

# W271-2 – Spring 2016 – HW 1

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## Data

The file `birthweight_w271.RData` contains data from the 1988 National Health Interview Survey, which may have been modified by the instructors to test your proficiency. This survey is conducted by the U.S. Census Bureau and has collected data on individual health metrics since 1957. Like all surveys, a full analysis would require advanced techniques such as those provided by the R survey package. For this exercise, however, you are to treat the data as a true random sample. You will use this dataset to practice interpreting OLS coefficients.

## Exercises

### Question 1

Load the `birthweight` dataset. Note that the actual data is provided in a data table named “`data`”.

Use the following procedures to load the data

- Step 1: put the provided R Workspace `birthweight w271.RData` in the directory of your choice.
- Step 2: Load the dataset using this command: `load("\birthweight.Rdata")`

```
load("birthweight_w271.rdata")
```

### Question 2

Examine the basic structure of the data set using `desc`, `str`, and `summary` to examine all of the variables in the data set. How many variables and observations in the data?

These commands will be useful:

1. `desc`
2. `str(data)`
3. `summary(data)`

```
desc
```

```
##      variable                label
## 1   faminc      1988 family income, $1000s
## 2   cigtax      cig. tax in home state, 1988
## 3   cigprice    cig. price in home state, 1988
## 4    bwght      birth weight, ounces
## 5   fatheduc      father's yrs of educ
## 6   motheduc      mother's yrs of educ
## 7    parity      birth order of child
## 8     male              =1 if male child
## 9    white              =1 if white
## 10    cigs    cigs smked per day while preg
## 11   lbwght              log of bwght
## 12 bwghtlbs      birth weight, pounds
## 13   packs    packs smked per day while preg
## 14  lfaminc              log(faminc)
```

```
str(data)
```

```
## 'data.frame': 1388 obs. of 14 variables:
## $ faminc : num 13.5 7.5 0.5 15.5 27.5 7.5 65 27.5 27.5 37.5 ...
## $ cigtax : num 16.5 16.5 16.5 16.5 16.5 16.5 16.5 16.5 16.5 16.5 ...
## $ cigprice: num 122 122 122 122 122 ...
## $ bwght : num 109 133 129 126 134 118 140 86 121 129 ...
## $ fatheduc: int 12 6 NA 12 14 12 16 12 12 16 ...
## $ motheduc: int 12 12 12 12 12 14 14 14 17 18 ...
## $ parity : int 1 2 2 2 2 6 2 2 2 2 ...
## $ male : int 1 1 0 1 1 1 0 0 0 0 ...
## $ white : int 1 0 0 0 1 0 1 0 1 1 ...
## $ cigs : int 0 0 0 0 0 0 0 0 0 0 ...
## $ lbwght : num 4.69 4.89 4.86 4.84 4.9 ...
## $ bwghtlbs: num 6.81 8.31 8.06 7.88 8.38 ...
## $ packs : num 0 0 0 0 0 0 0 0 0 0 ...
## $ lfaminc : num 2.603 2.015 -0.693 2.741 3.314 ...
## - attr(*, "datalabel")= chr ""
## - attr(*, "time.stamp")= chr "25 Jun 2011 23:03"
## - attr(*, "formats")= chr "%9.0g" "%9.0g" "%9.0g" "%8.0g" ...
## - attr(*, "types")= int 254 254 254 252 251 251 251 251 251 251 ...
## - attr(*, "val.labels")= chr "" "" "" "" ...
## - attr(*, "var.labels")= chr "1988 family income, $1000s" "cig. tax in home state, 1988" "cig. pri
## - attr(*, "version")= int 10
```

```
summary(data)
```

```
##      faminc      cigtax      cigprice      bwght
## Min.   : 0.50   Min.   : 2.00   Min.   :103.8   Min.   : 0.0
## 1st Qu.:14.50   1st Qu.:15.00   1st Qu.:122.8   1st Qu.:106.0
## Median :27.50   Median :20.00   Median :130.8   Median :119.0
## Mean   :29.03   Mean   :19.55   Mean   :130.6   Mean   :117.9
## 3rd Qu.:37.50   3rd Qu.:26.00   3rd Qu.:137.0   3rd Qu.:132.0
## Max.   :65.00   Max.   :38.00   Max.   :152.5   Max.   :271.0
##
##      fatheduc      motheduc      parity      male
## Min.   : 1.00   Min.   : 2.00   Min.   :1.000   Min.   :0.0000
## 1st Qu.:12.00   1st Qu.:12.00   1st Qu.:1.000   1st Qu.:0.0000
## Median :12.00   Median :12.00   Median :1.000   Median :1.0000
## Mean   :13.19   Mean   :12.94   Mean   :1.633   Mean   :0.5209
## 3rd Qu.:16.00   3rd Qu.:14.00   3rd Qu.:2.000   3rd Qu.:1.0000
## Max.   :18.00   Max.   :18.00   Max.   :6.000   Max.   :1.0000
## NA's   :196     NA's   :1
##      white      cigs      lbwght      bwghtlbs
## Min.   :0.0000   Min.   : 0.000   Min.   :0.000   Min.   : 0.000
## 1st Qu.:1.0000   1st Qu.: 0.000   1st Qu.:4.663   1st Qu.: 6.625
## Median :1.0000   Median : 0.000   Median :4.779   Median : 7.438
## Mean   :0.7846   Mean   : 2.087   Mean   :4.726   Mean   : 7.366
## 3rd Qu.:1.0000   3rd Qu.: 0.000   3rd Qu.:4.883   3rd Qu.: 8.250
## Max.   :1.0000   Max.   :50.000   Max.   :5.602   Max.   :16.938
##
##      packs      lfaminc
## Min.   :0.0000   Min.   : -0.6931
```

```
## 1st Qu.:0.0000    1st Qu.: 2.6741
## Median :0.0000    Median : 3.3142
## Mean   :0.1044    Mean    : 3.0713
## 3rd Qu.:0.0000    3rd Qu.: 3.6243
## Max.    :2.5000    Max.     : 4.1744
##
```

