W271-2 - Spring 2016 - Lab 2

Juanjo Carin, Kevin Davis, Ashley Levato, Minghu Song

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```
##
## Please cite as:
##
## Please cite as:
##
## Hlavac, Marek (2015). stargazer: Well-Formatted Regression and Summary Statistics Tables.
## R package version 5.2. http://CRAN.R-project.org/package=stargazer
##
##
## Attaching package: 'zoo'
##
## The following objects are masked from 'package:base':
##
## as.Date, as.Date.numeric
```

Question 1: Broken Rulers

You have a ruler of length 1 and you choose a place to break it using a uniform probability distribution. Let random variable X represent the length of the left piece of the ruler. X is distributed uniformly in [0,1]. You take the left piece of the ruler and once again choose a place to break it using a uniform probability distribution. Let random variable Y be the length of the left piece from the second break.

- 1. Find the conditional expectation of Y given X, E(Y|X).
- 2. Find the unconditional expectation of Y. One way to do this is to apply the law of iterated expectations, which states that E(Y) = E(E(Y|X)). The inner expectation is the conditional expectation computed above, which is a function of X. The outer expectation finds the expected value of this function.
- 3. Write down an expression for the joint probability density function of X and Y, $f_{X,Y}(x,y)$.
- 4. Find the conditional probability density function of X given Y, $f_{X|Y}$.
- 5. Find the expectation of X, given that Y is 1/2, E(X|Y=1/2).

Question 2: Investing

Suppose that you are planning an investment in three different companies. The payoff per unit you invest in each company is represented by a random variable. A represents the payoff per unit invested in the first company, B in the second, and C in the third. A, B, and C are independent of each other. Furthermore, Var(A) = 2Var(B) = 3Var(C).

You plan to invest a total of one unit in all three companies. You will invest amount a in the first company, b in the second, and c in the third, where $a,b,c \in [0,1]$ and a+b+c=1. Find, the values of a, b, and c that minimize the variance of your total payoff.

Question 3: Turtles

Next, suppose that the lifespan of a species of turtle follows a uniform distribution over $[0, \theta]$. Here, parameter θ represents the unknown maximum lifespan. You have a random sample of n individuals, and measure the lifespan of each individual i to be y_i .

- 1. Write down the likelihood function, $l(\theta)$ in terms of y_1, y_2, \dots, y_n .
- 2. Based on the previous result, what is the maximum-likelihood estimator for θ ?
- 3. Let $\hat{\theta}_{ml}$ be the maximum likelihood estimator above. For the simple case that $n \ge 1$, what is the expectation of $\hat{\theta}_{ml}$, given θ ?
- 4. Is the maximum likelihood estimator biased?
- 5. For the more general case that $n \ge 1$, what is the expectation of $\hat{\theta}_{ml}$?
- 6. Is the maximum likelihood estimator consistent?

Question 4: CLM 1

Background

The file WageData2.csv contains a dataset that has been used to quantify the impact of education on wage. One of the reasons we are proving another wage-equation exercise is that this area by far has the most (and most well-known) applications of instrumental variable techniques, the endogenity problem is obvious in this context, and the datasets are easy to obtain.

The Data

You are given a sample of 1000 individuals with their wage, education level, age, working experience, race (as an indicator), father's and mother's education level, whether the person lived in a rural area, whether the person lived in a city, IQ score, and two potential instruments, called z1 and z2.

The dependent variable of interest is wage (or its transformation), and we are interested in measuring "return" to education, where return is measured in the increase (hopefully) in wage with an additional year of education.

Question 4.1

Conduct an univariate analysis (using tables, graphs, and descriptive statistics found in the last 7 lectures) of all of the variables in the dataset.

Also, create two variables: (1) natural log of wage (name it logWage) (2) square of experience (name it experienceSquare)

```
d<-read.csv("WageData2.csv")
summary(d)</pre>
```

```
##
          X
                           wage
                                          education
                                                           experience
               5.0
                             : 127.0
                                                                 : 0.000
##
    Min.
           :
                      Min.
                                               : 2.00
                      1st Qu.: 400.0
##
    1st Qu.: 715.5
                                        1st Qu.:12.00
                                                         1st Qu.: 6.000
##
   Median :1431.5
                      Median: 543.0
                                        Median :12.00
                                                         Median: 8.000
           :1466.7
                              : 578.8
                                                :13.22
##
    Mean
                      Mean
                                        Mean
                                                         Mean
                                                                 : 8.788
##
    3rd Qu.:2212.0
                      3rd Qu.: 702.5
                                        3rd Qu.:16.00
                                                         3rd Qu.:11.000
           :3009.0
                                                :18.00
##
    Max.
                      Max.
                              :2404.0
                                        Max.
                                                         Max.
                                                                 :23.000
##
##
         age
                       raceColor
                                      dad_education
                                                       mom_education
##
    Min.
           :24.00
                            :0.000
                                      Min.
                                             : 0.00
                                                       Min.
                                                              : 0.00
                     Min.
##
    1st Qu.:25.00
                     1st Qu.:0.000
                                      1st Qu.: 8.00
                                                       1st Qu.: 8.00
   Median :27.00
                     Median : 0.000
                                      Median :11.00
                                                       Median :12.00
##
##
    Mean
           :28.01
                     Mean
                            :0.238
                                      Mean
                                             :10.18
                                                       Mean
                                                              :10.45
    3rd Qu.:30.00
##
                     3rd Qu.:0.000
                                      3rd Qu.:12.00
                                                       3rd Qu.:12.00
##
    Max.
           :34.00
                     Max.
                            :1.000
                                      Max.
                                             :18.00
                                                       Max.
                                                              :18.00
##
                                      NA's
                                              :239
                                                       NA's
                                                               :128
                          city
##
        rural
                                            z.1
                                                            z2
           :0.000
                                             :0.00
##
   Min.
                     Min.
                             :0.000
                                      Min.
                                                      Min.
                                                              :0.000
    1st Qu.:0.000
                     1st Qu.:0.000
                                      1st Qu.:0.00
                                                      1st Qu.:0.000
    Median :0.000
##
                     Median :1.000
                                      Median:0.00
                                                      Median :1.000
           :0.391
                            :0.712
                                                      Mean
    Mean
                     Mean
                                      Mean
                                             :0.44
                                                              :0.686
```

