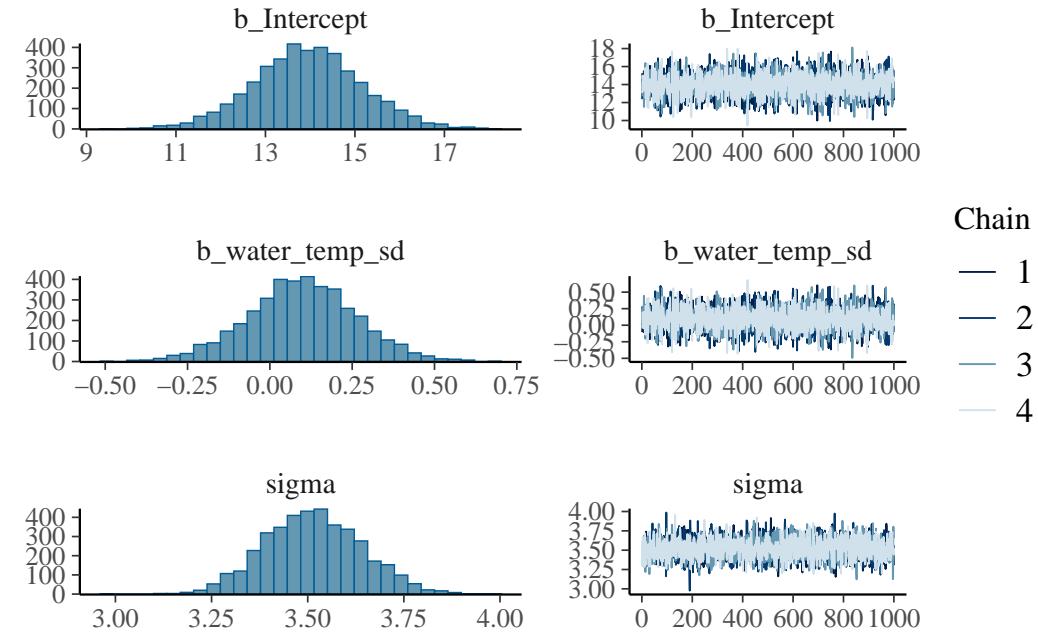
Q1.6) It does not look like size changes with the sd of water temperature. We are moderately confident with this assessment due to the lack of slope in the regression line.

Q1.7)

```
# water temp sd model
m.crab.watersd <-
  brm(data = pie_crab, # Give the model the pie_crab data
       # Choose a gaussian (normal) distribution
       family = gaussian,
       # Specify the model here.
       size ~ water_temp_sd,
       # Here's where you specify parameters for executing the Markov chains
       # We're using similar to the defaults, except we set cores to 4 so the analysis runs faster
       iter = 2000, warmup = 1000, chains = 4, cores = 4,
       # Setting the "seed" determines which random numbers will get sampled.
       # In this case, it makes the randomness of the Markov chain runs reproducible
       # (so that both of us get the exact same results when running the model)
       seed = 4,
       # Save the fitted model object as output - helpful for reloading in the output later
       file = "output/m.crab.watersd")
```

Q1.8) Our model ran correctly because our Rhat is 1 and based on our MCMC graphs, our models all came to the same conclusion.

```
# show posteriors and chains
plot(m.crab.watersd)
```



```
# show summary, including rhat
summary(m.crab.watersd)
```

```
Family: gaussian
Links: mu = identity
Formula: size ~ water_temp_sd
Data: pie_crab (Number of observations: 392)
Draws: 4 chains, each with iter = 2000; warmup = 1000; thin = 1;
       total post-warmup draws = 4000
```

Regression Coefficients:

| | Estimate | Est.Error | l-95% CI | u-95% CI | Rhat | Bulk_ESS | Tail_ESS |
|---------------|----------|-----------|----------|----------|------|----------|----------|
| Intercept | 13.95 | 1.21 | 11.54 | 16.36 | 1.00 | 4569 | 2971 |
| water_temp_sd | 0.10 | 0.16 | -0.23 | 0.42 | 1.00 | 4615 | 2950 |

Further Distributional Parameters:

| | Estimate | Est.Error | l-95% | CI | u-95% | CI | Rhat | Bulk_ESS | Tail_ESS |
|-------|----------|-----------|-------|------|-------|------|------|----------|----------|
| sigma | 3.52 | 0.13 | 3.28 | 3.76 | 1.00 | 3960 | 2894 | | |

Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS and Tail_ESS are effective sample size measures, and Rhat is the potential scale reduction factor on split chains (at convergence, Rhat = 1).

