Equilibrium Effects of Housing Subsidies: Evidence from a Policy Notch in Colombia

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IS A MARKET-ORIENTED HOUSING POLICY EFFECTIVE?

- ► Governments implement various **market-oriented** policies to promote housing construction and promote homeownership
- Subsidies or tax incentives
- ► Affects Prices, Quantities, Type of housing that is build

- ► Is this market-oriented approach effective?
 - How big are the efficiency costs?
 - What are the unintended consequences?
 - Which households benefits the most?
 - What is the effect on developers?



COLOMBIAN HOUSING POLICY

- ► Policy tools:
 - Subsidies to low-income households.
 - Tax incentives to developers who build low-cost housing.
 - A price cap defining eligibility.
- Empirical advantages of Colombian setting:
 - Price cap on units qualifying for the subsidy.
 - Discontinuous Budget Constraint.
 - Incentives to developers and households to bunch.
 - Unique and novel data:
 - Census data for all new construction projects.
 - Administrative records for the subsidies.
 - Subsidy expansion between 2006-18

THIS PAPER

I. Descriptive evidence

- Characterization of observed equilibrium.
- Evidence of housing market responding to the subsidy scheme.

II. Hedonic equilibrium of housing supply and demand

- Product differentiation and heterogeneous developers and households.
- Identification using bunshing an policy changes

III. Policy Counterfactual and Welfare

- Tax reform proposed in Colombia in 2021– Remove tax incentives to developers.
- Proposed policy change phasing out price caps
- \rightarrow Effects on households and developers.

RESULTS

- I. Behavioural responses induced by the subsidy scheme.
 - Bunching at price cutoff
 - Larger response as the subsidies increase \rightarrow market share at cutoff went from 1% to 7%
 - Households downsize \rightarrow they buy units up to 30% percent smaller to benefit from the subsidy

II. Estimate a model that rationalizes the market observed equilibrium

Elasticity of substitution between on housing and consumption is 0.9

III. Effects of the proposed policies

- Colombian 2021 Tax proposal could create a housing shortage.
- Removing the price cap increases welfare.

LITERATURE AND CONTRIBUTION

Integrates the bunching and hedonic literatures to propose a method to think about welfare consequences of housing policy

Bunching	Hedonic	Housing Policy ► Evidence ► Method ► Welfare - Developers subsidies Baum-Snow and Marion (2009), Soltas (2020), Sinai and Waldfogel (2005) - Households Subsidies Carozzi et al. (2020) - Incidence and welfare Poterba (1992), Galiani et al. (2015)	
Housing MarketsSupply,DemandIdentification of SP	Policy NotchSupply sideIdentification		
 Housing market applications Best et al. (2019), DeFusco and Paciorek (2017) Methodology Notches >> Kinks: Kleven (2016), Bertanha et al. (2021), Blomquist et al. (2021) 	- Seminal paper S. Rosen (1974),Epple (1987) - Recent Contributions Bajari and Benkard (2005), Heckman et al. (2010), Epple et al. (2020), Chernozhukov et al. (2021) - Reviews Kuminoff et al. (2013), Greenstone (2017)		

I. Descriptive Analysis:

Equilibrium

Data, Policy and Observed

POLICY TOOLS

1. Demand Subsidies

- Downpayment
- Interest rate
 Income ≤ 4 monthly minimum wages (mMW) classify
- 2. Supply Subsidies
 - Value Added Tax (VAT) refund
- 3. Targeting tool for the subsidy:
 - Only new *low cost* units are eligible

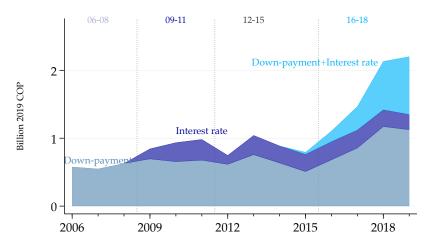
$$Low cost = \begin{cases} 1 & \text{if } P_t \leq 135 \text{ } mMW_t \\ 0 & \text{if } P_t > 135 \text{ } mMW_t \end{cases}$$