```
3rd Qu.:1.000
                  3rd Qu.:1.000
                                 3rd Qu.:1.00
                                               3rd Qu.:1.000
##
  Max. :1.000
                  Max. :1.000
                                 Max. :1.00
                                               Max. :1.000
##
##
      IQscore
                     logWage
##
  Min.
         : 50.0
                  Min.
                         :4.844
  1st Qu.: 93.0
                 1st Qu.:5.991
##
## Median :103.0
                 Median :6.297
## Mean
         :102.3
                  Mean :6.263
## 3rd Qu.:113.0
                  3rd Qu.:6.555
## Max. :144.0
                  Max. :7.785
## NA's
          :316
```

head(d)

```
##
       X wage education experience age raceColor dad_education mom_education
                                10 28
## 1 191 951
                     12
                                               0
                                                            NΑ
## 2 2059
          288
                      8
                                11 25
                                               1
                                                            NA
                                                                          7
                     12
## 3 2072 509
                                               0
                                                            12
                                                                          9
                                 6 24
## 4 945
          647
                     18
                                 5 29
                                               0
                                                            12
                                                                         12
                     10
                                11 27
                                                            5
                                                                          5
## 5 1920
          225
                                               1
## 6 1927 454
                     10
                                   27
                                               1
                                                            NA
                                                                           1
                                11
##
    rural city z1 z2 IQscore logWage
## 1
             1 1 1
                         122 6.857514
## 2
        1
             0 0 1
                          NA 5.662960
             1 0 0
## 3
        1
                         127 6.232448
             1 0 1
        0
## 4
                         110 6.472346
             0 0 1
## 5
        1
                          NA 5.416100
## 6
             0 0 1
                          NA 6.118097
        1
```

```
# Multiple plot function
# ggplot objects can be passed in ..., or to plotlist (as a list of ggplot objects)
# - cols: Number of columns in layout
# - layout: A matrix specifying the layout. If present, 'cols' is ignored.
# If the layout is something like matrix(c(1,2,3,3), nrow=2, byrow=TRUE),
# then plot 1 will go in the upper left, 2 will go in the upper right, and
# 3 will go all the way across the bottom.
multiplot <- function(..., plotlist=NULL, file, cols=1, layout=NULL) {
 library(grid)
  # Make a list from the ... arguments and plotlist
 plots <- c(list(...), plotlist)</pre>
 numPlots = length(plots)
  # If layout is NULL, then use 'cols' to determine layout
  if (is.null(layout)) {
   # Make the panel
    # ncol: Number of columns of plots
```

```
# nrow: Number of rows needed, calculated from # of cols
    layout <- matrix(seq(1, cols * ceiling(numPlots/cols)),</pre>
                     ncol = cols, nrow = ceiling(numPlots/cols))
  }
  if (numPlots==1) {
    print(plots[[1]])
  } else {
    # Set up the page
    grid.newpage()
    pushViewport(viewport(layout = grid.layout(nrow(layout), ncol(layout))))
    # Make each plot, in the correct location
    for (i in 1:numPlots) {
      # Get the i, j matrix positions of the regions that contain this subplot
      matchidx <- as.data.frame(which(layout == i, arr.ind = TRUE))</pre>
      print(plots[[i]], vp = viewport(layout.pos.row = matchidx$row,
                                      layout.pos.col = matchidx$col))
    }
  }
}
##########
p1<-ggplot(d, aes(x=wage)) + geom_histogram(binwidth=100)
p2<-ggplot(d, aes(x=education)) + geom_histogram(binwidth=2)</pre>
p3<-ggplot(d, aes(x=experience)) + geom_histogram(binwidth=2)
p4<-ggplot(d, aes(x=age)) + geom_histogram(binwidth=1)
p5<-ggplot(d, aes(x=raceColor)) + geom_histogram(binwidth=.5)
p6<-ggplot(d, aes(x=dad_education)) + geom_histogram(binwidth=1)
p7<-ggplot(d, aes(x=mom_education)) + geom_histogram(binwidth=1)
p8<-ggplot(d, aes(x=rural)) + geom_histogram(binwidth=.5)
p9<-ggplot(d, aes(x=city)) + geom_histogram(binwidth=.5)
multiplot(p1, p2, p3, p4, p5, p6, p7, p8, p9, cols=3)
```

```
d$logWage<-log(d$wage)
d$experienceSquare<-d$experience^2</pre>
```

8

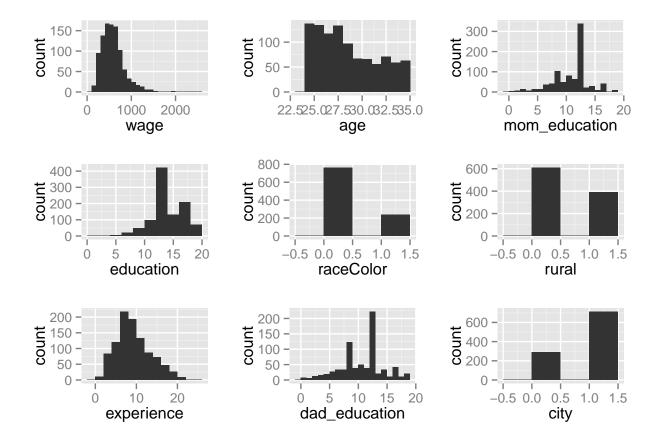


Figure 1:

Question 4.2

Conduct a bivariate analysis (using tables, graphs, descriptive statistics found in the last 7 lectures) of wage and logWage and all the other variables in the datasets.

