W271-2 - Spring 2016 - HW 2

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Data

In the United States, a 401K is a type of retirement savings plan that is tied to a worker's place of employment. Employees that put money into a 401K enjoy certain tax benefits. Moreover, many employers have a policy of promoting 401K use, by matching some percentage of an employee's contributions. If an employer matches at, say, 50%, for every dollar that an employee puts into a 401k, the employer will put in another 50 cents.

The file 401k_w271.RData contains data on 401k contributions that were filed with the IRS on form 5500. It was collected by Professor L. E. Papke and may have been further modified by the instructors to test your proficiency.

Exercises

Complete the following exercises, following the best practices outlined in class. Place your answers in a written report (pdf, word, or jupyter notebook format) along with relevant R statements and output.

Load the 401k_w271.RData dataset and look at the value of the function desc() to see what variables are included.

```
load("401k_w271.Rdata")
```

Question 1

Your dependent variable will be prate, representing the fraction of a company's employees participating in its 401k plan. Because this variable is bounded between 0 and 1, a linear model without any transformations may not be the most ideal way to analyze the data, but we can still learn a lot from it. Examine the prate variable and comment on the shape of its distribution.

```
# Descriptive statistics of the whole dataset desc
```

```
##
     variable
                                        label
## 1
                  participation rate, percent
       prate
## 2
       mrate
                         401k plan match rate
## 3 totpart
                      total 401k participants
## 4
      totelg
                 total eligible for 401k plan
## 5
                             age of 401k plan
## 6
       totemp total number of firm employees
         sole = 1 if 401k is firm's sole plan
## 7
## 8 ltotemp
                                log of totemp
```

str(data)

```
'data.frame':
                   1534 obs. of 8 variables:
   $ prate : num 26.1 100 97.6 100 82.5 ...
##
   $ mrate : num 0.21 1.42 0.91 0.42 0.53 ...
##
   $ totpart: num 1653 262 166 257 591 ...
##
  $ totelg : num 6322 262 170 257 716 ...
           : int 8 6 10 7 28 7 31 13 21 10 ...
##
   $ age
##
   $ totemp : num 8709 315 275 500 933 ...
   $ sole
           : int 0 1 1 0 1 1 1 0 1 1 ...
##
   $ ltotemp: num 9.07 5.75 5.62 6.21 6.84 ...
   - attr(*, "datalabel")= chr ""
##
   - attr(*, "time.stamp")= chr "25 Jun 2011 23:03"
##
   - attr(*, "formats")= chr "%7.0g" "%7.0g" "%7.0g" "%7.0g" ...
   - attr(*, "types")= int 254 254 254 254 251 254 251 254
  - attr(*, "val.labels")= chr "" "" "" ...
   - attr(*, "var.labels")= chr
                                "participation rate, percent" "401k plan match rate" "total 401k part
## - attr(*, "version")= int 10
```

summary(data)

```
##
                                            totpart
                                                                totelg
        prate
                          mrate
##
           : 3.00
                              :0.0100
                                                    50.0
                                                                        51.0
    Min.
                      Min.
                                                            Min.
                                        Min.
##
    1st Qu.: 78.10
                      1st Qu.:0.3000
                                                   156.2
                                                                       176.0
                                         1st Qu.:
                                                            1st Qu.:
    Median: 95.70
                      Median : 0.4600
                                         Median:
                                                   276.0
                                                                       330.0
##
                                                            Median :
           : 87.56
                              :0.7315
                                                : 1354.2
                                                                    : 1628.5
##
    Mean
                      Mean
                                        Mean
                                                            Mean
##
    3rd Qu.:100.00
                      3rd Qu.:0.8300
                                         3rd Qu.: 749.5
                                                            3rd Qu.: 890.5
                                                                    :70429.0
##
    Max.
           :200.00
                      Max.
                              :4.9100
                                        Max.
                                                :58811.0
                                                            Max.
##
         age
                          totemp
                                             sole
                                                             ltotemp
##
    Min.
           : 4.00
                             :
                                  58
                                               :0.0000
                                                                  : 4.060
                     Min.
                                        Min.
                                                          Min.
##
    1st Qu.: 7.00
                     1st Qu.:
                                 261
                                        1st Qu.:0.0000
                                                          1st Qu.: 5.565
##
    Median: 9.00
                     Median:
                                 588
                                        Median :0.0000
                                                          Median : 6.377
##
    Mean
            :13.18
                     Mean
                                3568
                                        Mean
                                               :0.4876
                                                          Mean
                                                                  : 6.686
                     3rd Qu.:
##
    3rd Qu.:18.00
                                1804
                                        3rd Qu.:1.0000
                                                          3rd Qu.: 7.498
            :51.00
    Max.
                     Max.
                             :144387
                                        Max.
                                               :1.0000
                                                          Max.
                                                                  :11.880
```

