

# Equilibrium Effects of Housing Subsidies: Evidence from a Policy Notch in Colombia

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# ARE MARKET-ORIENTED HOUSING POLICIES EFFECTIVE?

- ▶ Governments implement various **market-oriented** policies to promote housing construction and home-ownership
  - Subsidies or tax incentives
- ▶ Housing market effect?
  - Prices, quantities, **type of housing**
- ▶ Does incentivizing home-ownership work?
  - How big are the efficiency costs?
  - Are there any unintended consequences?
  - How much households and developers benefit?
  - What happens if these policies are removed?
- ▶ I use quasi-experimental variation to estimate a housing market equilibrium model.
- ▶ Counterfactual policy evaluation and welfare analysis.



# COLOMBIAN HOUSING POLICY

## ► Policy tools:

- Subsidies to low-income households low-cost housing.
- Tax incentives to developers who build low-cost housing.
- A price cap defining low-cost housing.

135 monthly minimum wages (*mMW*)  $\approx$  40,000 \$USD

## ► Empirical advantages of Colombian setting:

- Price cap
  - Discontinuous incentives for developers and households to bunch at the cutoff.
- Unique and novel data
  - Census data for all new construction projects.
  - Administrative records for the subsidies.
- Subsidy expansion (2006-18)

# THIS PAPER

## I. Descriptive evidence

- Policy description and characterization of observed equilibrium.
- Evidence of housing market responding to the subsidy scheme.

## II. Hedonic equilibrium of housing supply and demand

- Product differentiation and heterogeneous developers and households.
- Identification using bunching and policy changes.

## III. Proposed policy counterfactual and welfare

- Colombian 2021 tax reform - Remove tax incentives to developers.
  - Policy change – phasing out price caps
- Effects on households and developers

# RESULTS

## I. Behavioural responses induced by the subsidy scheme.

- Bunching at price cutoff
- Larger response as the subsidies increase → market share at cutoff went from 1% to 7%
- Households downsize → they buy units up to 30% percent smaller to benefit from the subsidy

## II. Estimate a model that rationalizes the market observed equilibrium

- Elasticity of substitution between housing and consumption is 0.9

## III. Effects of the proposed policies

- Colombian 2021 tax reform proposal could create a housing shortage.
- Removing the price cap increases welfare.

# LITERATURE AND CONTRIBUTION

Integrates the bunching and hedonic literatures to propose a method to think about welfare consequences of housing policies

Bunching	Hedonic	Housing Policy
<ul style="list-style-type: none"><li>▶ Housing market</li><li>▶ Link to model</li><li>▶ Supply and demand</li></ul>	<ul style="list-style-type: none"><li>▶ Policy notch</li><li>▶ Supply side</li><li>▶ Identification</li></ul>	<ul style="list-style-type: none"><li>▶ Evidence</li><li>▶ Method</li><li>▶ Welfare</li></ul>
<ul style="list-style-type: none"><li>- Housing market applications Best et al. (2019), DeFusco and Paciorek (2017)</li><li>- Methodology <i>Notches &gt;&gt; Kinks</i>: Kleven (2016), Bertanha et al. (2021), Blomquist et al. (2021)</li></ul>	<ul style="list-style-type: none"><li>- Seminal paper S. Rosen (1974), Epple (1987)</li><li>- Recent Contributions Bajari and Benkard (2005), Heckman et al. (2010), Epple et al. (2020), Chernozhukov et al. (2021)</li><li>- Reviews Kuminoff et al. (2013), Greenstone (2017)</li></ul>	<ul style="list-style-type: none"><li>- Developers subsidies Baum-Snow and Marion (2009), Soltas (2020), Sinai and Waldfogel (2005)</li><li>- Households Subsidies Carozzi et al. (2020)</li><li>- Incidence and welfare Poterba (1992), Galiani et al. (2015)</li></ul>

I. DESCRIPTIVE ANALYSIS:  
DATA, POLICY AND OBSERVED  
EQUILIBRIUM

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# POLICY TOOLS

## 1. Supply Subsidies

- Value Added Tax (VAT) refund

## 2. Demand Subsidies

- Downpayment
- Interest rate

Income  $\leq$  4 monthly minimum wages (mMW) classify

## 3. Targeting tool for the subsidy:

- Only new *low cost* units are eligible

$$\text{Low cost} = \begin{cases} 1 & \text{if } P_t \leq \mathbf{135} \text{ mMW}_t \\ 0 & \text{if } P_t > \mathbf{135} \text{ mMW}_t \end{cases}$$

Note: **135 mMW**  $\approx$  40,000 \$USD





# DATA

## 1. Administrative Records from Minister of Housing

- Subsidy size
- Mortgage information

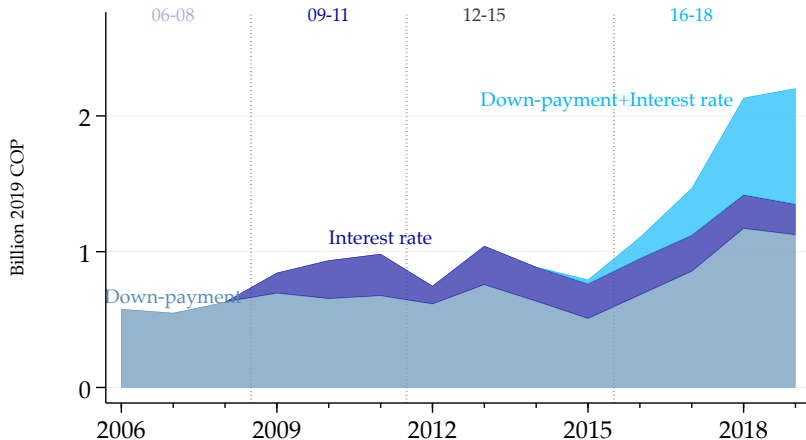
→ Government expenditure on each subsidy

## 2. New Construction Census (Camacol)

- 126 Municipalities
- Years: 2006-2018
- Sale prices and quantities
- Unit characteristics: **size**, location, # rooms, # bathrooms, etc.
- Development characteristics: lot size, # towers, # floors, developer id, etc.

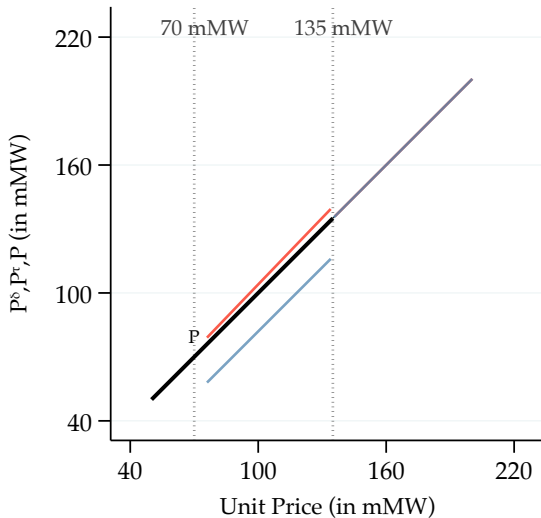
Everything measured in monthly minimum wages ( *mMW*) or 2019 *COP* Inflation and *mMW* change

# GOVERNMENT EXPENDITURE AND POLICY EXPANSION



- Total housing subsidies beneficiaries 100'000 in 2019
- 2 billion COP  $\sim$  0.25% Colombian GDP
- Colombian Conditional Cash Transfers 3, 6 billion COP for 2.3 million households

