Core dynamo simulations of A-type stars Master's thesis project

Juan Pablo Hidalgo

Supervisor: Dr. Dominik Schleicher

Universidad de Concepción.

September 20, 2023









Stellar structure

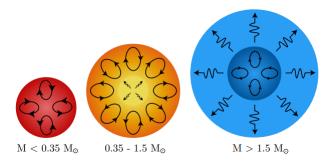


Figure: Diagram of convective and radiative zones for different ranges of stellar masses. Stars with $M\lesssim 0.3M_{\odot}$ are fully convective, intermediate mass stars have a radiative core and a convective core. Finally, stars with $M\gtrsim 1.5M_{\odot}$ have convective cores and radiative envelopes.

Stellar structure

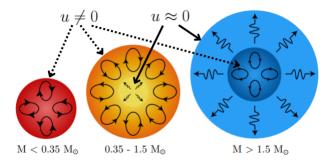


Figure: Diagram of convective and radiative zones for different ranges of stellar masses. Stars with $M\lesssim 0.3M_{\odot}$ are fully convective, intermediate mass stars have a radiative core and a convective core. Finally, stars with $M\gtrsim 1.5M_{\odot}$ have convective cores and radiative envelopes.

Astrophysical Dynamos

We refer to a *dynamo* as any process of amplification and maintenance of magnetic fields inside a plasma.

$$\frac{\partial \vec{B}}{\partial t} = \vec{\nabla} \times (\vec{u} \times \vec{B}) + \eta \nabla^2 \vec{B}$$

These processes are most likely to occur inside the convection zones (see Brandenburg & Subramanian 2004), where $u \neq 0$.

Radiative zone?

Ap/Bp stars (1.5 M_{\odot} to $6M_{\odot}$) host magnetic fields with mean strengths ranging from 200 G to 30 kG (Aurière et al., 2007).



Possible explanations

The dynamo is driven by the convective core of the star (Krause & Oetken, 1976).

Possible explanations

The dynamo is driven by the convective core of the star (Krause & Oetken, 1976).

Previous work

Brun et al. (2005) performed simulations of the inner 30% by radius (where 15% is the core) of a $2~M_{\odot}$ A-type star, obtaining magnetic fields with typical strengths around the equipartition values with the kinetic energy.

Possible explanations (2)

Surface magnetic field?

In principle, magnetic structures created by the core dynamo could reach the surface under the action of buoyancy, however, this process has a timescale longer than the main-sequence life of the star (Parker, 1979; Moss, 1989), unless we consider very small structures (MacGregor & Cassinelli, 2003).

Possible explanations (3)

Fossil field surviving from the early stages (Cowling, 1945).

Possible explanations (3)

Fossil field surviving from the early stages (Cowling, 1945).

Previous work

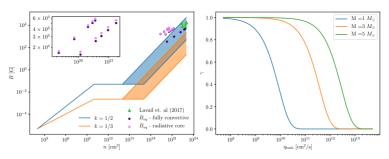
Braithwaite & Nordlund (2005) performed 3D simulations of a $2M_{\odot}$, $R=1.8R_{\odot}$ A-type star, inside a box of side l=4.5R using a grid of 96^3 . They found stable axisymmetric magnetic field configurations in a radiative interior starting with random field initial conditions. Recently, similar results were found by Becerra et al. (2022).

Possible explanations (4)

Survival of fossil fields during the pre-main sequence evolution of intermediate-mass stars

Dominik R.G. Schleicher¹, Juan Pablo Hidalgo¹, and Daniele Galli²

June 30, 2023



Departamento de Astronomía, Facultad Ciencias Físicas y Matemáticas, Universidad de Concepción, Av. Esteban Iturra s/n,Barrio Universitario. Concepción. Chile. e-mail: dschleicher@astro-udec.cl

² INAF - Osservatorio Astrofisico di Arcetri, Largo E. Fermi 5, 50125 Firenze, Italy

Main-sequence model

In this project, we performed 3D MHD simulations of an A-type star with a radiative envelope and a convective core assumed to encompass 20% of the stellar radius (similar to Brun et al. 2005 and Featherstone et al. 2009)

Objectives:

 Analyze the dynamo solutions given by the core, and possible surface magnetic fields.