```
p2.1<-ggplot(d, aes(wage, education)) +
  geom point() +
  labs(x = "Wage",
       y = "Education") +
  geom_smooth(method = "lm")
p2.2<-ggplot(d, aes(log(wage), education)) +
  geom_point() +
  labs(x = "Log(Wage)",
       y = "Education") +
  geom_smooth(method = "lm")
p2.3<-ggplot(d, aes(wage, experience)) +
  geom point() +
  labs(x = "Wage",
       y = "Experience") +
  geom_smooth(method = "lm")
p2.4<-ggplot(d, aes(log(wage), experience)) +
  geom_point() +
  labs(x = "Log(Wage)",
       y = "Experience") +
  geom_smooth(method = "lm")
p2.5<-ggplot(d, aes(wage, age)) +
  geom_point() +
  labs(x = "Wage",
       y = "Age") +
  geom_smooth(method = "lm")
p2.6<-ggplot(d, aes(log(wage), age)) +
  geom_point() +
  labs(x = "Log(Wage)",
       y = "Age") +
  geom_smooth(method = "lm")
p2.7<-ggplot(d, aes(wage, raceColor)) +
  geom_point() +
  labs(x = "Wage",
       y = "Race") +
  geom_smooth(method = "lm")
p2.8<-ggplot(d, aes(log(wage), raceColor)) +
  geom_point() +
  labs(x = "Log(Wage)",
       y = "Race") +
  geom_smooth(method = "lm")
p2.9<-ggplot(d, aes(wage, dad_education)) +
```

```
geom_point(na.rm = T) +
  labs(x = "Wage",
       y = "Father's Education") +
  geom_smooth(method = "lm", na.rm = T)
p2.10<-ggplot(d, aes(log(wage), dad_education)) +
  geom_point(na.rm = T) +
  labs(x = "Log(Wage)",
       y = "Father's Education") +
  geom_smooth(method = "lm", na.rm = T)
p2.11<-ggplot(d, aes(wage, mom_education)) +</pre>
  geom_point(na.rm = T) +
  labs(x = "Wage",
       y = "Mother's Education") +
  geom_smooth(method = "lm", na.rm = T)
p2.12<-ggplot(d, aes(log(wage), mom_education)) +
  geom_point(na.rm = T) +
  labs(x = "Log(Wage)",
       y = "Mother's Education") +
  geom_smooth(method = "lm", na.rm = T)
p2.13<-ggplot(d, aes(wage, rural)) +
  geom_point(na.rm = T) +
  labs(x = "Wage",
       y = "Location - Rural") +
  geom_smooth(method = "lm", na.rm = T)
p2.14<-ggplot(d, aes(log(wage), rural)) +
  geom_point(na.rm = T) +
  labs(x = "Log(Wage)",
       y = "Location - Rural") +
  geom_smooth(method = "lm", na.rm = T)
p2.15<-ggplot(d, aes(wage, city)) +
  geom_point(na.rm = T) +
  labs(x = "Wage",
       y = "Location - City") +
  geom_smooth(method = "lm", na.rm = T)
p2.16<-ggplot(d, aes(log(wage), city)) +
  geom_point(na.rm = T) +
  labs(x = "Log(Wage)",
       y = "Location - City") +
  geom_smooth(method = "lm", na.rm = T)
p2.17<-ggplot(d, aes(wage, IQscore)) +
  geom_point(na.rm = T) +
  labs(x = "Wage",
       y = "IQ") +
  geom_smooth(method = "lm", na.rm = T)
```

```
p2.18<-ggplot(d, aes(log(wage), IQscore)) +
  geom_point(na.rm = T) +
  labs(x = "Log(Wage)",
        y = "IQ") +
  geom_smooth(method = "lm", na.rm = T)

multiplot(p2.1, p2.2, p2.3, p2.4, cols=2)</pre>
```

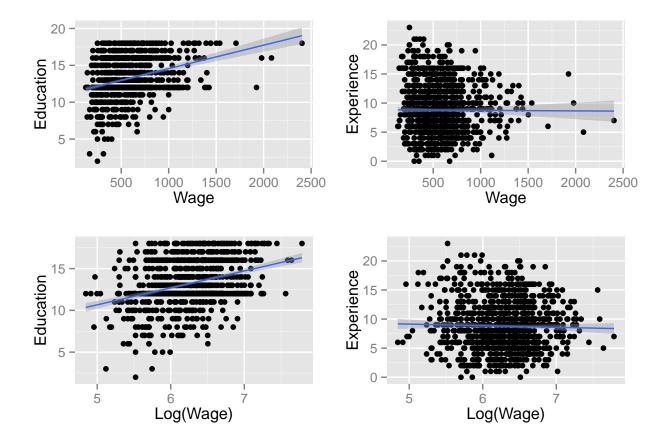


Figure 2:

```
multiplot(p2.5, p2.6, p2.7, p2.8, cols=2)
multiplot(p2.9,p2.10, p2.11, p2.12, cols=2)
multiplot(p2.13, p2.14, p2.15, p2.16, cols=2)
multiplot(p2.17, p2.18, cols=2)
```

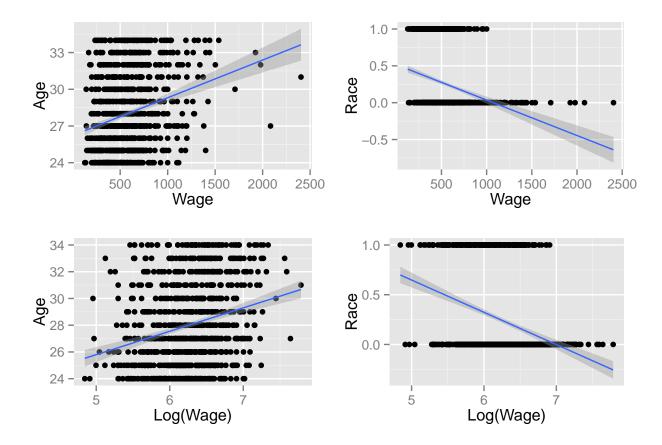


Figure 3:

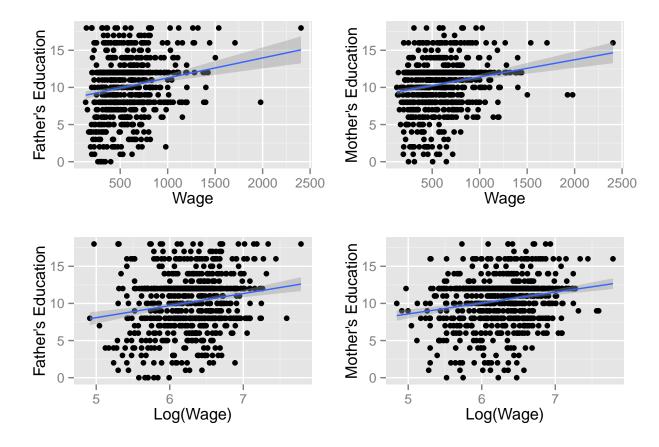


Figure 4:

14

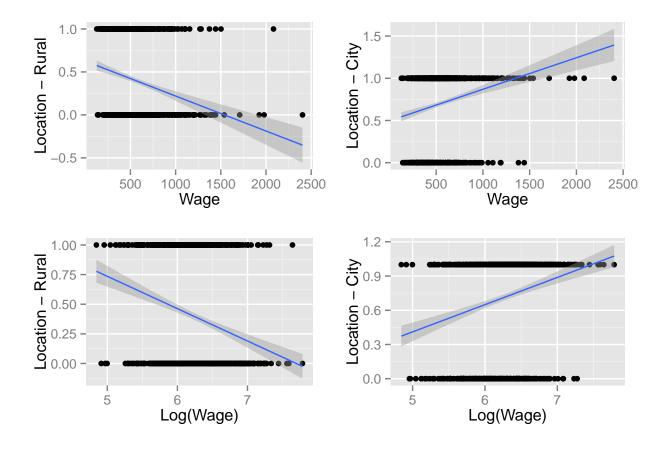


Figure 5:

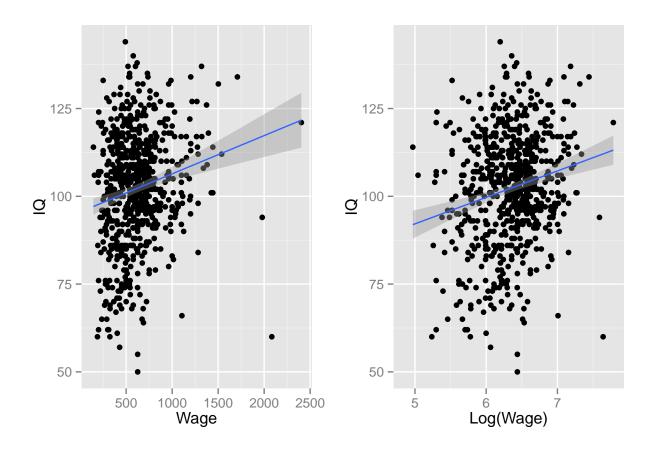


Figure 6:

Question 4.3

Regress log(wage) on education, experience, age, and raceColor.

