

hw2

February 25, 2025

1 Homework 2

1.1 Artificial Intelligence For Robotics

1.1.1 Julian Torres

2 1) Problem 7.7

2.0.1 a) sentence is false iff B and C are false. happens in 4 cases for A and D. $\rightarrow 12$

2.0.2 b) False only if A,B,C,D are false, which occurs in 1 case $\rightarrow 15$

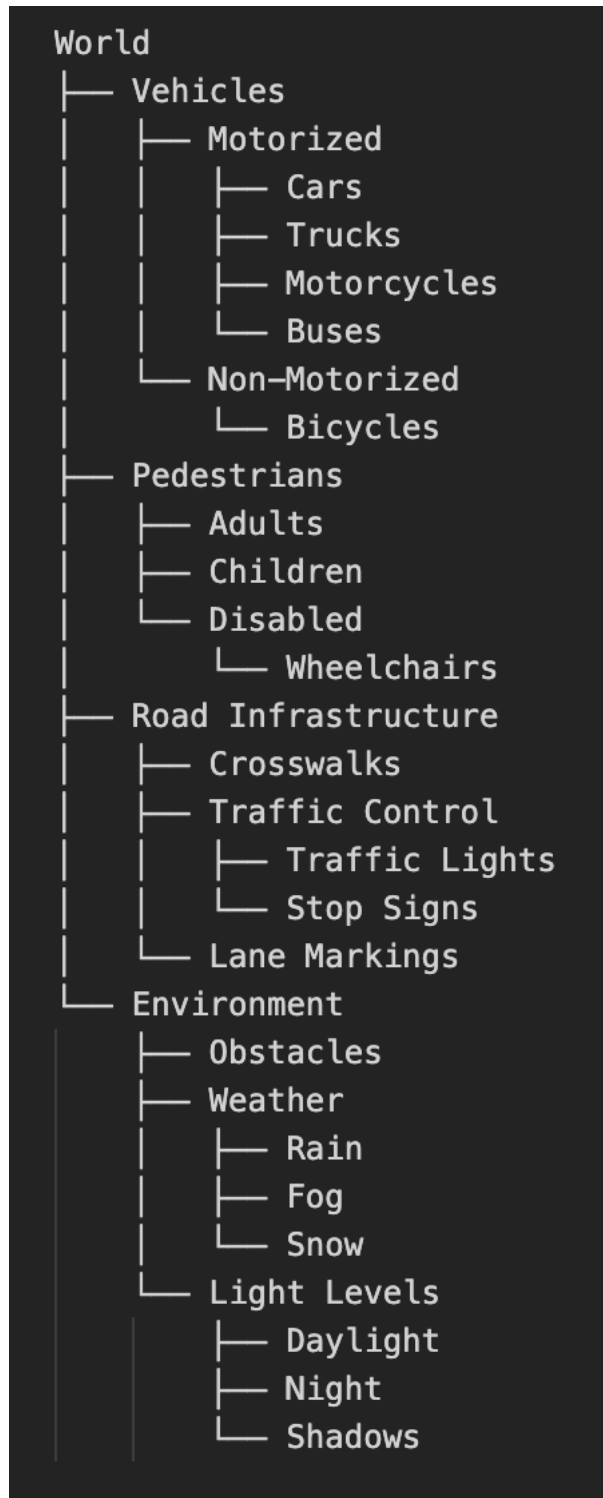
2.0.3 c) gives a model in which the first conjunct is false $\rightarrow 0$

3 2)

Objects

- Vehicles: cars, trucks, motorcycles, buses, etc.
- Pedestrians: adults, children, disabled individuals
- Road Infrastructure: crosswalks, traffic lights, stop signs, lane markings
- Environment: Obstacles, weather conditions, daytime light levels

Taxonomic Tree



Events

1. Vehicle Approaching:
 - Detect vehicles approaching the crosswalk.

- Estimate the speed and trajectory of vehicles.
-

3.1 Identify if vehicles are likely to stop or pose a threat to pedestrians.

2. Pedestrian Waiting to Cross:

- Identify pedestrians waiting at the crosswalk.
-

3.2 Classify types of pedestrians (e.g., children, disabled).

3. Crosswalk Clearance:

- Monitor the crosswalk to ensure that it is clear of obstacles and pedestrians.
-

