nat La(p,x) XS Review

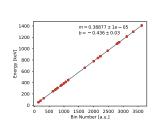
Jonathan Morrell

November 28, 2017

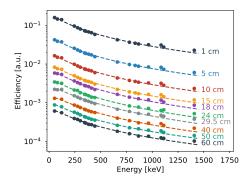
Methodology

- Detector calibration
- Peak fitting
- Verify $T_{1/2}$
- Determining beam current and energies
- Generate cross-sections
- Compare results to EXFOR, TALYS and EMPIRE

Calibration



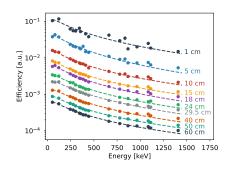
$$E = m \cdot i + b$$

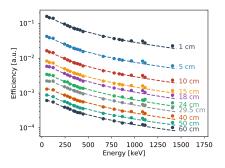


$$\epsilon(E) = \exp[a \cdot \ln(E)^2 + b \cdot \ln(E) + c]$$

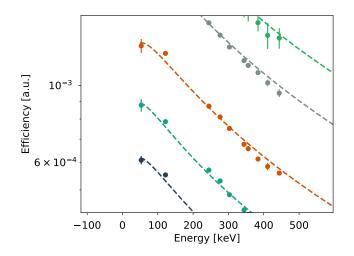


Normalizing to 137 Cs and 54 Mn





Efficiency Turnaround Region



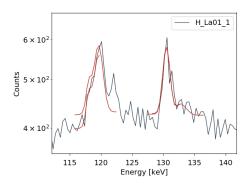
Peak Fitting

Fit to
$$P(i) = A \cdot e^{-\frac{(i-\mu)^2}{2\sigma^2}} + m \cdot i + b$$

where i is bin $\#$.
 $N = \sqrt{2\pi}\sigma A$

$$N(130.4keV) = 577 \pm 135,$$

 $(\chi^2_{\nu} = 22.13)$



Cross-section Equations

$$\begin{array}{l} A_0 = \frac{\lambda N_c}{(1 - e^{-\lambda t_m})e^{-\lambda t_c} I_{\gamma^c}} \\ A_0 = \sigma I_p \rho \Delta r (1 - e^{-\lambda t_i}) \end{array}$$

 A_0 : End-of-beam activity t_m : Measurement time t_c : Cooling time t_i : Irradiation time l_p : Beam current

 $\rho\Delta r$: Areal density

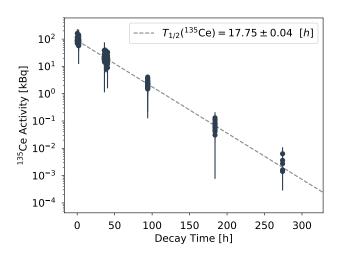
Calculating A_0

$$\begin{split} N(130.4keV) &= 577 \pm 135 \\ I_{\gamma} &= 0.209\%, \ \epsilon(1cm, 130.4keV) = 0.095 \\ \lambda &= 2.53E - 06s^{-1}, \ t_m = 8603s, \\ t_c &= 6.62E05s \\ A_0 &= \frac{\lambda N_c}{(1 - e^{-\lambda t_m})e^{-\lambda t_c}I_{\gamma}\epsilon} \\ A_0 &= \frac{2.53E - 06s^{-1}577}{(1 - e^{-2.53E - 06s^{-1}8603s})e^{-2.53E - 06s^{-1}6.62E05s}0.00209 \cdot 0.095} \\ A_0 &= 1822.9s^{-1} = 1.82kBq \end{split}$$

 A_0 : End-of-beam activity t_m : Measurement time t_c : Cooling

time

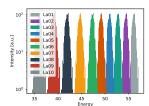
Verifying $T_{1/2}$ of fits



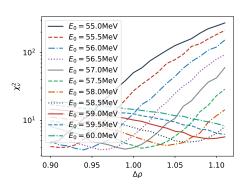
Accepted $T_{1/2} = 17.7 \pm 0.3 h$.



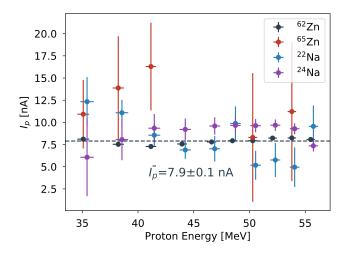
Determining Beam Current



Optimum E_0 and $\Delta \rho$ determined by χ^2 minimization using Anderson and Ziegler