DATA

- 1. Administrative Records from Minister of Housing
 - Subsidy size
 - Mortgage information
 - → Government expenditure on each subsidy
- 2. New Construction Census (Camacol)
 - 126 Municipalities
 - Years: 2006-2018
 - Unit Characteristics: **size**,location, # rooms, # bathrooms, etc.
 - Prices sales prices.
 - Quantities

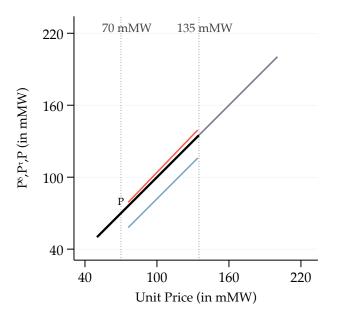
GOVERNMENT EXPENDITURE AND POLICY EXPANSION



- Total housing subsidies beneficiaries 100'000 in 2019
- 2 billion COP $\sim 0.25\%$ Colombian GDP
- Colombian Conditional Cash Transfers 3, 6 billon COP for 2.3 million households

THE NOTCH

Agents benefit from buying/selling *low cost housing* ($P \le 135$ *mMW*)



Transaction Price

Developers Price

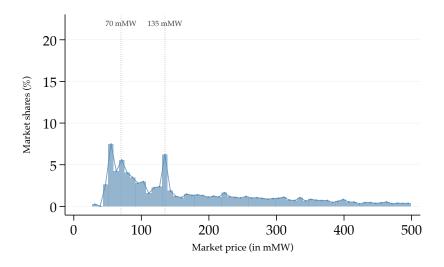
$$\mathbf{P}^{\delta} = P \cdot (1 + \delta):$$

 $\delta = \text{Tax refund}$

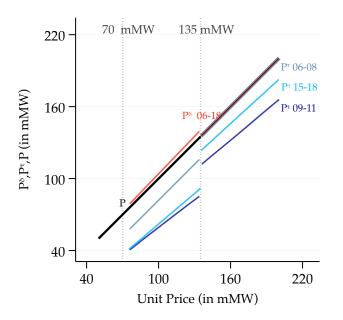
Households price

$$\mathbf{P}^{\tau} = P - \tau$$
$$\tau = \text{Subsidy}$$

BUNCHING AT THE LOW-COST HOUSING PRICE LIMIT



THE DEMAND NOTCH INCREASES OVER TIME



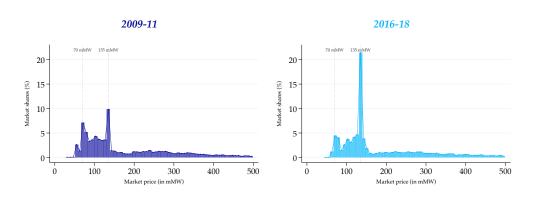
Supply Notch δ 2006-18 4%

Demand Notch τ_t

2006-08: 19.7 *mMW* 2009-11: 26.4 *mMW* 2016-18: 33.1 *mMW*

2012-15 Too many changes and free housing at 70mMW

LARGER BUNCHING AS NOTCH INCREASES

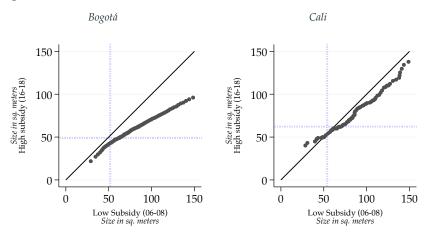


Notch: 33.1 mMW

Notch: 19.7 mMW

CHANGES IN HOUSING STOCK CHARACTERISTICS

Changes in unit size



- ► Not only changes in prices
- ► Size is not the only characteristic

HEDONIC PRICES AND STANDARDIZED HOUSING UNIT

► Hedonic price/Implicit price for housing size

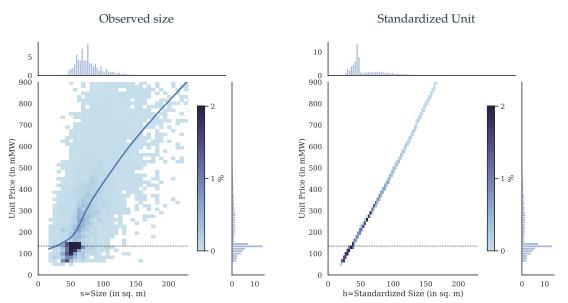
$$P_{ltc} = \rho \left(s_{ltc} \right) + \Gamma' X_{ltc} + \omega_{ltc} \tag{1}$$