Q1.9)

1. We found that standard deviation has a miniscule effect on body size. With every 1 standard deviation in water temperature, we see an increase of 0.1 mm of carapace width.
2. The effect is not reasonably different than 0 because our confidence interval includes 0 (-0.23 to 0.42).

2. Back to Pikas!

```
head(nwt_pikas)
```

```
# A tibble: 6 x 8
  date      site    station utm_easting utm_northing sex concentration_pg_g
  <date>    <fct>   <fct>        <dbl>        <dbl> <fct>           <dbl>
1 2018-06-08 Cable Ga~ Cable ~       451373     4432963 male            11563.
2 2018-06-08 Cable Ga~ Cable ~       451411     4432985 male            10629.
3 2018-06-08 Cable Ga~ Cable ~       451462     4432991 male            10924.
4 2018-06-13 West Kno~ West K~      449317     4434093 male            10414.
5 2018-06-13 West Kno~ West K~      449342     4434141 male            13531.
6 2018-06-13 West Kno~ West K~      449323     4434273 <NA>             7799.
# i 1 more variable: elev_m <dbl>
```

```
nwt_pikas_doy <- nwt_pikas %>%
  # Add a new column called day_of_year
  # yday extracts the day of year from the date column
  mutate(day_of_year = yday(date)) %>%
  # relocate the day_of_year column after the date column
  relocate(day_of_year, .after = date)
```

```

head(nwt_pikas_doy)

# A tibble: 6 x 9
  date      day_of_year site       station      utm_easting utm_northing sex
  <date>          <dbl> <fct>        <fct>           <dbl>           <dbl> <fct>
1 2018-06-08      159 Cable Gate Cable Gate 1     451373        4432963 male
2 2018-06-08      159 Cable Gate Cable Gate 2     451411        4432985 male
3 2018-06-08      159 Cable Gate Cable Gate 3     451462        4432991 male
4 2018-06-13      164 West Knoll West Knoll 3    449317        4434093 male
5 2018-06-13      164 West Knoll West Knoll 4    449342        4434141 male
6 2018-06-13      164 West Knoll West Knoll 5    449323        4434273 <NA>
# i 2 more variables: concentration_pg_g <dbl>, elev_m <dbl>

```

Q2.1) How does stress vary based on the day of the year?

Q2.2) We expect pika stress to increase as the year progresses. We think think this because as the year progresses, temperature increases making the pikas more stressed.

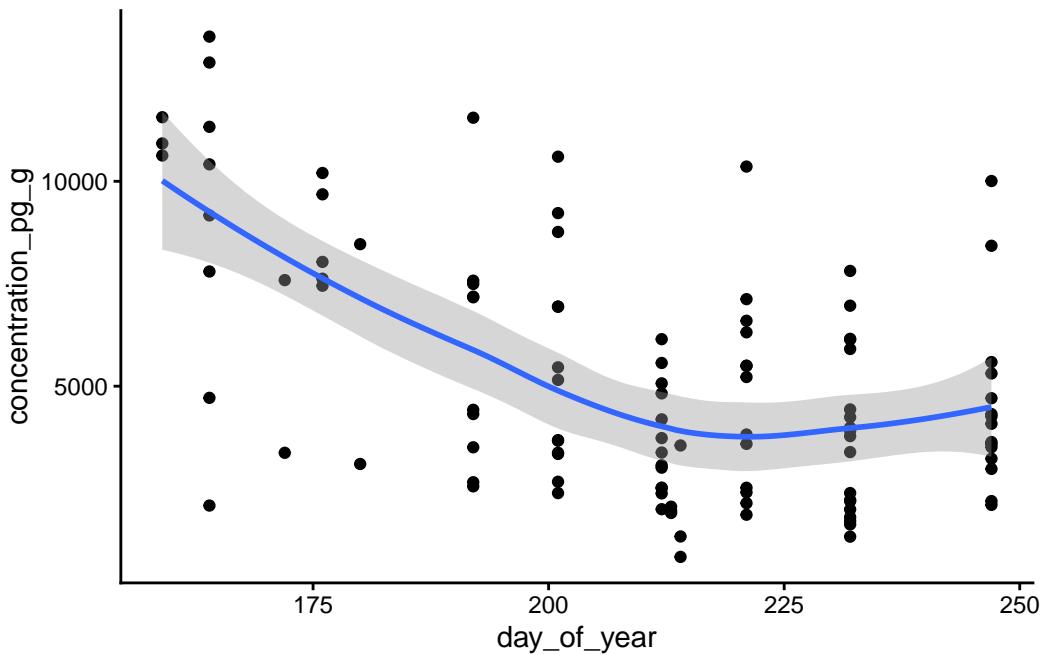
Q2.3)

```

nwt_pikas_doy |>
  ggplot(aes(x = day_of_year, y = concentration_pg_g))+
  geom_point()+
  theme_classic()+
  geom_smooth()

`geom_smooth()` using method = 'loess' and formula = 'y ~ x'

