

# Parity bit:

## Function to Generate Parity bit and Parity Checker

```
def Check_Sum_Even(input: np.ndarray) -> bool:
    """
    # Input: an array of bit
    # Calculate the sum of bits given and consider whether it is EVEN number or not.
    # Output: Boolean whether it is EVEN or not (TRUE = EVEN / FALSE = ODD)

    count = 0
    for bin in input:
        count = count + int(bin)
    return bool(count % 2 == 0) # Return the boolean whether the number is even or not?

def addBit(parity_type: str):
    """
    #Input: type of parity bit
    #Calculate the key for odd and even parity bit
    # Depend on TYPE

    first = '0' if parity_type in (
        TYPE_OF_PARITY[0], TYPE_OF_PARITY[2]) else '1'

    second = '1' if parity_type in (
        TYPE_OF_PARITY[0], TYPE_OF_PARITY[2]) else '0'

    return [first, second] #Output: Array of key of parity bit

def gen_CheckBit(dataword: np.ndarray, parity_type: str, axis='x') -> np.ndarray:
    """
    Input: dataword, type of parity bit, and axis of parity bit
    Generate the parity bit and append into original dataword given
    Output: the dataword combined with parity bit
    """

    # Get key that depends on the parity type
    [first, second] = addBit(parity_type)

    # if two dimension and want to generate the parity bit for y axis, transpose them to x
    if axis == 'y':
        dataword = dataword.T

    # Append generated parity bit to original array of bit
    dataword = np.array( # even or not if type 0 2 , even add 0 else 1
        [np.append(w, [first if Check_Sum_Even(w) else second]) for w in dataword])

    if axis == 'y':
        return dataword.T # transpose back

    return dataword

def VerifyBits(c_word, parity_type):
    """
    Input: codeword, type of parity bit
    For Check whether the bit has changed or not
    Output: Validity of parity bit
    """

    [first, second] = addBit(parity_type) # Get key that depends on the parity type

    for word in c_word:
        keyCheck = first if Check_Sum_Even(word[0:-1]) else second
        if word[-1] != keyCheck: # If the key check is not equal the key for codeword -> the codeword has been damaged
            return 'FAILED'
    return 'PASSED'

def mergeStringFromList(arr: list): # Input: Array of array of bit or string
    """
    # This function will Merge a bit or string in array to be 1 string

    return ''.join(l for l in (d.tolist() for d in arr)) # Output: Array of string_
    """
```

**Generator: codeword = parity\_gen(dataword, word\_size, parity\_type, array\_size)**

```
def parity_gen(dataword: list, word_size: int, parity_type: str, array_size: int):  
    #codeword: bit string of any size up to word_size  
    #word_size: size of each dataword where word_size ≥ 5  
  
    d_word = np.array([np.array(list(f)) for f in dataword]) # Create Numpy Array from the Dataword Array  
  
    d_word = gen_CheckBit(d_word, parity_type) # Generate Bit in x axis  
  
    # If the word is less than data word size provided in parameters, add 0 until it reaches data word size given.  
    for i in range(len(d_word)):  
        while d_word[i].size < word_size:  
            d_word[i] = np.append(d_word[i], [0]) # Add 0 in word array in Dataword Numpy array  
  
    if parity_type in TYPE_OF_PARITY[0:2]:  
        return mergeStringFromList(d_word) # If type is 1D, return to codeword  
  
    d_word = gen_CheckBit(d_word, parity_type, axis='y') # Generate Bit in y axis  
    return mergeStringFromList(d_word) # Return codeword
```

## How to run the code for the generator

Input the dataword      Input word size      Input the  
TYPE\_OF\_PARITY[0,1,2,3]

Input the array size

```
pbg_1 = parity_gen(['10110', '10010', '11101'], 5, TYPE_OF_PARITY[0], 3)  
pbg_2 = parity_gen(['10110', '10010', '11101'], 5, TYPE_OF_PARITY[2], 3)  
pbg_3 = parity_gen(['1011', '1000', '1010'], 4, TYPE_OF_PARITY[1], 3)  
pbg_4 = parity_gen(['10110101', '10110000', '10010101'], 8, TYPE_OF_PARITY[1], 3)  
pbg_5 = parity_gen(['101011', '010111', '000111'], 6, TYPE_OF_PARITY[2], 3)  
pbg_6 = parity_gen(['111110', '001100', '101001'], 6, TYPE_OF_PARITY[3], 3)  
pbg_7 = parity_gen(['10111', '10110', '00110', '10100'], 5, TYPE_OF_PARITY[3], 4)  
pbg_8 = parity_gen(['10110000', '01101100', '10010101', '10110111'], 8, TYPE_OF_PARITY[2], 4)  
pbg_9 = parity_gen(['111110', '001100', '101001', '101101'], 6, TYPE_OF_PARITY[3], 4)  
pbg_10 = parity_gen(['10111', '01000', '11111', '10110'], 5, TYPE_OF_PARITY[2], 4)  
  
print(f'Parity Bit Generation 1 : {pbg_1}')  
print(f'Parity Bit Generation 2 : {pbg_2}')  
print(f'Parity Bit Generation 3 : {pbg_3}')  
print(f'Parity Bit Generation 4 : {pbg_4}')  
print(f'Parity Bit Generation 5 : {pbg_5}')  
print(f'Parity Bit Generation 6 : {pbg_6}')  
print(f'Parity Bit Generation 7 : {pbg_7}')  
print(f'Parity Bit Generation 8 : {pbg_8}')  
print(f'Parity Bit Generation 9 : {pbg_9}')  
print(f'Parity Bit Generation 10 : {pbg_10}')
```