ightharpoonup Standard Unit Size h_{ltc}

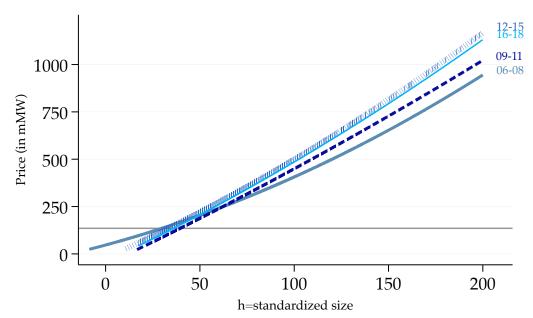
$$\rho\left(h_{ltc}\right) + \Gamma'\bar{X}_{ltc} + \bar{\omega}_{ltc} = \rho\left(s_{ltc}\right) + \Gamma'X_{ltc} + \omega_{ltc} \tag{2}$$

- Characteristics of the standard house: \bar{X}_{ltc} , $\bar{\omega}_{ltc}$
- Simplifying assumption: $\rho(s_{ltc}) = \rho_1 \cdot s_{ltc} + \rho_2 \cdot s_{ltc}^2$
- Identifying assumption: $E(s_{ltc}|X_{ltc},\omega_{ltc})=0$
- ► Why size?
 - Continuous, easy to measure, monotonic relationship with price.
 - In contrast to most datasets, I observe it.

OBSERVED EQUILIBRIUM: PRICES, QUANTITIES, AND SIZE 2016-18



IMPLICIT PRICES FOR HOUSING SIZE OVER TIME



BEHAVIOURAL RESPONSES INDUCED BY THE POLICY

Recovered by comparing observed and counterfactual distribution

Observed Distribution $f_{h^*} o \text{histogram}$

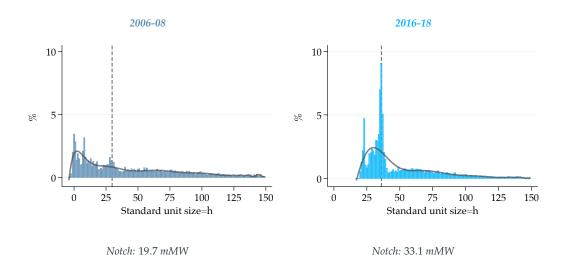
Counterfactual Distribution $f_{h_0} \rightarrow$ predicted density excluding observations around the cutoff (Kleven, 2016)

$$h_b = \sum_{p=0}^{T} \hat{\iota}_p h_b^p + \sum_{k=L}^{H} \kappa_k \cdot \mathbb{1} [h_k = h_b] + v_b$$

$$\hat{f}_{h_0} = \hat{l}(h_b) = \sum_{p=0}^{T} \hat{\iota}_p h_b^p$$

Choice parameters: bin size, bounds for excluded area (L,H) and polynomial degree p

BUNCHING IN HOUSING CHARACTERISTICS (SIZE OF STD. UNIT)



THE POLICY EFFECT ON OBSERVED OUTCOMES

Table 1: Behavioral Responses Estimates'

	06-08	09-11	12-15	16-18
$\int_{h_{min}}^{\underline{h}^{-}} T(h) dh$	1.03	0.86	3.83	7.28
$\hat{T}(\underline{h})$	0.50	2.02	4.02	6.97
$\int_{h_{min}}^{\underline{h}} T(h) dh$	1.53	2.88	7.85	14.2
$\int_h^{\overline{h}} T(h) dh$	-0.096	-6.25	-4.13	-3.42
h_{h^0} (\underline{h})	0.72	1.28	1.06	1.44
h_{min}	26	37	29	32
$\frac{h}{h}$	29.8	39.4	33.0	36.0
\overline{h}	40	53	45	49

