

Practicando los lenguajes libres de contexto

Equipo con Leonardo Luna

4.1 Give context-free grammars generating the following sets.

- a) The set of palindromes (strings that read the same forward as backward) over alphabet $\{a,b\}$.

$$S \rightarrow \varepsilon \mid a \mid b \mid aSa \mid bSb$$

- c) The set of all strings over alphabet $\{a,b\}$ with exactly twice as many a's as b's.

$$S \rightarrow \varepsilon \mid aSaSb \mid aSbSa \mid bSaSa \mid SS$$

- d) The set of all strings over alphabet $\{a, b, \cdot, +, *, (,), \varepsilon, \emptyset\}$ that are well-formed regular expressions over alphabet $\{a,b\}$. Note that we must distinguish between ε as the empty string and as a symbol in a regular expression. We use ε in the latter case.

$$S \rightarrow \emptyset \mid A$$

$$A \rightarrow \varepsilon \mid a \mid b \mid A + A \mid A \cdot A \mid (A) \mid A^*$$

4.10 Find a CFG with no useless symbols equivalent to

$$S \rightarrow AB \mid CA \quad B \rightarrow BC \mid AB$$

$$A \rightarrow a \quad S \rightarrow aB \mid b$$

We remove B since it does not generate terminals.

$$S \rightarrow CA \quad A \rightarrow a \quad C \rightarrow b$$

4.14 Find a Greibach normal-form grammar equivalent to the following CFG:

$$S \rightarrow AA|0 \quad A \rightarrow SS|1$$

The CFG is already in ChNF as there are no more than 2 terminal symbols and only generators without them being mixed.

$$S \rightarrow AA | 0$$

$$A \rightarrow SS | 1$$

$$Z_1 = S$$

$$Z_2 = A$$

$$Z_1 = Z_2 Z_2 | 0 \quad \text{This is in order}$$

$$Z_2 = Z_1 Z_1 | 1 \quad \text{This is not in order as } Z_2 > Z_1 \text{ So, we substitute}$$

$$Z_2 = Z_2 Z_2 Z_1 | 0Z_1 | 1 \text{ Now it's in order,}$$

$$Z_1 = Z_2 Z_2 | 0 \quad \text{However, there is now recursivity from the left.}$$

So, we create a new generator.

$$Y_1 = Z_2 Z_1 | Z_2 Z_1 Y_1$$

$$Z_1 = Z_2 Z_2 | 0$$

$$Z_2 = 0Z_1 Y_1 | 0Y_1 | 1Y_1 | 1$$

We now have these 3 expressions.

$$Z_1 = 0Z_1 Y_2 Z_2 | 0Z_1 Z_2 | 1Y_1 Z_2 | 1Z_2 | 0$$

$$Z_2 = 0Z_1 Y_1 | 0Y_1 | 1Y_1 | 1$$

$$Y_1 = 0Z_1 Z_1 | 0Z_1 Y_1 Z_1 | 0Z_1 Z_1 Y_1 | 0Z_1 Y_1 Z_1 Y_1 | 1Z_1 | 1Y_1 Z_1 | 1Z_1 Y_1 | 1Y_1 Z_1 Y_1$$