```

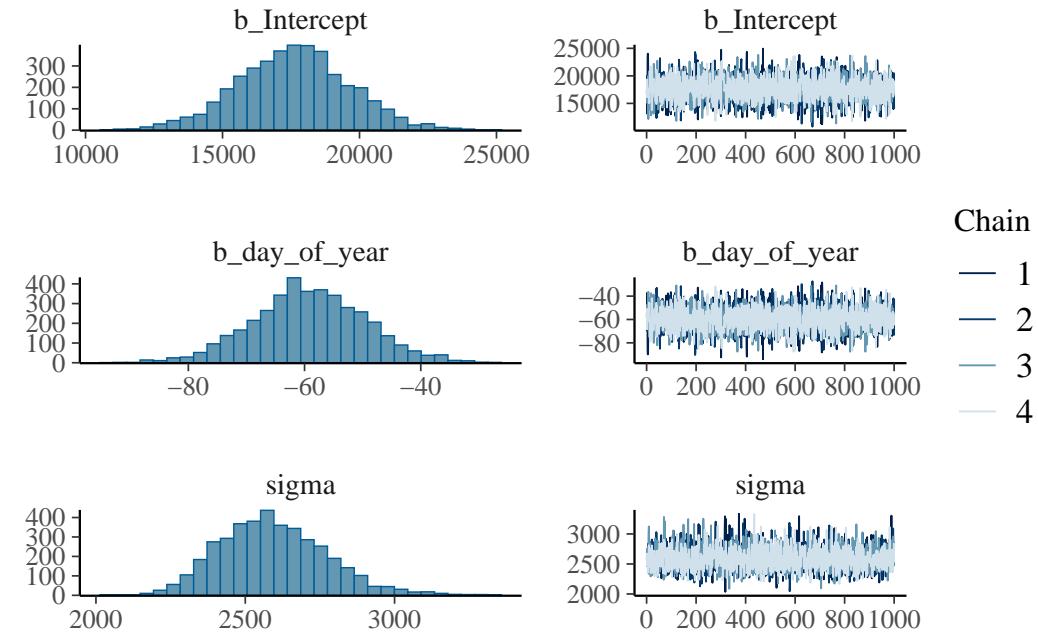


Q2.4)

```
# Pika stress over year model
pika.s.day <-
  brm(data = nwt_pikas_doy,
    # Choose a gaussian (normal) distribution
    family = gaussian,
    # Specify the model here.
    concentration_pg_g ~ day_of_year,
    # Here's where you specify parameters for executing the Markov chains
    # We're using similar to the defaults, except we set cores to 4 so the analysis runs faster
    iter = 2000, warmup = 1000, chains = 4, cores = 4,
    # Setting the "seed" determines which random numbers will get sampled.
    # In this case, it makes the randomness of the Markov chain runs reproducible
    # (so that both of us get the exact same results when running the model)
    seed = 4,
    # Save the fitted model object as output - helpful for reloading in the output later
    file = "output/pika.s.day")
```