II. Equilibrium Model of

Housing Supply and Demand

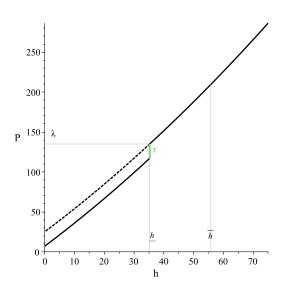
A STYLIZED HOUSING MARKET MODEL

1. Housing

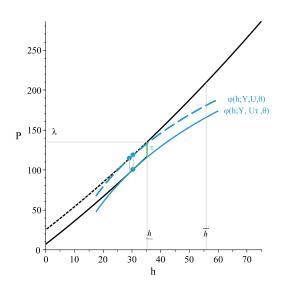
- Differentiated product described by its size $h \in \mathcal{H}$
- Price depends on size P(h)
- 2. **Households** $i \in I$, Heterogeneous in Income $Y_i \sim F_Y$
 - Choose h_i and consumption C_i to maximize Utility $U(C_i, h_i; \theta)$
- 3. **Developers** $j \in J$, Heterogeneous in Productivity $A_j \sim G_A$
 - Pick h_i to maximize profits
 - Building costs $B(h_j, Q(h_j); \beta)$

4. Competitive Market Equilibrium

• Price function $P^*(h) \rightarrow$ clears the market $\forall h$



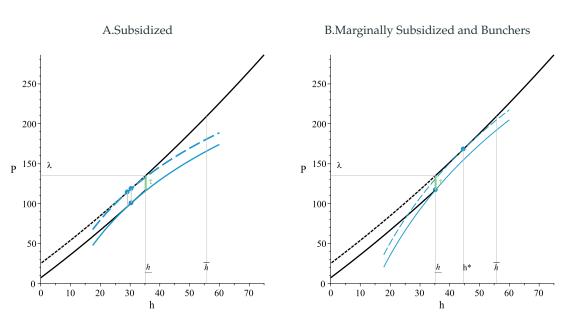
- Implicit Price Function: P(h)
- Subsidy au

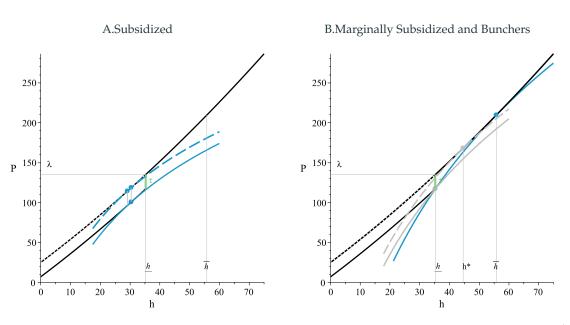


- Implicit Price Function: P(h)
- Subsidy τ
- Bid functions $\varphi_D(h, Y, \bar{U}; \theta)$

$$\bar{U} = U(h, Y_i - \varphi_D; \theta)$$

$$\bar{U}_{\tau} = U(h, Y_i - \varphi_D + \tau; \theta)$$





HOUSEHOLDS' DEMAND FUNCTION

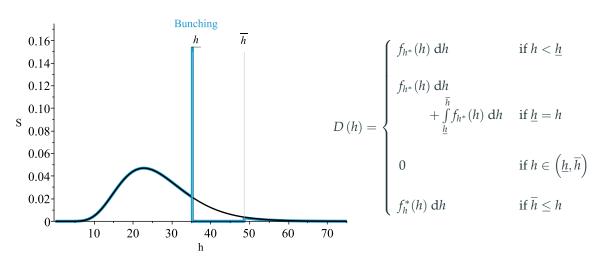
Tangency conditions: $h^*(Y_i, \tau; \theta, \boldsymbol{\rho}, \lambda)$

► Housing demand:

$$h^{\mathrm{D}}(Y_{i}) = \begin{cases} h^{*}(Y_{i}, \tau; \theta, \boldsymbol{\rho}, \lambda) & \text{if } Y_{i} \leq \underline{Y} \\ \\ \underline{h} & \text{if } \underline{Y} < Y_{i} < \overline{Y} \\ \\ h^{*}(Y_{i}, \tau; \theta, \boldsymbol{\rho}, \lambda) & \text{if } \overline{Y} \leq Y_{i} \end{cases}$$