3.3 Signal when it is safe for pedestrians to cross.

4. Traffic Light State Change:

- Detect changes in the state of traffic lights.
-

3.4 Adjust crossing signals and timing based on the traffic light state.

5. Pedestrian Crossing:

- Monitor pedestrians while they are crossing the road.
-

3.5 Identify any hazards or sudden changes in pedestrian behavior.

6. Emergency Situations:

- Detect emergency vehicles and respond accordingly (e.g., halting pedestrian crossings temporarily).
-

3.6 Respond to sudden obstacles or accidents in the crosswalk area.

7. Weather Changes:

- Detect weather conditions that may impact visibility or safety.
- Adapt behavior based on weather (e.g., allow extra time for pedestrians to cross during rain).

4 3)

4.1 i. $A \wedge B$

4.2 ii. $A \implies B$

4.3 iii. $(S \implies W) \wedge (W \implies S)$

4.4 iv. $(\text{dry} \wedge \text{raining outside}) \implies (\text{have umbrella} \vee \text{have hoodie}) \wedge \neg \text{raining heavily}$

v. $\neg (\text{student handed homework late or incomplete} \implies \text{the student will not lose points})$

5 4)

A is true if and only if it is not the case that A, B, and C are all true

6 5)

6.0.1 Translation of English Sentences into First-Order Logic (Markdown Format)

vi. **Some students pass English but not Math.**

Let:

- $(S(x))$: (x) is a student.
- $(P_E(x))$: (x) passes English.
- $(P_M(x))$: (x) passes Math.

$$\exists x (S(x) \wedge P_E(x) \wedge \neg P_M(x))$$

vii. **Every student is registered in a class and enrolled at a university.**

Let:

- $(S(x))$: (x) is a student.
- $(R(x))$: (x) is registered in a class.
- $(E(x))$: (x) is enrolled at a university.

$$\forall x (S(x) \implies (R(x) \wedge E(x)))$$

viii. **If someone is an aunt or uncle, then someone must be their niece or nephew.**

Let:

- $(A(x))$: (x) is an aunt.
- $(U(x))$: (x) is an uncle.
- $(N(y, x))$: (y) is a niece or nephew of (x) .

$$\forall x ((A(x) \vee U(x)) \implies \exists y N(y, x))$$

ix. The old that is strong does not wither.

Let:

- ($O(x)$): (x) is old.
- ($S(x)$): (x) is strong.
- ($W(x)$): (x) withers.

$$\forall x ((O(x) \wedge S(x)) \implies \neg W(x))$$

7 6)

7.0.1 10.2

Fly(P1, JFK, SFO) Fly(P1, JFK, JFK) Fly(P2, SFO, JFK) Fly(P2, SFO, SFO)

7.0.2 10.9

- negative effects happen in S1, they are mutex with their positive counterparts
- **Fly** and **Load** actions are possible at A0
- planes can fly even if they are empty

8 7)

8.1

a)
town
mark-
ers,
road
sym-
bols,
mon-
u-
ments,
wa-
ter,
high-
ways

b)

8.1

a)
town
mark-
ers,
road
sym-
bols,
mon-
u-
ments,
wa-
ter,
high-
ways

Explicit

1.
The
city
of
Boston
is lo-
cated
at co-
ordi-
nates
(42.3601,
-
71.0589).
2.
There
is a
road
con-
nect-
ing
City
A
and
City
B. 3.
City
X is
lo-
cated
north
of
City
Y.

8.1

a)
town
mark-
ers,
road
sym-
bols,
mon-
u-
ments,
wa-
ter,
high-
ways

Implicit

1.
City
A is
east
of
City
B. 2.
There
is a
path
from
City
X to
City
Z via
City
Y. 3.
The
dis-
tance
be-
tween
Point
P
and
Point
Q is
greater
than
the
dis-
tance⁷
be-
tween
Point

8.1

a)
town
mark-
ers,
road
sym-
bols,
mon-
u-
ments,
wa-
ter,
high-
ways

8.0.1 c)

1. Cultural/Historical significance of locations (i.e. Gettysburg)
2. Demographic Information
3. Climate

8.1 8.6

8.1.1 a) Valid

8.1.2 b) Valid

8.1.3 c) Valid

9 8)

10 A CSP-Based Integrated Task and Motion Planning for Assembly Robots

This document explains how to formulate and solve a task and motion planning problem for assembly robots using a Constraint Satisfaction Problem (CSP) approach, as discussed in “CSP-Based Integrated Task & Motion Planning for Assembly Robots.”

