

$$\mathbf{Y}_{(\mathbf{t})}=\mathbf{K}_{(\mathbf{t})}^{\alpha}\mathbf{H}_{(\mathbf{t})}^{\beta}\mathbf{L}_{(\mathbf{t})}^{1-\alpha-\beta},\ \ \alpha+\beta\in(0,1)$$

$$\begin{array}{l} \dot{L}_{(t)}=nL_{(t)}\\ L_{(0)}>0 \end{array}$$

$$\dot{k}=s_k k_{(t)}^{\alpha} h_{(t)}^{\beta}-(\delta+n)k_{(t)}$$

$$\dot{h}=s_h k_{(t)}^{\alpha} h_{(t)}^{\beta}-(\delta+n)h_{(t)}$$

$$\begin{cases} k^*=\left[\frac{s_k^{1-\beta}s_h^{\beta}}{\delta+n}\right]^{\frac{1}{1-\alpha-\beta}}\\ h^*=\left[\frac{s_h^{1-\alpha}s_k^{\alpha}}{\delta+n}\right]^{\frac{1}{1-\alpha-\beta}} \end{cases}$$

$$G(k,h)=\left(s_k k^{\alpha} h^{\beta}-(\delta+n)k\;;\; s_h k^{\alpha} h^{\beta}-(\delta+n)h\right)$$

$$\begin{pmatrix} \dot{k} \\ \dot{h} \end{pmatrix} = G(k^*,h^*)+\mathbb{J}_G \begin{pmatrix} k-k^* \\ h-h^* \end{pmatrix} \quad \text{siendo} \quad \mathbb{J}_G = \begin{pmatrix} (\delta+n)(\alpha-1) & \frac{s_k}{s_h}\beta(\delta+n) \\ \frac{s_h}{s_k}\alpha(\delta+n) & (\delta+n)(\beta-1) \end{pmatrix}$$

$$\begin{array}{l} \lambda_1=|(\delta+n)(\alpha+\beta-1)|<1\longrightarrow \text{ velocidad de convergencia}\\ \lambda_2=|-(\delta+n)|<1 \end{array}$$

$$\begin{array}{l} L_{(t+1)}=P\left(L_{(t)}\right)\\ L_{(0)}>0 \end{array}$$

$$P\left(L\right)\geq L>0,\,\forall L\leq L_{\infty}$$

$$\frac{P(L_t)}{L_{(t)}} \geq \frac{P(L_{t+1})}{L_{(t+1)}}, \forall L \leq L_\infty$$

$$\lim_{t \rightarrow +\infty} \frac{P(L_t)}{L_{(t)}} - 1 = 0$$

$$\lim_{t \rightarrow +\infty} L_t = L_\infty / L_t \leq L_\infty \forall t$$

$$Y_{(t)} = K_{(t)}^\alpha H_{(t)}^\beta L_{(t)}^{1-\alpha-\beta}, \quad \alpha + \beta \in (0, 1)$$

$$k_{t+1} = \frac{s_k k_t^\alpha h_t^\beta + (1-\delta)k_t}{P(L_t)/L_t}$$

$$h_{t+1} = \frac{s_h k_t^\alpha h_t^\beta + (1-\delta)h_t}{P(L_t)/L_t}$$

$$L_{t+1} = P(L_t)$$

$$\begin{cases} k^* = \left[\frac{s_k^{1-\beta} s_h^\beta}{\delta} \right]^{\frac{1}{1-\alpha-\beta}} \\ h^* = \left[\frac{s_h^{1-\alpha} s_k^\alpha}{\delta} \right]^{\frac{1}{1-\alpha-\beta}} \\ L^* = L_\infty \end{cases}$$

$$T(k, h, L) = \left(\frac{s_k k_t^\alpha h_t^\beta + (1-\delta)k_t}{P(L_t)/L_t}; \frac{s_h k_t^\alpha h_t^\beta + (1-\delta)h_t}{P(L_t)/L_t}; P(L_t) \right)$$

$$\mathbb{J}_T = \begin{pmatrix} \delta(\alpha-1)+1 & \frac{\beta s_k \delta}{s_h} & k^* \left(\frac{1-P'(L_\infty)}{L_\infty} \right) \\ \frac{\alpha s_h \delta}{s_k} & \delta(\beta-1)+1 & h^* \left(\frac{1-P'(L_\infty)}{L_\infty} \right) \\ 0 & 0 & P'(L_\infty) \end{pmatrix}$$

$$\lambda_1 = \delta(\alpha + \beta - 1) < 1$$

$$\lambda_2 = 1 - \delta < 1$$

$$\lambda_3 = P'(L_\infty) < 1$$

Ley de poblacion de Verhulst (1838)

$$L_{t+1} = L_t \cdot e^{r(1-\frac{L_t}{M})}$$

Ley de poblacion de Beverton (1957)

$$L_{t+1} = \frac{aL_t}{1 + bL_t}$$

Ley de poblacion de Ricker (1954)

$$L_{t+1} = aL_t \cdot e^{-bL_t}$$

Ley de poblacion de Hassell (1975)

$$L_{t+1} = \frac{aL_t}{(1 + bL_t)^c}$$