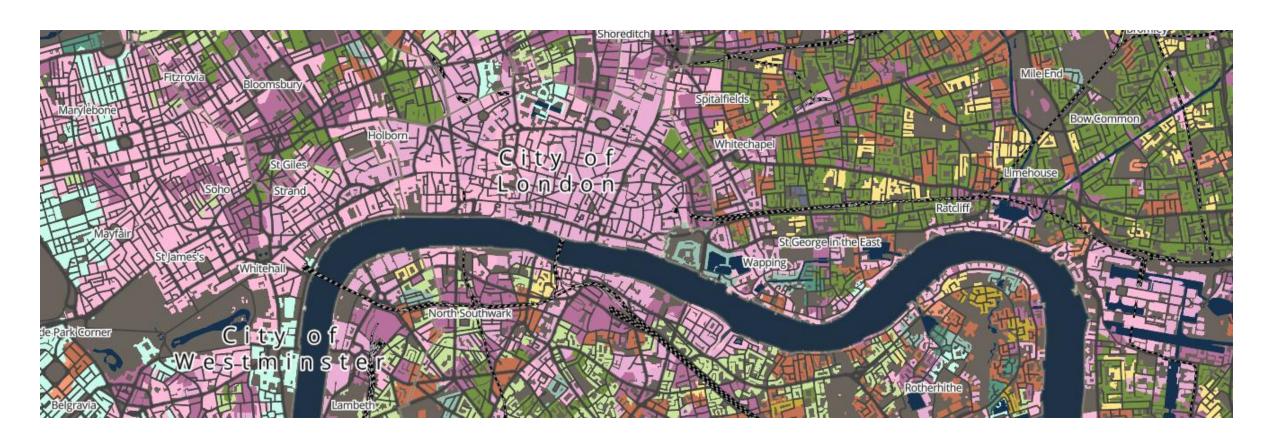
# Geocomputation Spatial Autocorrelation





#### This week

- Spatial dependence.
- Measuring spatial autocorrelation.
- Spatial weights matrix.

# Spatial dependence

### Spatial dependence

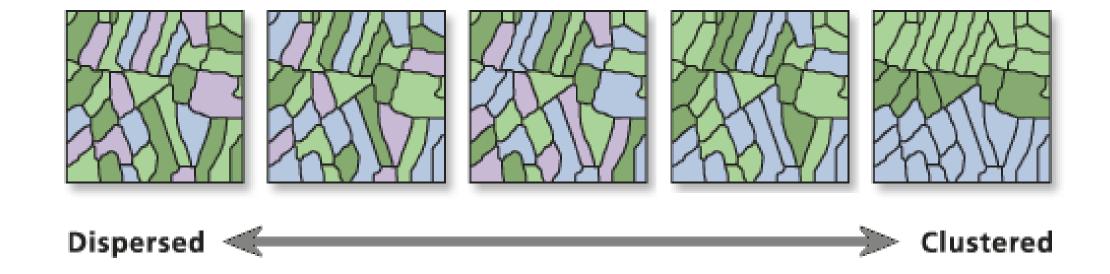
"Everything is related to everything else, but near things are more related than distant things."