## Test:

```
pbg_1 = parity_gen(['10110', '10010', '11101'], 5, TYPE_OF_PARITY[0], 3)
pbg_2 = parity_gen(['10110', '10010', '11101'], 5, TYPE_OF_PARITY[2], 3)
pbg_3 = parity_gen(['1011', '1000', '1010'], 4, TYPE_OF_PARITY[1], 3)
pbg_4 = parity_gen(['10110101', '10110000', '10010101'], 8, TYPE_OF_PARITY[1], 3)
pbg_5 = parity_gen(['101011', '010111', '000111'], 6, TYPE_OF_PARITY[2], 3)
pbg_6 = parity_gen(['111110', '001100', '101001'], 6, TYPE_OF_PARITY[3], 3)
pbg_7 = parity_gen(['10111', '10110', '00110', '10100'], 5, TYPE_OF_PARITY[3], 4)
pbg_8 = parity_gen(['10110000', '01101100', '10010101', '10110111'], 8, TYPE_OF_PARITY[2], 4)
pbg_9 = parity_gen(['111110', '001100', '101001', '101101'], 6, TYPE_OF_PARITY[3], 4)
pbg_10 = parity_gen(['10111', '01000', '11111', '10110'], 5, TYPE_OF_PARITY[2], 4)

print(f'Parity Bit Generation 1 : {pbg_1}')
print(f'Parity Bit Generation 2 : {pbg_2}')
print(f'Parity Bit Generation 3 : {pbg_3}')
print(f'Parity Bit Generation 4 : {pbg_4}')
print(f'Parity Bit Generation 5 : {pbg_5}')
print(f'Parity Bit Generation 6 : {pbg_6}')
print(f'Parity Bit Generation 7 : {pbg_7}')
print(f'Parity Bit Generation 8 : {pbg_8}')
print(f'Parity Bit Generation 9 : {pbg_9}')
print(f'Parity Bit Generation 10 : {pbg_10}')
```

## Result:

```
Parity Bit Generation 1 : ['101101', '100100', '111010']
Parity Bit Generation 2 : ['101101', '100100', '111010', '110011']
Parity Bit Generation 3 : ['10110', '10000', '10101']
Parity Bit Generation 4 : ['101101010', '101100000', '100101011']
Parity Bit Generation 5 : ['1010110', '0101110', '0001111', '1110111']
Parity Bit Generation 6 : ['1111100', '0011001', '1010010', '1001000']
Parity Bit Generation 7 : ['101111', '101100', '001101', '101001', '011000']
Parity Bit Generation 8 : ['101100001', '011011000', '100101010', '101101110', '111111101']
Parity Bit Generation 9 : ['1111100', '0011001', '1010010', '1011011', '0010011']
Parity Bit Generation 10 : ['1011110', '010001', '111111', '101101', '101101']
```

Checker: validity = parity\_check(codeword, parity\_type, size)

```
def parity_check(codeword: list, parity_type: str, size: int): # Parity Checker

    checkValid = 'PASSED' # Initialize Check Status

    c_word = np.array([np.array(list(w)) for w in codeword]) # Create Numpy Array from the Codeword Array

    checkValid = VerifyBits(c_word, parity_type) # Verify Checkbit in X axis

    if parity_type in TYPE_OF_PARITY[0:2] or checkValid == 'FAILED':
        return checkValid

    return VerifyBits(c_word.T, parity_type) # Verify Checkbit in Y axis
```

How to run the Parity\_check:

Input the  
TYPE\_OF\_PARITY[0,1,2,3]