```
model4.3<-lm(logWage~education + experience + age + raceColor, d)</pre>
```

1. Report all the estimated coefficients, their standard errors, t-statistics, F-statistic of the regression, R^2 , R_{adj}^2 , and degrees of freedom.

```
stargazer(model4.3, type="latex", title="Question 4.3-1")
```

- % Table created by stargazer v.5.2 by Marek Hlavac, Harvard University. E-mail: hlavac at fas.harvard.edu
- % Date and time: Wed, Mar 02, 2016 4:27:47 PM

Table 1: Question 4.3-1

	$Dependent\ variable:$
	logWage
education	0.080***
	(0.006)
experience	0.035***
-	(0.004)
age	
raceColor	-0.261***
	(0.030)
Constant	4.962***
	(0.113)
Observations	1,000
\mathbb{R}^2	0.236
Adjusted R ²	0.234
Residual Std. Error	0.392 (df = 996)
F Statistic	$102.582^{***} (df = 3; 996)$
Note:	*p<0.1; **p<0.05; ***p<0.01

2. Explain why the degrees of freedom takes on the specific value you observe in the regression output.

The degrees of freedom on the residual errors is 1000 - 4 = 996 where the 1000 is the number of observations and 4 is subtracted for the enumber of covariates included in the model. For the F-statistic the degrees of freedom is 4000 - 4 = 3996 where the 4000 accounts for the 1000 observations for each covariate and the 4 is again for the four covariates in the model.

3. Describe any unexpected results from your regression and how you would resolve them (if the intent is to estimate return to education, condition on race and experience).

There is no output for the age variable and

4. Interpret the coefficient estimate associated with education.

The coefficient on education is 0.080 ± 0.012 which indicates that for 1 additional year of education wage would increase by an estimated 8 percent.

5. Interpret the coefficient estimate associated with experience.

The coefficient on experience is 0.035 ± 0.008 which indicates that for 1 additional year of experience wage would increase by an estimated 3.5 percent.

Question 4.4

Regress log(wage) on education, experience, experienceSquare, and race-Color.

```
model4.4<-lm(logWage~education + experience + experienceSquare + raceColor, data=d)
stargazer(model4.3, model4.4, type="latex", title="Question 4.4")</pre>
```

- % Table created by stargazer v.5.2 by Marek Hlavac, Harvard University. E-mail: hlavac at fas.harvard.edu % Date and time: Wed, Mar 02, 2016 4:27:47 PM
 - 1. Plot a graph of the estimated effect of experience on wage.

```
#Note: I am not sure this is what is being asked for, not sure if I am interpreting the question correct
#pull out the coefficients from the model
coefs<-coef(model4.4)

#set x values to be the experence data
x<-d$experience

#set y to be just the effect from experience
#so we pull the coefficient for expereience and for experienceSquared
y<-coefs[3]*x+coefs[4]*x^2

#put the data in a new dataframe to use for plotting
dat<-data.frame(x,y)

