

Nombre: Steven Landajuri, Juan Valle, Jaime Juan de la Guz

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Taller N° 1

$$F(x) = 3x + 2$$

$$F'(x) = 3$$

$$f(x) = 3$$

$$f(x) = \int 3 dx$$

$$f(x) = 3x + C$$

$$e^x x^8 - e^x x^2 + e^x \frac{x}{3} - e^x \frac{1}{12} = f(x)$$

$$\bullet f(x) = 2x^3 + 4x^2 - 5x + 1$$

$$f'(x) = \frac{d}{dx}(2x^3) + \frac{d}{dx}(4x^2) - \frac{d}{dx}(5x) + \frac{d}{dx}(1)$$

$$f'(x) = 3(2x^{3-1}) + 2(4x^{2-1}) - 5$$

$$f'(x) = 6x^2 + 8x - 5$$

Encontrar la antiderivada; usando la derivada $f'(x)$ y la condición inicial $f(1) = 2$ encuentra la función $f(x)$ original.

$$f'(x) = 6x^2 + 8x - 5$$

$$f(1) = 2$$

$$f(x) = \int (6x^2 + 8x - 5) dx$$

$$f(x) = \int 6x^2 dx + \int 8x dx - \int 5 dx$$

$$f(x) = 6 \int x^2 dx + 8 \int x dx - 5 \int dx$$

Blywers. Aa

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$$f(x) = 6 \left(\frac{x^2+1}{2+1} \right) + 8 \left(\frac{x^1+1}{1+1} \right) - 5x$$

$$f(x) = 6 \left(\frac{x^3}{3} \right) + 8 \left(\frac{x^2}{2} \right) - 5x + c$$

$$f(x) = 2x^3 + 4x^2 - 5x + c$$

$$2 = 2(1)^3 + 4(1)^2 - 5(1) + c$$

$$2 = 2 + 4 - 5 + c$$

$$2 - 1 = c$$

$$1 = c$$

$$f(x) = 2x^3 + 4x^2 - 5x + 1$$

$$f(x) = \frac{1}{4}x^4 - \frac{2}{3}x^3 + 5x^2 - 8x + 3$$

$$f'(x) = \frac{d}{dx} \left(\frac{1}{4}x^4 \right) - \frac{d}{dx} \left(\frac{2}{3}x^3 \right) + \frac{d}{dx} \left(5x^2 \right) - \frac{d}{dx} \left(8x \right) + \frac{d}{dx} (3)$$

$$f'(x) = 4 \left(\frac{1}{4}x^{4-1} \right) - 3 \left(\frac{2}{3}x^{3-1} \right) + 2 \left(5x^{2-1} \right) - 8$$

$$f'(x) = x^3 - 2x^2 + 10x - 8$$

$$f(x) = x^3 - 2x^2 + 10x - 8$$

$$\int x^3 - 2x^2 + 10x - 8$$
$$\int x^3 dx - 2 \int x^2 dx + 10 \int x dx - 3 \int dx$$

$$\left(\frac{x^4}{4} \right) - 2 \left(\frac{x^3}{3} \right) + 10 \left(\frac{x^2}{2} \right) - 8x + c$$

$$f(2) = 2$$

$$2 = \frac{x^4}{4} - 2 \left(\frac{x^3}{3} \right) + 5x^2 - 8x + c$$

$$2 = 2^4 - 2 \left(\frac{2^3}{3} \right) + 5(2)^2 - 8(2) + c$$

$$2 = \frac{16}{3} + c$$

$$\frac{19}{3} = c$$

$$\frac{x^4}{4} - 2 \left(\frac{x^3}{3} \right) + 5x^2 - 8x + c$$

$$f(x) = 2x^3 + 4x^2 - 5x + C \quad f(1) = 2$$

$$2 = 2(1)^3 + 4(1)^2 - 5(1) + C$$

$$2 = 2 + 4 - 5 + C$$

$$2 = 1 + C$$

$$1 = C$$

$$1 = C$$

$$f(x) = 2x^3 + 4x^2 - 5x + 1$$

Encontrar la derivada:

$$f(x) = \frac{1}{4}x^4 - \frac{2}{3}x^3 + 5x^2 - 8x + 3$$

$$f'(x) = \frac{d}{dx}\left(\frac{1}{4}x^4\right) - \frac{d}{dx}\left(\frac{2}{3}x^3\right) + \frac{d}{dx}(5x^2) - \frac{d}{dx}(8x) + \frac{d}{dx}(3)$$

$$f'(x) = 4\left(\frac{1}{4}x^{4-1}\right) - 3\left(\frac{2}{3}x^{3-1}\right) + 2(5x^1) - 8$$

$$f'(x) = x^3 - 2x^2 + 10x - 8$$

$$2. \quad f'(x) < x^3 - 2x^2 + 10x - 8$$

$$= \int (x^3 - 2x^2 + 10x - 8) dx$$

$$= \int x^3 dx - \int 2x^2 dx - \int 10x dx - \int 8 dx$$

$$= \frac{x^4}{4} - 2 \frac{x^3}{3} + 5x^2 - 8x + C$$

$$3. \quad f(0) = 2$$

$$S = \frac{x^4}{4} - 2 \frac{x^3}{3} + 5x^2 - 8x + C$$

$$S = \frac{2^4}{4} - 2 \frac{(2)^3}{3} + 5(2)^2 - 8(2) + C$$

$$S = \frac{8}{3} + C$$

$$\frac{10}{3} = C$$