Input the codeword

Input the array size

```
pbv_1 = parity_check(['101101', '100100', '111010', '110011'], TYPE_OF_PARITY[0], 4)
pbv_2 = parity_check(['101101', '100100', '111010'], TYPE_OF_PARITY[1], 3)
pbv_3 = parity_check(['111010', '110011', '100100', '110001'], TYPE_OF_PARITY[2], 3)
pbv_4 = parity_check(['101111', '101100', '111010'], TYPE_OF_PARITY[3], 2)
pbv_5 = parity_check(['101101', '100100', '111010', '110011'], TYPE_OF_PARITY[2], 3)
pbv_6 = parity_check(['101111', '010111', '010110', '111111'], TYPE_OF_PARITY[3], 3)
pbv_7 = parity_check(['101101', '101100', '010001'], TYPE_OF_PARITY[0], 3)
pbv_8 = parity_check(['111000', '010100', '010011'], TYPE_OF_PARITY[1], 3)
pbv_9 = parity_check(['101101', '010101', '000001', '111010'], TYPE_OF_PARITY[1], 4)
pbv_10 = parity_check(['101001', '110011', '101010'], TYPE_OF_PARITY[0], 3)

print(f'Parity Bit Validation 1 : {pbv_1}')
print(f'Parity Bit Validation 2 : {pbv_2}')
print(f'Parity Bit Validation 3 : {pbv_3}')
print(f'Parity Bit Validation 4 : {pbv_4}')
print(f'Parity Bit Validation 5 : {pbv_5}')
print(f'Parity Bit Validation 6 : {pbv_6}')
print(f'Parity Bit Validation 7 : {pbv_7}')
print(f'Parity Bit Validation 8 : {pbv_8}')
print(f'Parity Bit Validation 9 : {pbv_9}')
print(f'Parity Bit Validation 10 : {pbv_10}')
```

## Test:

```
pbv_1 = parity_check(['101101', '100100', '111010', '110011'], TYPE_OF_PARITY[0], 4)
pbv_2 = parity_check(['101101', '100100', '111010'], TYPE_OF_PARITY[1], 3)
pbv_3 = parity_check(['111010', '110011', '100100', '110001'], TYPE_OF_PARITY[2], 3)
pbv_4 = parity_check(['101111', '101100', '111010'], TYPE_OF_PARITY[3], 2)
pbv_5 = parity_check(['101101', '100100', '111010', '110011'], TYPE_OF_PARITY[2], 3)
pbv_6 = parity_check(['101111', '010111', '010110', '111111'], TYPE_OF_PARITY[3], 3)
pbv_7 = parity_check(['101101', '101100', '010001'], TYPE_OF_PARITY[0], 3)
pbv_8 = parity_check(['111000', '010100', '010011'], TYPE_OF_PARITY[1], 3)
pbv_9 = parity_check(['101101', '010101', '000001', '111010'], TYPE_OF_PARITY[1], 4)
pbv_10 = parity_check(['101001', '110011', '101010'], TYPE_OF_PARITY[0], 3)

print(f'Parity Bit Validation 1 : {pbv_1}')
print(f'Parity Bit Validation 2 : {pbv_2}')
print(f'Parity Bit Validation 3 : {pbv_3}')
print(f'Parity Bit Validation 4 : {pbv_4}')
print(f'Parity Bit Validation 5 : {pbv_5}')
print(f'Parity Bit Validation 6 : {pbv_6}')
print(f'Parity Bit Validation 7 : {pbv_7}')
print(f'Parity Bit Validation 8 : {pbv_8}')
print(f'Parity Bit Validation 9 : {pbv_9}')
print(f'Parity Bit Validation 10 : {pbv_10}')
```

## Output:

```
Parity Bit Validation 1 : PASSED
Parity Bit Validation 2 : FAILED
Parity Bit Validation 3 : FAILED
Parity Bit Validation 4 : FAILED
Parity Bit Validation 5 : PASSED
Parity Bit Validation 6 : FAILED
Parity Bit Validation 7 : FAILED
Parity Bit Validation 8 : FAILED
Parity Bit Validation 9 : FAILED
Parity Bit Validation 10 : FAILED
```

