



# Co-optimizing Integrated Transmission-Distribution Systems using PowerModelsTD.jl

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# Acknowledgements - Team & Funding

- David M. Fobes (A-1 LANL)
- Russell Bent (T-5 LANL)
- Andreas Wächter (Northwestern University)
- Xinyi Luo (Northwestern University)

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# Outline

- Background & Challenges
- Introduction to **PowerModelsITD.jl**
- Using **PowerModelsITD.jl**
- Use Cases & Tests



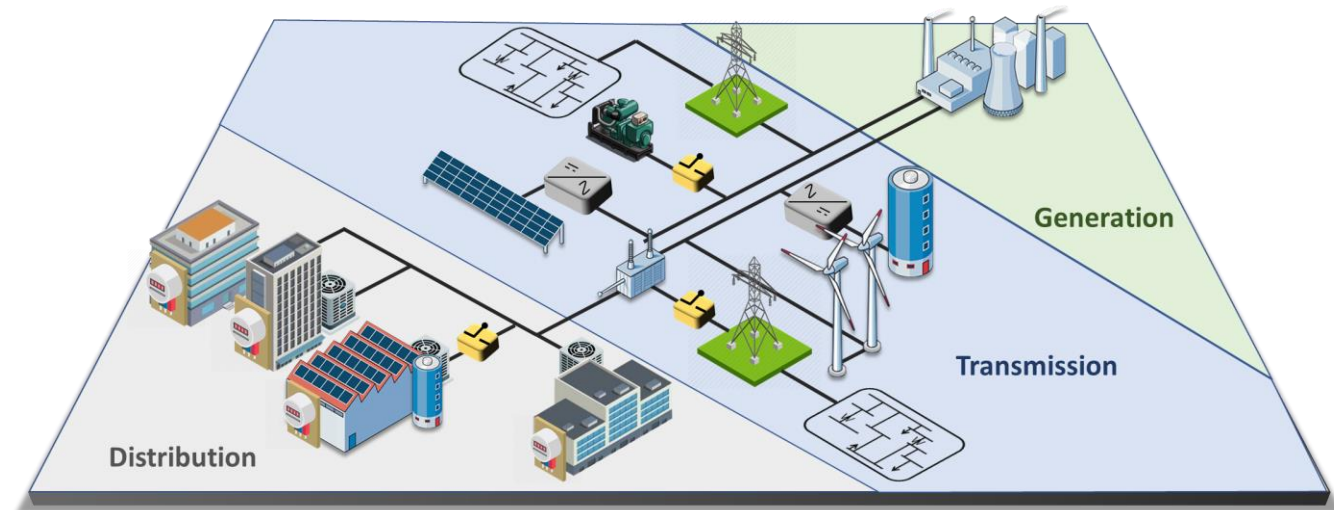


# Background & Challenges

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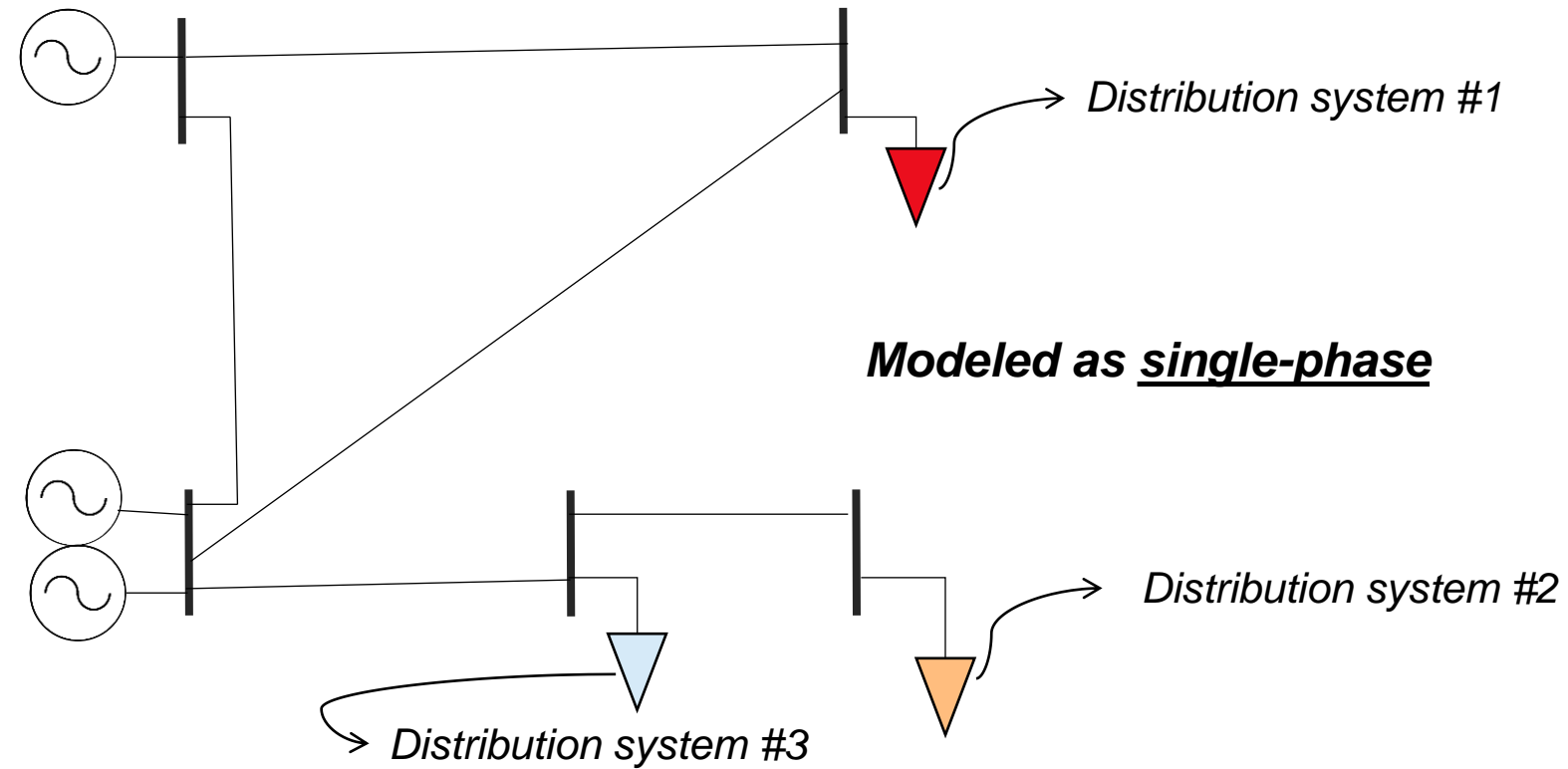
# Background

- Conventional electric power systems (EPS) are composed of:
  - **Generation**
  - **Transmission**
  - **Distribution**
- Managed independently by:
  - Transmission system (TSOs)
  - Distribution system operators (DSOs).