#plot the estimated effect of expereience (with the squared term) on the log(wage)
ggplot(dat, aes(x,y))+
geom_smooth(na.rm=T) +
labs(x="experience", y="log(wage)")</pre>
```

geom_smooth: method="auto" and size of largest group is >=1000, so using gam with formula: y ~ s(x,

2. What is the estimated effect of experience on wage when experience is 10 years?

When experience equals 10 the estimated effect on wage is about 64 percent which can be read from the plot or derived from the coefficients $estimatedeffect = 0.0925 \cdot 10 + -0.003 \cdot 10^2 = 0.637$.

Table 2: Question 4.4

	$Dependent \ variable:$		
	\log Wage		
	(1)	(2)	
education	0.080***	0.079***	
	(0.006)	(0.006)	
experience	0.035***	0.092***	
•	(0.004)	(0.012)	
age			
experienceSquare		-0.003***	
		(0.001)	
raceColor	-0.261^{***}	-0.263***	
	(0.030)	(0.030)	
Constant	4.962***	4.736***	
	(0.113)	(0.120)	
Observations	1,000	1,000	
\mathbb{R}^2	0.236	0.257	
Adjusted R ²	0.234	0.254	
Residual Std. Error	0.392 (df = 996)	0.387 (df = 995)	
F Statistic	$102.582^{***} (df = 3; 996)$		

Note:

*p<0.1; **p<0.05; ***p<0.01

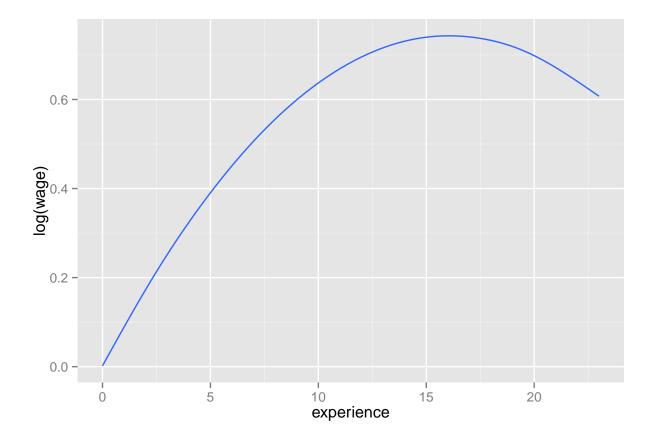


Figure 7:

Question 4.5

Regress logWage on education, experience, experienceSquare, raceColor, dad_education, mom_education, rural, city.

- % Table created by stargazer v.5.2 by Marek Hlavac, Harvard University. E-mail: hlavac at fas.harvard.edu % Date and time: Wed, Mar 02, 2016 4:27:49 PM
 - 1. What are the number of observations used in this regression? Are missing values a problem? Analyze the missing values, if any, and see if there is any discernible pattern with wage, education, experience, and raceColor.

The number of observations is only 723 out of the total 1000 so there are missing values that may be causing issues. From the code below we see that the missing values are in the dad_education and mom_education variables. Those entries are seperated out to explore any patterns. The plots that follow explore the education, experience, and raceColor for those that are not complete cases (ie have missing data). No discernible pattern is present.

```
#check which variables have the missing data
sum(is.na(d$education))

## [1] 0

sum(is.na(d$experience))

## [1] 0

sum(is.na(d$experienceSquare))

## [1] 0

sum(is.na(d$raceColor))

## [1] 0

sum(is.na(d$raceColor))

## [1] 10

sum(is.na(d$dad_education))

## [1] 239

sum(is.na(d$mom_education))

## [1] 128
```

Table 3: Question 4.5

	$Dependent\ variable:$			
		\log Wage		
	(1)	(2)	(3)	
education	0.080*** (0.006)	0.079*** (0.006)	0.068*** (0.008)	
experience	0.035^{***} (0.004)	0.092*** (0.012)	0.097*** (0.013)	
age				
experienceSquare		-0.003^{***} (0.001)	$-0.003^{***} $ (0.001)	
raceColor	-0.261^{***} (0.030)	-0.263^{***} (0.030)	$-0.213^{***} $ (0.043)	
${\it dad_education}$			-0.001 (0.005)	
$mom_education$			0.011* (0.006)	
rural			-0.092*** (0.031)	
city			0.178*** (0.032)	
Constant	4.962*** (0.113)	4.736*** (0.120)	4.642*** (0.141)	
Observations R ² Adjusted R ² Residual Std. Error F Statistic	$ \begin{array}{c} 1,000 \\ 0.236 \\ 0.234 \\ 0.392 \text{ (df} = 996) \\ 102.582*** \text{ (df} = 3; 996) \end{array} $	$ \begin{array}{r} 1,000 \\ 0.257 \\ 0.254 \\ 0.387 (df = 995) \\ 85.978^{***} (df = 4; 995) \end{array} $	723 0.275 0.267 $0.379 (df = 714)$ $33.793^{***} (df = 8; 714)$	

Note:

*p<0.1; **p<0.05; ***p<0.01

```
sum(is.na(d$rural))
## [1] 0
sum(is.na(d$city))
## [1] O
#identify rows that have an NA value
row.has.na <- apply(d, 1, function(x){any(is.na(x))})</pre>
#make a dataframe of only those rows with missing values to look at
d_missing<-d[row.has.na,]</pre>
#create plots to try and identify any patterns
p4.1<-ggplot(d_missing, aes(wage, education)) +
  geom point() +
  labs(x = "Wage",
       y = "Education") +
  geom_smooth(method = "lm")
p4.2<-ggplot(d missing, aes(log(wage), education)) +
  geom_point() +
  labs(x = "Log(Wage)",
       y = "Education") +
  geom_smooth(method = "lm")
p4.3<-ggplot(d_missing, aes(wage, experience)) +
  geom_point() +
  labs(x = "Wage",
       y = "Experience") +
  geom_smooth(method = "lm")
p4.4<-ggplot(d_missing, aes(log(wage), experience)) +
  geom_point() +
  labs(x = "Log(Wage)",
       y = "Experience") +
  geom_smooth(method = "lm")
p4.5<-ggplot(d_missing, aes(wage, raceColor)) +
  geom_point() +
  labs(x = "Wage",
       y = "Experience") +
  geom_smooth(method = "lm")
p4.6<-ggplot(d_missing, aes(log(wage), raceColor)) +
  geom_point() +
  labs(x = "Log(Wage)",
       y = "raceColor") +
  geom_smooth(method = "lm")
#create historgrams to try and idenfiy patterns
```

```
p4.7<-ggplot(d_missing, aes(x=education)) + geom_histogram(binwidth=2)
p4.8<-ggplot(d_missing, aes(x=experience)) + geom_histogram(binwidth=2)
p4.9<-ggplot(d_missing, aes(x=raceColor)) + geom_histogram(binwidth=.5)

#show the plots
multiplot(p4.7, p4.8, p4.9)
```

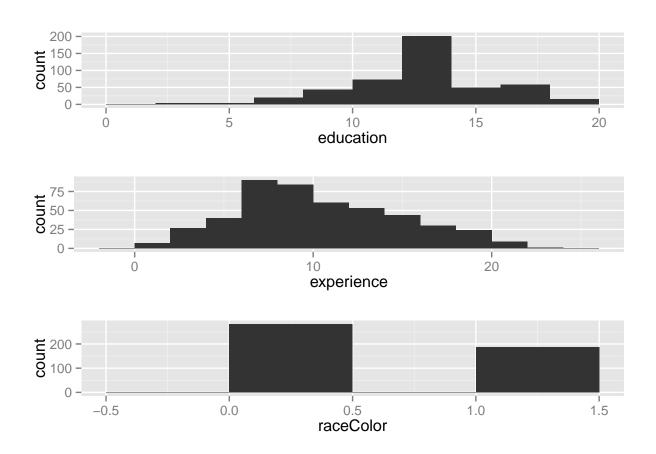


Figure 8:

```
multiplot(p4.1, p4.2, p4.3, p4.4, p4.5, p4.6, cols=2)
```

2. Do you just want to "throw away" these observations?

Ideally we would not want to just "throw away" these data points becuas they still contian some useful information. However, we need to be careful on how we handle the missing values.

3. How about blindly replace all of the missing values with the average of the observed values of the corresponding variable? Rerun the original regression using all of the observations?