## CRC:

```
def xor(x, y):
    res = []
    for i in range(1, len(y)):
        #xor logic, same = 0, difference = 1
        if x[i] == y[i]:
            res.append('0')
        else:
            res.append('1')
    return ''.join(res)

#modulo-2 division
def mod2div(dividend, divisor):
    j = len(divisor)
    k = dividend[0 : j]
    while j < len(dividend):
        if k[0] == '1':
            k = xor(divisor, k) + dividend[j]
        else:
            #if the left bit is "0", use "0s" divisor
            k = xor('0'*j, k) + dividend[j]
        j += 1
    #Fix Index out of bound error
    if k[0] == '1':
        k = xor(divisor, k)
    else:
        k = xor('0'*j, k)
    return k

def CRC_gen(dataword, word_size, CRC_type): #Encoder
    if(word_size != len(dataword)): return "Please Re-Enter"
    if(CRC_type == "CRC-32"): binary = "100000100110000010001110110110111"
    elif(CRC_type == "CRC-24"): binary = "1100000000101000100000001"
    elif(CRC_type == "CRC-16"): binary = "11000000000000101"
    elif(CRC_type == "Reversed CRC-16"): binary = "1010000000000011"
    elif(CRC_type == "CRC-8"): binary = "111010101"
    elif(CRC_type == "CRC-4"): binary = "11111"
    key = len(binary)
    appended_dataword = dataword + '0'*(key-1)
    remain = mod2div(appended_dataword, binary)
    codeword = dataword + remain
    return codeword

def CRC_check(dataword, CRC_type): #Decoder
    if(CRC_type == "CRC-32"): binary = "100000100110000010001110110110111"
    elif(CRC_type == "CRC-24"): binary = "1100000000101000100000001"
    elif(CRC_type == "CRC-16"): binary = "11000000000000101"
    elif(CRC_type == "Reversed CRC-16"): binary = "1010000000000011"
    elif(CRC_type == "CRC-8"): binary = "111010101"
    elif(CRC_type == "CRC-4"): binary = "11111"
    key = len(binary)
    appended_dataword = dataword + '0'*(key-1)
    remain = mod2div(appended_dataword, binary)
    remain = int(remain)
    if(remain == 0): return 1
    else: return 0
```

## Test:

```
test1 = CRC_gen("101011", 6, "CRC-8")
test2 = CRC_gen("1010", 4, "CRC-4")
test3 = CRC_gen("1100101", 7, "CRC-8")
test4 = CRC_gen("1011010", 7, "CRC-16")
test5 = CRC_gen("101001", 6, "Reversed CRC-16")
test6 = CRC_gen("100110010", 9, "CRC-24")
test7 = CRC_gen("11100101", 8, "CRC-16")
test8 = CRC_gen("1010010010", 10, "CRC-16")
test9 = CRC_gen("1010", 4, "CRC-4")
test10 = CRC_gen("1010010010100010", 16, "CRC-32")
print("codeword 1: ", test1)
print("codeword 2: ", test2)
print("codeword 3: ", test3)
print("codeword 4: ", test4)
print("codeword 5: ", test5)
print("codeword 6: ", test6)
print("codeword 7: ", test7)
print("codeword 8: ", test8)
print("codeword 9: ", test9)
print("codeword 10: ", test10)
print("check 1: ", CRC_check(test1, "CRC-8"))
print("check 2: ", CRC_check(test2, "CRC-4"))
print("check 3: ", CRC_check(test3, "CRC-8"))
print("check 4: ", CRC_check(test4, "CRC-16"))
print("check 5: ", CRC_check(test5, "Reversed CRC-16"))
print("check 6: ", CRC_check(test6, "CRC-24"))
print("check 7: ", CRC_check(test7, "CRC-16"))
print("check 8: ", CRC_check(test8, "CRC-16"))
print("check 9: ", CRC_check(test9, "CRC-4"))
print("check 10: ", CRC_check(test10, "CRC-32"))
```

## Output:

```
PS C:\Python> python -u "c:\Python\Computer Data\q2.py"
codeword 1: 10101100100111
codeword 2: 10100101
codeword 3: 110010100010010
codeword 4: 10110100000000111011100
codeword 5: 10100101000000001100011
codeword 6: 100110010011010110001110111011100
codeword 7: 111001011000001001011101
codeword 8: 10100100100000111101101100
codeword 9: 10100101
codeword 10: 101001001010001000011111101001101010001001110111
check 1: 1
check 2: 1
check 3: 1
check 4: 1
check 5: 1
check 6: 1
check 7: 1
check 8: 1
check 9: 1
check 10: 1
```

Generator: codeword = CRC\_gen(dataword, word\_size, CRC\_type)

```
def CRC_gen(dataword, word_size, CRC_type): #Encoder
    if(word_size != len(dataword)): return "Please Re-Enter"
    if(CRC_type == "CRC-32"): binary = "100000100110000010001110110110111"
    elif(CRC_type == "CRC-24"): binary = "1100000000101000100000001"
    elif(CRC_type == "CRC-16"): binary = "11000000000000101"
    elif(CRC_type == "Reversed CRC-16"): binary = "1010000000000011"
    elif(CRC_type == "CRC-8"): binary = "111010101"
    elif(CRC_type == "CRC-4"): binary = "11111"
    key = len(binary)
    appended_dataword = dataword + '0'*(key-1)
    remain = mod2div(appended_dataword, binary)
    codeword = dataword + remain
    return codeword
```