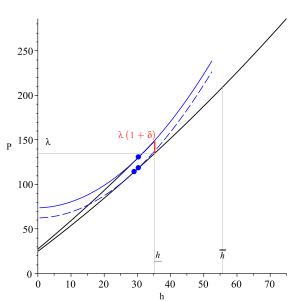
- ► How to aggregate:
 - Income and unit size: $Y_i = \tilde{Y}(h, \tau; \theta, \rho, \lambda) = h^{*-1}(h_i, \tau; \theta, \rho, \lambda)$
 - change of variable formula using the distribution of income

AGGREGATE DEMAND DENSITY



DEVELOPERS' CHOICES



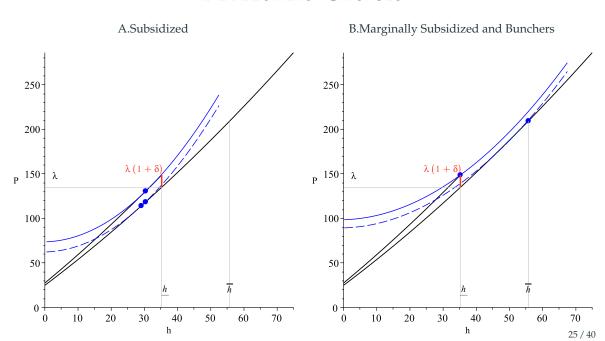


- Implicit Price Function: P(h)
- Tax incentives: $P(h) \cdot (1 + \delta)$
- Offer Functions $\varphi_S\left(h,A_j,\bar{\pi},\boldsymbol{\beta}\right)$

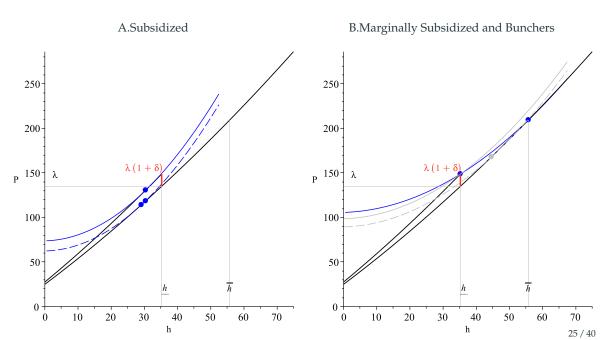
$$\bar{\pi} = (h, A_j, P(h), \beta,)$$

$$\bar{\pi}_{\delta} = (h, A_j, P(h) * (1 + \delta)), \beta,)$$

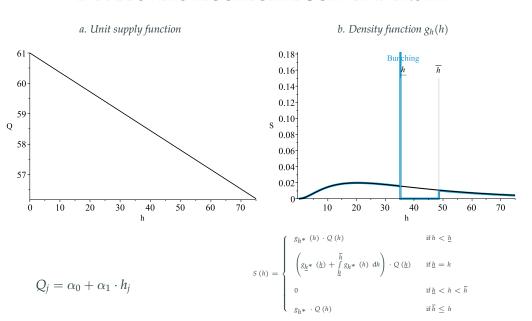
DEVELOPERS' CHOICES



DEVELOPERS' CHOICES



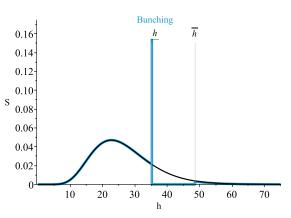
DEVELOPERS AGGREGATE SUPPLY DENSITY

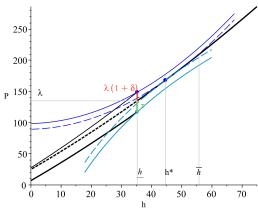


EQUILIBRIUM

Price function makes the market clear:

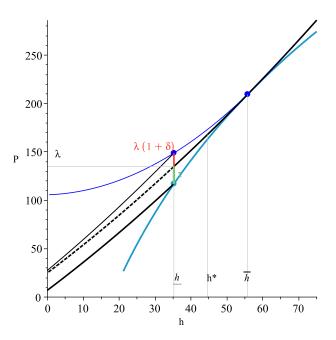
$$E = \left\{ P(h; \boldsymbol{\rho}) \in \mathcal{P} : D(h; \tau, \theta, \boldsymbol{\rho}, \boldsymbol{\gamma}, \lambda) = S(h; A_j, \boldsymbol{\rho}, \boldsymbol{\phi}) \, \forall h \in \mathcal{H} \right\}$$