# THE NOTCH



**Transaction Price**

$P$

**Developers Price**

$$P^\delta = P \cdot (1 + \delta):$$

$\delta$  = Tax refund

**Households price**

$$P^\tau = P - \tau$$

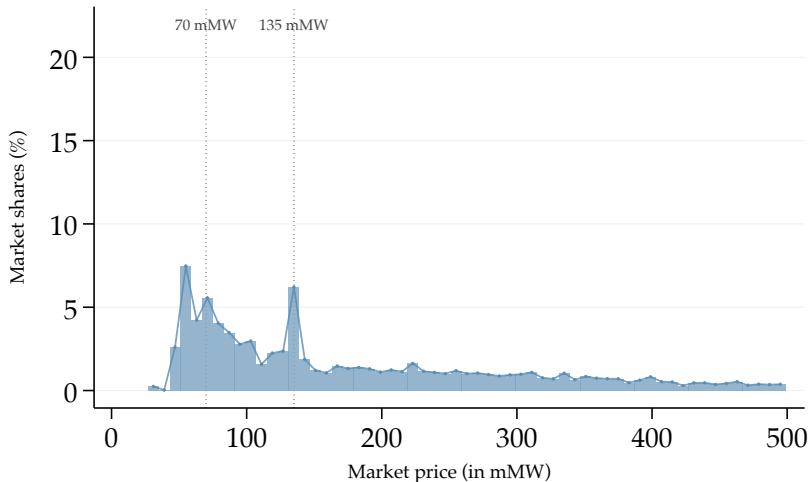
$\tau$  = Subsidy

Agents benefit from buying/selling *low cost housing* ( $P \leq 135mMW$ )

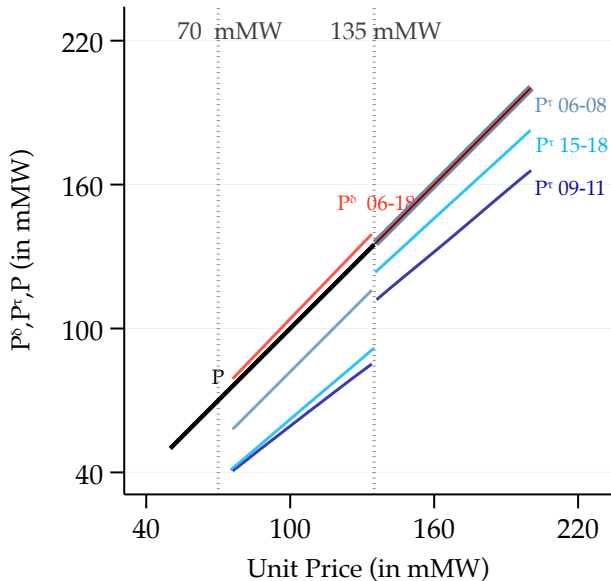
# BUNCHING AT THE LOW-COST HOUSING PRICE LIMIT

Only downpayment subsidy

2006-08



# THE DEMAND NOTCH INCREASES OVER TIME



Supply Notch  $\delta$

2006-18 4%

Demand Notch  $\tau_t$

2006-08: 18 mMW

2009-11: 26 mMW

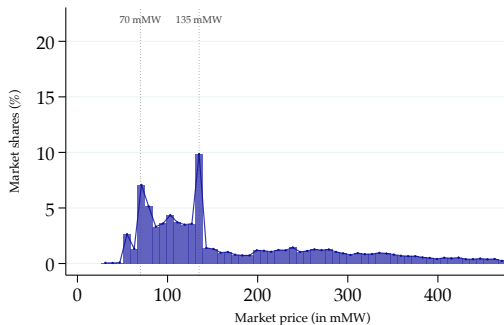
2016-18: 33 mMW

Note: 2012-15 Too many changes and free housing at 70 mMW

# LARGER BUNCHING AS NOTCH INCREASES

*Downpayment and interest rate subsidies*

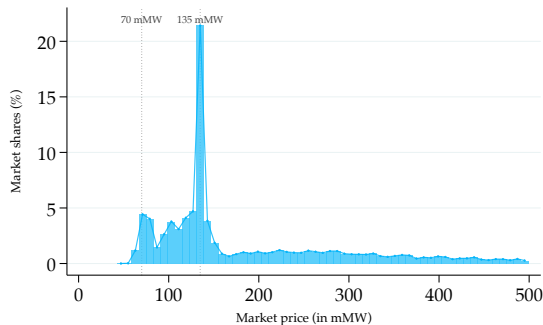
**2009-11**



*Notch: 18 mMW*

*Subsidy expansion*

**2016-18**

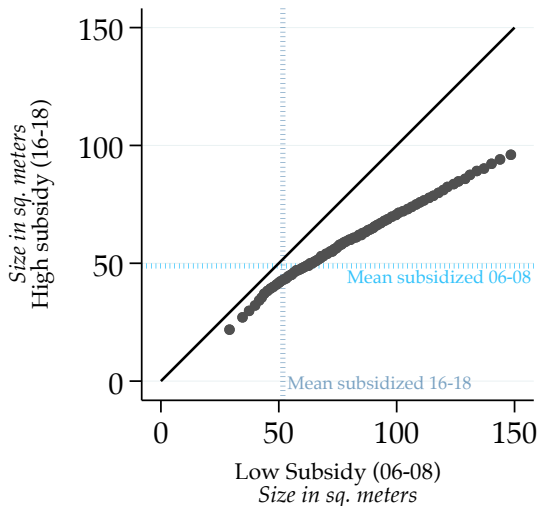


*Notch: 33 mMW*

# CHANGES IN HOUSING STOCK CHARACTERISTICS

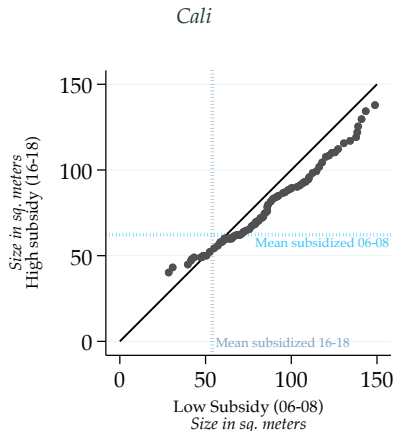
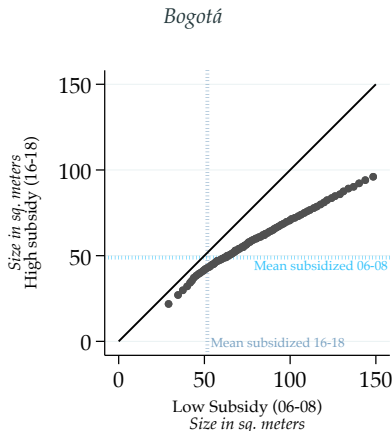
- Changes in unit size (quantile to quantile plot)

*Bogotá*



# CHANGES IN HOUSING STOCK CHARACTERISTICS

## ► Changes in unit size



## ► Why size?

- Continuous, easy to measure, monotonic relationship with price and income.
- In contrast to most datasets, I observe it.



## II. EQUILIBRIUM MODEL OF HOUSING SUPPLY AND DEMAND

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# A STYLIZED HOUSING MARKET MODEL

## 1. Housing

- Differentiated product described by its size  $h \in \mathcal{H}$
- Price depends on size  $P(h)$

## 2. Households $i \in I$ , Heterogeneous in Income $Y_i \sim F_Y$

- Choose  $h_i$  and consumption  $C_i$  to maximize Utility  $U(C_i, h_i; \theta)$

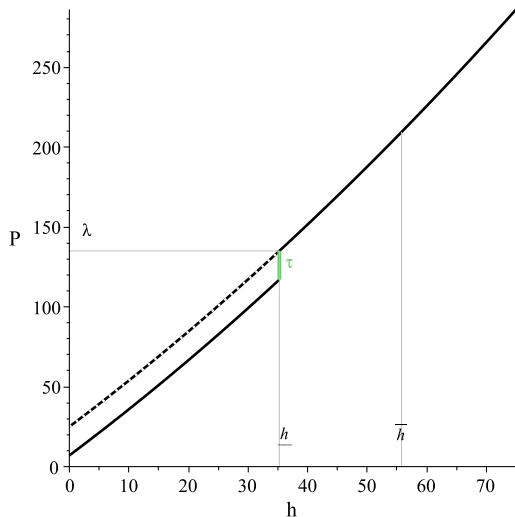
## 3. Developers $j \in J$ , Heterogeneous in Productivity $A_j \sim G_A$

- Choose  $h_j$  to maximize profits
- Building costs  $B(A_j, h_j, Q(h_j); \beta)$