How to run CRC\_gen

```
test1 = CRC_gen("101011", 6, "CRC-8")
test2 = CRC_gen("1010", 4, "CRC-4")
test3 = CRC_gen("1100101", 7, "CRC-8")
test4 = CRC_gen("1011010", 7, "CRC-16")
test5 = CRC_gen("101001", 6, "Reversed CRC-16")
test6 = CRC_gen("100110010", 9, "CRC-24")
test7 = CRC_gen("11100101", 8, "CRC-16")
test8 = CRC_gen("1010010010", 10, "CRC-16")
test9 = CRC_gen("1010", 4, "CRC-4")
test10 = CRC_gen("1010010010100010", 16, "CRC-32")
```

- input dataword
- input word\_size according to dataword length
- input CRC-type



Checker: `validity = CRC_check(codeword, CRC-type)`

```
def CRC_check(dataword, CRC_type): #Decoder
    if(CRC_type == "CRC-32"): binary = "100000100110000010001110110110111"
    elif(CRC_type == "CRC-24"): binary = "1100000000101000100000001"
    elif(CRC_type == "CRC-16"): binary = "11000000000000101"
    elif(CRC_type == "Reversed CRC-16"): binary = "1010000000000011"
    elif(CRC_type == "CRC-8"): binary = "111010101"
    elif(CRC_type == "CRC-4"): binary = "11111"
    key = len(binary)
    appended_dataword = dataword + '0'*(key-1)
    remain = mod2div(appended_dataword, binary)
    remain = int(remain)
    if(remain == 0): return 1
    else: return 0
```

How to run `CRC_check`

```
print("check 1: ", CRC_check(test1, "CRC-8"))
print("check 2: ", CRC_check(test2, "CRC-4"))
print("check 3: ", CRC_check(test3, "CRC-8"))
print("check 4: ", CRC_check(test4, "CRC-16"))
print("check 5: ", CRC_check(test5, "Reversed CRC-16"))
print("check 6: ", CRC_check(test6, "CRC-24"))
print("check 7: ", CRC_check(test7, "CRC-16"))
print("check 8: ", CRC_check(test8, "CRC-16"))
print("check 9: ", CRC_check(test9, "CRC-4"))
print("check 10: ", CRC_check(test10, "CRC-32"))
```

- input dataword
- input CRC-type

## Checksum:

Generator: `codeword = Checksum_gen(dataword, word_size, num_blocks)`

```
# This function created for inverse the dataword
def bi_inverse(dataword):
    result = ''
    for i in dataword:
        if i == '1':
            result = result + '0'
        else:
            result = result + '1'
    return result
```

```
def Checksum_gen(dataword, word_size, num_blocks):

    dataw = []
    w = list(dataword)

    #Split dataword into [...,...,...] following the numblock

    for i in range(num_blocks): # i * word_size = start assume that word_size = 5 > 0:5, 5:10
        dataw.append(''.join(w[i * word_size: i * word_size + word_size]))
        print("Dataword:",dataword, "\n", dataw)

    #for summation

    sum = '0'

    for i in dataw: #[ '11100' (0), '01010'(i), '10001'(i)]
        sum =(int(sum, 2) + int(i, 2))
        sum = bin(sum)[2:]
        #print("Summation: ", sum)

    # In case the lenght of summation longer than word_size
    while len(sum) > word_size:
        sum = (int(sum[len(sum) - word_size:],2) + int(sum[0: len(sum) - word_size], 2))
        sum = bin(sum)[2:]

    # In case the length of summation less than word_size, add "0" in front of the result
    while len(sum) < word_size:
        sum = '0' + sum

    dataw.append(bi_inverse(sum))

    print("Sum: ",sum, "\n" "Checksum: ",(bi_inverse(sum)), "\nThe codeword is "+ " ".join(dataw))
```

## How to run Checksum\_gen

Input the dataword      Input word size      Input num blocks

```
print('-----1-----')
cgs_1 = Checksum_gen('101010010011100100011101', 8, 3)

print('-----2-----')
cgs_2 = Checksum_gen('1011001101011010', 4, 4)

print('-----3-----')
cgs_3 = Checksum_gen('110110010100', 4, 3)

print('-----4-----')
cgs_4 = Checksum_gen('1100100101001010110', 4, 5)

print('-----5-----')
cgs_5 = Checksum_gen('010110001101', 4, 3)

print('-----6-----')
cgs_6 = Checksum_gen('1011011010101010', 4, 4)

print('-----7-----')
cgs_7 = Checksum_gen('010010101010010111101011', 4, 5)

print('-----8-----')
cgs_8 = Checksum_gen('101001111111', 4, 3)

print('-----9-----')
cgs_9 = Checksum_gen('0110110101010010', 4, 4)

print('-----10-----')
cgs_10 = Checksum_gen('11101111111010110111', 5, 3)

print('-----11-----')
cgs_11 = Checksum_gen('1010100100111001', 8, 2)
```

