HW Week 1

JLaw

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library(rethinking)

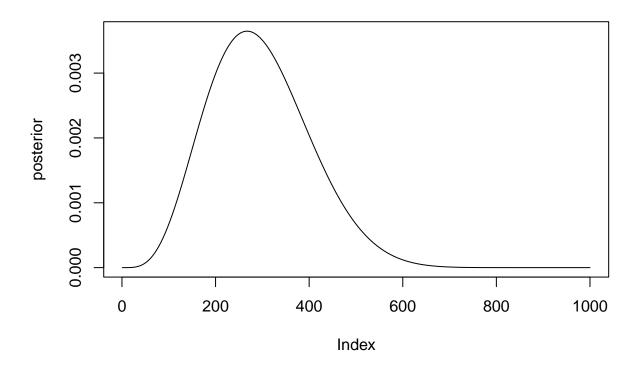
Week 1 Homework

HW1 Questions

Q1:

Suppose the globe tossing data (Chapter 2) had turned out to be 4 water in 15 tosses. Construct the posterior distribution using grid approximation. Use the same flat prior as before.

```
#Compute values of P to try
p_grid <- seq(0, 1, length.out = 1000)
# Define the Prior
prob_p <- rep(1, 1000)
# Define the likelihood for each value of P from the Grid
prob_data <- dbinom(x = 4, size = 15, prob = p_grid)
# Calculate Posterior
posterior <- prob_p * prob_data
# Normalize Posterior
posterior <- posterior / sum(posterior)</pre>
plot(posterior, type = 'l')
```

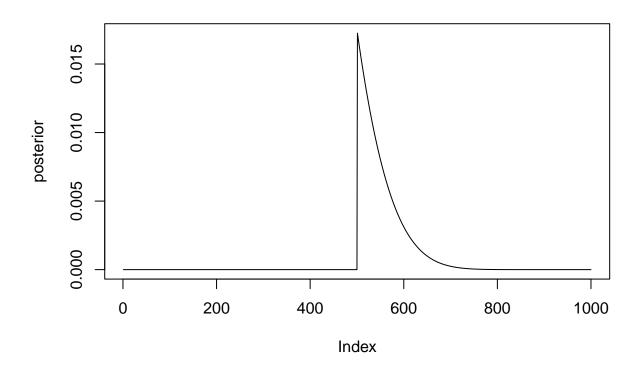


Q2:

Start over in 1, but now use a prior that is zero below p = 0.5 and constant above p = 0.5. The corresponds to prior information that a majority of the Earth's surface is water. What difference does a better prior makes?

```
#Compute values of P to try
p_grid <- seq(0, 1, length.out = 1000)
# Define the Prior
prob_p <- ifelse(p_grid < .5, 0, 1)
# Define the likelihood for each value of P from the Grid
prob_data <- dbinom(x = 4, size = 15, prob = p_grid)
# Calculate Posterior
posterior <- prob_p * prob_data
# Normalize Posterior
posterior <- posterior / sum(posterior)

plot(posterior, type = 'l')</pre>
```



Q3:

For the posterior distribution of 2, compute 89% percentile and HPDI intervals. Compare the widths of these intervals. Which is wider, why? If you had only the information in the interval, what might you misunderstand about the sape of the posterior distribution?

```
#Get Posterior Samples
samples <- sample(p_grid, size = 1000, replace = TRUE, prob = posterior)

#89th Percentile Credible Intervals with Equal Tails
PI(samples, prob = .89)

## 5% 94%
## 0.5035035 0.6327427

#89th Percentile Highest Posterior Dentist
HPDI(samples, prob = .89)

## | 0.89 0.89|
## | 0.5005005 0.6086086
```