Descriptive statistics of prate summary(data\$prate)

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 3.00 78.10 95.70 87.56 100.00 200.00
```

round(stat.desc(data\$prate, desc = TRUE, basic = TRUE, norm = TRUE), 2)

```
##
         nbr.val
                      nbr.null
                                       nbr.na
                                                         min
                                                                       max
##
         1534.00
                           0.00
                                         0.00
                                                        3.00
                                                                    200.00
##
                                                                   SE.mean
           range
                            sum
                                       median
                                                        mean
##
          197.00
                                        95.70
                                                       87.56
                                                                      0.44
                     134314.70
##
   CI.mean.0.95
                            var
                                      std.dev
                                                   coef.var
                                                                  skewness
##
            0.87
                        300.95
                                        17.35
                                                        0.20
                                                                     -0.95
##
       skew.2SE
                      kurtosis
                                     kurt.2SE
                                                 normtest.W
                                                               normtest.p
##
                           4.36
           -7.56
                                        17.44
                                                        0.78
                                                                      0.00
```

```
## 1% 5% 10% 25% 50% 75% 90% 95% 99% 100% ## 31.8 54.0 62.8 78.1 95.7 100.0 100.0 100.0 100.0 200.0
```

data\$prate[data\$prate > 100]

```
## [1] 200.0 177.2 200.0
```

Based on the R output above, prate is one of the 8 variables contained in the dataset. There are 1534 observations of prate, and 0 of them correspond to NA values.

Its minimum and **maximum** values are 3.0 and **200.0**, respectively: the latter must correspond to an error, since a rate cannot be greater than 100%. A further analysis reveals that there are **3 observations** in which **prate** exceeds 100, so we should and shall **discard** them from our analysis.

Its mean and median values are 87.6 and 95.7, respectively.

The excess kurtosis (the kurtosis minus 3) is positive (4.36), which indicates that the distribution of the sample is **leptokurtic** (a more acute peak around the mean and fatter tails than the normal distribution). Its skewness is negative (-0.95), which indicates that the distribution of the sample is **left-skewed** (it has a long left tail). The following Figures confirm both aspects.

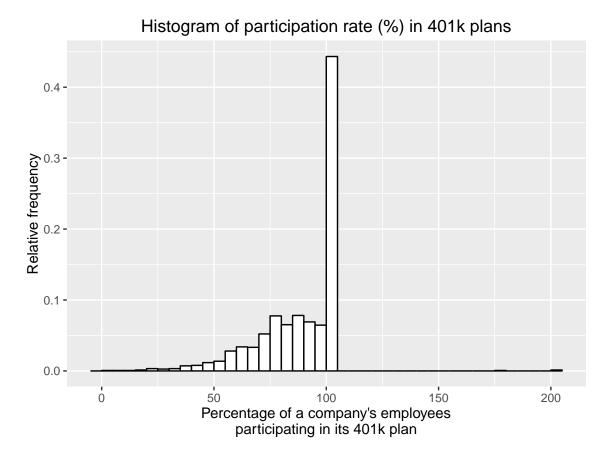


Figure 1: Histogram of participation rate (%) in 401k plans of a company's employees (bin width = 5)