```
#create a copy of the dataset for this problem d4.3<-d
```

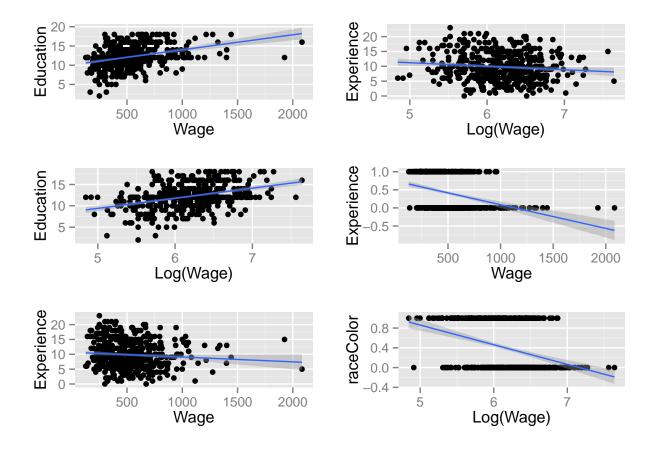


Figure 9:

```
stargazer(model4.5, model4.5.3, type="latex", title="Question 4.5-3")
```

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 - 4. How about regress the variable(s) with missing values on education, experience, and raceColor, and use this regression(s) to predict (i.e., "impute") the missing values and then rerun the original regression using all of the observations?

```
d4<-d
model_dad<-lm(dad_education~education+experience+raceColor, data=d4)
model_mom<-lm(mom_education~education+experience+raceColor, data=d4)
coef_dad<-coef(model_dad)</pre>
coef_mom<-coef(model_mom)</pre>
#Note this functon is not working quite right yet, I am still workign on it
rep<-function(d) {</pre>
  for (i in 1:nrow(d)) {
    if (is.na(d$dad_education[i])==TRUE) {
      d$dad_education[i] = coef_dad[1] + coef_dad[2] *d$education[i] +
        coef_dad[3]*d$experience[i]+coef_dad[4]*d$raceColor[i]
    }
    if (is.na(d$mom education[i])==TRUE) {
      d$mom_education[i] = coef_mom[1] + coef_mom[2] *d$education[i] +
        coef_mom[3]*d$experience[i]+coef_mom[4]*d$raceColor[i]
    }
 }
}
rep(d4)
#re-run the origional regression
model4.5.4<-lm(logWage~education + experience + experienceSquare + raceColor +</pre>
                  dad_education + mom_education + rural + city, data=d4)
```

```
#show the results of the the original regression the final regression and the two sub regressions stargazer(model4.5, model4.5.4, model_dad, model_mom, type="latex", title="Question 4.5-4", column.sep.
```

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 - 5. Compare the results of all of these regressions. Which one, if at all, would you prefer?

Table 4: Question 4.5-3

	Dependen	et variable:	
	\log Wage		
	(1)	(2)	
education	0.068***	0.071***	
	(0.008)	(0.006)	
experience	0.097***	0.090***	
	(0.013)	(0.011)	
experienceSquare	-0.003***	-0.003***	
	(0.001)	(0.001)	
raceColor	-0.213***	-0.231***	
	(0.043)	(0.031)	
dad_education	-0.001	-0.00004	
	(0.005)	(0.004)	
mom_education	0.011*	0.003	
	(0.006)	(0.005)	
rural	-0.092***	-0.095***	
	(0.031)	(0.026)	
city	0.178***	0.167***	
	(0.032)	(0.027)	
Constant	4.642***	4.729***	
	(0.141)	(0.123)	
Observations	723	1,000	
\mathbb{R}^2	0.275	0.298	
Adjusted R ²	0.267	0.292	
Residual Std. Error	0.379 (df = 714)	0.376 (df = 991)	
F Statistic	$33.793^{***} (df = 8; 714)$	$52.617^{***} (df = 8; 991)$	

Note:

*p<0.1; **p<0.05; ***p<0.01

Table 5: Question 4.5-4

	Dependent variable:			
	$ \log$ Wage		dad_education	mom_education
	(1)	(2)	(3)	(4)
education	0.068***	0.068***	0.502***	0.433***
	(0.008)	(0.008)	(0.057)	(0.046)
experience	0.097***	0.097***	-0.148***	-0.077^{**}
	(0.013)	(0.013)	(0.037)	(0.030)
experienceSquare	-0.003***	-0.003***		
	(0.001)	(0.001)		
raceColor	-0.213***	-0.213***	-2.121^{***}	-1.468***
	(0.043)	(0.043)	(0.312)	(0.232)
dad_education	-0.001	-0.001		
	(0.005)	(0.005)		
mom_education	0.011^{*}	0.011^{*}		
	(0.006)	(0.006)		
rural	-0.092***	-0.092***		
	(0.031)	(0.031)		
city	0.178***	0.178***		
-	(0.032)	(0.032)		
Constant	4.642***	4.642***	4.939***	5.593***
	(0.141)	(0.141)	(1.019)	(0.827)
Observations	723	723	761	872
\mathbb{R}^2	0.275	0.275	0.309	0.274
Adjusted R ²	0.267	0.267	0.306	0.271
Residual Std. Error	0.379 (df = 714)	0.379 (df = 714)	3.122 (df = 757)	2.669 (df = 868)
F Statistic	$33.793^{***} (df = 8; 714)$	$33.793^{***} (df = 8; 714)$	112.815^{***} (df = 3; 757)	108.992^{***} (df = 3; 86)

Note: *p<0.1; **p<0.05; ***p<0.01

stargazer(model4.5, model4.5.3, model4.5.4, type="latex", title="Question 4.5-5")

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Table 6: Question 4.5-5

		$Dependent\ variable:$	
		logWage	
	(1)	(2)	(3)
education	0.068***	0.071***	0.068***
	(0.008)	(0.006)	(0.008)
experience	0.097***	0.090***	0.097***
	(0.013)	(0.011)	(0.013)
experienceSquare	-0.003***	-0.003***	-0.003***
	(0.001)	(0.001)	(0.001)
raceColor	-0.213***	-0.231***	-0.213***
	(0.043)	(0.031)	(0.043)
dad_education	-0.001	-0.00004	-0.001
	(0.005)	(0.004)	(0.005)
mom_education	0.011*	0.003	0.011*
	(0.006)	(0.005)	(0.006)
rural	-0.092***	-0.095***	-0.092***
	(0.031)	(0.026)	(0.031)
city	0.178***	0.167***	0.178***
	(0.032)	(0.027)	(0.032)
Constant	4.642***	4.729***	4.642***
	(0.141)	(0.123)	(0.141)
Observations	723	1,000	723
\mathbb{R}^2	0.275	0.298	0.275
Adjusted R^2	0.267	0.292	0.267
Residual Std. Error	0.379 (df = 714)	0.376 (df = 991)	0.379 (df = 714)
F Statistic	$33.793^{***} (df = 8; 714)$	$52.617^{***} (df = 8; 991)$	33.793^{***} (df = 8; 714)

Note:

*p<0.1; **p<0.05; ***p<0.01

Question 4.6

1. Consider using z_1 as the instrumental variable (IV) for education. What assumptions are needed on z_1 and the error term (call it, u)?

- 2. Suppose z_1 is an indicator representing whether or not an individual lives in an area in which there was a recent policy change to promote the importance of education. Could z_1 be correlated with other unobservables captured in the error term?
- 3. Using the same specification as that in Question 4.5, estimate the equation by 2SLS, using both z_1 and z_2 as instrument variables. Interpret the results. How does the coefficient estimate on education change?

Question 5: CLM 2

The dataset, wealthy candidates.csv, contains candidate level electoral data from a developing country. Politically, each region (which is a subset of the country) is divided in to smaller electoral districts where the candidate with the most votes wins the seat. This dataset has data on the financial wealth and electoral performance (voteshare) of electoral candidates. We are interested in understanding whether or not wealth is an electoral advantage. In other words, do wealthy candidates fare better in elections than their less wealthy peers?

1. Begin with a parsimonious, yet appropriate, specification. Why did you choose this model? Are your results statistically significant? Based on these results, how would you answer the research question? Is there a linear relationship between wealth and electoral performance?

To start off with we need to examine the vairables and omit outliers. In this case there are some NA values in the absolute_wealth variable and there are a lot of data points very close to zero, which screw the data. This first model omits those entries. Additionally we transform the absolute_wealth into a log(absolute_wealth) to rescale the values for regression.