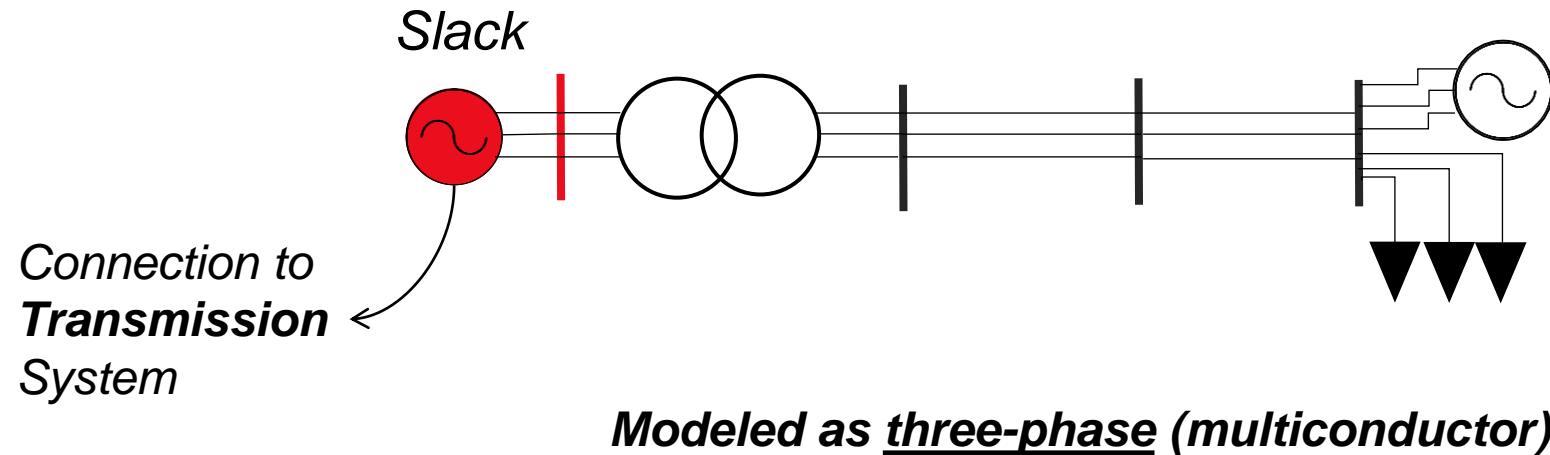
# Background: TSOs

- TSOs traditionally model distribution systems as consumers (**loads**).



# Background: DSOs

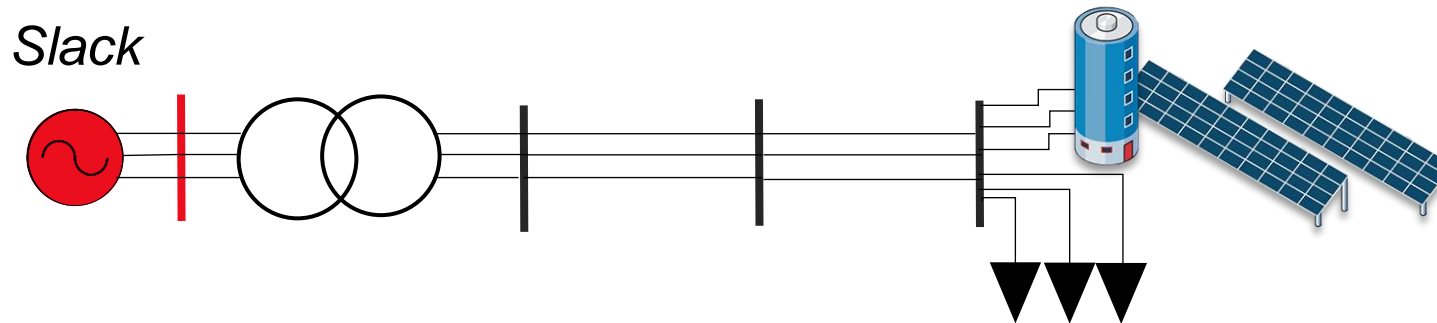
- DSOs traditionally regard transmission systems as slack buses with unlimited resources (often modeled as **voltage sources**).



# Background: Integration of DERs

Distribution systems are becoming more **active**:

- Integration of **Distributed Energy Resources** (DERs)
- Integration of **Information & Communication Technologies** (ICTs).



The **assumption** of distribution being just **passive loads** is **unreasonable** for **optimal T&D operation**.



# Challenges

- Traditionally owned and operated by **separate entities**.
- **Centralized models** may not be scalable and hard to solve. (*Assumption*)
- **Convergence issues with AC OPF (nonlinear, nonconvex formulations)**
- **Unable** to coordinate or **co-optimize** resources across T&D boundaries

**Coordination (Co-optimization)** between **T&D** networks will be **imperative** for the **optimal operation** of the (future) power grid.

To fill this gap, we developed a **first-of-its-kind tool** that **supports** and **enables** the **Co-optimization** of **T&D systems**