## 4. Competitive Market Equilibrium

- Price function  $P(h) \rightarrow$  clears the market  $\forall h \in \mathcal{H}$

# HOUSEHOLDS' OPTIMAL CHOICES



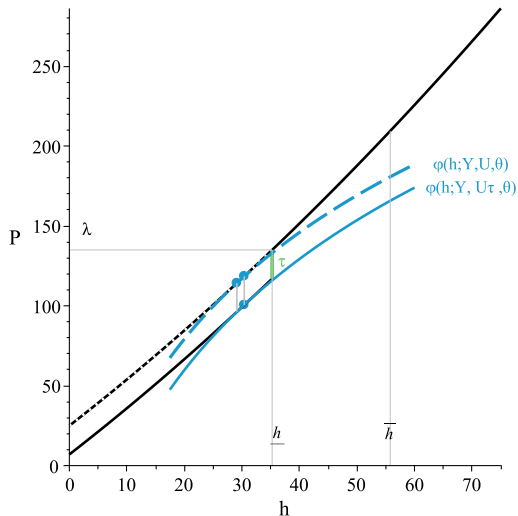
- **Implicit Price Function**

$$P(h)$$

- **Subsidy**

$$\tau$$

# HOUSEHOLDS' OPTIMAL CHOICES



- **Implicit Price Function**

$$P(h)$$

- **Subsidy**

$$\tau$$

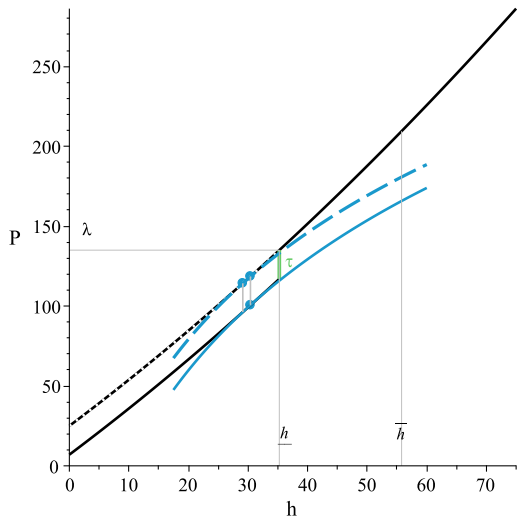
- **Bid functions**

$$\varphi_D(h, Y, \bar{U}; \theta)$$

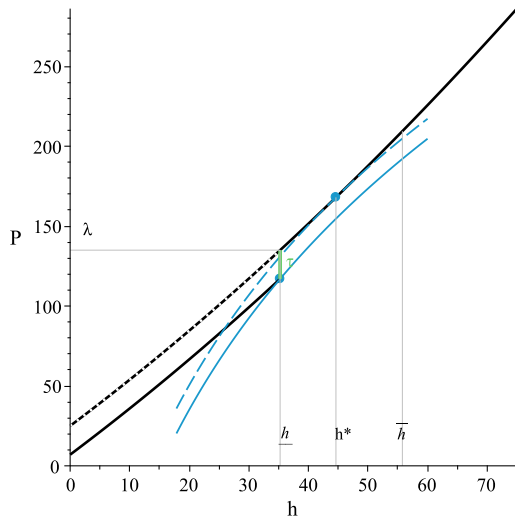
- $\bar{U} = U(h, Y_i - \varphi_D; \theta)$
- $\bar{U}_\tau = U(h, Y_i - \varphi_D + \tau; \theta)$

# HOUSEHOLDS' OPTIMAL CHOICES

A. Subsidized

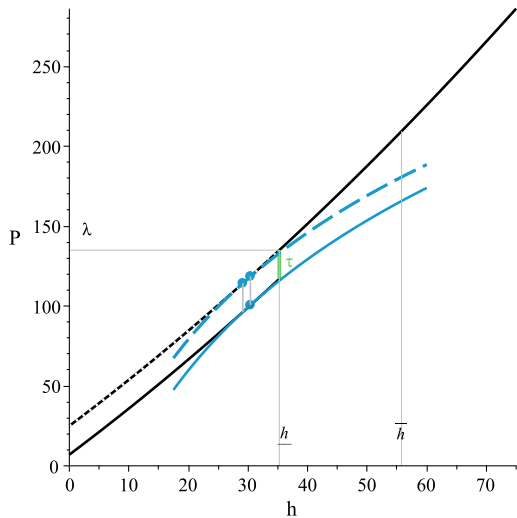


B. Marginally Subsidized and Bunchers

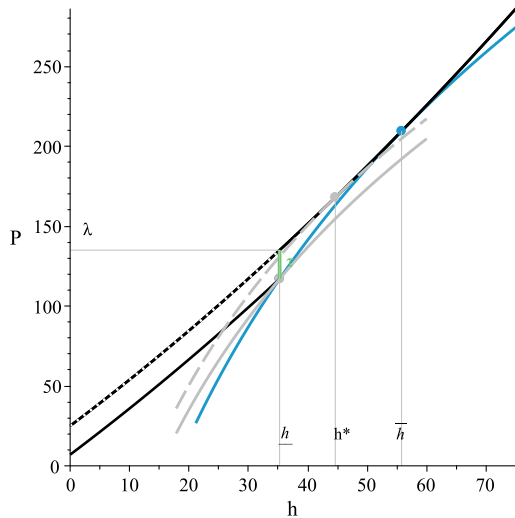


# HOUSEHOLDS' OPTIMAL CHOICES

A. Subsidized



B. Marginally Subsidized and Bunchers



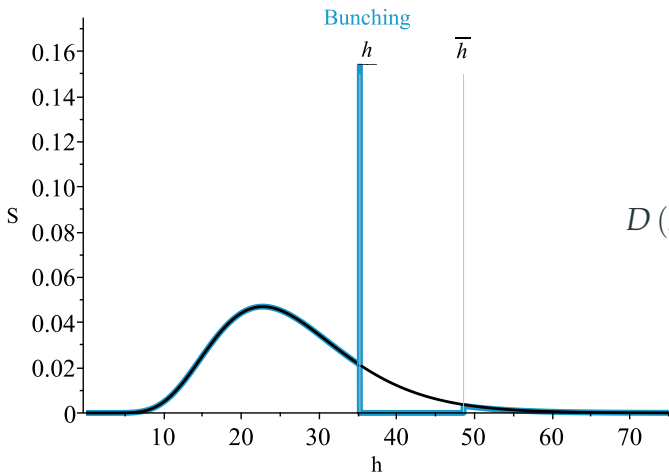
## HOUSEHOLDS' DEMAND FUNCTION

$$h^D(Y_i) = \begin{cases} h^*(Y_i, \tau; \theta, \boldsymbol{\rho}, \lambda) & \text{if } Y_i \leq \underline{Y} \\ \underline{h} & \text{if } \underline{Y} < Y_i < \bar{Y} \\ h^*(Y_i, \tau; \theta, \boldsymbol{\rho}, \lambda) & \text{if } \bar{Y} \leq Y_i \end{cases}$$

- Tangency conditions:  $h^*(Y_i, \tau; \theta, \boldsymbol{\rho}, \lambda)$
- Income and unit size:  $Y_i = \tilde{Y}(h, \tau; \theta, \boldsymbol{\rho}, \lambda) = h^{*-1}(h_i, \tau; \theta, \boldsymbol{\rho}, \lambda)$

