Chapter 2, Problem 2.7

James Topor February 8, 2016

2.7 Swing voters. A 2012 Pew Research survey asked 2,373 randomly sampled registered voters their political affiliation (Republican, Democrat, or Independent) and whether or not they identify as swing voters. 35% of respondents identified as Independent, 23% identified as swing voters, and 11% identified as both.⁵⁸

- (a) Are being Independent and being a swing voter disjoint, i.e. mutually exclusive?
- (b) Draw a Venn diagram summarizing the variables and their associated probabilities.
- (c) What percent of voters are Independent but not swing voters?
- (d) What percent of voters are Independent or swing voters?
- (e) What percent of voters are neither Independent nor swing voters?
- (f) Is the event that someone is a swing voter independent of the event that someone is a political Independent?

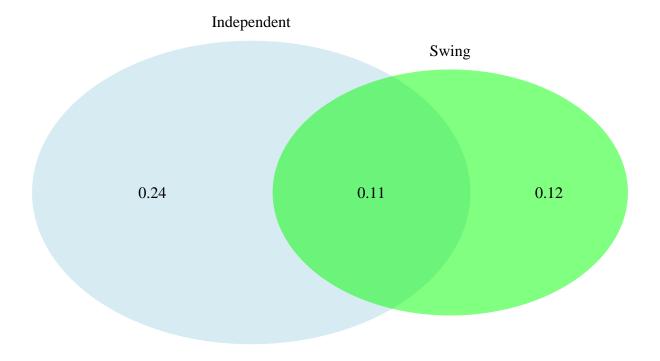
a) Are being Independent and being a swing voter disjoint, i.e. mutually exclusive?

No they are not disjoint since 11% of voters identify as both independent and swing voters.

b) Draw a Venn diagram summarizing the variables and their associated probabilities.

Loading required package: grid

Loading required package: futile.logger



(polygon[GRID.polygon.1], polygon[GRID.polygon.2], polygon[GRID.polygon.3], polygon[GRID.polygon.4],

c) What percent of voters are Independent but not swing voters?

We are told that 35% of voters are independent, and 11% of voters identify as both independent AND swing voters. Therefore, the percentage of voters that are independent but not swing voters is:

$$.35 - .11 = .24 = 24\%$$

d) What percent of voters are Independent or swing voters?

We are told that 35% of voters are Independent, 23% are swing voters, and 11% identify as both Independent AND swing. Therefore, the percentage of voters that are Independent OR swing voters is:

$$.35 + .23 - .11 = .47 = 47\%$$

e) What percent of voters are neither Independent nor swing voters?

The percentage of voters that are neither independent nor swing voters is the **complement** of the percentage of voters that are EITHER independent or swing, which we calculated in our answer to part **d**) above as 47%. Therefore, we can simply subtract .47 from 1 to find our answer:

$$1 - .47 = .53 = 53\%$$

f) Is the event that someone is a swing voter independent of the event that someone is a political Independent?

No since there is overlap between the two groups. As we're told, 11% of voters identify as both independent and swing.

We can also show this mathematically by testing for equivalence of P(A) * P(B) = P(A, B) where P(A) is the probability of being independent and P(B) is the probability of being a swing voter:

- P(Independent) = .35 = P(A)
- P(Swing) = .23 = P(B)
- P(A) * P(B) = .35 * .23 = 0.0805
- P(A,B) = .11 (given to us in text)

As we can see, (P(A) * P(B) = .0805)! = (P(A, B) = .11) so these events are NOT independent.