

①

$$\left\langle \begin{bmatrix} 1 \\ i \\ 1-3i \end{bmatrix}; \begin{bmatrix} 2+i \\ i \\ 2 \end{bmatrix} \right\rangle$$

$$\langle V_1, V_2 \rangle = V_1^T V_2$$

$$V^T = \overline{A^T}$$

$$= \begin{bmatrix} 1 & -i & 1+3i \end{bmatrix} \begin{bmatrix} 2+i \\ i \\ 2 \end{bmatrix} = 2+i - i^2 + 2 + 6i$$

$$\boxed{= 5 + 7i}$$

②

$$\text{norm}(A) = \sqrt{\langle A, A \rangle}$$

$$= \sqrt{(5.1 + 6.6i)(5.1 - 6.6i) + (7.1 + 7.7i)(7.1 - 7.7i)}$$

$$0.5 = 10i^2$$

$$10i^2 = a^2 + b^2$$

$$= \sqrt{5.1^2 + 6.6^2 + 7.1^2 + 7.7^2} = \sqrt{179.27} = 13.39 \approx 13.39$$

④

$$VA = C \cdot A$$

$$[1 \times 2] \cdot [2 \times 2] = 1 \times 2 \quad [2 \times 2] \cdot [1 \times 1] = 2 \times 1$$

$$VA = \begin{bmatrix} 0+2i & -2i^2 \end{bmatrix}$$

$$\boxed{AV = CV}$$

$$A \cdot V = \begin{bmatrix} 0 & 2i \\ -2i & 0 \end{bmatrix} \begin{bmatrix} i \\ 1 \end{bmatrix} = \begin{bmatrix} 0+2i \\ -2i^2+0 \end{bmatrix} = \begin{bmatrix} 2i \\ -2i^2 \end{bmatrix} = \begin{bmatrix} 2i \\ 2 \end{bmatrix} = 2 \begin{bmatrix} i \\ 1 \end{bmatrix}$$

$$C \cdot V = \begin{bmatrix} 2i \\ 2 \end{bmatrix} \Rightarrow C = 2$$

$$AV = cV$$

$$AV = A \cdot V$$

$$AV = \begin{bmatrix} 0 & -2i \\ +2i & 0 \end{bmatrix} \begin{bmatrix} i \\ 1 \end{bmatrix} = \begin{bmatrix} -2i \\ +2i^2 \end{bmatrix} = \begin{bmatrix} -2i \\ -2 \end{bmatrix}$$

$$c \cdot V = \begin{bmatrix} -2i \\ -2 \end{bmatrix} \Rightarrow c = -2$$