As shown by `desc` and `str(data)`, there are 14 variables and 1388 observations in the data.

### Question 3

As we mentioned in the live session, it is important to start with a question (or a hypothesis) when conducting regression modeling. In this exercise, we are in the question: “Do mothers who smoke have babies with lower birth weight?”

The dependent variable of interest is `bwght`, representing birthweight in ounces. Examine this variable using both tabulated summary and graphs. Specifically,

1. Summarize the variable `bwght`: `summary(data$bwght)`

```
summary(data$bwght)
```

```
##      Min. 1st Qu.  Median      Mean 3rd Qu.      Max.
##      0.0   106.0   119.0   117.9   132.0   271.0
```

2. You may also use the quantile function: `quantile(data$bwght)`. List the following quantiles: 1%, 5%, 10%, 25%, 50%, 75%, 90%, 95%, 99%

```
quantile(data$bwght, probs = c(1, 5, 10, 25, 50, 75, 90, 95, 99)/100)
```

```
##      1%      5%     10%     25%     50%     75%     90%     95%     99%
## 42.35  83.00  93.00 106.00 119.00 132.00 143.00 149.00 160.13
```

3. Plot the histogram of `bwght` and comment on the shape of its distribution. Try different bin sizes and comment how it affects the shape of the histogram. Remember to label the graph clearly. You will also need a title for the graph.

We tested several bin widths, though here only three (5, 10, and 20) are plotted—they’re enough to show that the smaller the bin size, the closer the histogram looks to the density plot (which is close to the normal distribution—except for a long left tail—in this case).

The first bin size (5) is plotted below using `hist` and `ggplot`. The rest are plotted using `ggplot` exclusively.

```
# Use hist and bin width = 5
bin_width = 5
hist(data$bwght, breaks = seq(floor(min(data$bwght)/bin_width)*bin_width,
                              ceiling(max(data$bwght)/bin_width)*bin_width,
                              by = bin_width),
      xlab = "Birth weight (ounces)", ylab = "Count",
      main = "Histogram of birth weight")
```