## Test:

```
print('-----1-----')
cgs_1 = Checksum_gen('101010010011100100011101', 8, 3)

print('-----2-----')
cgs_2 = Checksum_gen('1011001101011010', 4, 4)

print('-----3-----')
cgs_3 = Checksum_gen('110110010100', 4, 3)

print('-----4-----')
cgs_4 = Checksum_gen('1100100101001010110', 4, 5)

print('-----5-----')
cgs_5 = Checksum_gen('010110001101', 4, 3)

print('-----6-----')
cgs_6 = Checksum_gen('1011011010101010', 4, 4)

print('-----7-----')
cgs_7 = Checksum_gen('010010101010010111101011', 4, 5)

print('-----8-----')
cgs_8 = Checksum_gen('101001111111', 4, 3)

print('-----9-----')
cgs_9 = Checksum_gen('0110110101010010', 4, 4)

print('-----10-----')
cgs_10 = Checksum_gen('11101111111010110111', 5, 3)

print('-----11-----')
cgs_11 = Checksum_gen('1010100100111001', 8, 2)
```

## Output:

```
-----1-----
Dataword: 101010010011100100011101
['10101001', '00111001', '00011101']
Sum: 11111111
Checksum: 00000000
The codeword is 10101001 00111001 00011101 00000000
-----2-----
Dataword: 1011001101011010
['1011', '0011', '0101', '1010']
Sum: 1110
Checksum: 0001
The codeword is 1011 0011 0101 1010 0001
-----3-----
Dataword: 110110010100
['1101', '1001', '0100']
Sum: 1011
Checksum: 0100
The codeword is 1101 1001 0100 0100
-----4-----
Dataword: 11001001010010100110
['1100', '1001', '0100', '1010', '0110']
Sum: 1011
Checksum: 0100
The codeword is 1100 1001 0100 1010 0110 0100
-----5-----
Dataword: 010110001101
['0101', '1000', '1101']
Sum: 1011
Checksum: 0100
The codeword is 0101 1000 1101 0100
-----6-----
Dataword: 1011011010101010
['1011', '0110', '1010', '1010']
Sum: 0111
Checksum: 1000
The codeword is 1011 0110 1010 1010 1000
```

```
-----7-----
Dataword: 010010101010010111101011
['0100', '1010', '1010', '0101', '1110']
Sum: 1101
Checksum: 0010
The codeword is 0100 1010 1010 0101 1110 0010
-----8-----
Dataword: 101001111111
['1010', '0111', '1111']
Sum: 0010
Checksum: 1101
The codeword is 1010 0111 1111 1101
-----9-----
Dataword: 0110110101010010
['0110', '1101', '0101', '0010']
Sum: 1011
Checksum: 0100
The codeword is 0110 1101 0101 0010 0100
-----10-----
Dataword: 1110111111010110111
['11101', '11111', '10101']
Sum: 10011
Checksum: 01100
The codeword is 11101 11111 10101 01100
-----11-----
Dataword: 1010100100111001
['10101001', '00111001']
Sum: 11100010
Checksum: 00011101
The codeword is 10101001 00111001 00011101
```

---

Checker: validity = Checksum\_check(codeword, word\_size, num\_blocks)

```
def Checksum_check(codeword, word_size, num_blocks):

    d = list(codeword)
    dataw = []

    for i in range(num_blocks+1):
        # print(i)
        dataw.append("".join(d[i * word_size: i * word_size + word_size]))
    print(dataw)

    sum = '0'

    for i in dataw: #['11100' (0), '01010'(i), '10001'(i)]
        sum = (int(sum, 2) + int(i, 2))
        sum = bin(sum)[2:]
        #print("Summation: ", sum)

    # In case the length of summation longer than word_size
    while len(sum) > word_size:
        sum = (int(sum[len(sum) - word_size:], 2) + int(sum[0: len(sum) - word_size], 2))
        sum = bin(sum)[2:]

    # In case the length of summation less than word_size, add "0" in front of the result
    while len(sum) < word_size:
        sum = '0' + sum

    # For check validation
    check = ''

    for i in range(word_size):
        check += '0'

    print("Codeword: "+" ".join(dataw))

    if bi_inverse(sum) == check:
        print("Validity of the array of codewords: PASS")
    else:
        print("Validity of the array of codewords: FAIL")
```