Q2.5) We believe the model ran correctly because our Rhat is equal to 1 and our MCMC all overlap.

```
# show posteriors and chains
plot(pika.s.day)
```



```
# show summary, including rhat
summary(pika.s.day)
```

```
Family: gaussian
Links: mu = identity
Formula: concentration_pg_g ~ day_of_year
Data: nwt_pikas_doy (Number of observations: 109)
Draws: 4 chains, each with iter = 2000; warmup = 1000; thin = 1;
       total post-warmup draws = 4000
```

Regression Coefficients:

| | Estimate | Est.Error | 1-95% CI | u-95% CI | Rhat | Bulk_ESS | Tail_ESS |
|-------------|----------|-----------|----------|----------|------|----------|----------|
| Intercept | 17607.56 | 2056.61 | 13452.87 | 21661.70 | 1.00 | 3755 | 2585 |
| day_of_year | -59.17 | 9.73 | -78.41 | -39.66 | 1.00 | 3708 | 2696 |

Further Distributional Parameters:

| | Estimate | Est.Error | 1-95% CI | u-95% CI | Rhat | Bulk_ESS | Tail_ESS |
|-------|----------|-----------|----------|----------|------|----------|----------|
| sigma | 2594.85 | 180.48 | 2282.99 | 2985.71 | 1.00 | 3668 | 2754 |

Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS and Tail_ESS are effective sample size measures, and Rhat is the potential scale reduction factor on split chains (at convergence, Rhat = 1).

Q2.6)

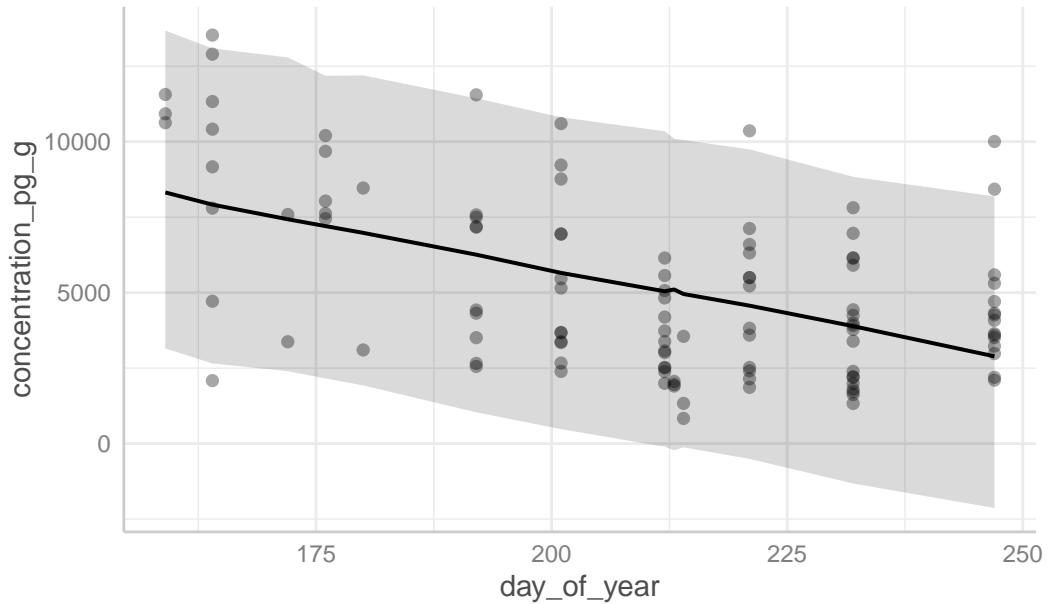
1. For every 1 day increase, there is a -59.17 picogram per gram (parts per trillion) concentration change in Pika stress.
2. Our effect is reasonably different than 0 because our confidence interval doesn't include 0 (-78.41, -39.66).

Q2.7) Prediction Interval

```
# prediction interval. this shows uncertainty in the data around the average response.
pred.pika.day <- predict_response(pika.s.day, interval = 'prediction')
plot(pred.pika.day, show_data = TRUE)
```

Data points may overlap. Use the `jitter` argument to add some amount of random variation to the location of data points and avoid overplotting.

Predicted values of concentration_pg_g



Q2.8) We found a decrease of (-)59.17 picogram per gram of stress concentration per one additional day of the year. Since our 95% credible intervals does not include 0 (-78.41, -39.66), this suggests that given our model, Pika stress decreases as the year progresses.