```
data<-read.csv('wealthy_candidates.csv')
summary(data)</pre>
```

```
##
          X
                            region
                                             urb
                                                                 lit
##
                1.0
                      Region 1:1183
                                               :0.02835
                                                                   :0.2418
    Min.
                                        Min.
                                                           Min.
                                        1st Qu.:0.08387
                                                           1st Qu.:0.3846
    1st Qu.: 625.2
                      Region 2: 690
##
    Median :1249.5
                      Region 3: 625
                                        Median :0.14657
                                                           Median :0.4602
##
    Mean
            :1249.5
                                        Mean
                                               :0.18729
                                                           Mean
                                                                   :0.4512
##
    3rd Qu.:1873.8
                                        3rd Qu.:0.24319
                                                           3rd Qu.:0.5105
##
    Max.
            :2498.0
                                        Max.
                                               :0.80234
                                                           Max.
                                                                   :0.6524
##
##
                        absolute_wealth
      voteshare
##
    Min.
            :0.006037
                                :2.000e+00
##
    1st Qu.:0.199620
                        1st Qu.:1.875e+05
##
    Median :0.293398
                        Median :1.337e+06
##
            :0.287860
                                :5.034e+06
    Mean
                        Mean
##
    3rd Qu.:0.367978
                        3rd Qu.:4.092e+06
##
    Max.
            :0.693324
                        Max.
                                :1.216e+09
##
                        NA's
                                :1
```

head(data)

```
##
     X
         region
                                  lit voteshare absolute_wealth
                       urb
## 1 1 Region 2 0.14909884 0.4283742 0.4168488
                                                     5110593.00
## 2 2 Region 2 0.14909884 0.4283742 0.1137623
                                                       99999.97
## 3 3 Region 2 0.09182214 0.4579071 0.2983904
                                                       55340.00
## 4 4 Region 2 0.10168768 0.3063438 0.4835877
                                                      206999.94
## 5 5 Region 2 0.06139975 0.2731756 0.3106902
                                                     1307408.00
## 6 6 Region 2 0.41726938 0.5199646 0.4023529
                                                     5864785.50
```

#look at the variables
hist(data\$voteshare)

Histogram of data\$voteshare

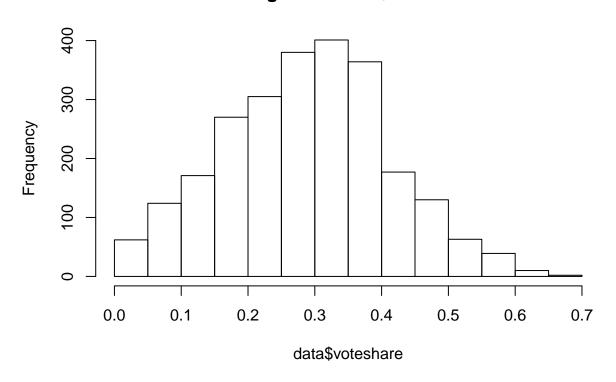


Figure 10:

hist(data\$absolute_wealth)

```
#subset the data and only keep the complete cases
data2<-data[, c("voteshare", "absolute_wealth", "region")]
data2<-data2[complete.cases(data),]

data2$logwealth<-log(data2$absolute_wealth)
min(data2$logwealth)</pre>
```

[1] 0.6931472

hist(data2\$logwealth, breaks=20)