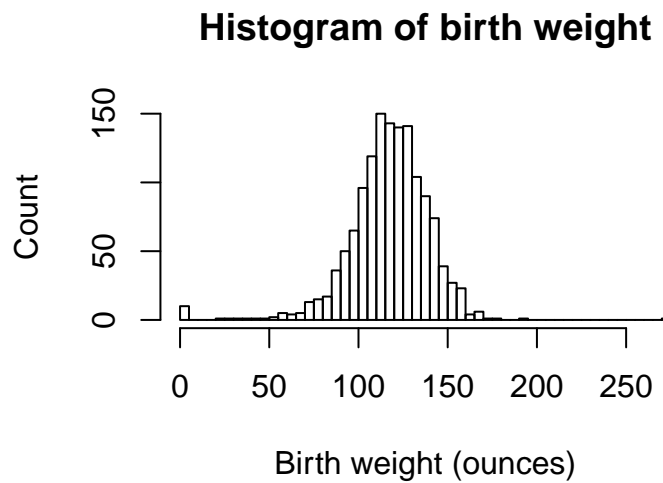


Figure 1: Histogram of birth weight (in ounces), using `hist` and bin width = 5

```
# Use ggplot and bin width = 5
ggplot(data = data, aes(bwght)) +
  geom_histogram(colour = 'black', fill = 'white',
                 binwidth = bin_width) +
  labs(x = "Birth weight (ounces)", y = "Count",
       title = "Histogram of birth weight")
```

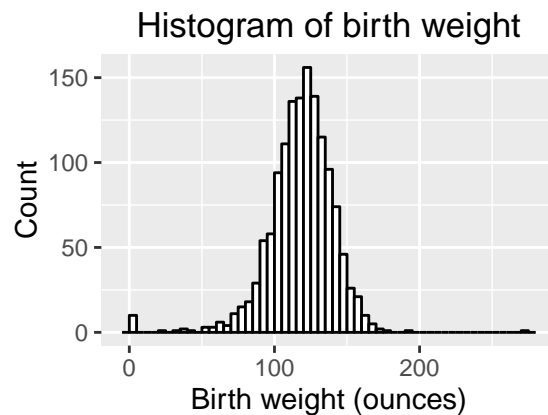


Figure 2: Histogram of birth weight (in ounces), using `ggplot` and bin width = 5

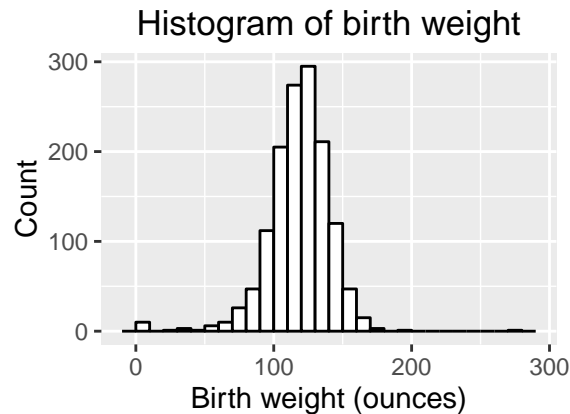


Figure 3: Histogram of birth weight (in ounces), using `ggplot` and bin width = 10

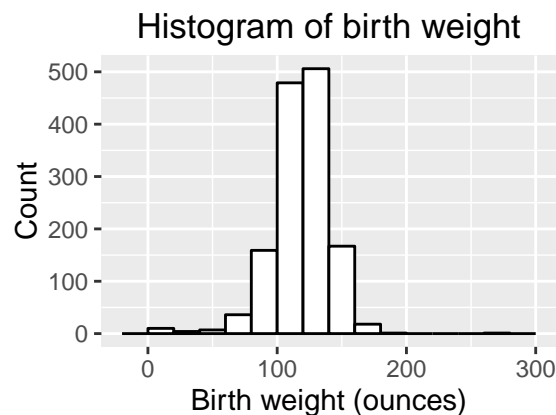


Figure 4: Histogram of birth weight (in ounces), using `ggplot` and bin width = 20

4. **This is a more open-ended question:** Have you noticed anything “strange” with the `bwght` variable and the shape of histogram this variable? If so, please elaborate on your observations and investigate any issues you have identified.