Main-sequence model

In this project, we performed 3D MHD simulations of an A-type star with a radiative envelope and a convective core assumed to encompass 20% of the stellar radius (similar to Brun et al. 2005 and Featherstone et al. 2009)

Objectives:

- Analyze the dynamo solutions given by the core, and possible surface magnetic fields.
- Study the large scale flows in the core of the star.

Main-sequence model

In this project, we performed 3D MHD simulations of an A-type star with a radiative envelope and a convective core assumed to encompass 20% of the stellar radius (similar to Brun et al. 2005 and Featherstone et al. 2009)

Objectives:

- Analyze the dynamo solutions given by the core, and possible surface magnetic fields.
- Study the large scale flows in the core of the star.
- Compare these results with previous work showed before.



The setup

Using The Pencil Code (Pencil Code Collaboration et al., 2021), we model a massive early-type star of radius R, inside a box of side l=2.2R.

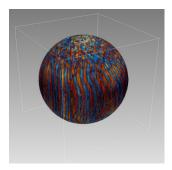


Figure: Star-in-a-box model, from Käpylä (2021).

Stellar parameters:

$$R_* = 2R_{\odot}$$

$$L_* = 23 L_{\odot}$$

$$\rho_* = 5.6 \cdot 10^4 \text{ g/m}^3$$

$$g_* = 150 \text{ m/s}^2$$

The model

Solving the fully-compressible non-ideal MHD equations:

$$\frac{\partial \vec{A}}{\partial t} = \vec{u} \times \vec{B} - \eta \mu_0 \vec{J} \tag{1}$$

$$\frac{D\ln\rho}{Dt} = -\vec{\nabla}\cdot\vec{u} \tag{2}$$

$$\frac{D\vec{u}}{Dt} = -\vec{\nabla}\Phi - \frac{1}{\rho} \left(\vec{\nabla}p - \vec{\nabla} \cdot 2\nu\rho \mathbf{S} + \vec{J} \times \vec{B} \right) - 2\vec{\Omega} \times \vec{u} + \vec{f}_d \quad (3)$$

$$T\frac{Ds}{Dt} = -\frac{1}{\rho} \left[\vec{\nabla} \cdot (\vec{F}_{\text{rad}} + \vec{F}_{\text{SGS}}) + \mathcal{H} - \mathcal{C} \right] + 2\nu S^2 + \mu_0 \eta J^2 \quad (4)$$

where $D/Dt = \partial/\partial t + \vec{u} \cdot \vec{\nabla}$ is the advective derivative, also $\vec{B} = \vec{\nabla} \times \vec{A}$, the relation between \vec{J} and \vec{B} is given by the Ohm's law $\vec{J} = \vec{\nabla} \times \vec{B}/\mu_0$ and the explicit heating and cooling terms, are extracted from Käpylä (2021).



Simulations

MHD simulations have a radial profile in the diffusivities, with $r_{\rm start}=0.35R$ and w=0.06R.

* indicates $r_{\text{start}} = 0.30R$ and w = 0.03R.

Run	$P_{\rm rot}$ [days]	$\langle u_{\rm rms} \rangle \ [{\rm m/s}]$	$\langle B_{\rm rms} \rangle [{\rm kG}]$	Co	Re	Re_M
MHDr1	20	179	no dynamo	1.8	146	102
MHDr2	15	82	113	5.3	67	47
MHDr2*	15	80	114	5.4	65	46
MHDr3	10	62	111	10.4	51	36
MHDr3*	10	61	122	10.7	50	35
MHDr4	8	56	110	14.4	46	32
MHDr4*	8	56	103	14.5	46	32

$$\mathrm{Re} = \frac{u_{\mathrm{rms}}}{\nu k_R} \qquad \qquad \mathrm{Re_M} = \frac{u_{\mathrm{rms}}}{\eta k_R} \qquad \qquad \mathrm{Co} = \frac{2\Omega_0}{u_{\mathrm{rms}}k_R}$$



Analysis

All the analysis in this work, was made during the thermally and magneticaly relaxation of the runs.