```
#eliminate the large column on near 0 absoluate wealth
data2<-subset(data2, logwealth>1, )
#plot the data to get a sense if there might be a linear relationship
```

Histogram of data\$absolute_wealth

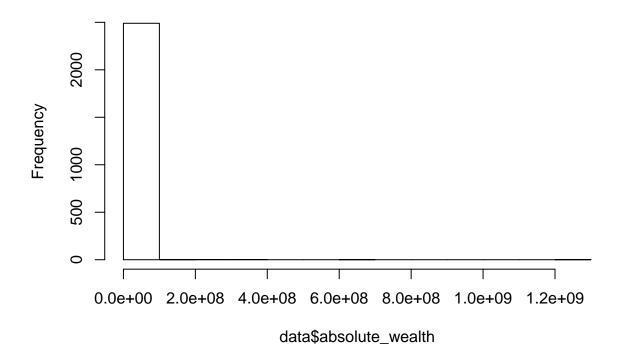


Figure 11:

Histogram of data2\$logwealth

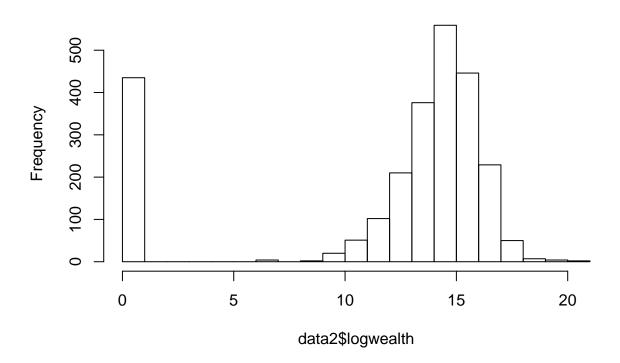


Figure 12:

```
scatter1<-ggplot(data2, aes(voteshare, logwealth))
scatter1+geom_point()</pre>
```

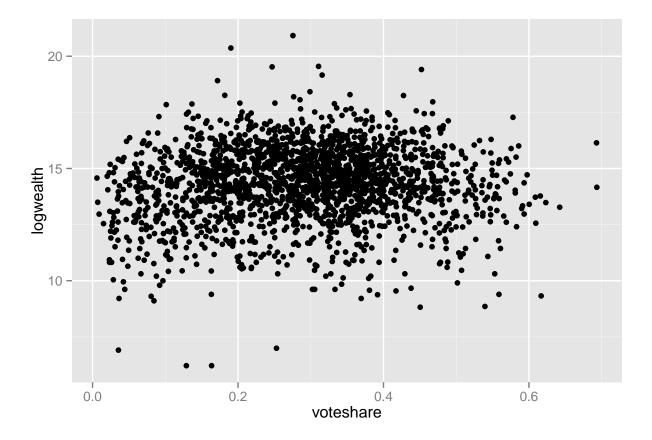


Figure 13:

```
#run the basic model
model1<-lm(voteshare~logwealth, data=data2)
stargazer(model1, type="latex", title="Question 5.1")</pre>
```

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 - 2. A team-member suggests adding a quadratic term to your regression. Based on your prior model, is such an addition warranted? Add this term and interpret the results. Do wealthier candidates fare better in elections?

```
#run the model with the squared term added in
model2<-lm(voteshare~logwealth+ logwealth*logwealth, data=data2)
stargazer(model1, model2, type="latex", title="Question 5.2")</pre>
```

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Table 7: Question 5.1

	Dependent variable:
	voteshare
logwealth	0.005***
	(0.002)
Constant	0.216***
	(0.024)
Observations	2,062
\mathbb{R}^2	0.005
Adjusted \mathbb{R}^2	0.004
Residual Std. Error	0.125 (df = 2060)
F Statistic	$9.513^{***} (df = 1; 2060)$
Note:	*p<0.1; **p<0.05; ***p<0.0

Table 8: Question 5.2

	Dependent variable: voteshare	
	(1)	(2)
logwealth	0.005***	0.005***
	(0.002)	(0.002)
Constant	0.216***	0.216***
	(0.024)	(0.024)
Observations	2,062	2,062
\mathbb{R}^2	0.005	0.005
Adjusted R^2	0.004	0.004
Residual Std. Error $(df = 2060)$	0.125	0.125
F Statistic (df = 1 ; 2060)	9.513***	9.513***
Note:	*p<0.1; **p	<0.05; ***p<

3. Another team member suggests that it is important to take into account the fact that different regions have different electoral contexts. In particular, the relationship between candidate wealth and electoral performance might be different across states. Modify your model and report your results. Test the hypothesis that this addition is not needed.

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Table 9:	Question	5.3
----------	----------	-----

		$Dependent\ variable:$	
		voteshare	
	(1)	(2)	(3)
logwealth	0.005***	0.005***	0.012***
	(0.002)	(0.002)	(0.002)
Constant	0.216***	0.216***	0.088***
	(0.024)	(0.024)	(0.028)
Region Fixed effects	No	No	Yes
Observations	2,062	2,062	2,062
\mathbb{R}^2	0.005	0.005	0.039
Adjusted R ²	0.004	0.004	0.038
Residual Std. Error	0.125 (df = 2060)	0.125 (df = 2060)	0.123 (df = 2058)
F Statistic	$9.513^{***} (df = 1; 2060)$	$9.513^{***} (df = 1; 2060)$	28.109***(df = 3; 2058)

Note:

*p<0.1; **p<0.05; ***p<0.01

- 4. Return to your parsimonious model. Do you think you have found a causal and unbiased estimate? Please state the conditions under which you would have an unbiased and causal estimates. Do these conditions hold?
- 5. Someone proposes a difference in difference design. Please write the equation for such a model. Under what circumstances would this design yield a causal effect?

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Question 6: CLM 3

Your analytics team has been tasked with analyzing aggregate revenue, cost and sales data, which have been provided to you in the R workspace/data frame retailSales.Rdata.

W271 - Lab 2

Your task is two fold. First, your team is to develop a model for predicting (forecasting) revenues. Part of the model development documentation is a backtesting exercise where you train your model using data from the first two years and evaluate the model's forecasts using the last two years of data.

Second, management is equally interested in understanding variables that might affect revenues in support of management adjustments to operations and revenue forecasts. You are also to identify factors that affect revenues, and discuss how useful management's planned revenue is for forecasting revenues.

Your analysis should address the following:

- Exploratory Data Analysis: focus on bivariate and multivariate relationships.
- Be sure to assess conditions and identify unusual observations.
- Is the change in the average revenue different from 95 cents when the planned revenue increases by \$1?
- Explain what interaction terms in your model mean in context supported by data visualizations.
- Give two reasons why the OLS model coefficients may be biased and/or not consistent, be specific.
- Propose (but do not actually implement) a plan for an IV approach to improve your forecasting model.