The left tail of the distribution is quite long for such variable. Actually, there are 10 observations with a weight equal to zero, which makes no sense. If we exclude those observations, the minimum birth weight is 23 ounces, which still seems very low but might be possible.

There are no NA values for `data$bwght` so it seems likely that missing values have been coded as 0.

## Question 4

Examine the variable `cigs`, which represents number of cigarettes smoked each day by the mother while pregnant. Conduct the same analysis as in question 3.

```
summary(data$cigs)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##    0.000  0.000   0.000   2.087  0.000   50.000
```

```
## 1% 5% 10% 25% 50% 75% 90% 95% 99%
## 0 0 0 0 0 0 10 20 20
```

```
# Use ggplot and bin width = 1
bin_width = 1
ggplot(data = data, aes(cigs)) +
  geom_histogram(colour = 'black', fill = 'white',
                binwidth = bin_width) +
  labs(x = "Cigarettes smoked each day\nby the mother while pregnant",
       y = "Count",
       title = "Histogram of cigarettes smoked each day\nby the mother while pregnant")
```

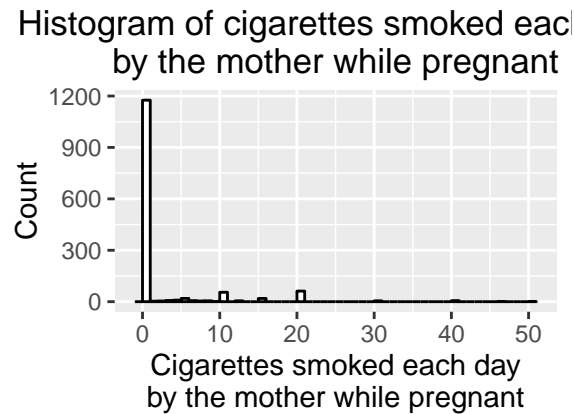


Figure 5: Histogram of cigarettes smoked each day by the mother while pregnant, bin width = 1

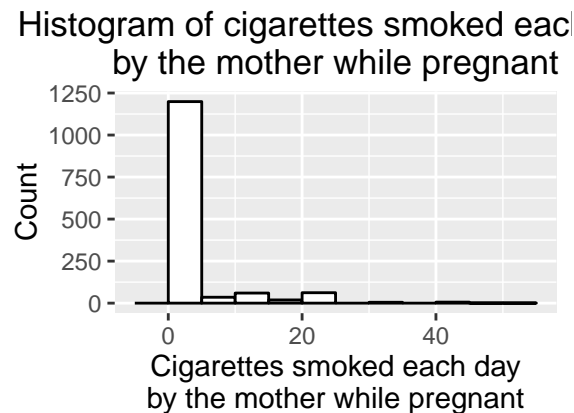


Figure 6: Histogram of cigarettes smoked each day by the mother while pregnant, bin width = 5

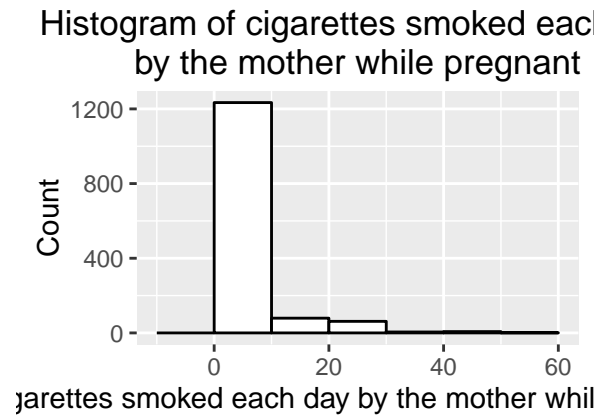


Figure 7: Histogram of cigarettes smoked each day by the mother while pregnant, bin width = 10

cigs has a heavy-tailed distribution, similar to a Pareto one. This makes sense, since most of the women do not smoke while pregnant.

