

1.

| | | | |
|--------|---------------|---------------|---------------|
| y | 1 | 2 | 5 |
| $f(y)$ | $\frac{1}{5}$ | $\frac{2}{5}$ | $\frac{2}{5}$ |

2.

(1)

| | | | | | | |
|--------|----------------|----------------|----------------|-----------------|----------------|----------------|
| w | -2 | 1 | 3 | 4 | 6 | 9 |
| $f(w)$ | $\frac{2}{31}$ | $\frac{5}{31}$ | $\frac{1}{31}$ | $\frac{10}{31}$ | $\frac{4}{31}$ | $\frac{9}{31}$ |

(2)

| | | |
|--------|-----------------|-----------------|
| z | -1 | 0 |
| $f(z)$ | $\frac{17}{31}$ | $\frac{14}{31}$ |

$$E(z) = -\frac{17}{31}$$

3.

| | | | | | | | |
|--------|----------------|-----------------|-----------------|-----------------|----------------|----------------|----------------|
| w | -2 | -1 | 0 | 1 | 2 | 3 | 4 |
| $f(w)$ | $\frac{5}{60}$ | $\frac{14}{60}$ | $\frac{23}{60}$ | $\frac{12}{60}$ | $\frac{1}{60}$ | $\frac{2}{60}$ | $\frac{3}{60}$ |

4.

$$f_Y(y) = \frac{y-1}{4} |2y-5|, \quad y = 1, \frac{3}{2}, 2, \frac{5}{2}, 3$$

5.

$$\therefore f_Y(y) = \frac{1}{2\sqrt{y}}, 0 < y < 1$$

6.

$$f_U(u) = \begin{cases} u, & 0 \leq u \leq 1 \\ 2-u, & 1 < u \leq 2 \end{cases}$$

7.

$$f(y_1, y_2) = \frac{2y_2}{y_1}, \quad 0 < y_2 < y_1, 0 < y_1 y_2 < 1$$

8.

$$f_Y(y) = 8(y-1), 1 < y \leq \frac{3}{2}$$

9.

$$f_Y(y) = \lambda e^{-\lambda y}, \quad y > 0$$

10.

$$f(y) = \begin{cases} \frac{e^{-\sqrt{y}}}{2\sqrt{y}}, & y > 0 \\ 0, & o.w. \end{cases}$$

11.

$$(1) f_Y(y) = \frac{y-\beta}{4\alpha^2} e^{-\frac{y-\beta}{2\alpha}}, y > \beta$$

$$(2) f_Z(z) = \frac{1}{4z\sqrt{z}} \ln z, z > 1$$

$$(3) f_Y(y) = \frac{1}{4y^3} e^{-\frac{1}{2y}}, y > 0$$

$$(4) f_Z(z) = \frac{z^3}{2} e^{-\frac{z^2}{2}}, z > 0$$

12.

| | | | | | |
|--------|---|---------------|---------------|---------------|---------------|
| y | 1 | $\frac{3}{2}$ | 2 | $\frac{5}{2}$ | 3 |
| $f(y)$ | 0 | $\frac{2}{8}$ | $\frac{2}{8}$ | 0 | $\frac{4}{8}$ |

13.

(1)

| | | |
|----------|---------------|---------------|
| z_1 | 0 | 1 |
| $f(z_1)$ | $\frac{2}{6}$ | $\frac{4}{6}$ |

(2)

| | | | | | |
|-----------|----------------|----------------|-----------------|----------------|-----------------|
| z_2 | -1 | -2 | 0 | 1 | 2 |
| $f(x, y)$ | $\frac{2}{42}$ | $\frac{5}{42}$ | $\frac{14}{42}$ | $\frac{6}{42}$ | $\frac{15}{42}$ |

(3)

| | | | |
|--|---------------|---------------|---------------|
| $\begin{matrix} x \\ z_1 \end{matrix}$ | -1 | 0 | 1 |
| 0 | 0 | $\frac{2}{6}$ | 0 |
| 1 | $\frac{1}{6}$ | 0 | $\frac{3}{6}$ |

14.

| | | | |
|--------------------------------------|---------------|---------------|---------------|
| $\begin{matrix} y \\ z \end{matrix}$ | 0 | 1 | 4 |
| -1 | 0 | $\frac{1}{3}$ | 0 |
| 0 | $\frac{1}{6}$ | 0 | 0 |
| 1 | 0 | $\frac{1}{6}$ | 0 |
| 8 | 0 | 0 | $\frac{1}{3}$ |

15.

| | | | | |
|--------------|---------------|---------------|---------------|---------------|
| $ x - y $ | 3 | 1 | 1 | 3 |
| $f(x - y)$ | $\frac{1}{8}$ | $\frac{3}{8}$ | $\frac{3}{8}$ | $\frac{1}{8}$ |

16.

$$f(u, v) = \frac{1}{4}uv, \quad 0 < u < 2, 0 < v < 2$$

17.

$$\therefore f(z) = \begin{cases} z, & 0 < z \leq 1 \\ 2 - z, & 1 < z < 2 \end{cases}$$

18.

$$f(w) = \int_0^{\infty} ze^{-z} dz = 1, \quad 0 \leq w \leq 1$$

19.

$$f(y) = \frac{1}{8}, \quad -2 < y < 6$$

20.

$$f(y) = \begin{cases} \frac{\sqrt{y}}{6}, & 0 \leq y < 1 \\ \frac{\sqrt{y}}{3}, & 1 \leq y \leq 4 \\ 0, & o.w. \end{cases}$$

21.

$$f(y) = \frac{1}{2\sqrt{y-b}\sqrt{a}} f_x\left(\sqrt{\frac{y-b}{a}}\right), \quad y > b \circ$$

22.

$$\therefore f(u) = \frac{5}{64}u^{2.5}, \quad 0 < u < 4$$

23.

$$\therefore f(y_1, y_2) = y_1 e^{-y_1}, \quad 0 \leq y_1 < \infty, 0 \leq y_2 \leq 1$$

24.

$$f(w) = \begin{cases} 1+w, & -1 \leq w < 0 \\ 1-w, & 0 \leq w \leq 1 \end{cases}$$