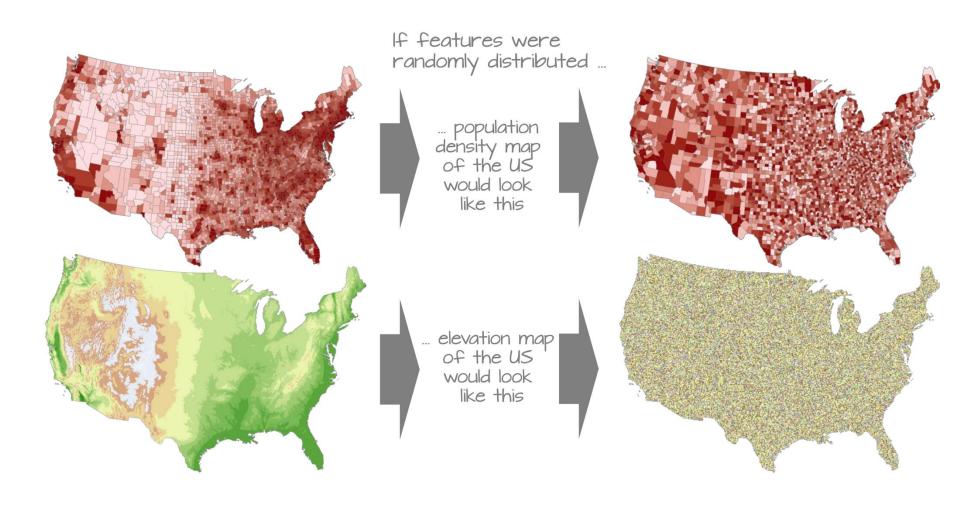
Walter Tobler 1970

### Spatial dependence

- Spatial dependence refers to the concept that the value of a variable at one location is influenced, to some extent, by the value of the same variable at nearby locations.
- This is often understood through the concept of distance decay, where the influence decreases as distance increases.
- Spatial dependence is a key principle in various geographical applications, such as spatial interpolation and spatial interaction modeling.

- Measurement of spatial autocorrelation is the idea of formalising spatial dependency: measuring the degree to which similar values cluster together in space.
- By measuring spatial autocorrelation, we try to identify hotspots where high values are concentrated versus areas where low values are concentrated.
- Spatial Autocorrelation indicates the absence of Complete Spatial Randomness (CSR).
- CSR suggests that a pattern is entirely the result of random chance, with no underlying spatial structure.





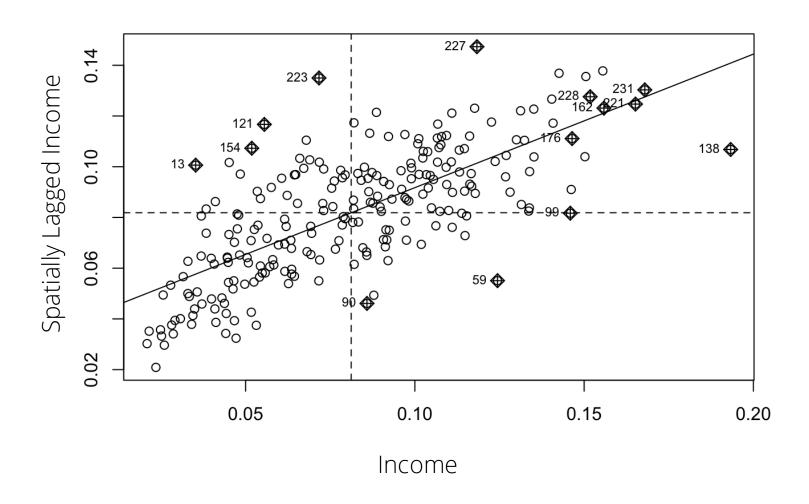
Gimond, M. 2021. Intro to GIS and Spatial Analysis. [online] https://mgimond.github.io/Spatial/introGIS.html

Spatial Autocorrelation can be measured in two ways:

- 1) Global Spatial Autocorrelation: This assesses the overall spatial dependence across the entire dataset.
- Local Spatial Autocorrelation: This focuses on the differences between each unit of analysis and its neighbors.