### Question 5

Generate a scatterplot of bwght against cigs. Based on the appearance of this plot, how much of the variation in bwght do you think can be explained by cigs?

```
ggplot(data = data, aes(cigs, bwght)) +  
  geom_point() +  
  labs(x = "Cigarettes smoked each day by the mother while pregnant",  
       y = "Birth weight (ounces)",  
       title = "Cigarettes smoked by the mother\nagainst birth weight") +  
  geom_smooth(method = "lm")
```



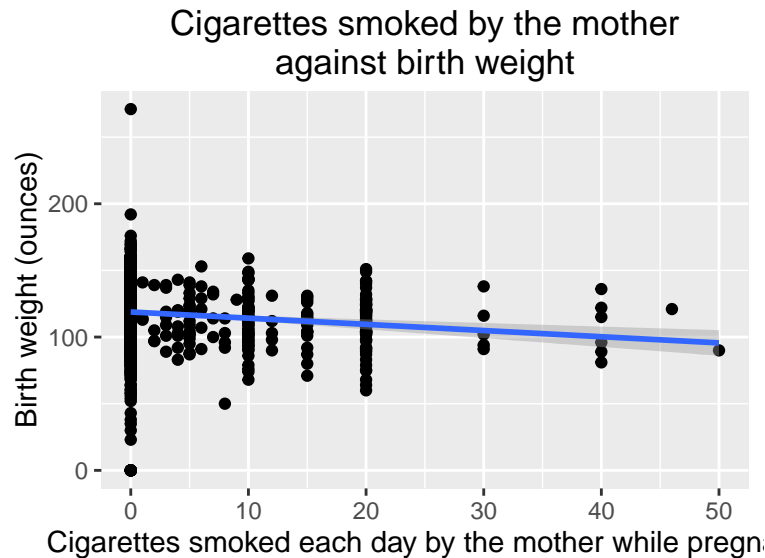


Figure 8: Scatterplot of birth weight (in ounces) against cigarettes smoked each day by the mother while pregnant

There seems to be a negative relationship between the number of cigarettes smoked each day by the mother while pregnant and the birth weight of the child (i.e., the more a mother smokes, the less her child will weigh), but since `cigs` only takes a few values (mainly 0) I don't think it explains a lot of the variation in `bwght`.

## Question 6

Estimate the simple linear regression of `bwght` on `cigs`. What coefficient estimates and the standard errors associated with the coefficient estimates do you get? Interpret the results. Note that you may have to “take care of” any potential data issues before building a regression model.

```
params <- "cigs"
model <- lm(as.formula(paste("bwght", paste(params, sep = "",
                                           collapse = " + "), sep = " ~ ")),
           data = data[data$bwght != 0, ])
summary(model)
```

```
##
## Call:
## lm(formula = as.formula(paste("bwght", paste(params, sep = "",
##      collapse = " + "), sep = " ~ ")), data = data[data$bwght !=
##      0, ])
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -96.790 -11.790   0.357  13.210 151.210
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 119.78960    0.57595  207.987  < 2e-16 ***
```

```
## cigs          -0.51470    0.09073  -5.673 1.71e-08 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 20.17 on 1376 degrees of freedom
## Multiple R-squared:  0.02285,    Adjusted R-squared:  0.02214
## F-statistic: 32.18 on 1 and 1376 DF,  p-value: 1.711e-08

## [1] 3 2
```

Table 1: Effect of the number of cigarettes smoked each day by the mother while pregnant on the birth weight

	Birth weight (ounces)
Cigarettes smoked each day by the mother	-0.515*** (0.091)
Baseline (Intercept)	119.790*** (0.576)
$R^2$	0.023
F	32.179
p	0.000
N	1388

Regression showed a small negative effect of maternal cigarette smoking on birthweight ( $\beta_1 = -0.45$  (0.10),  $p < .001$ ,  $R^2 = 0.014$ ). This represents a practically small but not meaningless effect. For example, among smokers, the average daily cigarettes smoked is 13.7. Thus, the mean cigarette smoker would have a 6 Oz. lower expected birth weight, other factors held constant.