Identification

MARGINAL BUNCHER CONDITION



MARGINAL BUNCHER CONDITION

Marginal Buncher Condition					
Household	$V_{D} = U\left(\overline{Y} - P\left(\overline{h}\right), \overline{h}; \theta\right) - U\left(\overline{Y} - P^{\tau}\left(\underline{h}\right), \underline{h}; \theta\right) = 0$				
Developer	$V_{D} = U\left(\overline{Y} - P\left(\overline{h}\right), \overline{h}; \boldsymbol{\theta}\right) - U\left(\overline{Y} - P^{\tau}(\underline{h}), \underline{h}; \boldsymbol{\theta}\right) = 0$ $V_{S} = \pi\left(Q(\overline{h}), \overline{A}, P\left(\overline{h}\right); \boldsymbol{\beta}\right) - \pi\left(Q(\underline{h}), \overline{A}; P^{\delta}(\underline{h}); \boldsymbol{\beta}\right) = 0$				
Optimality Conditions					
Income	$\overline{Y} = \tilde{Y}\left(\overline{h}; \theta, P(h), \lambda\right)$				
Productivity	$egin{aligned} \overline{Y} &= \widetilde{Y}\left(\overline{h}; oldsymbol{ heta}, P(h), \lambda ight) \ \overline{A} &= \widetilde{A}\left(\overline{h}; oldsymbol{eta}, P(h), \lambda ight) \end{aligned}$				
Functional For	ns				
Implicit Price	$P = \rho_0 + \rho_1 \cdot h + \rho_2 \cdot h^2$				
Utility	$U = \left[rac{1}{2}\cdot C^{ heta} + rac{1}{2}\cdot h^{ heta} ight]^{rac{1}{ heta}}$				
Unit Supply	$Q = \alpha_0 + \alpha_1 h$				
Cost	$B = A_j \cdot Q \cdot h^{\beta}$				

Estimation

STEP I

1. Price function:

$$\boldsymbol{\rho_t} = \rho_{0t}, \rho_{1t}, \rho_{2t}$$

2. Policy Parameters:

Notches: τ_t , δ

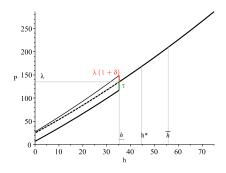
Size threshold: $\underline{h} = P^{-1}(\lambda; \boldsymbol{\rho})$

3. Unit Supply Function:

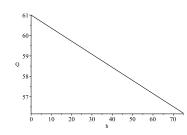
$$\alpha = \alpha_0, \alpha_1$$

4. Behavioural Responses:

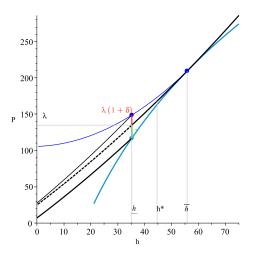
Housing size for marginal buncher without subsidy: \bar{h}



Unit Supply Function Q(h)



STEP II



$$\begin{split} V_{D}\left(\boldsymbol{\theta}|\underline{h},\overline{h},P\left(h\right),\tau,\tilde{Y}\left(\overline{h},\boldsymbol{\theta},P\left(h\right),\lambda\right)\right) &= 0\\ V_{S}\left(\boldsymbol{\beta}|\underline{h},\overline{h},P\left(h\right),\boldsymbol{\alpha},\delta,\tilde{A}\left(\overline{h};\boldsymbol{\beta},P\left(h\right),\lambda\right)\right) &= 0 \end{split}$$

ESTIMATES

	06-08	09-11	12-15	16-18			
Price Function							
ρ_0	17.0	-300.0	-243.5	-240.6			
ρ_1	2.70	4.75	4.48	4.66			
ρ_2	0.90	0.32	0.73	0.60			
Policy Parameters							
au	18.0	25.9	29.5	32.6			
Bunchers Interval							
\overline{h}	40	53	45	49			
<u>h</u>	29.8	39.4	33.0	36.0			
Unit Supply Function							
α_0	70.5	12.7	81.1	33.3			
α_1	-0.068	-0.020	-0.020	-0.042			
Structural Parameters							
β	2.53	1.67	1.77	1.70			
σ	0.85	0.97	0.90	0.90			
θ	-0.17	-0.028	-0.11	-0.11			