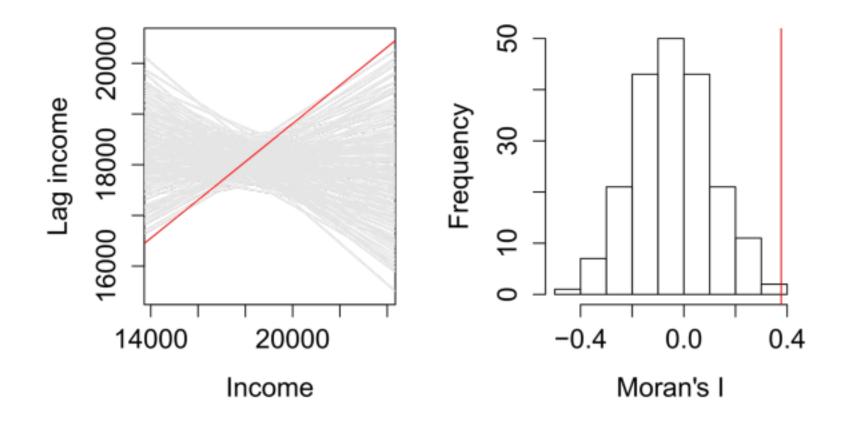
# Global spatial autocorrelation

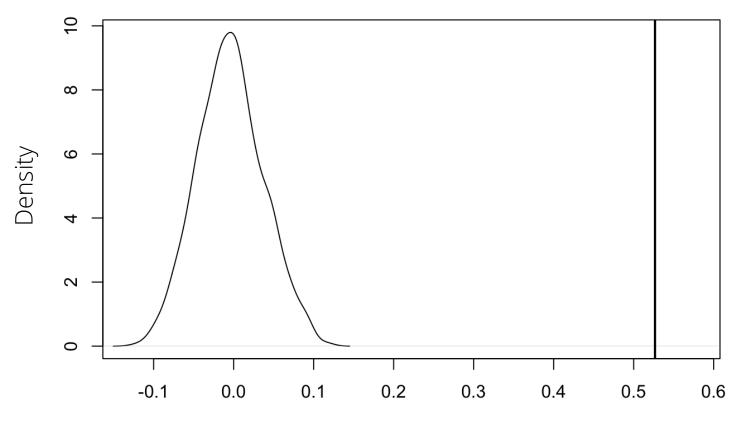
- Moran's I: The most commonly used indicator of global spatial autocorrelation.
- Identifies neighbours for each target feature (e.g. polygon) and summarises their values by computing their means to create a spatially lagged variable value.
- Plots the target feature's value against its spatially lagged mean value and fits a linear model to the points.
- The slope of the fitted line ( $\beta$  estimate) is the Moran's I statistic.



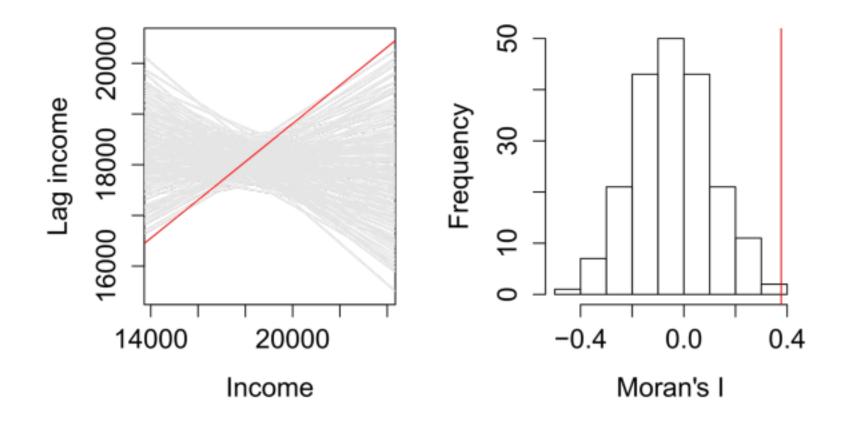
- The Moran's I statistic typically ranges from -1 to +1:
  - +1 Indicates perfect clustering (positive spatial autocorrelation).
  - **0** Suggests a random pattern (no spatial autocorrelation).
  - -1 Indicates perfect dispersion (negative spatial autocorrelation).
- How to assess the significance of the relationship?