# AGGREGATE DEMAND DENSITY

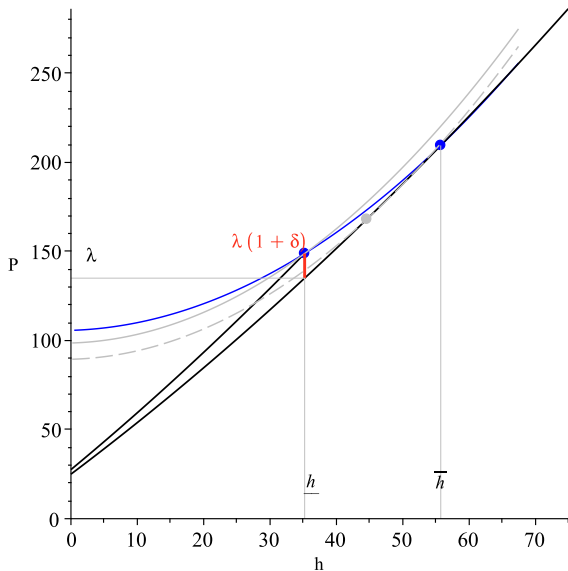
How to aggregate? → Change of variable formula using  $F_y$



$$D(h) = \begin{cases} f_{h^*}(h) \, dh & \text{if } h < \underline{h} \\ f_{h^*}(h) \, dh + \int_{\underline{h}}^{\bar{h}} f_{h^*}(h) \, dh & \text{if } \underline{h} = h \\ 0 & \text{if } h \in (\underline{h}, \bar{h}) \\ f_{h^*}(h) \, dh & \text{if } \bar{h} \leq h \end{cases}$$



# DEVELOPERS' CHOICES



- **Implicit Price Function**

$$P(h)$$

- **Tax incentives**

$$P(h) \cdot (1 + \delta)$$

- **Offer Functions**

$$\varphi_S(h, A_j, \bar{\pi}; \beta)$$

$$\bar{\pi} = \pi(h, A_j, P(h); \beta)$$

$$\bar{\pi}_\delta = \pi(h, A_j, P(h) \cdot (1 + \delta); \beta)$$

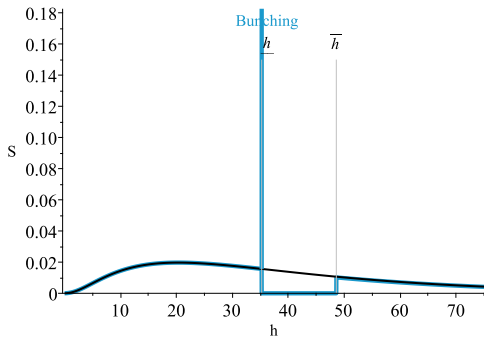
ASSUMPTION:

$$Q_j = \alpha_0 + \alpha_1 \cdot h_j$$

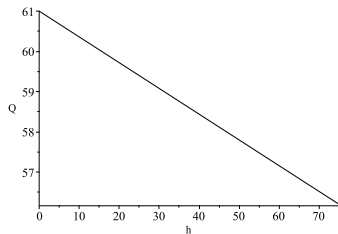
*exogenous*

# DEVELOPERS AGGREGATE SUPPLY DENSITY

Density function  $g_h(h)$

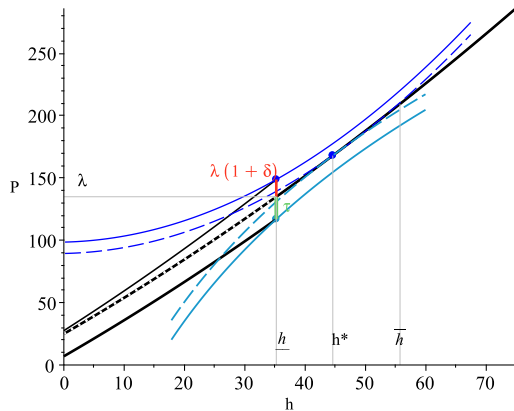
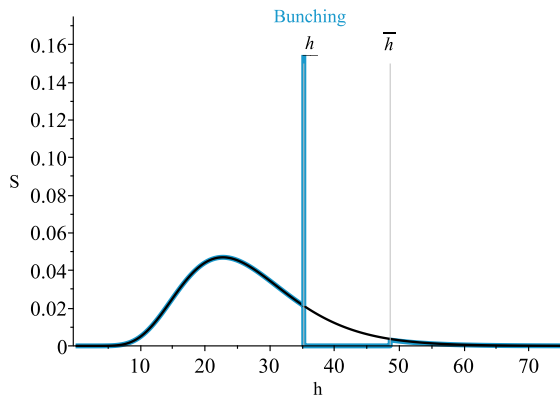


Unit supply function  $Q(h)$



$$S(h) = \begin{cases} g_{h^*}(h) \cdot Q(h) & \text{if } h < \underline{h} \\ \left( g_{\underline{h}^*}(\underline{h}) + \int_{\underline{h}}^{\bar{h}} g_{h^*}(h) \, dh \right) \cdot Q(\underline{h}) & \text{if } \underline{h} = h \\ 0 & \text{if } \underline{h} < h < \bar{h} \\ g_{h^*} \cdot Q(h) & \text{if } \bar{h} \leq h \end{cases}$$

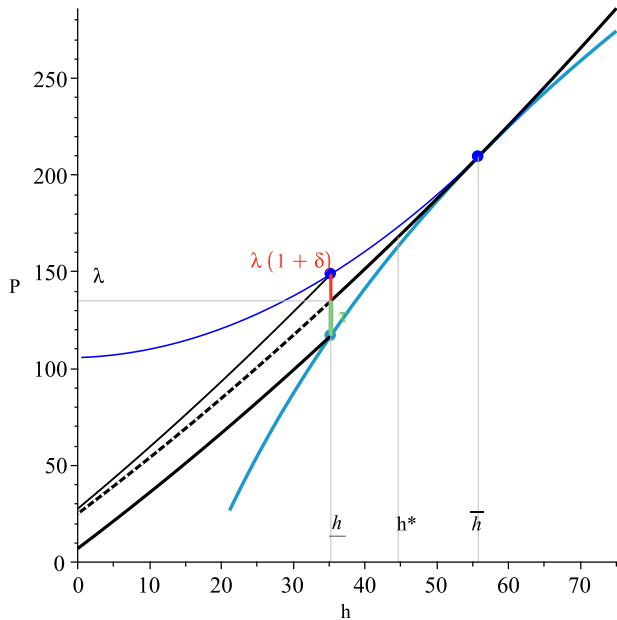
# EQUILIBRIUM



# IDENTIFICATION

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# MARGINAL BUNCHER CONDITION



# MARGINAL BUNCHER CONDITION

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## *Marginal Buncher Condition*

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Household	$V_D = U\left(\bar{Y} - P\left(\bar{h}\right), \bar{h}; \theta\right) - U\left(\bar{Y} - P^\tau\left(\underline{h}\right), \underline{h}; \theta\right) = 0$
Developer	$V_S = \pi\left(Q\left(\bar{h}\right), \bar{A}, P\left(\bar{h}\right); \beta\right) - \pi\left(Q\left(\underline{h}\right), \bar{A}; P^\delta\left(\underline{h}\right); \beta\right) = 0$

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## *Optimality Conditions*

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Income	$\bar{Y} = \tilde{Y}\left(\bar{h}; \theta, P(h), \lambda\right)$
Productivity	$\bar{A} = \tilde{A}\left(\bar{h}; \beta, P(h), \lambda\right)$

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## *Functional Forms*

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Implicit Price	$P = \rho_0 + \rho_1 \cdot h + \rho_2 \cdot h^2$
Utility	$U = \left[\frac{1}{2} \cdot C^\theta + \frac{1}{2} \cdot h^\theta\right]^{\frac{1}{\theta}}$
Unit Supply	$Q = \alpha_0 + \alpha_1 h$
Cost	$B = A_j \cdot Q \cdot h^\beta$

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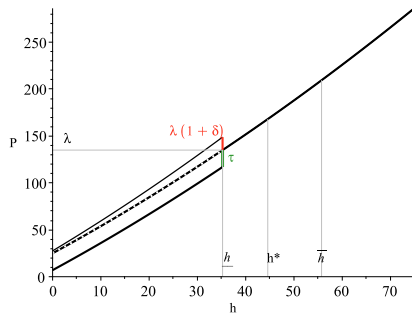
## ESTIMATION