## How to run Checksum\_check

Input the codeword      Input word size      Input num blocks



```
print('-----1-----')
case1 = Checksum_check('11100010101000100111', 5, 3)
print('-----2-----')
case2 = Checksum_check('111110111101111000000011011010', 5, 3)
print('-----3-----')
case3 = Checksum_check('1010101101001111', 5, 2)
print('-----4-----')
case4 = Checksum_check('1110111101010101001000111', 5, 3)
print('-----5-----')
case5 = Checksum_check('1110111101010101', 4, 3)
print('-----6-----')
case6 = Checksum_check('101101010011', 3, 3)
print('-----7-----')
case7 = Checksum_check('11101111111010101100', 5, 3)
print('-----8-----')
case8 = Checksum_check('1010011111111101', 4, 3)
print('-----9-----')
case9 = Checksum_check('101110111000', 3, 3)
print('-----10-----')
case10 = Checksum_check('101010010011100100011101', 8, 2)
print('-----11-----')
case11 = Checksum_check('10110011010110100001', 4, 4)
```

## Test:

```
print('-----1-----')
case1 = Checksum_check('11100010101000100111', 5, 3)
print('-----2-----')
case2 = Checksum_check('11111011110111100000011011010', 5, 3)
print('-----3-----')
case3 = Checksum_check('1010101101001111', 5, 2)
print('-----4-----')
case4 = Checksum_check('11101111010101001000111', 5, 3)
print('-----5-----')
case5 = Checksum_check('11101111010101', 4, 3)
print('-----6-----')
case6 = Checksum_check('101101010011', 3, 3)
print('-----7-----')
case7 = Checksum_check('1110111111010101100', 5, 3)
print('-----8-----')
case8 = Checksum_check('1010011111111101', 4, 3)
print('-----9-----')
case9 = Checksum_check('101110111000', 3, 3)
print('-----10-----')
case10 = Checksum_check('101010010011100100011101', 8, 2)
print('-----11-----')
case11 = Checksum_check('10110011010110100001', 4, 4)
```

## Output:

```
-----1-----
['11100', '01010', '10001', '00111']
Codeword: 11100 01010 10001 00111
Validity of the array of codewords: PASS
```

```
-----2-----
['11111', '01111', '01111', '00000']
Codeword: 11111 01111 01111 00000
Validity of the array of codewords: FAIL
```

```
-----3-----
['10101', '01101', '00111']
Codeword: 10101 01101 00111
Validity of the array of codewords: FAIL
```

```
-----4-----
['11101', '11101', '01010', '10010']
Codeword: 11101 11101 01010 10010
Validity of the array of codewords: FAIL
```

```
-----5-----
['1110', '1111', '0101', '0101']
Codeword: 1110 1111 0101 0101
Validity of the array of codewords: FAIL
```

```
-----6-----
['101', '101', '010', '011']
Codeword: 101 101 010 011
Validity of the array of codewords: FAIL
```

```
-----7-----
['11101', '11111', '10101', '01100']
Codeword: 11101 11111 10101 01100
Validity of the array of codewords: PASS
```

```
-----8-----
['1010', '0111', '1111', '1101']
Codeword: 1010 0111 1111 1101
Validity of the array of codewords: PASS
```

```
-----9-----
['101', '110', '111', '000']
Codeword: 101 110 111 000
Validity of the array of codewords: FAIL
```

```
-----10-----
['10101001', '00111001', '00011101']
Codeword: 10101001 00111001 00011101
Validity of the array of codewords: PASS
```

```
-----11-----
['1011', '0011', '0101', '1010', '0001']
Codeword: 1011 0011 0101 1010 0001
Validity of the array of codewords: PASS
```

## Hamming code:

```
def Hamming_gen(dataword):
    #Find Number of Redundancy Bit
    length = len(dataword)
    for i in range(length):
        if(2**i >= length + i + 1):
            r = i
            break
    #Place Redundancy Bit
    j = 0
    k = 1
    res = ''
    for i in range(1, length + r + 1):
        if(i == 2**j):
            res = res + '0'
            j += 1
        else:
            res = res + dataword[-1 * k]
            k += 1
    #Reversing
    output = res[::-1]
    #Finding Parity bit
    n = len(output)
    for i in range(r):
        x = 0
        for j in range(1, n + 1):
            if(j & (2**i) == (2**i)):
                x = x ^ int(output[-1 * j])
        output = output[:n-(2**i)] + str(x) + output[n-(2**i)+1:]
    return output

def Hamming_check(codeword):
    m = len(codeword)
    #Calculate Parity bit
    for i in range(m):
        if(2**i >= m + i + 1):
            nr = i
            break
    n = len(codeword)
    res = 0
    for i in range(nr):
        val = 0
        for j in range(1, n + 1):
            if(j & (2**i) == (2**i)):
                val = val ^ int(codeword[-1 * j])
        #Append Parity bit
        res = res + val*(10**i)
    if(int(str(res), 2) == 0): return -1
    else: return int(str(res), 2)
```