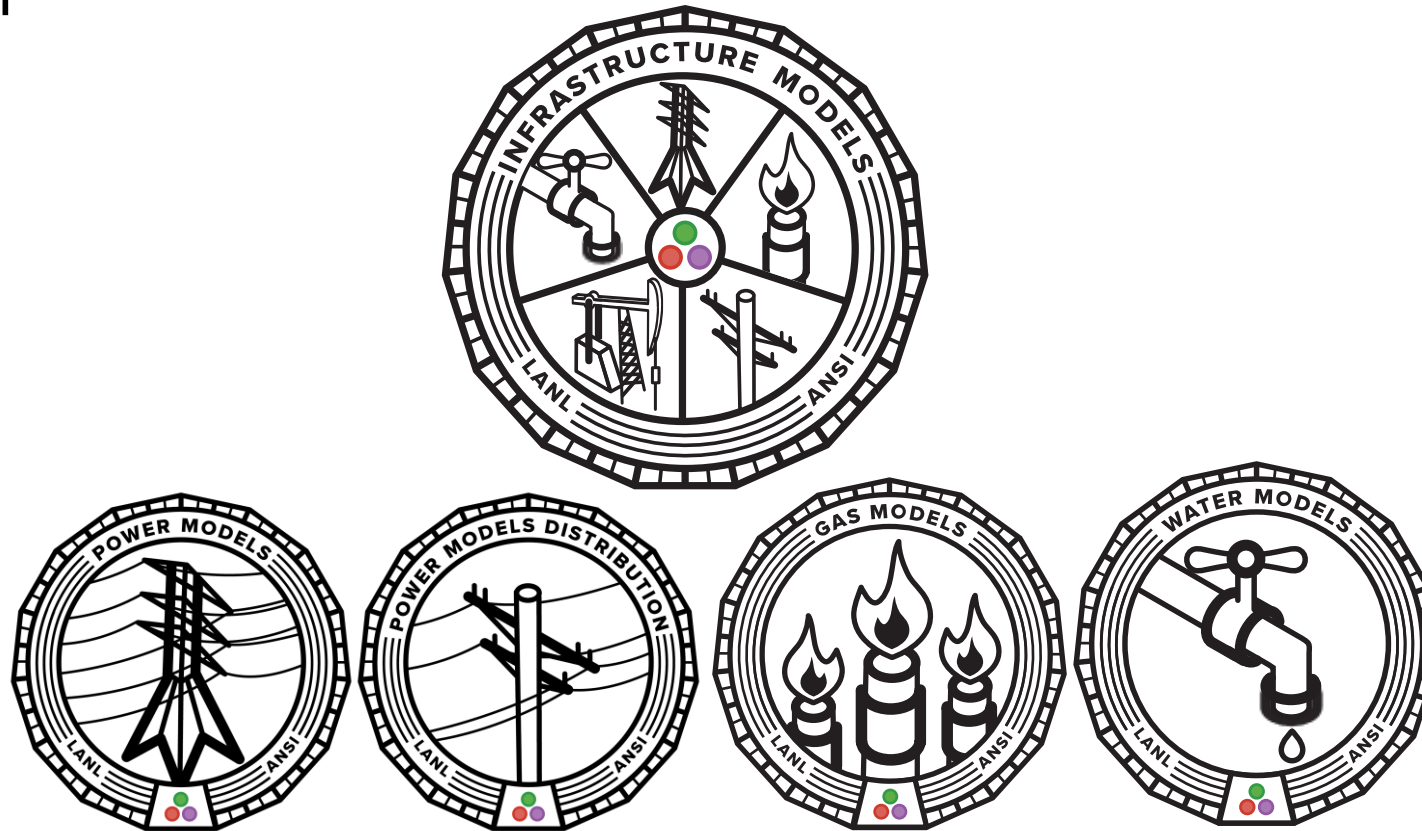


# Introduction to PowerModelsITD.jl

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# InfrastructureModels.jl

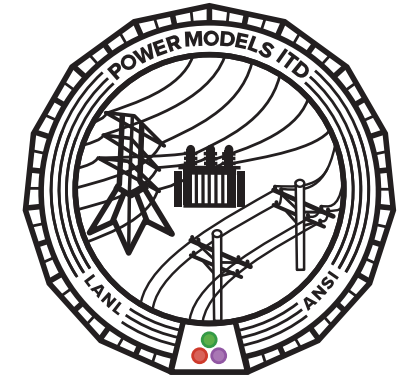
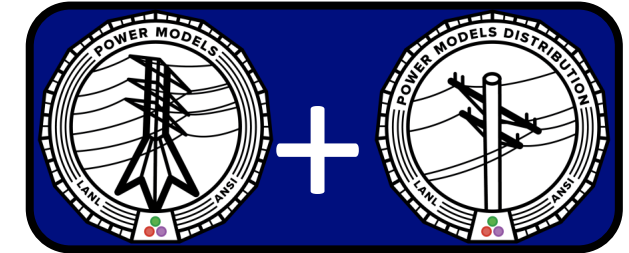
- **Core** package for **multi-infrastructure modeling** and **optimization** ecosystem



<https://github.com/lanl-ansi/InfrastructureModels.jl>

# PowerModelsITD.jl (PMITD)

- Open-source tool (Written in **Julia**)
- Based on **LANL multi-infrastructure ecosystem**
- Used for **modeling** and **optimizing T&D systems**
- Solve steady-state **ITD Optimal Power Flow (OPF)**
- Evaluate diverse **network formulations**
- Common research platform for **emerging formulations**



<https://github.com/lanl-ansi/PowerModelsITD.jl>



[1] <https://github.com/lanl-ansi/PowerModelsITD.jl>



[2] Ospina, J., et al. (2023). Modeling and Rapid Prototyping of Integrated Transmission-Distribution OPF Formulations with PowerModelsITD.jl. IEEE Transactions on Power Systems.



[3] Ospina, J., et al. (2023). On the Feasibility of Market Manipulation and Energy Storage Arbitrage via Load-Altering Attacks. Energies, 16(4), 1670.