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# ESTIMATING THE MODEL

## STEP I: Equilibrium Characterization

- Using the observed hedonic equilibrium
  - Price function:  $\rho_t = \rho_{0t}, \rho_{1t}, \rho_{2t}$
  - Size threshold:  $\underline{h} = P^{-1}(\lambda; \rho)$
  - Standard Unit Size:  $\bar{h}$
- Behavioural Responses:
  - Housing size for marginal buncher:  $\bar{h}$
- Unit Supply Function:
  - $Q = \alpha_0 + \alpha_1 \cdot h_{ltc}$
- Policy Parameters:
  - Notches:  $\tau_t, \delta$





## ESTIMATING THE MODEL

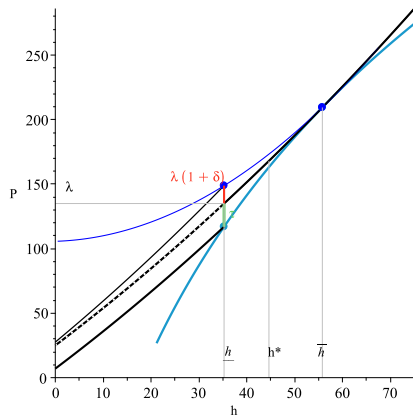
## STEP I: Equilibrium Characterization

- Observed hedonic equilibrium
  - Price function:  $\rho_t = \rho_{0t}, \rho_{1t}, \rho_{2t}$
  - Size threshold:  $\underline{h} = P^{-1}(\lambda; \rho)$
  - Standard Unit Size:  $h$
- Behavioural Responses:
  - Housing size for marginal buncher:  $\bar{h}$
- Unit Supply Function:
  - $Q = \alpha_0 + \alpha_1 \cdot h_{lhc}$
- Policy Parameters:
  - Notches:  $\tau_t, \delta$

## STEP II: Structural Parameters

$$V_D \left( \theta | \underline{h}, \bar{h}, P(h), \tau, \lambda \right) = 0$$

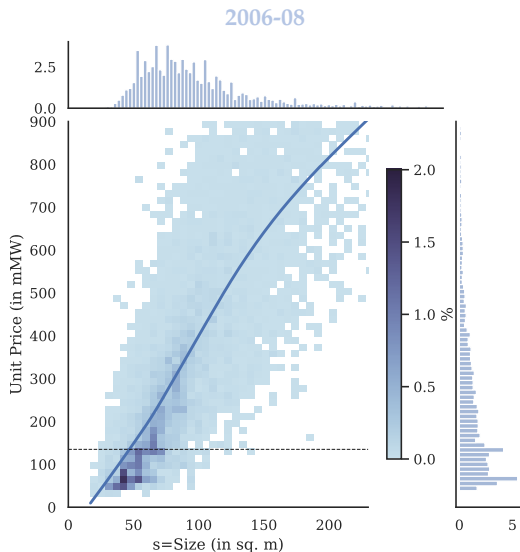
$$V_S \left( \beta | \underline{h}, \bar{h}, P(h), \alpha, \delta, \lambda \right) = 0$$



## STEP I. EQUILIBRIUM CHARACTERIZATION

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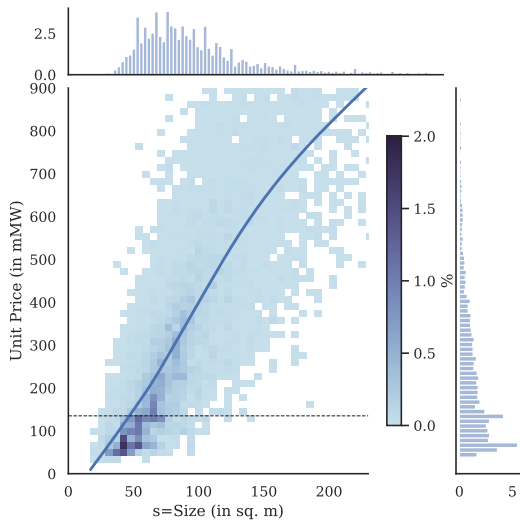
# OBSERVED EQUILIBRIUM: PRICES, QUANTITIES, AND SIZE



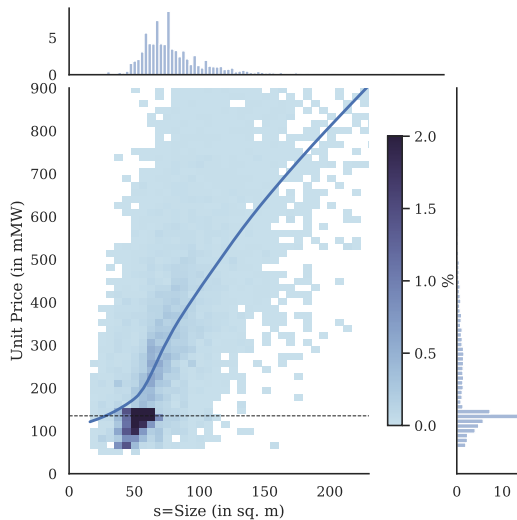
- Solid line: price vs size
- hedonic price function
- Multiple characteristics
- Reduce to a single characteristic

# OBSERVED EQUILIBRIUM: PRICES, QUANTITIES, AND SIZE

Only downpayment subsidy  
2006-08



Subsidy expansion  
2016-18



# HEDONIC PRICES AND STANDARDIZED HOUSING UNIT

- Hedonic price/Implicit price for housing size

$$P_{ltc} = \rho(s_{ltc}) + \Gamma'X_{ltc} + \omega_{ltc} \quad (1)$$

$l$ , house type in a development,  $t$  year,  $c$  city

- Simplifying assumption:  $\rho(s_{ltc}) = \rho_1 \cdot s_{ltc} + \rho_2 \cdot s_{ltc}^2$
- Identifying assumption:  $E(s_{ltc}|X_{ltc}, \omega_{ltc}) = 0$

- Standard Unit Size  $h_{ltc}$

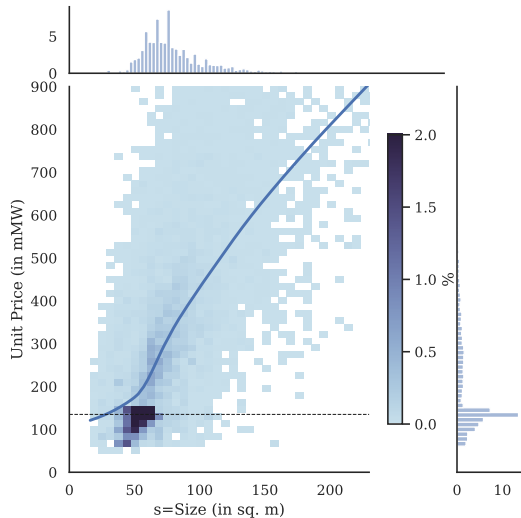
$$\rho(h_{ltc}) + \Gamma'\bar{X} + \bar{\omega} = \rho(s_{ltc}) + \Gamma'X_{ltc} + \omega_{ltc} \quad (2)$$

- Characteristics of the standard house:  $\bar{X}, \bar{\omega}$

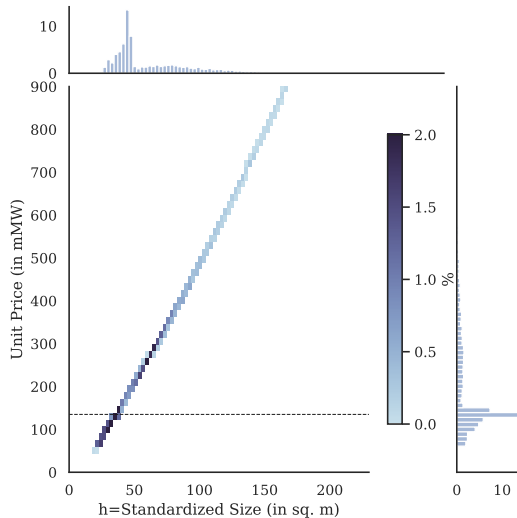
# FROM SIZE $s$ TO STANDARDIZED SIZE $h$