- To understand whether our relationship is significant, we can use either an analytical approach or a computational approach. The latter is the preferred option as it does not require making any assumption about the shape and layout of our data set for this we can use a Monte Carlo test.
- This approach randomly and repeatedly assigns values to polygons in the data set.
- The output is a sampling distribution of Moran's I values under the (null) hypothesis that attribute values are randomly distributed across the study area.



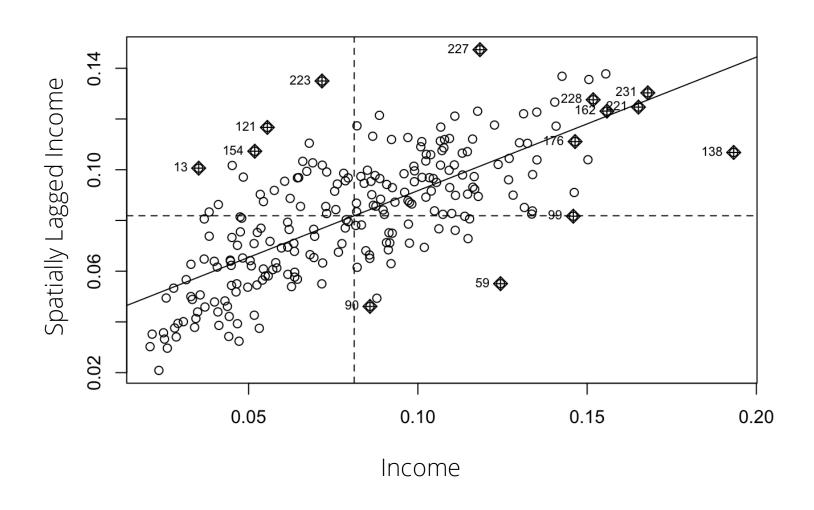


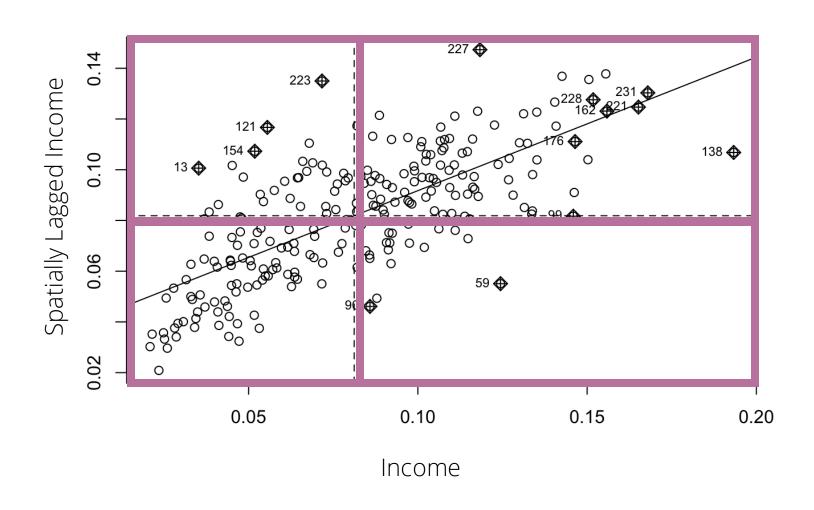
Monte Carlo Simulation of Moran's I

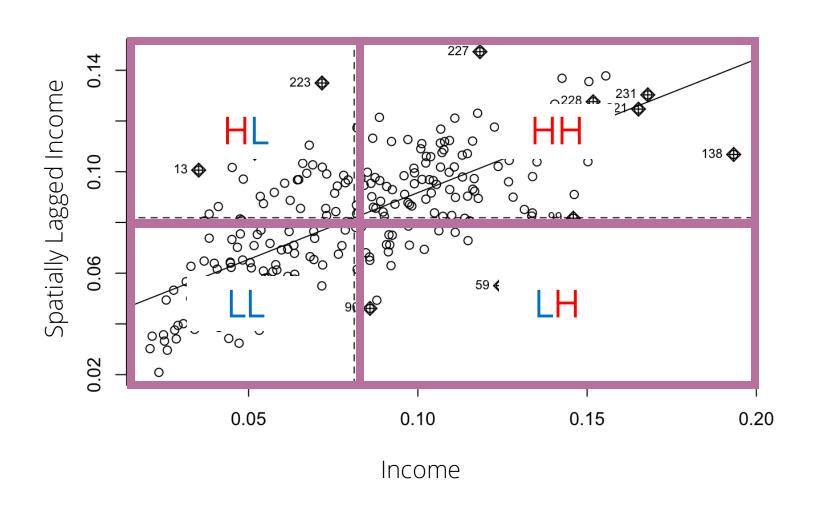


- A pseudo *p*-value is generated from the simulation results.