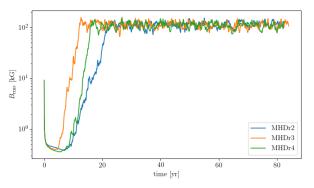


Figure: Time evolution of the volume-averaged root-mean-square magnetic field, from the runs in MHD group that generate core dynamos.



Dynamo solutions

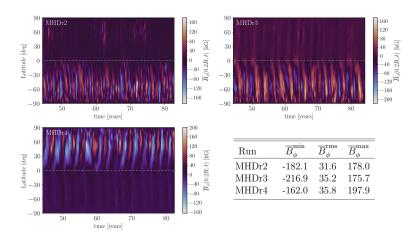


Figure: Time-latitude diagrams of the azimuthally averaged toroidal magnetic field $\overline{B}_\phi(r=0.2R,\theta,t)$ of the MHD group.



Dynamo solutions (2)

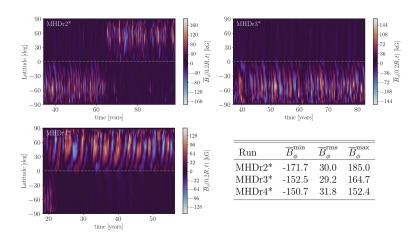


Figure: Time-latitude diagrams of the azimuthally averaged toroidal magnetic field $\overline{B}_\phi(r=0.2R,\theta,t)$ of the MHD* group.



Comparison with other simulations

THE ASTROPHYSICAL JOURNAL LETTERS, 902:L3 (6pp), 2020 October 10 © 2020. The Author(s). Published by the American Astronomical Society.

https://doi.org/10.3847/2041-8213/abb9a4



OPEN ACCESS

Single-hemisphere Dynamos in M-dwarf Stars

Benjamin P. Brown

Gradin P. B

⁴ Department of Engineering Science and Applied Mathematics, Northwestern University, 2145 Sheridan Road, Evanston, IL 60208, USA Department of Mathematics, Massachusetts Institute of Technology, Cambridge, MA 02139, USA Center for Computational Astrophysics, Flatinon Institute, New York, NY 10010, USA

Received 2020 August 4; revised 2020 September 11; accepted 2020 September 17; published 2020 October 7

50 atitude 0 r = 0.51000 2000 3000 4000 5000 6000 50 latitude $\langle A_{\dot{\alpha}} \rangle$ n r = 1.0-50 1000 2000 3000 4000 5000 6000 time $[\Omega^{-1}]$

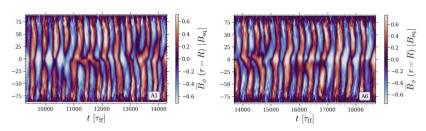


Comparison with other simulations (2)

Simulations of dynamo action in slowly rotating M dwarfs: Dependence on dimensionless parameters

C. A. Ortiz-Rodríguez¹, P. J. Käpylä^{2,3,4}, F. H. Navarrete^{5,4}, D. R. G Schleicher¹, R. E. Mennickent¹, J.P. Hidalgo¹, and B Toro¹

- Departamento de Astronomía, Facultad de Ciencias Físicas y Matemáticas, Universidad de Concepción, Av. Esteban Iturra s/n Barrio Universitario, Casilla 160-C, Chile
- ² Leibniz-Institut für Sonnenphysik (KIS), Schöneckstr. 6, 79104 Freiburg, Germany
- ³ Institut für Astrophysik und Geophysik, Georg-August-Universität Göttingen, Friedrich-Hund-Platz 1, 37077 Göttingen, Germany
- Nordita, KTH Royal Institute of Technology and Stockholm University, 10691 Stockholm, Sweden
- ⁵ Hamburger Sternwarte, Universität Hamburg, Goienbergsweg 112, 21029 Hamburg, Germany



Surface magnetic fields

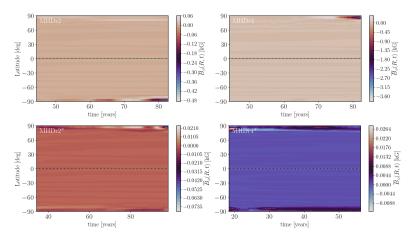


Figure: Time-latitude diagrams of the azimuthally averaged toroidal magnetic field $\overline{B}_\phi(r=R,\theta,t)$ of both groups.