## Question 7

Now, introduce a new independent variable, `faminc`, representing family income in thousands of dollars. Examine this variable using the same analysis as in question 3. In addition, produce a scatterplot matrix of `bwght`, `cigs`, and `faminc`. Use the following command (as a starting point):

```
library(car)
scatterplot.matrix(bwght + cigs + faminc, data = data2)
```

Note that the `car` package is needed in order to use the `scatterplot.matrix` function.

```
summary(data$faminc)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      0.50  14.50   27.50   29.03  37.50   65.00
```

```
quantile(data$faminc, probs = c(1, 5, 10, 25, 50, 75, 90, 95, 99)/100)
```

```
##      1%    5%   10%  25%  50%  75%  90%  95%  99%
##      0.5   3.5   6.5  14.5 27.5 37.5 65.0 65.0 65.0
```

```
bin_width = 2
ggplot(data = data, aes(faminc)) +
  geom_histogram(colour = 'black', fill = 'white',
                 binwidth = bin_width) +
  labs(x = "Family income (thousands of dollars)", y = "Count",
       title = "Histogram of family income")
```

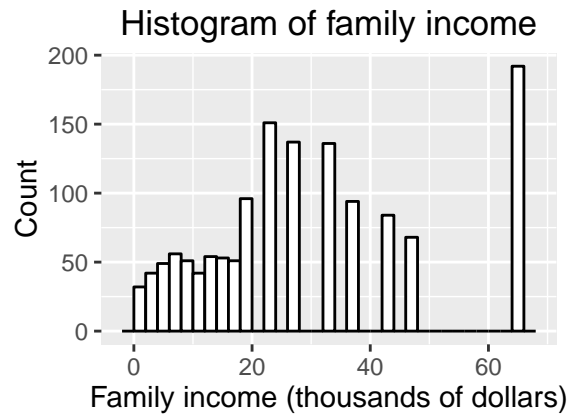


Figure 9: Histogram of family income (in thousands of dollars), bin width = 2

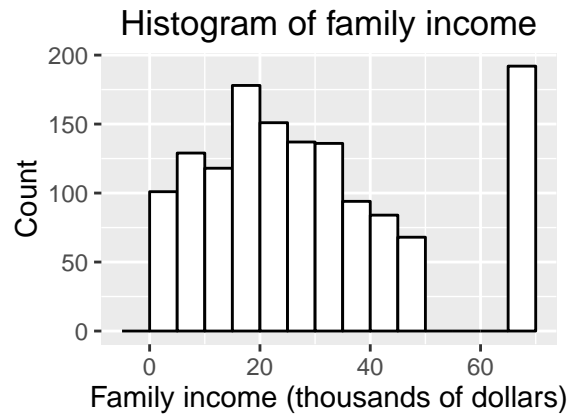


Figure 10: Histogram of family income (in thousands of dollars), bin width = 5

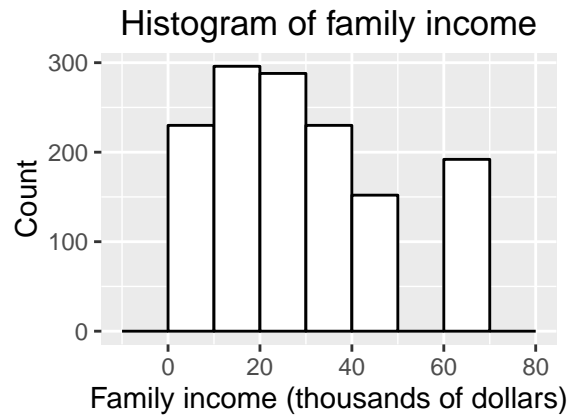


Figure 11: Histogram of family income (in thousands of dollars), bin width = 10

```
ggplot(data = data, aes(faminc, bwght)) +  
  geom_point() +  
  labs(x = "Family income (thousands of dollars)",  
       y = "Birth weight (ounces)",  
       title = "Family income against birth weight") +  
  geom_smooth(method = "lm")
```



Figure 12: Scatterplot of birth weight (in ounces) against family income (in thousands of dollars)

```
scatterplotMatrix(~ bwght + cigs + faminc, data[data$bwght !=0, ])
```