# PowerModelsITD.jl: Core Design

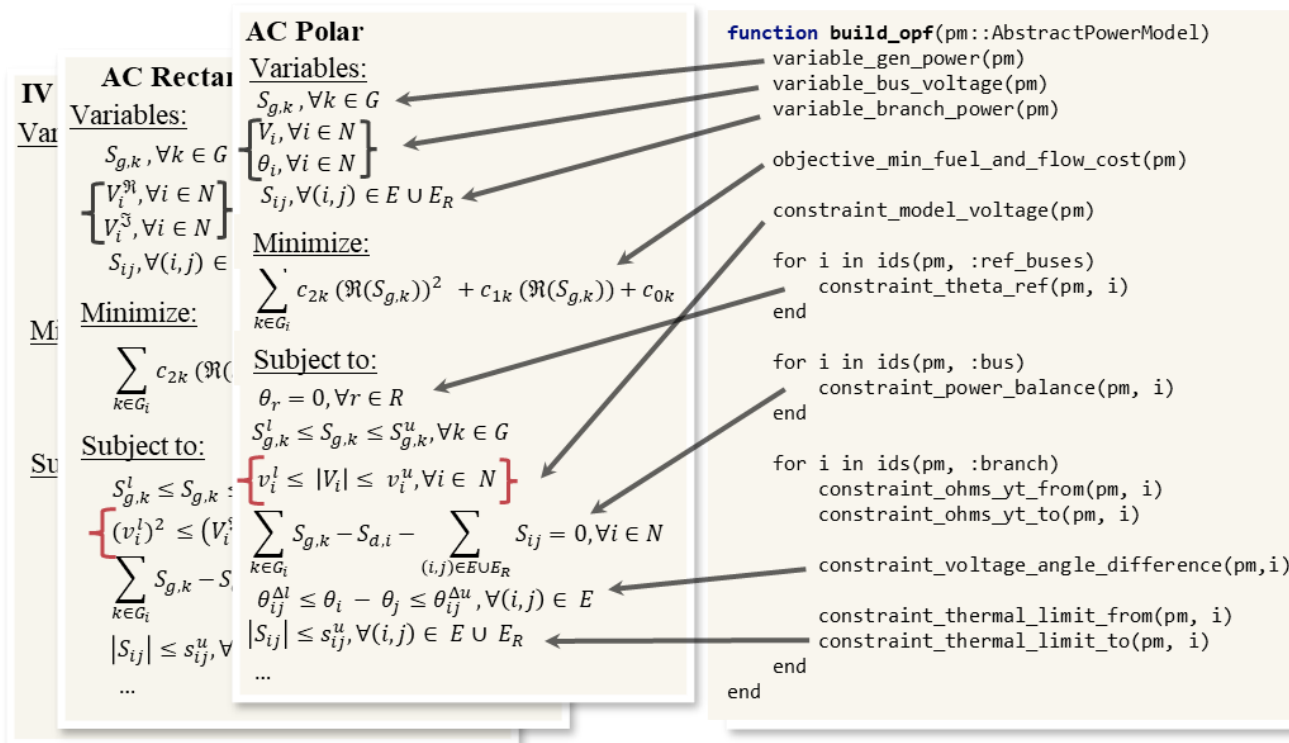
## Problem Specifications

Integrated T&D Power Flow (pfitd)  
 Integrated T&D Optimal Power Flow (opfitd)  
 ...

## Formulations

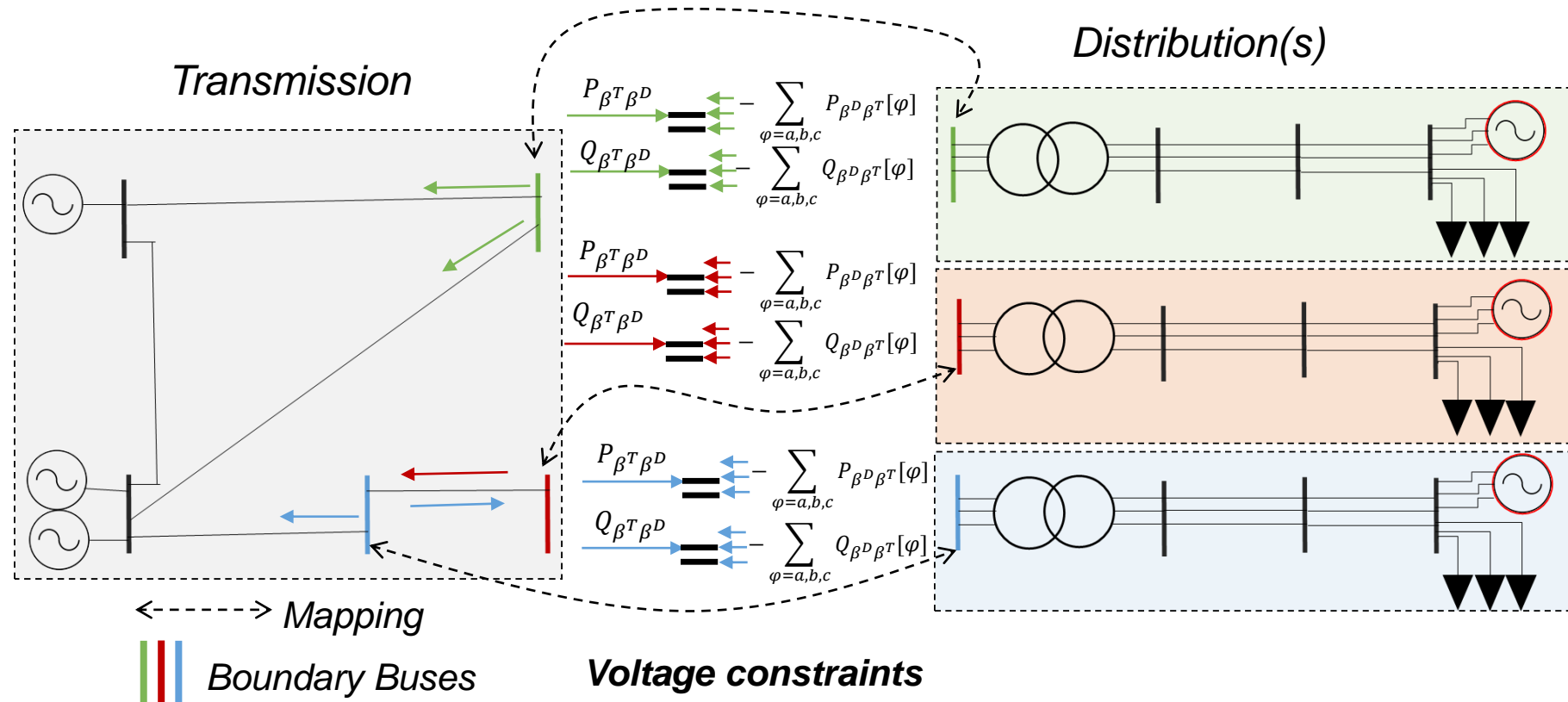
ACP-ACPU  
 ACR-ACRU  
 IVR-IVRU  
 NFA-NFAU  
 SOCBFM-  
 LinDis3Flow  
 ...