Subsidy expansion 2016-18

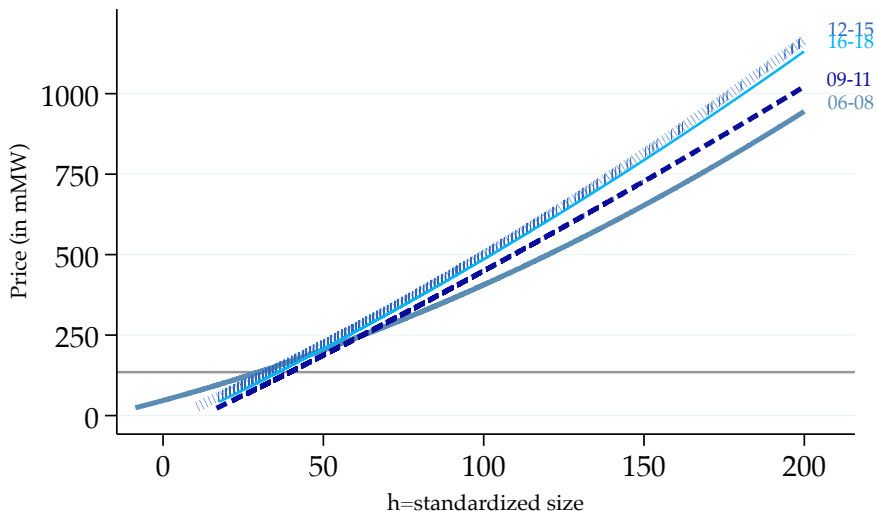
Observed size



Standardized Unit

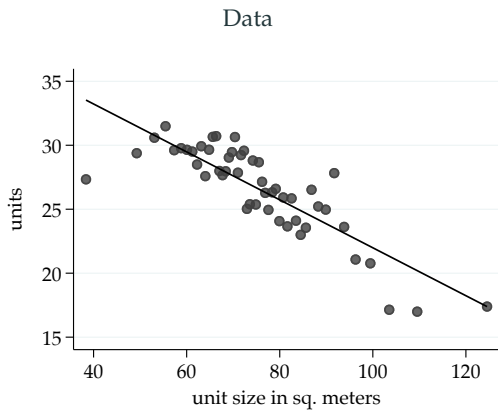


# IMPLICIT PRICES FOR HOUSING SIZE OVER TIME



Plotted lines:  $P_{ltc} = \hat{\rho}_1 \cdot h_{ltc} + \hat{\rho}_2 \cdot h_{ltc}^2 + \Gamma' \bar{X} + \bar{\omega}$

# UNIT SUPPLY FUNCTION



$$Q_{ltc} = \alpha_0 + \alpha_1 s_{ltc} + \alpha'_x X_{ltc} + \epsilon_{ltc}^Q$$

	06-08	09-11	12-15	16-18
$\alpha_0$	70.5	12.7	81.1	33.3
$\alpha_1$	-0.068	-0.020	-0.020	-0.042



# NOTCHES

## ► Demand Notch Overtime

	Notch ( <i>in mMW</i> )			# Subsidies ( <i>in thousand</i> )		
	$\tau^M$	$\tau^i$	$\tau$	<i>down payment</i>	<i>i rate</i>	<i>Mi Casa Ya</i>
2006-2008	18.0	.	18.0	47.1	.	.
2009-2011	20.0	5.85	25.9	46.4	16.7	.
2012-2015	19.9	9.55	29.5	41.1	22.2	.
2016-2018	25.3	7.24	32.6	44.5	23.4	16.8

## ► Supply Notch: 4 percent

## BEHAVIOURAL RESPONSES INDUCED BY THE POLICY

- Recovered by comparing observed and counterfactual distribution

*Observed*  $f_{h^*} \rightarrow$  histogram

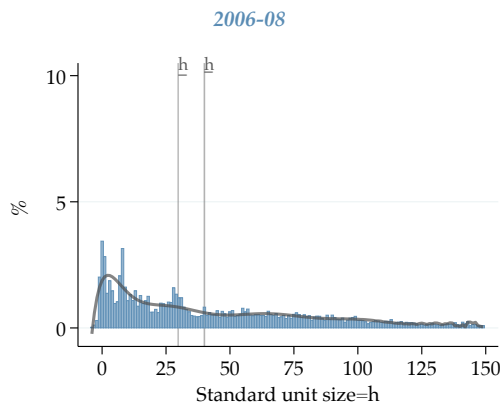
*Counterfactual*  $f_{h_0} \rightarrow$  predicted density excluding observations around the cutoff  
(Kleven, 2016)

$$h_b = \sum_{p=0}^T \hat{\iota}_p h_b^p + \sum_{k=L}^H \kappa_k \cdot \mathbb{1} [h_k = h_b] + v_b$$

$$\hat{f}_{h_0} = \sum_{p=0}^T \hat{\iota}_p h_b^p$$

Choice parameters: bin size, bounds for excluded area (L,H) and polynomial degree p

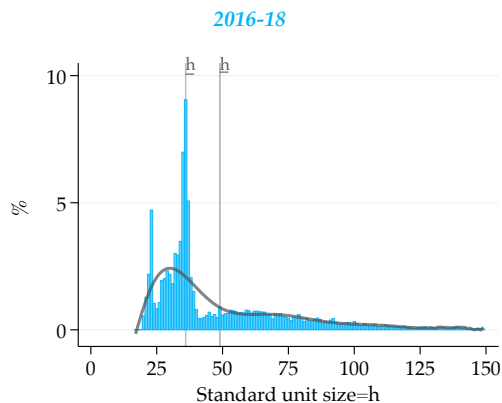
# BUNCHING IN HOUSING CHARACTERISTICS (SIZE OF STD. UNIT)



Notch: 19.7 *mMW*

Bunching: 1.53 % *market share*

$\Delta h$  11.2 *m*<sup>2</sup>



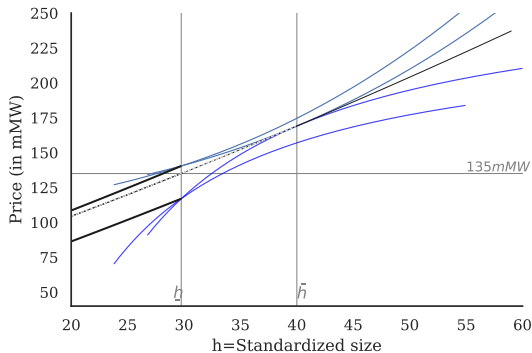
Notch: 33.1 *mMW*

Bunching: 14.2 % *market share*

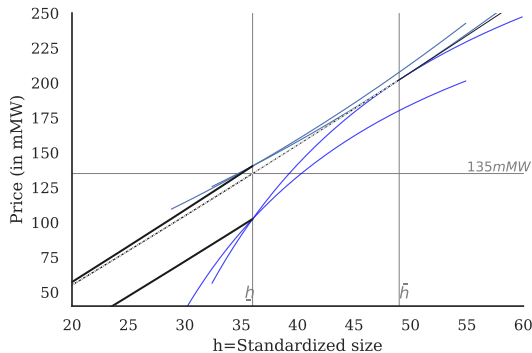
$\Delta h$  13 *m*<sup>2</sup>

# GRAPHICAL REPRESENTATION OF THE EQUILIBRIUM

2006-08



2016-18



$$B = A_j \cdot Q \cdot h^\beta$$

$$U = \left[ \frac{1}{2} \cdot C^\theta + \frac{1}{2} \cdot h^\theta \right]^{\frac{1}{\theta}}$$

Elasticity of Substitution:  $\sigma = \frac{1}{1 - \theta}$

*Structural Parameters*

	2006-08	2009-11	2012-15	2016-18
$\beta$	2.53	1.67	1.77	1.70
$\sigma$	0.85	0.97	0.90	0.90

### III. POLICY EVALUATION:

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## COUNTERFACTUAL POLICY I: PROPOSED TAX REFORM.

