

# Assignment 1

## 1 Case : $y = w \cdot x$

### 1.1 Generate Data

Generate  $(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)$  as follows.

1. Choose a number  $w^{opt}$  for  $w$ .
2. Generate 1000 random numbers from 0 to 1000. We call this set  $X$ .
3. For each  $x \in X$ , generate  $y = w^{opt} \cdot x$ . (You may generate the number  $y$  like  $x \sim N(w^{opt} \cdot x, 1)$ .)

### 1.2 Estimate $w$

1. Choose a number for  $\eta$ .
2. Find  $w$ .
  - 2-1. Choose a number for  $w$  arbitrarily.
  - 2-2.  $w \leftarrow w - \eta \sum_{i=1}^n (w \cdot x_i - y_i) \cdot x_i$  until convergence. Let the final  $w$  be  $w^*$ .
3. Check  $w^*$  with  $w^{opt}$ .

## 2 Case : $y = w \cdot x + b$

### 2.1 Generate Data

Generate  $(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)$  as follows.

1. Choose a number  $w^{opt}, b^{opt}$  for  $w, b$ , respectively.
2. Generate 1000 random numbers from 0 to 1000. We call this set  $X$ .
3. For each  $x \in X$ , generate  $y = w^{opt} \cdot x + b^{opt}$ . (You may generate the number  $y$  like  $x \sim N(w^{opt} \cdot x + b^{opt}, 1)$ .)

### 2.2 Estimate $w$ and $b$

1. Choose numbers for parameters.
  - 1-1. Choose a number for  $\eta_w$ .
  - 1-2. Choose a number for  $\eta_b$ .

2. Until convergence,
  - 2-1.  $w \leftarrow w - \eta_w \sum_{i=1}^n (w \cdot x_i + b - y_i) \cdot x_i$ .
  - 2-2.  $b \leftarrow b - \eta_b \sum_{i=1}^n (w \cdot x_i + b - y_i)$ .
  - 2-3. Let the final  $w, b$  be  $w^*, b^*$ , respectively.
3. Check  $w^*, b^*$  with  $w^{opt}, b^{opt}$ .

### 3 Next

Design the online versions of the above batch versions.