III. Policy Evaluation:

COUNTERFACTUAL POLICIES

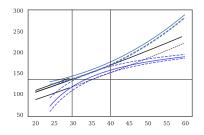
▶ Does the presence of a consumer housing subsidy and price caps create a problem of rationing in the absence of supply subsidies ?

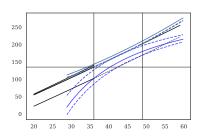
Ongoing policy debate:

If these items are repealed, in Valle del Cauca we would go from having an offer of SH and sales of 23,000 homes, average year, to one of sales of 4,600 homes El Tiempo (2021)

▶ What happens if the same households get the subsidy but there is not a price cutoff.

WELFARE EVALUATION ILLUSTRATION





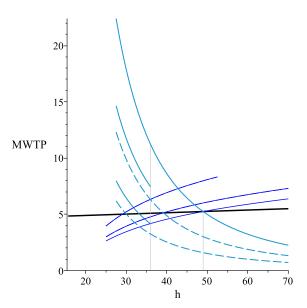
ESTIMATES: DEVELOPERS

	Developers			
	2006-08	2009-11	2012-15	2016-18
<u>A</u>	0.0068	0.26	0.19	0.25
A_*	0.0054	0.23	0.17	0.22
\overline{A}	0.0045	0.21	0.15	0.20
$MgC(\underline{h}, Q(\underline{h}), \underline{A})$	214.4	59.5	398.2	160.7
$MgC(\underline{h}, Q(\underline{h}), A_*)$	219.0	59.0	404.4	161.2
$MgC\left(h^{*},Q\left(h^{*}\right),A_{*}\right)$	172.4	53.7	356.0	144.9
$MgC\left(\overline{h},Q\left(\overline{h}\right),\overline{A}\right)$	223.4	58.6	410.6	161.7
$\pi\left(Q\left(\underline{h}\right),\underline{A};P\left(\underline{h}\right)\right)$	6725.5	205.8	3449.4	881.6
$\pi\left(Q\left(\underline{h}\right), A_{*}; P^{\delta}\left(\underline{h}\right)\right)$	7588.2	406.1	4668.9	1388.9
$\pi\left(Q\left(\underline{h}\right),A_{*};P\left(\underline{h}\right)\right)$	7218.6	341.6	4234.4	1217.2
$\pi\left(Q\left(h^{*}\right),A_{*};P^{\delta}\left(h^{*}\right)\right)$	7740.0	439.8	4889.1	1478.6
$\pi\left(Q\left(h^{*}\right),A_{*};P\left(h^{*}\right)\right)$	7326.4	359.9	4359.1	1266.4
$\pi\left(Q\left(\overline{h}\right), \overline{A}; P\left(\overline{h}\right)\right)$	7930.5	512.2	5262.2	1646.0

ESTIMATES: HOUSEHOLDS

	Households				
	2006-08	2009-11	2012-15	2016-18	
<u>Y</u>	215.7	324.0	275.6	291.5	
Y_*	248.7	392.5	333.7	355.6	
\overline{Y}	282.8	461.7	393.2	421.1	
$U(\underline{Y} - P(\underline{h}), \underline{h})$	47.9	85.6	66.3	72.9	
$U\left(\underline{Y}-P^{\tau}\left(\underline{h}\right),\underline{h}\right)$	52.5	91.2	72.4	79.5	
$U(Y_* - P(h^*), h^*)$	56.8	100.7	78.9	86.6	
$U\left(Y_{*}-P^{\tau}\left(\underline{h}\right),\underline{h}\right)$	59.6	104.3	82.7	90.7	
$U\left(Y_{*}-P^{\tau}\left(h^{*}\right),h^{*}\right)$	61.4	106.3	84.9	93.2	
$U\left(\overline{Y}-P\left(\overline{h}\right),\overline{h}\right)$	65.9	116.0	91.7	100.5	

ALTERNATIVE REPRESENTATION OF THE EQUILIBRIUM. DEMAND AND SUPPLY FOR SIZE



CONCLUSION (I): THE PAPER

- ► Characterization of the equilibrium.
- compelling evidence of the market responding to subsidies.
- An hedonic housing market equilibrium with heterogeneous agents can rationalize the response.
- ▶ Propose a identification strategy to recover the model parameters.
- ightharpoonup Model+estimates \rightarrow Welfare.
- ▶ Policy design matters: need to be careful of how agents respond to incentives.