- Policy proposal: Remove the tax incentives to developers

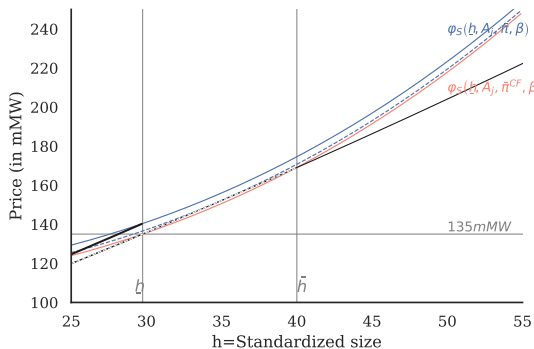
- Developers reaction:

*If these items are repealed, in Valle del Cauca we would go from having an offer of SH and sales of 23,000 homes, average year, to one of sales of 4,600 homes* El Tiempo (2021)

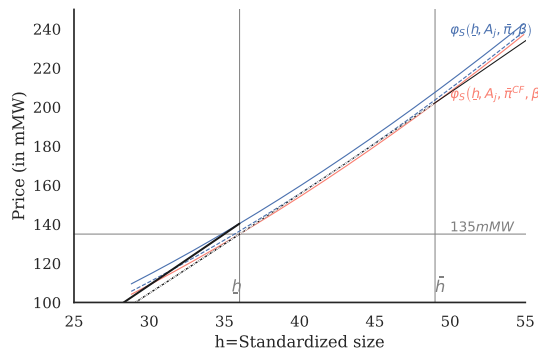
- Question: What happens to the marginally subsidized developers?

# EFFECT ON marginALLY SUBSIDIZED DEVELOPERS

2006-08



2016-18



*Changes in profits (%)*

	2006-08	2009-11	2012-15	2016-18
$\frac{\pi - \pi^{PC}}{\pi}$	4.9	15.9	9.3	12.3

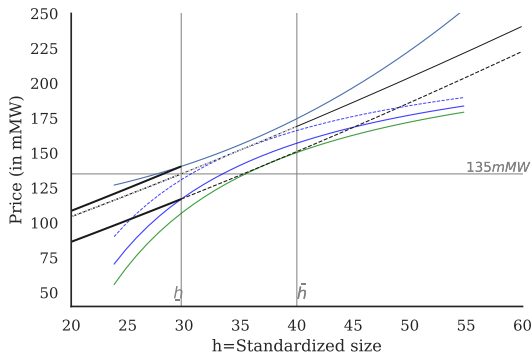
## COUNTERFACTUAL POLICY II: REMOVE PRICE CUTOFF

- ▶ Same households get subsidy but they can buy any house.
- ▶ Question: How much better off households are?

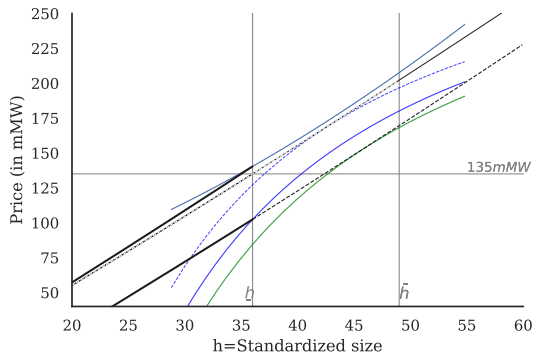


# EFFECT ON marginally SUBSIDIZED HOUSEHOLDS

2006-08



2016-18



*Changes in utility (%)*

	2006-08	2009-11	2012-15	2016-18
$\frac{U^{PC} - U}{U}$	2.9	1.9	2.7	2.7
$\frac{U - U^0}{U}$	4.7	3.4	4.5	4.5

## CONCLUSION (I): THE PAPER

- ▶ Characterization of the equilibrium.
- ▶ compelling evidence of the market responding to subsidies.
- ▶ An hedonic housing market equilibrium with heterogeneous agents can rationalize the response.
- ▶ Propose a identification strategy to recover the model parameters.
- ▶ Model+estimates  $\rightarrow$  Welfare.
- ▶ Policy design matters: need to be careful of how agents respond to incentives.

## CONCLUSION (II): GENERALIZATION

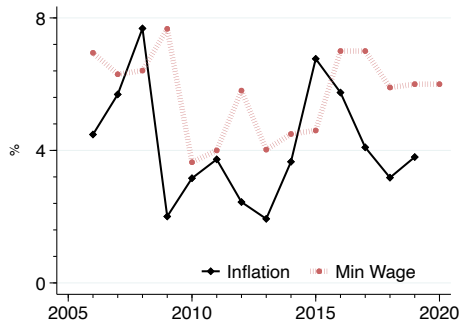
- ▶ The method I propose could be used to evaluate housing policy more generally.
- ▶ 2 facts suggest this could be potentially effective.
  1. There is increasing evidence to bunching responses to nonlinear incentives (e.g., help to buy, housing programs in the USA)
  2. Many other sources of non linear incentives in housing markets.



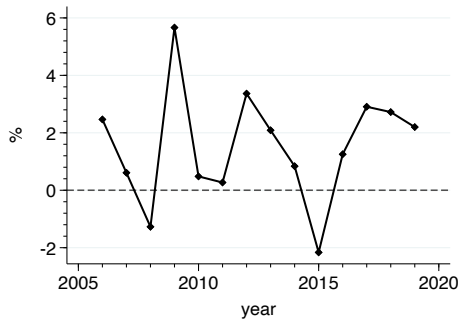
# Appendix

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# Inflation and minimum wages.



*a. Min wage and Inflation*



*b. Min wage and Inflation*

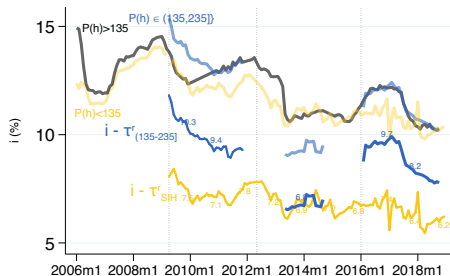
Data

# DATA: MORTGAGES AND INTEREST RATES

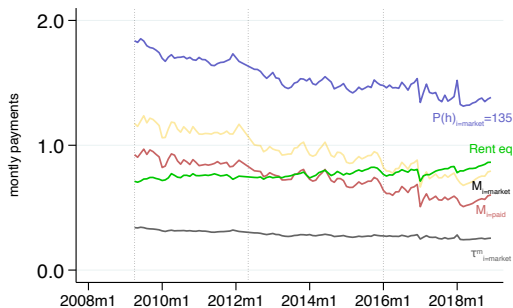
rent equivalent ((?, ?), (Bishop & Timmins, 2019) assume it is 0.05)

- Size of the mortgages and interest rate.
- Identifier for SIH.

Market interest rate  $i$  and subsidy  $\tau^r$



Monthly payments and monthly equivalent for relevant values.  $P(h) < 135$

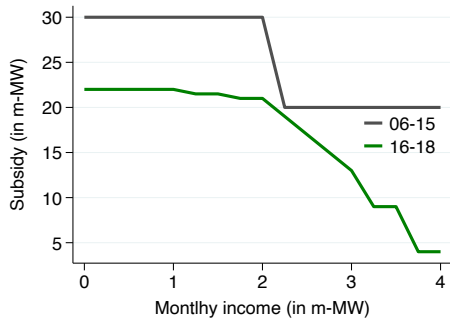


- To convert the magnitudes into monthly payments I use:

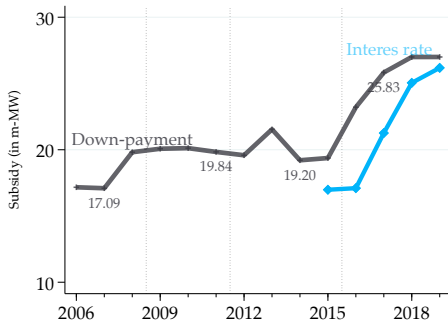
$$X_{monthly} = X \cdot \kappa(i, n); \kappa(i, n) = \frac{\frac{i}{12} \cdot \left(1 + \frac{i}{12}\right)^{12 \cdot n}}{\left(1 + \frac{i}{12}\right)^{n \cdot 12} - 1}$$

