

# 2 Arrays and matrices

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A brief introduction to working with arrays of numbers in Python.  
Last Modified: 27 Jan 2018 Humans Responsible: The Prickly Pythons

## 1 Lists and Numpy arrays

```
In [1]: # Python has built-in 'lists':  
x = [1, 2, 3]
```

```
In [2]: x
```

```
Out[2]: [1, 2, 3]
```

```
In [3]: # But they don't work as you would expect  
x*2
```

```
Out[3]: [1, 2, 3, 1, 2, 3]
```

```
In [4]: # And most vector-operations fail  
x*2.3
```

```
-----  
TypeError                                Traceback (most recent call last)  
  
<ipython-input-4-c4e56f154bc0> in <module>()  
    1 # And most vector-operations fail  
----> 2 x*2.3
```

```
TypeError: can't multiply sequence by non-int of type 'float'
```

```
In [5]: # Numpy: The module for scientific computing with python  
import numpy as np
```

```
In [6]: x = np.array([1,2,3])
```

```
In [7]: x
```

```
Out[7]: array([1, 2, 3])
```

```
In [8]: type(x)
```

```
Out[8]: numpy.ndarray
```

```

In [9]: x.nbytes # Number of Bytes required to store x

Out[9]: 24

In [10]: # Now you can manipulate your array in every way thinkable:
         x*2.3

Out[10]: array([ 2.3,  4.6,  6.9])

In [11]: x/100.

Out[11]: array([ 0.01,  0.02,  0.03])

In [12]: # numpy arrays can be combined with lists
         y = [10.,10,10]
         x+y

Out[12]: array([ 11.,  12.,  13.])

In [13]: x/y

Out[13]: array([ 0.1,  0.2,  0.3])

In [14]: x**2

Out[14]: array([1, 4, 9])

```

## 2 Matrix and vector operations

Let's define three quantities

```

In [15]: x = np.array([1,2,3])
         y = np.array([1,1,1])
         A = np.array([[2,3,5],[7,11,13],[17,19,23]]) # Setting up a matrix

         print(x)
         print(y)
         print(A)

[1 2 3]
[1 1 1]
[[ 2  3  5]
 [ 7 11 13]
 [17 19 23]]

```

**Operation 1:** The dot (or scalar) product,  $\mathbf{x} \cdot \mathbf{y}$ , is

```

In [16]: np.dot(x,y)

Out[16]: 6

```

**Operation 2:** The cross (or vector) product,  $\mathbf{x} \times \mathbf{y}$ , is

```

In [17]: np.cross(x,y)

Out[17]: array([-1,  2, -1])

```

**Operation 3:** The element-wise multiplication, sometimes known as a Hadamard product,  $\mathbf{x} \circ \mathbf{y}$ , is

```
In [18]: x*y
```

```
Out[18]: array([1, 2, 3])
```

**Operation 4:** This is  $A\mathbf{x}$

```
In [19]: np.dot(A,x)
```

```
Out[19]: array([ 23,  68, 124])
```

This is  $\mathbf{x}^T A$

```
In [20]: np.dot(x,A)
```

```
Out[20]: array([ 67,  82, 100])
```

Note: `np.dot(A,x)` is not the same as `A*x`. `A*x` gives the element-wise product of  $\mathbf{x}$  with each rows of  $A$

```
In [21]: A*x
```

```
Out[21]: array([[ 2,  6, 15],
                [ 7, 22, 39],
                [17, 38, 69]])
```

```
In [22]: x*A
```

```
Out[22]: array([[ 2,  6, 15],
                [ 7, 22, 39],
                [17, 38, 69]])
```

**Operation 5:** This is multiplication of the two matrices,  $AA$

```
In [23]: np.dot(A,A)
```

```
Out[23]: array([[110, 134, 164],
                [312, 389, 477],
                [558, 697, 861]])
```

This is element-wise multiplication of  $A$  with itself

```
In [24]: A*A
```

```
Out[24]: array([[ 4,  9, 25],
                [49, 121, 169],
                [289, 361, 529]])
```

### 3 Accessing elements in an array

```
In [25]: # How to access an element in an array:
         x
```

```
Out[25]: array([1, 2, 3])
```

```
In [26]: x[0]
```

```
Out[26]: 1
```

```
In [27]: # Normal parentheses are for callable functions only:
        x(0)
```

```
-----

TypeError                                Traceback (most recent call last)

<ipython-input-27-108f7c32fc4b> in <module>()
      1 # Normal parentheses are for callable functions only:
----> 2 x(0)

TypeError: 'numpy.ndarray' object is not callable
```

```
In [29]: # Slicing
        x[0:2]
```

```
Out[29]: array([1, 2])
```

## 4 Dictionary

```
In [30]: # A dictionary can contain a combination of lists and arrays:
        d = {'Your desired label':[1,2,3], 'A':A}
```

```
In [31]: d['Your desired label']
```

```
Out[31]: [1, 2, 3]
```

```
In [32]: d['A']
```

```
Out[32]: array([[ 2,  3,  5],
                [ 7, 11, 13],
                [17, 19, 23]])
```

```
In [ ]:
```