## Core language feature: Multiple dispatch





# PowerModelsITD.jl: Boundaries



$$|V^T| = \begin{cases} |V^D|[a] \\ |V^D|[b] \\ |V^D|[c] \end{cases} \quad \begin{cases} \angle V^T = \angle V^D[a] \\ \angle V^D[b] = \angle V^D[a] - 120^\circ \\ \angle V^D[c] = \angle V^D[a] + 120^\circ \end{cases}$$

# PowerModelsITD.jl: Formulations

## NLP Formulations

- ACP-ACPU
  - Power-Voltage, polar coordinates, non-linear ([NLP](#))
- ACR-ACRU
  - Power-Voltage, rectangular coordinates, non-linear ([NLP](#))
- IVR-IVRU
  - Current-Voltage, rectangular coordinates, non-linear ([NLP](#))

## Linear Approximations

- NFA-NFAU
  - Network Flow [Approximation](#)
  - Active power only, lossless, linear (LP)
- BFA-LinDist3Flow
  - Branch Flow [Approximation](#) - Linear [Approximation](#)

## Relaxations

- SOCBFM-SOCUBFM
  - Second Order Cone Branch Flow Model [Relaxations](#) – W-space.

## Hybrid Formulations (**Experimental**)

- ACR-FOTRU
  - Power-Voltage [NLP](#), rectangular coordinates, First-Order Taylor [Approximation](#)
- ACP-FOTPU
  - Power-Voltage [NLP](#), polar coordinates, First-Order Taylor [Approximation](#)
- ACR-FBSU
  - Power-Voltage [NLP](#), rectangular coordinates, Forward-Backward Sweep [Approximation](#)
- SOCBFM-LinDist3Flow
  - Second Order Cone Branch Flow Model [Relaxation](#) – W-space.
  - Linear [Approximation](#).



# Using PowerModelsITD.jl

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# Using PowerModelsITD.jl: Files

## Transmission file

```
function mpc = case5
mpc.version = '2';
mpc.baseMVA = 100.0;

%% bus data
% bus_i type Pd Qd Gs Bs area Vm Va baseKV zone
mpc.bus = [
1 2 0.0 0.0 0.0 0.0 1 1.07762 2.80377
2 1 300.0 98.61 0.0 0.0 1 1.08407 -0.73465
3 2 300.0 98.61 0.0 0.0 1 1.10000 -0.55972
4 3 390.0 131.47 0.0 0.0 1 1.06414 0.00000
5 2 0.0 0.0 0.0 0.0 1 1.00000 0.00000
10 2 0.0 0.0 0.0 0.0 1 1.06907 3.59033
];

%% generator data
% bus Pg Qg Qmax Qmin Vg mBase status Pmax Pmin
mpc.gen = [
1 40.0 30.0 30.0 -30.0 1.07762 100.0 1 40.0 0.0;
1 170.0 127.5 127.5 -127.5 1.07762 100.0 1 170.0 0.0;
3 324.498 390.0 390.0 -390.0 1.1 100.0 1 520.0 0.0;
4 0.0 -10.802 150.0 -150.0 1.06414 100.0 1 200.0 0.0;
10 470.694 -165.039 450.0 -450.0 1.06907 100.0 1
];

%% generator cost data
% 2 startup shutdown n c(n-1) ... c0
mpc.gencost = [
2 0.0 0.0 3 0.000000 14.000000 0.000000 2.000
2 0.0 0.0 3 0.000000 15.000000 0.000000 2.000
2 0.0 0.0 3 0.000000 30.000000 0.000000 2.000
2 0.0 0.0 3 0.000000 40.000000 0.000000 2.000
2 0.0 0.0 3 0.000000 10.000000 0.000000 2.000
];

%% branch data
% fbus tbus r x b rateA rateB rateC ratio angle status
mpc.branch = [
1 2 0.00281 0.0281 0.00712 400.0 400.0 400.0 0.0
1 4 0.00304 0.0304 0.00658 426 426 426 0.0
1 10 0.00064 0.0064 0.03126 426 426 426 0.0
2 3 0.00108 0.0108 0.01852 426 426 426 0.0
3 4 0.00297 0.0297 0.00674 426 426 426 1.05
4 10 0.00297 0.0297 0.00674 240.0 240.0 240.0 0.0
2 5 0.00297 0.0297 0.00674 426 426 426 0.0
];
```

**MATPOWER (“.m”)**

**PSS(R)E v33 specification (“.raw”)**

*(support PowerWorld for PSSE conversions)*

## Distribution

```
New Circuit.3bus_bal
! define a really stiff source
~ basekv=230 pu=1.00 MVAsc3=200000 MVAsc1=210000

! Substation Transformer
New Transformer.SubXF Phases=3 Windings=2 Xhl=0.01
~ wdg=1 bus=sourcebus conn=wyw kv=230 kva=25000 %r=0.0005
~ wdg=2 bus=Substation conn=wyw kv=13.8 kva=25000 %r=0.0005

! Define Linecodes
New Linecode.556MCM nphases=3 basefreq=60 ! ohms per 5 mile
~ rmatrix = ( 0.1088 0.0400 0.1088 0.0400 0.0400 0.1088 )
~ xmatrix = ( 0.0583 0.0233 0.0583 0.0233 0.0233 0.0583 )
~ cmatrix = ( 50.92958178940651 -0 50.92958178940651 -0 50.92958178940651 ) ! small cap

New Linecode.4/0QUAD nphases=3 basefreq=60 ! ohms per 100ft
~ rmatrix = ( 0.1167 0.0467 0.1167 0.0467 0.0467 0.1167 )
~ xmatrix = ( 0.0667 0.0267 0.0667 0.0267 0.0267 0.0667 )
~ cmatrix = ( 50.92958178940651 -0 50.92958178940651 -0 50.92958178940651 ) ! small ca

! Define lines
New Line.OHLine bus1=Substation.1.2.3 Primary.1.2.3 linecode = 556MCM length=1 normamps=600
New Line.Quad Bus1=Primary.1.2.3 loadbus.1.2.3 linecode = 4/0QUAD length=1 normamps=6000 e

! Loads - single phase
New Load.L1 phases=1 loadbus.1.0 ( 13.8 3 sqrt / ) kW=3000 kvar=1500 model=1
New Load.L2 phases=1 loadbus.2.0 ( 13.8 3 sqrt / ) kW=3000 kvar=1500 model=1
New Load.L3 phases=1 loadbus.3.0 ( 13.8 3 sqrt / ) kW=3000 kvar=1500 model=1

! GENERATORS DEFINITIONS
New generator.gen1 Bus1=loadbus.1.2.3 Phases=3 kv=( 13.8 3 sqrt / ) kW=2000 pf=1 conn=wyw Model

Set VoltageBases = "230,13.8"
Set tolerance=0.000001
set defaultbasefreq=60

! Loads - single phase
New Load.L1 phases=1 loadbus.1.0 ( 13.8 3 sqrt / ) kW=3000 kvar=1500 model=1
New Load.L2 phases=1 loadbus.2.0 ( 13.8 3 sqrt / ) kW=3000 kvar=1500 model=1
New Load.L3 phases=1 loadbus.3.0 ( 13.8 3 sqrt / ) kW=3000 kvar=1500 model=1

! GENERATORS DEFINITIONS
New generator.gen1 Bus1=loadbus.1.2.3 Phases=3 kv=( 13.8 3 sqrt / ) kW=2000 pf=1 conn=wyw Model

Set VoltageBases = "230,13.8"
Set tolerance=0.000001
set defaultbasefreq=60
```