- For instance: if out of 199 simulations, just one simulation result is more extreme than our observed statistic, p is equal to (1 + 1) / (199 + 1) = 0.01. This is interpreted as "there is a 1% probability that we would be wrong in rejecting the null hypothesis."
- Be aware, that the pseudo *p*-value is only a summary of the results from the reference distribution and should not be interpreted as an analytical *p*-value (assumption of normality and normal distribution).

# Local spatial autocorrelation





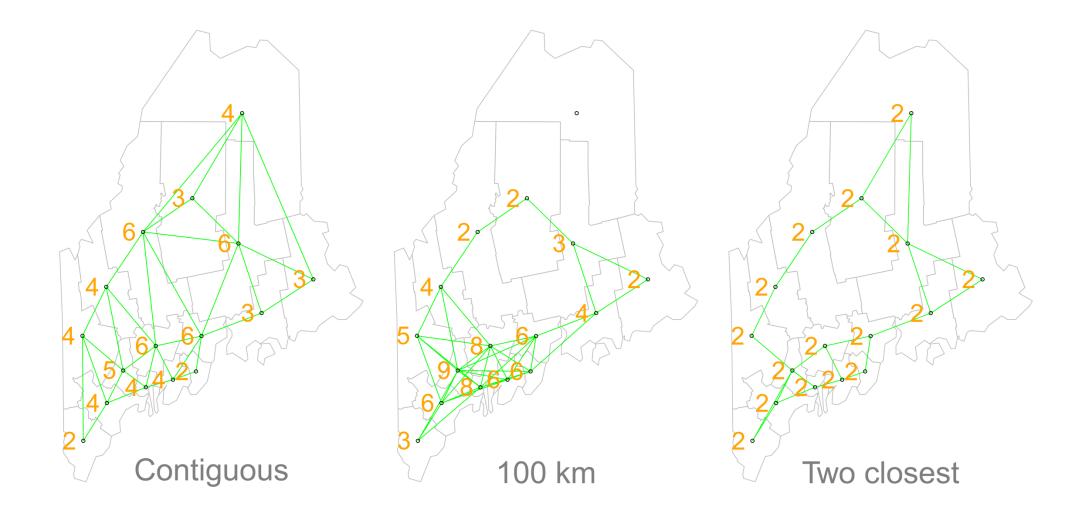


- Decomposing the Moran's I statistic: Local Moran's I
- Assesses spatial autocorrelation at the local level by evaluating each feature and its surrounding neighborhood.
- Four cluster types: high-high, low-low, but also outliers: high-low, low-high.
- Commonly known as cluster and outlier analysis.
- Monte Carlo simulation can be used to assess significance of these clusters.

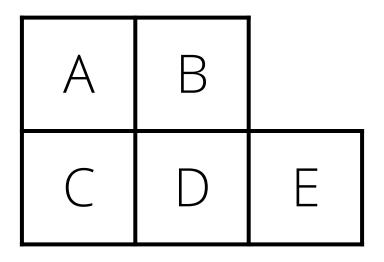
### Who is your neighbour?