## Test:

```
test1 = Hamming_gen("101011")
test2 = Hamming_gen("1010")
test3 = Hamming_gen("1100101")
test4 = Hamming_gen("1011010")
test5 = Hamming_gen("101001")
test6 = Hamming_gen("100110010")
test7 = Hamming_gen("11100101")
test8 = Hamming_gen("1010010010")
test9 = Hamming_gen("1010")
test10 = Hamming_gen("1010010010100010")
print("codeword 1: ", test1)
print("codeword 2: ", test2)
print("codeword 3: ", test3)
print("codeword 4: ", test4)
print("codeword 5: ", test5)
print("codeword 6: ", test6)
print("codeword 7: ", test7)
print("codeword 8: ", test8)
print("codeword 9: ", test9)
print("codeword 10: ", test10)
print("check 1: ", Hamming_check(test1))
print("check 2: ", Hamming_check(test2))
print("check 3: ", Hamming_check(test3))
print("check 4: ", Hamming_check(test4))
print("check 5: ", Hamming_check(test5))
print("check 6: ", Hamming_check(test6))
print("check 7: ", Hamming_check(test7))
print("check 8: ", Hamming_check(test8))
print("check 9: ", Hamming_check(test9))
print("check 10: ", Hamming_check(test10))
```

## Output:

```
PS C:\Python> python -u "c:\Python\Computer Data\q4.py"
codeword 1: 1011010111
codeword 2: 1010010
codeword 3: 11000101100
codeword 4: 10101010000
codeword 5: 1011001110
codeword 6: 1001110010011
codeword 7: 111010100100
codeword 8: 10100110011010
codeword 9: 1010010
codeword 10: 101000100101010010010
check 1: -1
check 2: -1
check 3: -1
check 4: -1
check 5: -1
check 6: -1
check 7: -1
check 8: -1
check 9: -1
check 10: -1
```

Generator: codeword = Hamming\_gen(dataword)

```
def Hamming_gen(dataword):
    #Find Number of Redundancy Bit
    length = len(dataword)
    for i in range(length):
        if(2**i >= length + i + 1):
            r = i
            break
    #Place Redundancy Bit
    j = 0
    k = 1
    res = ''
    for i in range(1, length + r + 1):
        if(i == 2**j):
            res = res + '0'
            j += 1
        else:
            res = res + dataword[-1 * k]
            k += 1
    #Reversing
    output = res[::-1]
    #Finding Parity bit
    n = len(output)
    for i in range(r):
        x = 0
        for j in range(1, n + 1):
            if(j & (2**i) == (2**i)):
                x = x ^ int(output[-1 * j])
        output = output[:n-(2**i)] + str(x) + output[n-(2**i)+1:]
    return output
```

How to run Hamming\_gen

```
test1 = Hamming_gen("101011")
test2 = Hamming_gen("1010")
test3 = Hamming_gen("1100101")
test4 = Hamming_gen("1011010")
test5 = Hamming_gen("101001")
test6 = Hamming_gen("100110010")
test7 = Hamming_gen("11100101")
test8 = Hamming_gen("1010010010")
test9 = Hamming_gen("1010")
test10 = Hamming_gen("1010010010100010")
```

Checker: error\_pos = Hamming\_check(codeword)

```
def Hamming_check(codeword):
    m = len(codeword)
    #Calculate Parity bit
    for i in range(m):
        if(2**i >= m + i + 1):
            nr = i
            break
    n = len(codeword)
    res = 0
    for i in range(nr):
        val = 0
        for j in range(1, n + 1):
            if(j & (2**i) == (2**i)):
                val = val ^ int(codeword[-1 * j])
        #Append Parity bit
        res = res + val*(10**i)
    if(int(str(res), 2) == 0): return -1
    else: return int(str(res), 2)
```

Howto run Hamming\_check

```
print("check 1: ", Hamming_check(test1))
print("check 2: ", Hamming_check(test2))
print("check 3: ", Hamming_check(test3))
print("check 4: ", Hamming_check(test4))
print("check 5: ", Hamming_check(test5))
print("check 6: ", Hamming_check(test6))
print("check 7: ", Hamming_check(test7))
print("check 8: ", Hamming_check(test8))
print("check 9: ", Hamming_check(test9))
print("check 10: ", Hamming_check(test10))
```