

Programming Language, 2022 Spring, Assignment 1

Due: March 20 Sun, 11:59 pm

Submission

Write the functions in problem 1 – 5 in a single file, named “*sol1.sml*”. Then upload the file to the course homepage (assignment 1). The function names (and their types) should be the same as is described for each problem. There should be no error when using the file in repl with the following command: use “*sol1.sml*”; Because we are going to test your solution with an automated script, if our script cannot import your file with [use “*sol1.sml*”] then your score for this assignment will be zero. So, make sure you test your code.

Problems

1. Merge Lists (10pt)

Write *merge* function that takes two sorted lists (in ascending order) and returns a sorted list that contains all the elements in the two lists. The signature of the function is as following:

```
merge: int list * int list -> int list
```

For example, `merge([1,4,5], [2,6,7])` should return `[1,2,4,5,6,7]`. You may assume that each of the input lists does not have repeating elements. For example, `[1,1,4,5]` cannot be used as an input to *merge* function because 1 is repeated. Also the two lists do not have common numbers. For example, we do not invoke `merge([1,5], [1,7])` because 1 is in both the lists.

2. Reverse List (10pt)

Write *reverse* function that takes a list and returns the reversed list. For example, `reverse([1,5,4])` returns `[4,5,1]`. The signature of the function is as following:

```
reverse: int list -> int list
```

For problem 2, you should not use the ML’s built-in function `rev`.

3. Pi Function (10pt)

Write *pi* function that takes two integers, *a* and *b*, and a function *f* and returns the following:

$$\prod_{n=a}^b f(n)$$

The signature of *pi* is as following:

```
pi: int * int * (int -> int) -> int
```

In other words, `pi(a,b,f)` computes $f(a) \times f(a+1) \times \dots \times f(b-1) \times f(b)$

4. Digits Function (10pt)

Write *digits* function that takes a positive integer and returns the list of digits of the integer. For example, `digits(253)` returns `[2, 5, 3]`. The function's signature should be:

```
digits: int -> int list
```

You may assume that the input is a positive number.

5. Digital Roots and Additive Persistence (20pt: 10pt for each function)

Consider the process of taking a number, adding its digits, then adding the digits of the number derived from it, etc., until the remaining number has only one digit. The number of additions required to obtain a single digit from a number n is called the *additive persistence* of n , and the digit obtained is called the *digital root* of n . For example, the sequence obtained from the starting number 9876 is (9876, 30, 3), so 9876 has an additive persistence of 2 and a digital root of 3. For the starting number 12349, the process produces (12349, 19, 10, 1), so 12349 has an additive persistence of 3 and a digital root of 1.

Write two functions *additivePersistence* and *digitalRoot* that take positive integer argument n and return the additive persistence and the digital root of n respectively. The signatures of the functions are as following:

```
additivePersistence: int -> int
```

```
digitalRoot: int -> int
```

You can use `digits` function defined in the previous question.