**OpenDSS (“.dss”)**

## Boundary file

```
[
{
"transmission_boundary": "5",
"distribution_boundary": "3bus_unbal.voltage_source.source"
},
{
"transmission_boundary": "6",
"distribution_boundary": "3bus_bal.voltage_source.source"
}
]
```

**JSON (“.json”)**

*other proprietary file  
formats supported  
via DiTTo [4]*

[4] “DiTTo (Distribution Transformation Tool),” 2021, Accessed: Aug. 06, 2021. [Online]. Available: <https://github.com/NREL/ditto>

# Using PowerModelsITD.jl: Solving

## Case w/ 1 distro. system

```

1 using PowerModelsITD
2 import Ipopt
3 ipopt = Ipopt.Optimizer
4
5 # Path for the files
6 pmitd_path = joinpath(dirname(pathof(PowerModelsITD)), "..")
7
8 # Files
9 pm_file = joinpath(pmitd_path, "test/data/transmission/case5_withload.m")
10 pmd_file = joinpath(pmitd_path, "test/data/distribution/case3_balanced.dss")
11 boundary_file = joinpath(pmitd_path, "test/data/json/case5_case3_bal.json")
12
13 pmitd_type = NLPowerModelITD{ACPPowerModel, ACPUPowerModel}
14
15 result = solve_opfitd(pm_file, pmd_files, boundary_file, pmitd_type, ipopt)
16

```

Simple User Interface

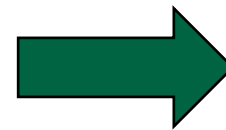
## Case w/ 2 distro. systems

```

1 using PowerModelsITD
2 import Ipopt
3 ipopt = Ipopt.Optimizer
4
5 # Path for the files
6 pmitd_path = joinpath(dirname(pathof(PowerModelsITD)), "..")
7
8 # Files
9 pm_file = joinpath(pmitd_path, "test/data/transmission/case5_with2loads.m")
10 pmd_file1 = joinpath(pmitd_path, "test/data/distribution/case3_unbalanced.dss")
11 pmd_file2 = joinpath(pmitd_path, "test/data/distribution/case3_balanced.dss")
12 boundary_file = joinpath(pmitd_path, "test/data/json/case5_case3x2_unbal_bal.json")
13
14 pmd_files = [pmd_file1, pmd_file2] # vector of files
15 pmitd_type = NLPowerModelITD{ACPPowerModel, ACPUPowerModel}
16
17 result = solve_opfitd(pm_file, pmd_files, boundary_file, pmitd_type, ipopt)
18

```

Easy User Adoption





# Using PowerModelsITD.jl: Results

```
julia> result
Dict{String, Any} with 8 entries:
  "solve_time"      => 0.12712
  "optimizer"       => "Ipopt"
  "termination_status" => LOCALLY_SOLVED
  "dual_status"      => FEASIBLE_POINT
  "primal_status"    => FEASIBLE_POINT
  "objective"        => 18146.3
  "solution"         => Dict{String, Any}{"multiinfrastructure"=>true, "it"=>Dict{String, Any}{"pmd..."
  "objective_lb"     => -Inf
```

## Transmission

```
julia> result["solution"]["it"]["pm"]
Dict{String, Any} with 6 entries:
  "baseMVA"      => 100.0
  "branch"        => Dict{String, Any}{"3"=>Dict{String, Any}{"qf"=>206.656, "qt"=>-202.276, "pt"=>221.006, "pf"=>-220.308}, "4"=>Dict{String, Any}{"qf"=>-217.108, "qt"=>221.882, "pt"=>79.0383, "pf"=>-78.3924}, "1"=...
  "gen"           => Dict{String, Any}{"4"=>Dict{String, Any}{"qg"=>56.3262, "pg"=>18.0328}, "1"=>Dict{String, Any}{"qg"=>30.0, "pg"=>40.0}, "5"=>Dict{String, Any}{"qg"=>-201.205, "pg"=>461.003}, "2"=>Dict{String, A...
  "multinetwork" => false
  "bus"           => Dict{String, Any}{"4"=>Dict{String, Any}{"va"=>-1.06955e-34, "vm"=>0.9}, "1"=>Dict{String, Any}{"va"=>3.95367, "vm"=>0.917681}, "5"=>Dict{String, Any}{"va"=>-0.949629, "vm"=>0.937736}, "2"=>Dict...
  "per_unit"      => false
```

## Distribution

```
julia> result["solution"]["it"]["pmd"]
Dict{String, Any} with 7 entries:
  "line"          => Dict{String, Any}{"3bus_unbal.quad"=>Dict{String, Any}{"qf"=>[1344.85, 1503.97, 1502.46], "qt"=>[-1333.33, -1500.0, -1500.0], "pt"=>[-3333.33, -2333.33, -2333.33], "pf"=>[3351.62, 2340.39, 2344.9...
  "settings"       => Dict{String, Any}{"sbase"=>100000.0}
  "transformer"    => Dict{String, Any}{"3bus_bal.subxf"=>Dict{String, Any}{"q"=>[[1508.51, 1508.51, 1508.51], [-1508.41, -1508.41, -1508.41]], "p"=>[[2351.59, 2351.59, 2351.59], [-2351.58, -2351.58, -2351.58]], "3bu...
  "generator"      => Dict{String, Any}{"3bus_unbal.gen1"=>Dict{String, Any}{"qg_bus"=>[-0.0, -0.0, -0.0], "qg"=>[-0.0, -0.0, -0.0], "pg"=>[666.668, 666.668, 666.668], "pg_bus"=>[666.668, 666.668, 666.668]}, "3bus_bal...
  "load"           => Dict{String, Any}{"3bus_unbal.l2"=>Dict{String, Any}{"qd_bus"=>[1500.0], "pd_bus"=>[3000.0], "qd"=>[1500.0], "pd"=>[3000.0]}, "3bus_bal.l3"=>Dict{String, Any}{"qd_bus"=>[1500.0], "pd_bus"=>[3000.0]...
  "bus"            => Dict{String, Any}{"3bus_unbal.loadbus"=>Dict{String, Any}{"va"=>[-1.10106, -120.971, 119.172], "vm"=>[7.38801, 7.42776, 7.41273]}, "3bus_bal.substation"=>Dict{String, Any}{"va"=>[-1.08179, -121.0...
  "per_unit"       => false
```