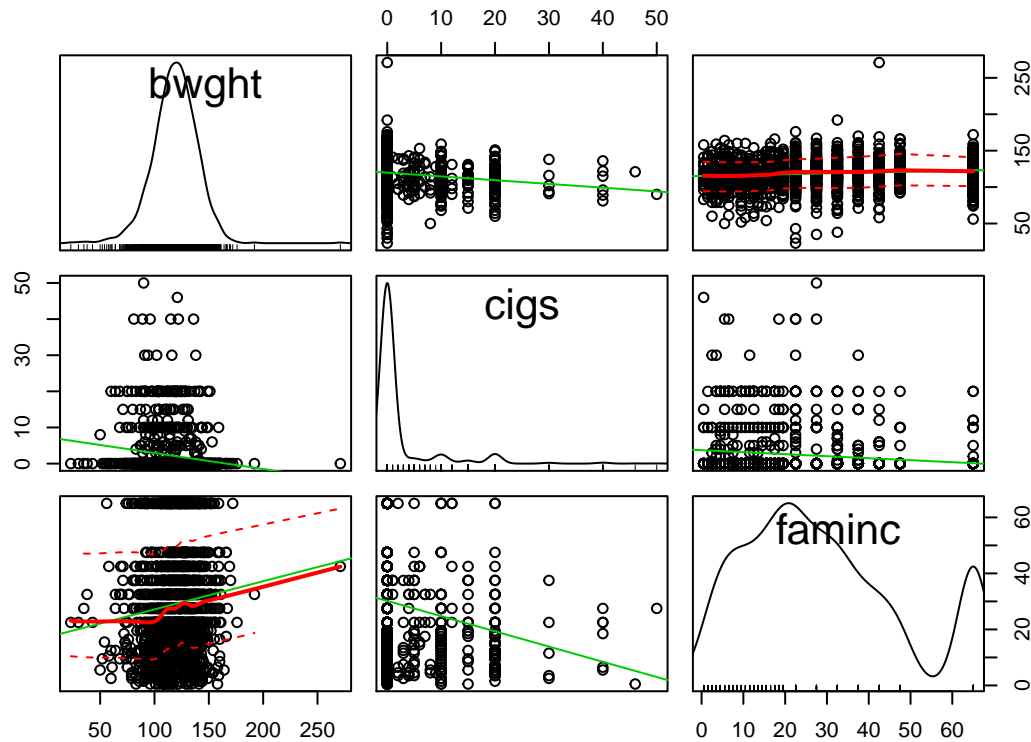


Figure 13: Scatterplot matrix of birth weight, cigarettes smoked each day by the mother while pregnant, and family income

## Question 8

Regress `bwght` on both `cigs` and `faminc`. What coefficient estimates and the standard errors associated with the coefficient estimates do you get? Interpret the results.

```
params <- c("cigs", "faminc")
model2 <- lm(as.formula(paste("bwght", paste(params, sep = "",
                                             collapse = " + "), sep = " ~ ")),
             data = data[data$bwght !=0, ])
summary(model2)
```

```
##
## Call:
## lm(formula = as.formula(paste("bwght", paste(params, sep = "",
##      collapse = " + "), sep = " ~ ")), data = data[data$bwght !=
##      0, ])
##
## Residuals:
```

```
##      Min      1Q  Median      3Q      Max
## -96.075 -11.592   0.722  13.262 150.062
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 116.97933    1.05363  111.025 < 2e-16 ***
## cigs        -0.46407    0.09182   -5.054 4.91e-07 ***
## faminc       0.09314    0.02928    3.181  0.0015 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 20.11 on 1375 degrees of freedom
## Multiple R-squared:  0.02999,    Adjusted R-squared:  0.02858
## F-statistic: 21.25 on 2 and 1375 DF,  p-value: 8.109e-10
```

Table 2: Effect of the number of cigarettes smoked each day by the mother while pregnant and the family income on the birth weight

	Birth weight (ounces)
Cigarettes smoked each day by the mother	-0.464*** (0.092)
Family income (thousands of dollars)	0.093** (0.029)
Baseline (Intercept)	116.979*** (1.054)
$R^2$	0.030
F	21.255
p	0.000
N	1388

### Question 9

Explain, in your own words, what the coefficient on `cigs` in the multiple regression means, and how it is different than the coefficient on `cigs` in the simple regression? Please provide the intuition to explain the difference, if any.

### Question 10

Which coefficient for `cigs` is more negative than the other? Suggest an explanation for why this is so.