Large-scale flows

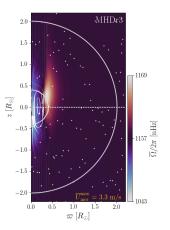


Figure: Profile of the temporally and azimuthally averaged rotation rate $\overline{\Omega}(\varpi,z)$ for MHDr3. The streamlines indicate the mass flux due to meridional circulation and the maximum averaged meridional flow is indicated in the lower left side of each plot.

Large-scale flows (2)

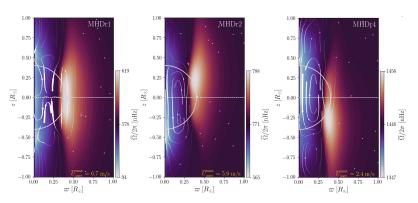


Figure: Profiles of the temporally and azimuthally averaged rotation rate $\overline{\Omega}(\varpi,z)$ for runs from the MHD group. The streamlines indicate the mass flux due to meridional circulation and the maximum averaged meridional flow is indicated in the lower left side of each plot.



Large-scale flows (3)

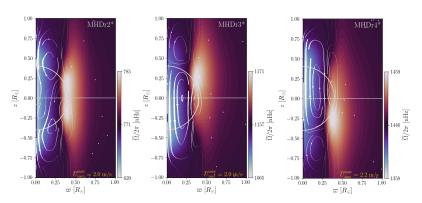


Figure: Profiles of the temporally and azimuthally averaged rotation rate $\overline{\Omega}(\varpi,z)$ for runs from the MHD* group. The streamlines indicate the mass flux due to meridional circulation and the maximum averaged meridional flow is indicated in the lower left side of each plot.



Energy analysis

From the time series, we have $E_{\rm mag}=\int_V \frac{1}{2\mu_0} {\bf B}^2 dV$ and $E_{\rm kin}=\int_V \frac{1}{2} \rho {\bf u}^2 dV$. Plotting these quantities:

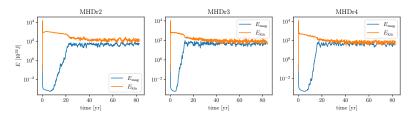


Figure: Temporal evolution of magnetic and kinetic energy from group MHD.

Conclusions

• The core of the star is able to produce very strong magnetic fields ($\overline{B}_{\phi}\sim 200$ kG).

- The core of the star is able to produce very strong magnetic fields ($\overline{B}_{\phi}\sim 200$ kG).
- A core dynamo does not seem to be sufficient to explain the large-scale magnetic fields of Ap stars.

- The core of the star is able to produce very strong magnetic fields ($\overline{B}_{\phi} \sim 200$ kG).
- A core dynamo does not seem to be sufficient to explain the large-scale magnetic fields of Ap stars.
- These fields have roughly equipartition values in fast rotators, similar to Brun et al. (2005) and Featherstone et al. (2009).

- The core of the star is able to produce very strong magnetic fields ($\overline{B}_{\phi} \sim 200$ kG).
- A core dynamo does not seem to be sufficient to explain the large-scale magnetic fields of Ap stars.
- These fields have roughly equipartition values in fast rotators, similar to Brun et al. (2005) and Featherstone et al. (2009).
- Vertical flows might be transporting the magnetic field to the surface, due to the high Coriolis number.