## Boundary

```
julia> result["solution"]["it"]["pmitd"]["boundary"]
Dict{String, Any} with 4 entries:
  "(100001, 5, voltage_source.3bus_unbal.source)" => Dict{String, Any}{"pbound_fr"=>[8068.8], "qbound_fr"=>[4367.42]}
  "(100001, voltage_source.3bus_unbal.source, 5)" => Dict{String, Any}{"pbound_to"=>[-3367.36, -2346.47, -2354.97], "qbound_to"=>[-1355.14, -1507.53, -1504.75]}
  "(100002, voltage_source.3bus_bal.source, 6)"    => Dict{String, Any}{"pbound_to"=>[-2351.62, -2351.62, -2351.62], "qbound_to"=>[-1508.64, -1508.64, -1508.64]}
  "(100002, 6, voltage_source.3bus_bal.source)"    => Dict{String, Any}{"pbound_fr"=>[7054.87], "qbound_fr"=>[4525.93]}
```

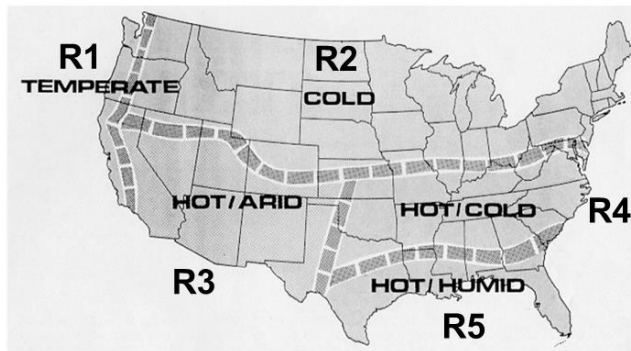


# Use Cases & Tests

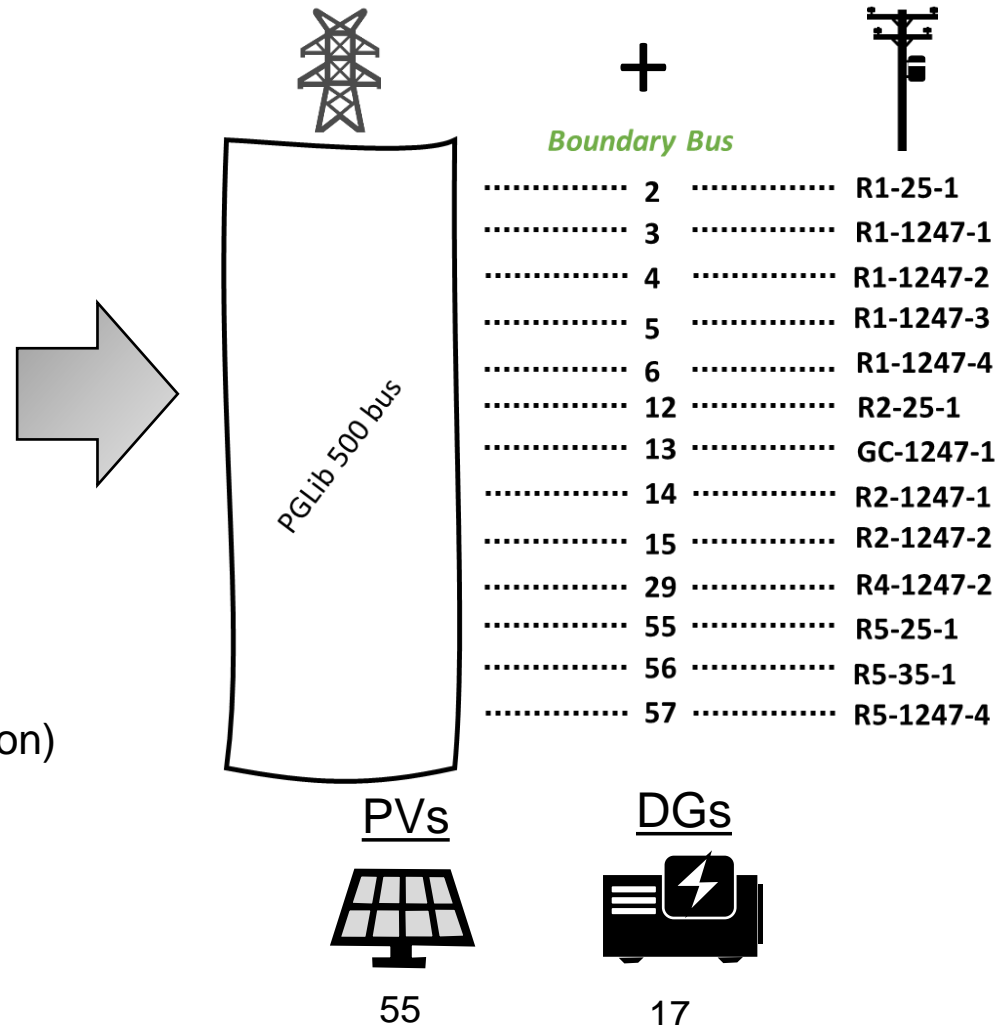
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# Use Cases & Tests: OPF

## Taxonomy PNNL Cases [5]



**Totals:**  
**Buses/Nodes:** 19,637  
 (w/ +500 from transmission)  
**Edges:** 20,595 (w/ +733  
 from transmission)



Test Cases	N	E
case_r1_25_1	759	762
case_r1_1247_1	3403	3583
case_r1_1247_2	1450	1527
case_r1_1247_3	168	165
case_r1_1247_4	970	981
case_r2_25_1	1617	1681
case_gc_1247_1	96	93
case_r2_1247_1	1731	1750
case_r2_1247_2	1207	1275
case_r4_1247_2	1155	1202
case_r5_25_1	3116	3250
case_r5_35_1	1435	1505
case_r5_1247_4	2030	2088