CONCLUSION (II): GENERALIZATION

► The method I propose could be used to evaluate housing policy more generally.

▶ 2 facts suggest this could be potentially effective.

1. There is increasing evidence to bunching responses to nonlinear incentives (e.g., help to buy, housing programs in the USA)

2. Many other sources of non linear incentives in housing markets.

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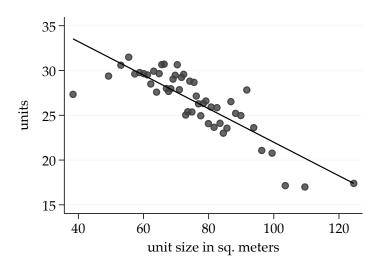
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 Cauber, J., Josson, A., & Xieven, H. (2023, May). Ex-people respond to the managage interest deduction? quasi-experimental
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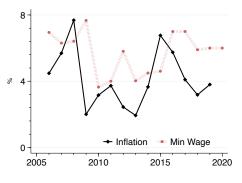
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Appendix

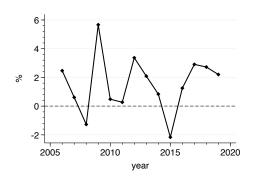
QUANTITIES BY SIZE



Inflation and minimum wages.



a. Min wage and Inflation



 $b.\ Min\ wage\ and\ Inflation$

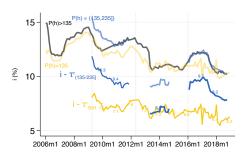
back

DATA: MORTGAGES AND INTEREST RATES

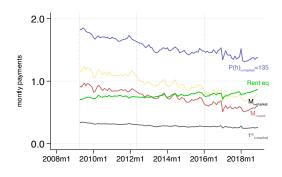
rent equivalent ((?, ?), (Bishop & Timmins, 2019) assume it is 0.05)

- ► Size of the mortgages and interest rate.
- ▶ Identifier for SIH.

Market interest rate i and subsidy τ^r



Monthly payments and monthly equivalent for relevant values. P(h) < 135

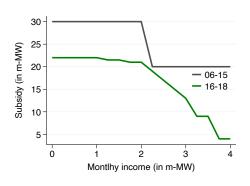


To convert the magnitudes into monthly payments I use:

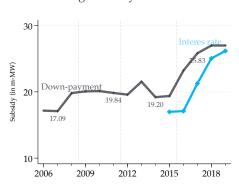
$$X_{monthy} = X \cdot \kappa(i,n) \, ; \kappa(i,n) = \frac{\frac{i}{12} \cdot \left(1 + \frac{i}{12}\right)^{12 \cdot n}}{\left(1 + \frac{i}{12}\right)^{n \cdot 12} - 1}$$

THE NOTCH: DOWN PAYMENT SUBSIDY

Subsidy by household income

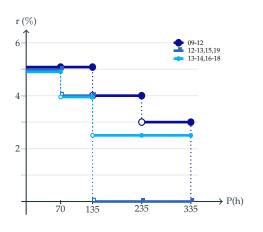


Average subsidy over time

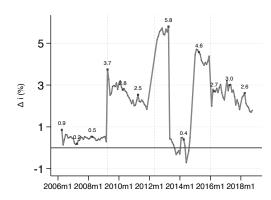


- ► Varies by income.
- ► Increase in 2016.
- Expanded trough *mi casa YA*

THE NOTCH: INTEREST RATE SUBSIDY



Comparing monthly payments around P(h)=135 m-MW



Subsidies and Government Expenditure (VIP-P(h) < 70)

This figure shows interest rate subsidies to all the different price levels