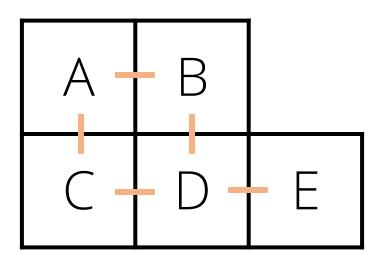
- To calculate any measure of spatial autocorrelation, it's essential to understand how spatial units relate to each other as neighbours, specifically how we define their spatial relationships.
- There are two primary approaches to defining neighbours:
  - Proximity: Neighbours are determined based on the distance between spatial units. A unit is considered a neighbour if it is within a certain distance from another unit.
  - Contiguity: Neighbours are defined by shared boundaries or edges. Spatial units are considered neighbours if they touch each other directly, either along edges (rook contiguity) or at corners (queen contiguity).

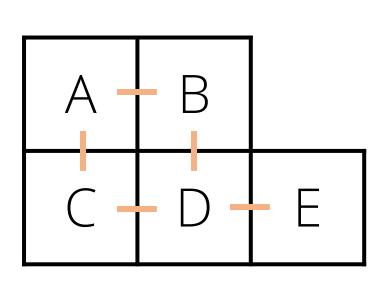
### Who is your neighbour?



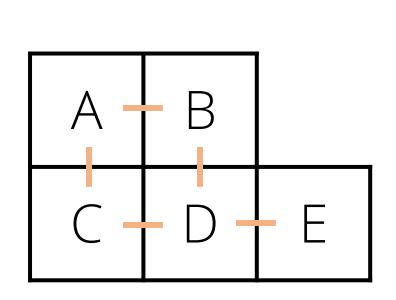
- How to use the relationships between neighbouring features?
- Spatial weight matrix: an N  $\times$  N positive matrix (W) that summarises all spatial relationships between the features in a dataset.
- It provides a formal expression of spatial dependency by quantifying the influence of each feature on every other feature based on their spatial proximity or other relevant criteria.



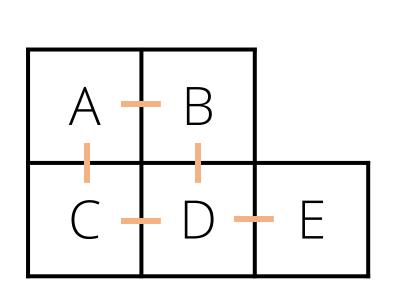




	а	р	С	d	е
а	0	1	1	0	0
b	1	0	0	1	0
С	1	0	0	1	0
d	0	1	1	0	1
е	0	0	0	1	0

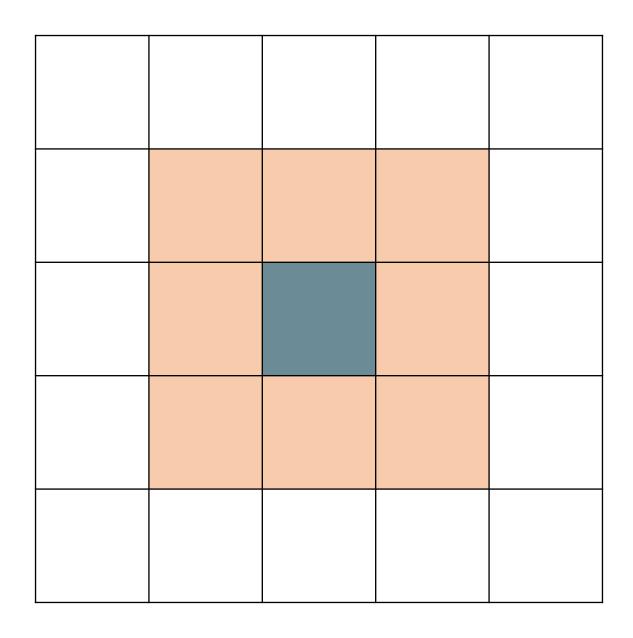


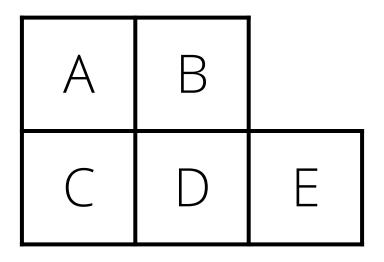
	a	b	С	d	e		W
а	0	1	1	0	0		2
р	1	0	0	1	0	_	2
С	1	0	0	1	0	_	2
d	0	1	1	0	1		3
е	0	0	0	1	0		1