**Totals:** 19,137 19,862

# Use Cases & Tests: OPF Results



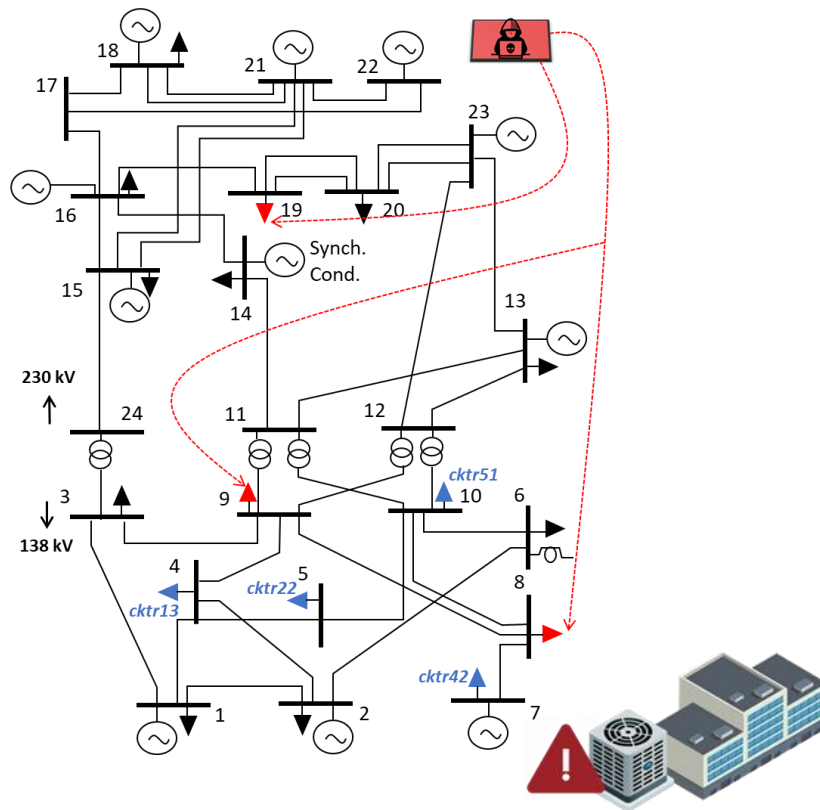
**CPU:** x6 Cores @ 2.80 Ghz  
**RAM:** 128 GB

**Ipopt vers.:** 3.14.4  
**MUMPS vers.:** 5.4.1

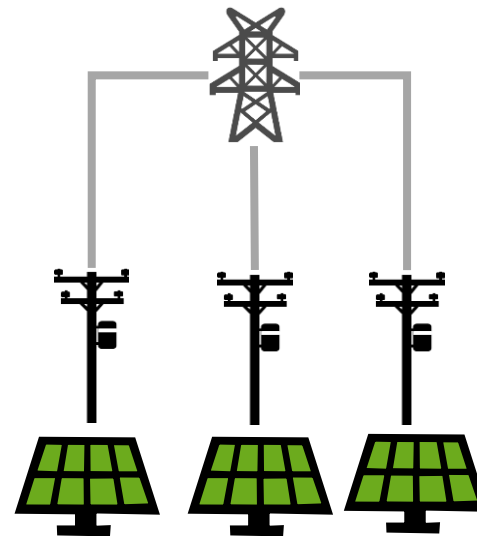
Case PNNL - All Regions			
Formulation	\$/hr	Time (s)	Iterations
ACP-ACPU	422,095.2350	525.154	94
IVR-IVRU	422,095.2348	360.954	99
NFA-NFAU	412,286.7567	10.860	24
ACR-FBSUBF	422,074.7218	226.852	97
BFA-LinDist3	412,286.7567	146.084	45
SOCBF-LinDist3	421,529.7893	241.203	75

# Use Cases & Tests: Other Use Cases

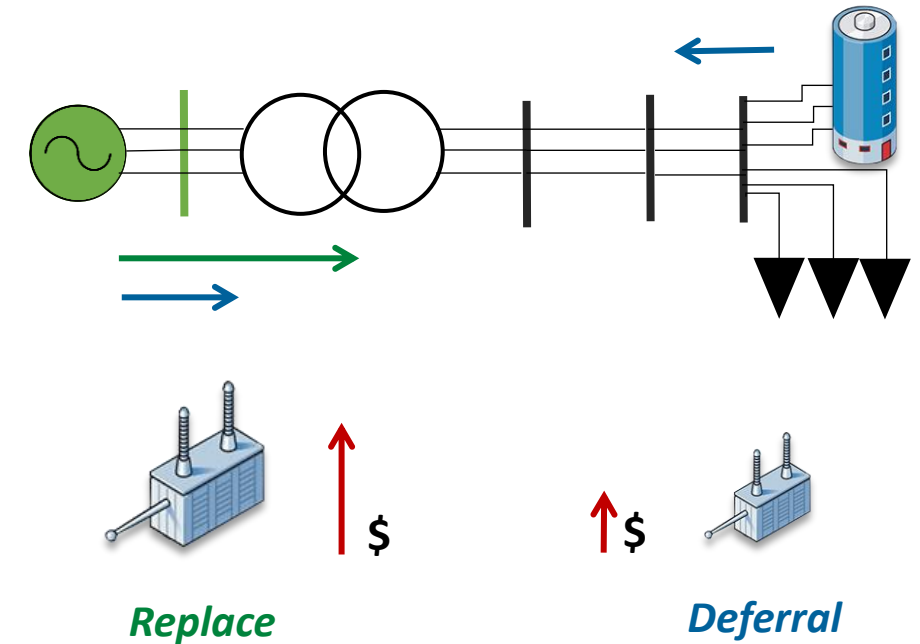
## T&D Market Manipulation via Load-Altering Attacks [6]



## Hosting Limit Capacity for T&D



## T&D Coordination Transformer Deferral







# Thank you Questions?

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## Contacts:

- Juan Ospina: [jjospina@lanl.gov](mailto:jjospina@lanl.gov)
- David M. Fobes: [dfobes@lanl.gov](mailto:dfobes@lanl.gov)

