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$$F(x) - P(x) = \frac{F^{(n+1)}(\xi(x))}{(n+1)!} \prod_{k=0}^n (x - x_k)$$

Demostración:

$$g(t) = f(t) - P(t) - (F(x) - P(x)) \prod_{k=0}^n \frac{t - x_k}{x - x_k}$$

$$g^{(n)}(\xi) = F^{(n)}(\xi) - (F(x) - P(x)) \cdot \frac{n!}{\prod_{k=0}^n (x - x_k)}$$

Despejando...

$$(F(x) - P(x)) = \frac{F^{(n+1)}(\xi)}{(n+1)!} \prod_{k=0}^n (x - x_k)$$