Though hard to see (roughly 44.3% of the observations correspond to the exact value of 100%), the histogram above reveals the one observation with a value of 177.2 and the two observations with a value of 200.0.

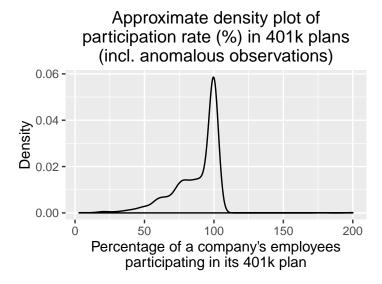


Figure 2: Approximate density plot of participation rate (%) in 401k plans of a company's employees

If we omit the 3 anomalous observations (which we'll do from now on), the (approximate) density plot looks like this (not normal at all):

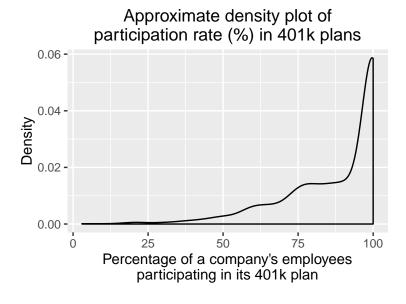


Figure 3: Approximate density plot of participation rate (%) in 401k plans of a company's employees (excluding wrong values, higher than 100%)

Question 2

Your independent variable will be mrate, the rate at which a company matches employee 401k contributions. Examine this variable and comment on the shape of its distribution.

```
# First, discard anomalous observations of prate
data2 <- data[data$prate <= 100, ]</pre>
# Descriptive statistics of prate
summary(data2$mrate)
                    Median
##
      Min. 1st Qu.
                               Mean 3rd Qu.
                                                 Max.
##
     0.010
             0.300
                      0.460
                               0.732
                                       0.830
                                                4.910
round(stat.desc(data2$mrate, desc = TRUE, basic = TRUE, norm = TRUE), 2)
##
        nbr.val
                     nbr.null
                                     nbr.na
                                                      min
                                                                    max
##
        1531.00
                         0.00
                                       0.00
                                                     0.01
                                                                   4.91
##
                          sum
                                     median
                                                     mean
                                                                SE.mean
          range
##
           4.90
                      1120.71
                                                                   0.02
                                       0.46
                                                     0.73
##
  CI.mean.0.95
                          var
                                    std.dev
                                                 coef.var
                                                               skewness
##
           0.04
                         0.61
                                       0.78
                                                     1.07
                                                                   2.59
##
       skew.2SE
                     kurtosis
                                   kurt.2SE
                                               normtest.W
                                                             normtest.p
                                      30.35
##
          20.71
                         7.59
                                                     0.70
                                                                   0.00
round(quantile(data2$mrate, probs = c(1, 5, 10, 25, 50, 75, 90, 95, 99,
                                       100)/100), 1)
```