10.1 1. Formulating Task and Motion Planning as a CSP

A CSP for assembly robots can be defined as a triple $(\mathbf{X}, \mathbf{D}, \mathbf{C})$ where: - \mathbf{X} : Set of variables representing different aspects of the robot and assembly process. - \mathbf{D} : Set of domains specifying possible values for each variable - \mathbf{C} : Set of constraints that define valid relationships between variables.

10.1.1 Variables (X)

Key variables include: - **loc**: Represents the configuration of each arm (such as left arm, right arm) over time. - **slotOcc**: Represents which part occupies which slot. - **pos**: Represents the location of each part (e.g., held by an arm or placed in a specific slot).

10.2 2. Domains (D)

- **loc**: All possible configurations for each arm.
 - **slotOcc**: A set of possible parts or an empty value for each slot.
 - **pos**: All possible locations for each part (e.g., in a slot or held by a gripper).
-

10.3 3. Constraints (C)

These constraints ensure that the task and motion planning are valid: - **State Constraints**: Define allowable configurations of the robot to prevent collisions. - **Initial State Constraints**: Define the starting conditions of the robot and the assembly process. - **Goal Constraints**: Define the desired final state, such as all workpieces being assembled. - **Dynamic Constraints**: Ensure that transitions between successive states are valid (e.g., ensuring collision-free movement).

Ex):

```
constraint forall(c in Cells, r in Arms)(  
  blocking(c, loc(r))  occupant(c) == r  
);
```

4. Cost Function

Should be defined such that it minimizes metrics such as execution time and energy expended
Ex)

“minimize

```
cost = |Arms| * k^2 + sum(t in 1..(k-1), r in Arms)(  
  if loc[r][t] != loc[r][t-1] then 1 else 0 endif  
);  
“
```

where k is number of steps, loc[r][t] is location of arm r at time t,

10.4 5. Designing a CSP Solver

First, I would define the structure of a CSP with the following components:

- **Variables**: The entities that need to be assigned values.
- **Domains**: The set of possible values for each variable.
- **Constraints**: Rules that specify which value combinations are allowed.

I would also implement a class that holds the CSP's variables, domains, and constraints, with methods to:

- Add constraints.

- Check consistency for variable assignments.
- Perform backtracking search for a solution.

Here is partially implemented code that uses the github repo as a reference

```
from abc import ABC, abstractmethod
from typing import Dict, List, Generic, TypeVar

V = TypeVar('V') # Variable type
D = TypeVar('D') # Domain type

class AbstractConstraint(Generic[V, D], ABC):
    def __init__(self, variables: List[V]) -> None:
        self.variables = variables

    @abstractmethod
    def satisfied(self, assignment: Dict[V, D]) -> bool:
        ...

class CSP(Generic[V, D]):
    def __init__(self, variables: List[V], domains: Dict[V, List[D]]) -> None:
        self.variables = variables
        self.domains = domains
        self.constraints = {var: [] for var in variables}

    def add_constraint(self, constraint: AbstractConstraint[V, D]) -> None:
        for variable in constraint.variables:
            self.constraints[variable].append(constraint)

    def consistent(self, variable: V, assignment: Dict[V, D]) -> bool:
        return all(constraint.satisfied(assignment) for constraint in self.constraints[variable])

    def backtracking_search(self, assignment: Dict[V, D] = {}) -> Optional[Dict[V, D]]:
        if len(assignment) == len(self.variables):
            return assignment

        unassigned = [v for v in self.variables if v not in assignment]
        first = unassigned[0]

        for value in self.domains[first]:
            local_assignment = assignment.copy()
            local_assignment[first] = value
            if self.consistent(first, local_assignment):
                result = self.backtracking_search(local_assignment)
                if result is not None:
                    return result
        return None

class UniqueConstraint(AbstractConstraint):
    def __init__(self, variables):
```

```
super().__init__(variables)

def satisfied(self, assignment):
    values = list(assignment.values())
    return len(values) == len(set(values))
```