- The core of the star is able to produce very strong magnetic fields ($\overline{B}_{\phi} \sim 200$ kG).
- A core dynamo does not seem to be sufficient to explain the large-scale magnetic fields of Ap stars.
- These fields have roughly equipartition values in fast rotators, similar to Brun et al. (2005) and Featherstone et al. (2009).
- Vertical flows might be transporting the magnetic field to the surface, due to the high Coriolis number.
- The envelope has approximately-rigid rotation like the radiative interior of the Sun (see Howe 2009). And the core has solar-like differential rotation in all runs.



Future work

Next steps

• Explore more rotation rates.

Future work

Next steps

- Explore more rotation rates.
- Study how a fossil field would affect the nature of the core dynamo.

Future work

Next steps

- Explore more rotation rates.
- Study how a fossil field would affect the nature of the core dynamo.
- Are these two elements enough to explain the large-scale magnetic fields of Ap/Bp stars?

References I

```
Aurière M., et al., 2007, A&A, 475, 1053
Becerra L., Reisenegger A., Valdivia J. A., Gusakov M. E., 2022, MNRAS, 511, 732
Braithwaite J., Nordlund A., 2005, Astronomy and Astrophysics, 450
Brandenburg A., Subramanian K., 2004, Phys. Rep., 417
Brun A. S., Browning M. K., Toomre J., 2005, ApJ, 629, 461
Cowling T. G., 1945, MNRAS, 105, 166
Featherstone N. A., Browning M. K., Brun A. S., Toomre J., 2009, ApJ, 705, 1000
Howe R., 2009, Living Reviews in Solar Physics, 6, 1
Käpylä P. J., 2021, A&A, 651, A66
Krause F., Oetken L., 1976, in Weiss W. W., Jenkner H., Wood H. J., eds, IAU
   Collog. 32: Physics of Ap Stars. p. 29
Käpylä P. J., Gent F. A., Olspert N., Käpylä M. J., Brandenburg A., 2020,
   Geophysical & Astrophysical Fluid Dynamics, 114, 8
Lyra W., McNally C. P., Heinemann T., Masset F., 2017, AJ, 154, 146
MacGregor K. B., Cassinelli J. P., 2003, ApJ, 586, 480
Moss D., 1989, MNRAS, 236, 629
Parker E. N., 1979, Ap&SS, 62, 135
```

Physical Units

The Pencil Code expresses all the relevant quantities in code units, so to give them physical meaning it is required to do some conversions:

$$[x] = \left(\frac{R_*}{R_{\text{sim}}}\right) \qquad [t] = \left(\frac{\Omega_{\text{sim}}}{\Omega_*}\right)$$
$$[u] = \left(\frac{\Omega_* R_*}{\Omega_{\text{sim}} R_{\text{sim}}}\right) \qquad [B] = \left[\frac{\mu_0 \rho_* (\Omega_* R_*)^2}{\mu_{\text{sim}} \rho_{\text{sim}} (\Omega_{\text{sim}} R_{\text{sim}})^2}\right]^{1/2}$$

where (see Appendix A of Käpylä et al. 2020):

$$\frac{\Omega_{\text{sim}}}{\Omega_*} = L_{\text{ratio}}^{1/3} \left(\frac{g_{\text{sim}}}{g_*} \frac{R_*}{R_{\text{sim}}} \right)^{1/2}$$



Schwarzschild criterion

According to the Schwarzschild criterion, we can expect convection to occur if:

$$\vec{\nabla}_{\rm rad} = \frac{3}{16\pi acG} \frac{P}{T^4} \frac{\kappa l}{m} > \vec{\nabla}_{\rm ad}$$

This is:

- A large value of the opacity κ . Since low-mass stars are cooler than high-mass stars, we may expect low-mass stars to have convective envelopes.
- Regions with a large energy flux (i.e. large l/m), stars which nuclear energy production is strongly peaked towards the centre can be expected to have convective cores.



