

9.

$$T_{dp}(a,b) \leq T_{bp}(a,b)$$

Supongamos $a=1$

$$T_{dp}(a,b) = b \leq \max\{0, b\} = \max\{0, b+1-1\} = \max\{0, a+b-1\}$$

Análisis para $b=1$.

Supongamos $a, b < 1$

$$T_{dp}(a,b) = b \leq T_{bp}(a,b)$$

$$T_{bp}(a,b) \leq T_{ap}(a,b)$$

Supongamos $a+b-1 \geq 0$

$$T_{bp}(a,b) = a+b-1$$

Como $a, b \in [0,1] \rightarrow 1-a, 1-b \in [0,1]$

Luego, $(1-a)(1-b) \geq 0$

$$1-(a+b)+ab \geq 0$$

$$a+b-1 \leq ab = T_{ap}(a,b)$$

Supongamos $a+b-1 < 0$

$$T_{bp}(a,b) = 0 \leq T_{ap}(a,b)$$

$$T_{ap}(a,b) \leq T_{min}(a,b)$$

Supongamos $a < b$

$$T_{ap}(a,b) = \underbrace{ab}_{a,b \in [0,1]} \leq a = T_{min}(a,b)$$

Análisis a $b < a$.