# THE NOTCH: DOWN PAYMENT SUBSIDY

Subsidy by household income



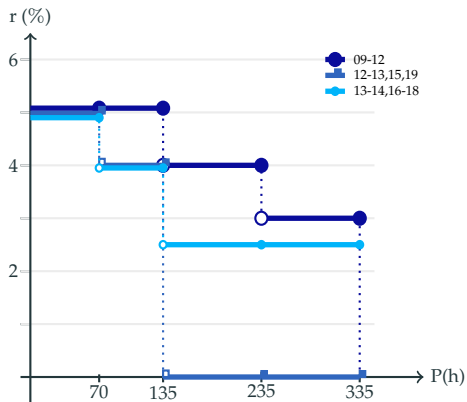
Average subsidy over time



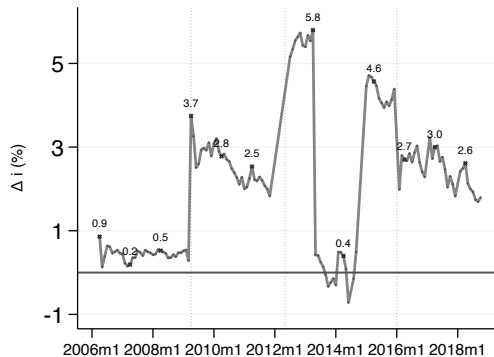
- Varies by income.
- Increase in 2016.
- Expanded trough *mi casa* YA



# THE NOTCH: INTEREST RATE SUBSIDY



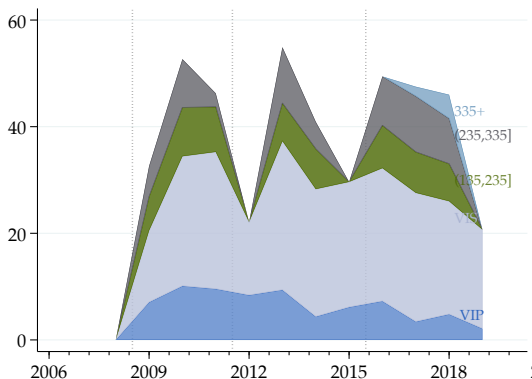
Comparing monthly payments around  $P(h)=135$  m-MW



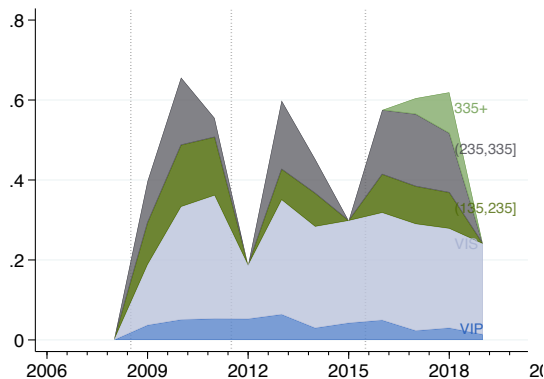
# SUBSIDIES AND GOVERNMENT EXPENDITURE (VIP- $P(h) < 70$ )

This figure shows interest rate subsidies to all the different price levels

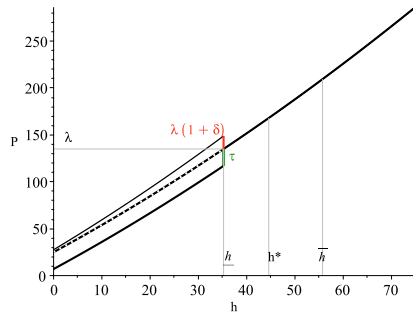
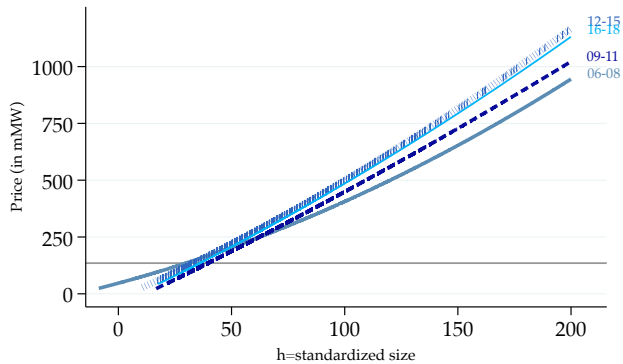
*a. Total # of subsidies*



*b. Total amount of subsidies*



# PRICES



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# THE POLICY EFFECT ON OBSERVED OUTCOMES

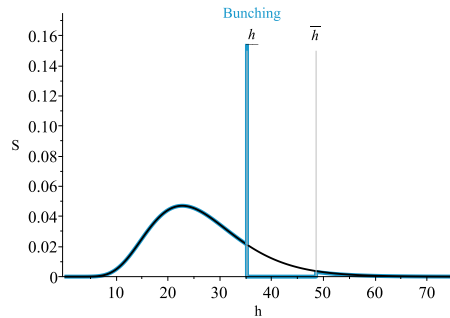
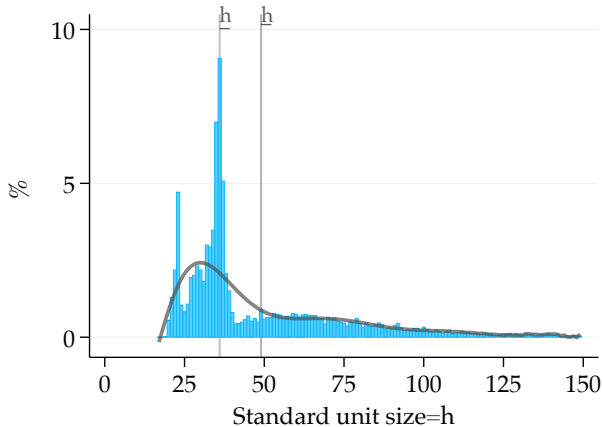
**Table 1:** Behavioral Responses Estimates'

	06-08	09-11	12-15	16-18
$\int_{h_{min}}^{\underline{h}} T(h)dh$	1.03	0.86	3.83	7.28
$\hat{T}(\underline{h})$	0.50	2.02	4.02	6.97
$\int_{h_{min}}^{\underline{h}} T(h)dh$	1.53	2.88	7.85	14.2
$\int_{\underline{h}}^{\bar{h}} T(h)dh$	-0.096	-6.25	-4.13	-3.42
$h_{h^0}(\underline{h})$	0.72	1.28	1.06	1.44
$h_{min}$	26	37	29	32
$\underline{h}$	29.8	39.4	33.0	36.0
$\bar{h}$	40	53	45	49

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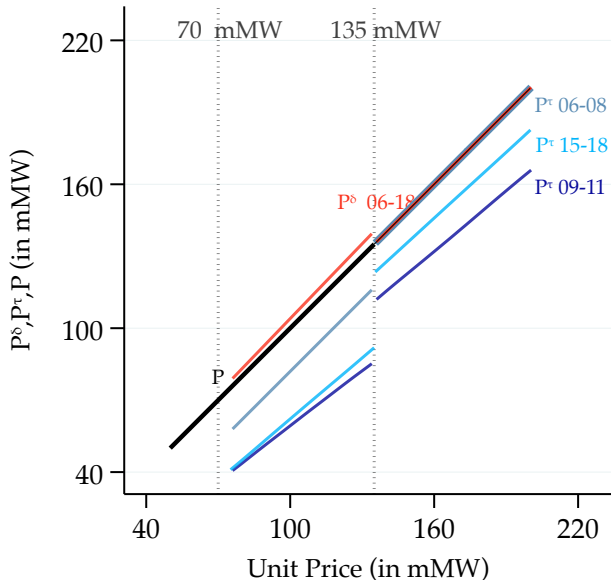
# BEHAVIORAL RESPONSES

2016-18



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# THE DEMAND NOTCH INCREASES OVER TIME



Supply Notch  $\delta$

2006-18 4%

Demand Notch  $\tau_t$

2006-08: 19.7 mMW

2009-11: 26.4 mMW

2016-18: 33.1 mMW

2012-15 Too many changes and  
free housing at 70mMW

# ALTERNATIVE REPRESENTATION OF THE EQUILIBRIUM.

## DEMAND AND SUPPLY FOR SIZE