Hyper-diffusivities

The code offers numerical sixth-order tools which smooths out the smallest scales, dissipating the energy and preventing instabilities. Here, we used the mesh method implemented by Alex Brandenburg described in Lyra et al. (2017):

$$f_{\mathrm{visc}}^{(\mathrm{hyper})} = \nu_3^{\mathrm{mesh}} \frac{\Delta^6 \nu}{\Delta q^6}, \qquad f_{\mathrm{diff}}^{(\mathrm{hyper})} = \eta_3^{\mathrm{mesh}} \frac{\Delta^6 \eta}{\Delta q^6}$$

Differential rotation (2)

The differential rotation is studied using the following parameters:

$$\Delta_{\Omega}^{(r)} = \frac{\overline{\Omega}(r_{\text{top}}, \theta_{\text{eq}}) - \overline{\Omega}(r_{\text{bot}}, \theta_{\text{eq}})}{\overline{\Omega}(r_{\text{top}}, \theta_{\text{eq}})},$$
$$\Delta_{\Omega}^{(\overline{\theta})} = \frac{\overline{\Omega}(r_{\text{top}}, \theta_{\text{eq}}) - \overline{\Omega}(r_{\text{top}}, \overline{\theta})}{\overline{\Omega}(r_{\text{top}}, \theta_{\text{eq}})},$$

where $r_{\rm top}=0.9R$ and $r_{\rm bot}=0.1R$ are the radius at the top and bottom of the star, respectively. $\overline{\theta}$ is an average of $\overline{\Omega}$ between latitudes $-\theta$ and θ .

Differential rotation (3)

Run	$\Delta_{\Omega}^{\mathrm{CZ}(r)}$	$\Delta_{\Omega}^{\mathrm{CZ}\overline{\theta}}(60^{\circ})$	$\Delta_{\Omega}^{\mathrm{CZ}\overline{\theta}}(75^{\circ})$	$\Delta_{\Omega}^{(r)}$	$\Delta_{\Omega}^{\overline{\theta}}(60^{\circ})$	$\Delta_{\Omega}^{\overline{\theta}}(75^{\circ})$
MHDr2	0.1131	0.0699	0.1142	0.0505	-0.0001	-0.0006
MHDr2*	0.1101	0.0683	0.1133	0.0485	-0.0001	-0.0006
MHDr3	0.0538	0.0295	0.0484	0.0251	-0.0000	-0.0004
MHDr3*	0.0489	0.0283	0.0438	0.0224	-0.0001	-0.0006
MHDr4	0.0405	0.0213	0.0350	0.0197	-0.0000	-0.0003
MHDr4*	0.0387	0.0208	0.0333	0.0169	-0.0001	-0.0006

Figure: Differential rotation parameters for all simulations, obtained from the averaged (azimuthally and temporally) angular velocity $\overline{\Omega}$.

The radiative envelope has almost rigid rotation, and the core has solar-like rotation in all runs.



Initial conditions

The convective core is assumed to encompass 20% of the stellar radius (similar to Brun et al. 2005 and Featherstone et al. 2009).

We assumed a piecewise polytropic initial state: $p(\rho)=K_0\rho^\gamma$, where $\gamma=1+\frac{1}{n}$, and:

$$n = \left\{ \begin{array}{ll} 1.5 & \text{if} & r < 0.2R \\ \\ 3.25 & \text{if} & r > 0.2R \end{array} \right. ,$$

is the polytropic index.



Possible explanations (4)

Interaction between a core dynamo and a fossil field.

Previous work

Featherstone et al. (2009) performed 3D simulations of the inner 30% by radius of a $2M_{\odot}$ A-type star (excluding the innermost values), modeling a core dynamo surrounded by a radiative envelope. The inclusion of a fossil field in this envelope can lead to a very strong super-equipartition field.

Possible explanations (6)

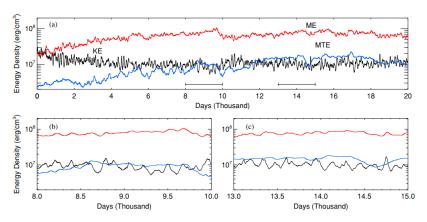


Figure: Temporal evolution of overall energy densities after imposing a mixed poloidal–toroidal magnetic (fossil) field configuration. The magnetic energy (ME) grows until it reaches 10 times the value of the kinetic energy (KE). Extracted from Featherstone et al. (2009).