```
##
     1%
          5%
               10%
                    25%
                          50%
                               75%
                                     90%
                                          95%
                                               99% 100%
              0.2
                    0.3
                          0.5
                                          2.4
##
    0.0
         0.1
                               0.8
                                    1.7
                                               4.1
```

As with prate, there are no NA values of mrate.

Its minimum and maximum values are 0.0 and 4.9 (these values, as those of prate, correspond to percentages).

Its **mean** and **median** values are 0.732 and 0.460, respectively.

The excess kurtosis (the kurtosis minus 3) is positive (7.59), which indicates that the distribution of the sample is **leptokurtic** (a more acute peak around the mean and fatter tails than the normal distribution). Its skewness is positive (2.59), which indicates that the distribution of the sample is **right-skewed** (it has a long right tail). The following Figures confirm both aspects.

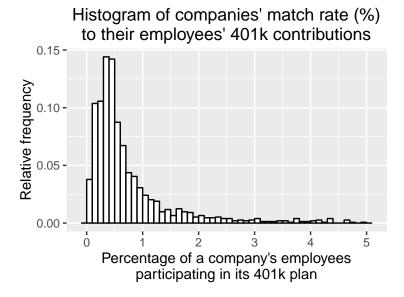


Figure 4: Histogram of companies' match rate (%) to their employees' 401k contributions (bin width = 0.1)

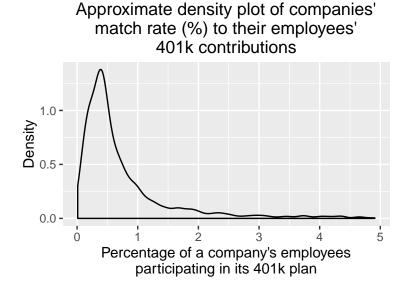


Figure 5: Approximate density plot of companies' match rate (%) to their employees' 401k contributions

Question 3

Generate a scatterplot of prate against mrate. Then estimate the linear regression of prate on mrate. What slope coefficient did you get?

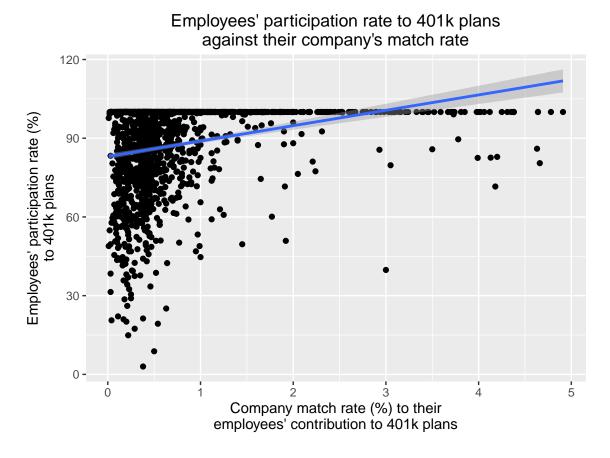


Figure 6: Scatterplot of the participation rate (%) to 401k plans of a company's employees against the match rate (%) of that company to their employees' contributions

```
##
## Call:
## lm(formula = as.formula(paste("prate", paste(params, sep = "",
## collapse = " + "), sep = " ~ ")), data = data2)
##
## Residuals:
## Min    1Q Median   3Q   Max
## -82.289   -8.200   5.186   12.723   16.821
##
## Coefficients:
```

```
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 83.0618  0.5641 147.24  <2e-16 ***
## mrate  5.8623  0.5275 11.11  <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 16.09 on 1529 degrees of freedom
## Multiple R-squared: 0.07475, Adjusted R-squared: 0.07414
## F-statistic: 123.5 on 1 and 1529 DF, p-value: < 2.2e-16
```

Table 1: Effect of a company match rate to 401k plans on its employees' contribution

	Employees' participation rate (%) to 401k plans
Company match rate (%)	5.862***
	(0.527)
Baseline (Intercept)	83.062***
	(0.564)
R^2	0.075
F	123.525
p	0.000
N	1531

Question 4

Is the assumption of zero-conditional mean realistic? Explain your evidence. What are the implications for your OLS coefficients?

Question 5

Is the assumption of homoskedasticity realistic? Provide at least two pieces of evidence to support your conclusion. What are the implications for your OLS analysis?

Question 6

Is the assumption of normal errors realistic? Provide at least two pieces of evidence to support your conclusion. What are the implications for your OLS analysis?

Question 7

Based on the above considerations, what is the standard error of your slope coefficient?

Question 8

Is the effect you find statistically significant, and is it practically significant?

See Figure 6

See Table 1