

$$T(a,b) = \begin{cases} a \leq c \\ b \leq d \end{cases} \rightarrow a+b \leq c+d$$

Luego es claro que:

$$a+b-1 \leq c+d-1$$

$$\max\{0, a+b-1\} \leq \max\{0, c+d-1\}$$

Así: $\underline{T(a,b) \leq T(c,d)}$ ✓

• $T(a,b) = T(b,a)$

Observe que:

$$T(a,b) = \max\{0, a+b-1\}$$

$$\Rightarrow \max\{0, b+a-1\} = T(b,a) \checkmark$$

• $T(T(a,b), c) = T(a, T(b, c))$

Supongamos que $\underline{a+b-1 < 0}$ y $\underline{b+c-1 < 0}$. Luego

$$T(T(a,b), c) = \max\{0, \max\{0, a+b-1\} + c - 1\}$$

$$= \max\{0, 0 + c - 1\} = \max\{0, c-1\}$$

(Como $c < 1 \rightarrow = 0 = \max\{0, a-1\}$

$$= \max\{0, a+0-1\}$$

$$= \max\{0, a + \max\{0, b+c-1\} - 1\}$$

$$= \underline{T(a, T(b, c))} \checkmark \quad c)$$