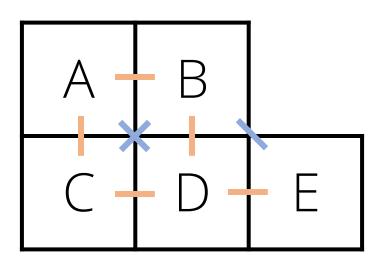


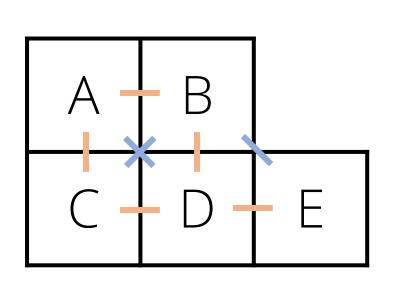
	а	р	С	d	e		W
а	0	.5	.5	0	0		2
b	.5	0	0	.5	0	_	2
С	.5	0	0	.5	0	_	2
d	0	.33	.33	0	.33		3
е	0	0	0	1	0		1

# Queen

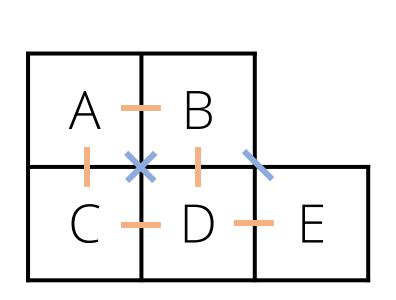




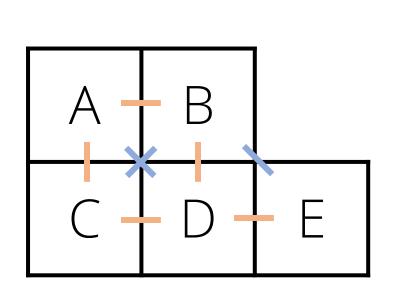




	a	b	С	d	е
а	0	1	1	1	0
b	1	0	1	1	1
С	1	1	0	1	0
d	1	1	1	0	1
е	0	1	0	1	0



	а	р	С	d	e		W
а	0	1	1	1	0		3
b	1	0	1	1	1	_	4
С	1	1	0	1	0	=	3
d	1	1	1	0	1		4
е	0	1	0	1	0		2



	а	b	С	d	e		W
а	0	.33	.33	.33	0		3
D	.25	0	.25	.25	.25	_	4
С	.33	.33	0	.33	0	_	3
d	.25	.25	.25	0	.25		4
е	0	.5	0	.5	0		2

Standardisation can be done in different ways. In spdep package:

_	"B" coding scheme	no standardisation (heterogeneity between zones)	)
	O	lacksquare	/

_	"W" coding scheme	row standardisation
_	W Coding scheine	1011 Standardisation

	"C"					
_	"C" coding scheme	global	standardisation;	weights are	standardised so tha	Jť

the sum of all weights is equal to the total number of

entities

- "U" coding scheme weights are standardised so that the sum of

all weights equals 1

# Topology







#### Conclusion

- Measuring spatial autocorrelation is essential for understanding spatial relationships and patterns in data.
- We discussed two common measures of spatial autocorrelation, though other methods also exist.
- A spatial weights matrix is required to calculate the spatially lagged variable used in these measures.
- The way neighbours are defined (proximity or contiguity) can affect the results of spatial autocorrelation tests.

### Questions

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