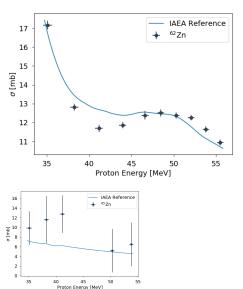


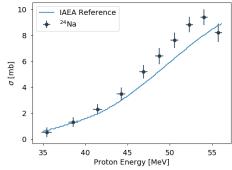
Optimized Beam Current

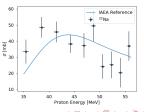


Optimum values of E_0 and $\Delta \rho$: 57.0 MeV, 0.99

Monitor Cross-Sections

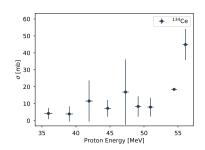




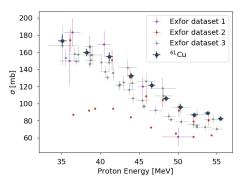


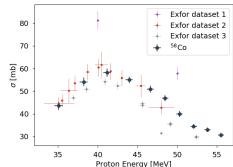
Calculating Cross-Section

$$\begin{split} \sigma &= \frac{A_0}{I_p \rho \Delta r (1 - e^{-\lambda t_i})} \\ I_p &= 7.9 nA = 4.93 E 10 s^{-1}, \ \rho \Delta r = \\ 14.6 mg/cm^2 &= 6.32 E - 08 mb^{-1}, \\ t_i &= 5844 s, \ \lambda = 2.53 E - 06 s^{-1} \ \text{and} \\ A_0 &= 1.82 k B q \\ \sigma &= \frac{1822.9}{4.93 E 106.32 E - 08 (1 - e^{-2.53 E - 06 s^{-1}.5844 s})} \\ \sigma &= 39.86 mb \end{split}$$

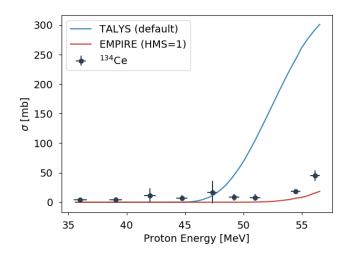


Verifying Method with EXFOR Data

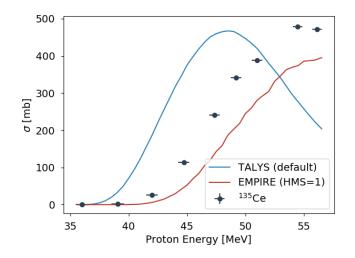




Comparison to TALYS, EMPIRE

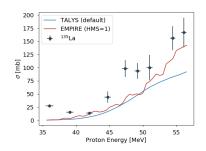


¹³⁵Ce Cross-Section

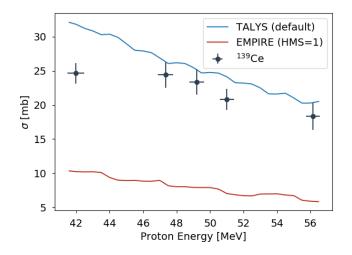


Daughter Nuclide Cross-Sections

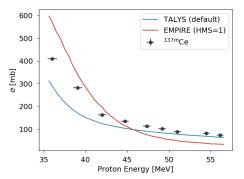
From 1^{st} Batemann eqn. $N_D(t) = N_{p0} \frac{\lambda_p}{\lambda_D - \lambda_p} (e^{-\lambda_p t} - e^{-\lambda_D t}) + N_{D0} e^{-\lambda_D t}$ Rewrite for activity: $A_D(t) = A_{p0} \frac{\lambda_D}{\lambda_D - \lambda_p} (e^{-\lambda_p t} - e^{-\lambda_D t}) + A_{D0} e^{-\lambda_D t}$ So initial daughter activity is $A_{D0} = A_D(t) - A_{p0} \frac{\lambda_D}{\lambda_D - \lambda_p} (e^{-(\lambda_p - \lambda_D)t} - 1)$ Here t is cooling time (previously t_c)

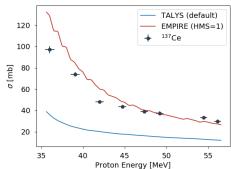


¹³⁹Ce Cross-Section

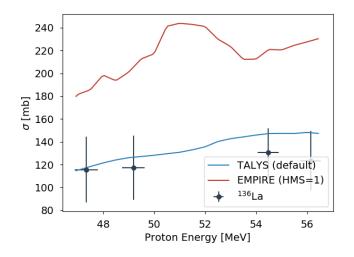


^{137m}Ce and ¹³⁷Ce Cross-Sections

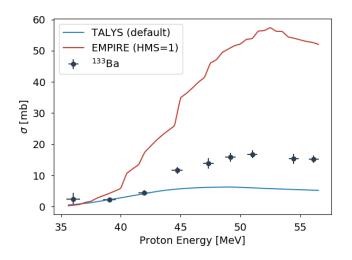




¹³⁶La Cross-Section



¹³³Ba Cross-Section



¹³²Cs Cross-Section

