

# DRAFT – Infinite Swapping in Bayesian Inverse Problems. – DRAFT

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## Abstract

**Keywords:** Bayesian inversion; Parallel tempering; Measurement noise; Markov Chain Monte Carlo; uncertainty quantification.

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- 1 Introduction
- 2 Bayesian inverse problems
- 3 Parallel Tempering and the infinite swapping limit
- 4 Numerical experiments

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