# COMP3811: Computer Graphics Coursework 2

# Interactive Animated Scenes with OpenGL

Juan Camacho sid: 201356237 sc19jcm

January 8, 2022

# Contents

1	Inti	roduction						
	1.1	Aims						
	1.2	Context						
<b>2</b>	Bar	nd 4 (40%-50%)						
	2.1	Basic objects						
	2.2	Complex scene						
		2.2.1 Planets						
		2.2.2 Spaceship						
		2.2.3 Gear						
		2.2.4 Background						
	2.3	Materials and lighting						
3	Rar	nd 3 (50%-60%)						
•		User interaction						
	0.1							
4		Band 2 (60%-70%)						
	4.1	Animation						
		4.1.1 Orbit						
		4.1.2 Oscillation						
	4.2	Convex objects						
	4.3	Texture mapping						
5	Bar	nd 1 (70%-100%)						
	5.1	Hierarchical modelling						
	5.2	User interaction						
6	Cor	nclusion 3						
Ü	6.1	Source code instructions						
	6.2	Video demonstrations						
		•						
7	Rof	Orongos 9						

# 1 Introduction

Space exploration allows humans to prove or disprove theories that scientists rise, and the technology takes credit for it. Space simulations are used a many research areas to make future predictions from data. From the given textures for this project, the Earth map texture immediately gave me the idea to create a simulation of our solar system.

## 1.1 Aims

- Meet the requirements of each band of the project specification.
- Create a scene using real physics formulas to generate the movement of the space objects.

# 1.2 Context

For a better understanding of the context of this project, the final result is given in Figure 1. This will hopefully justify the design choices on each phase of the development.

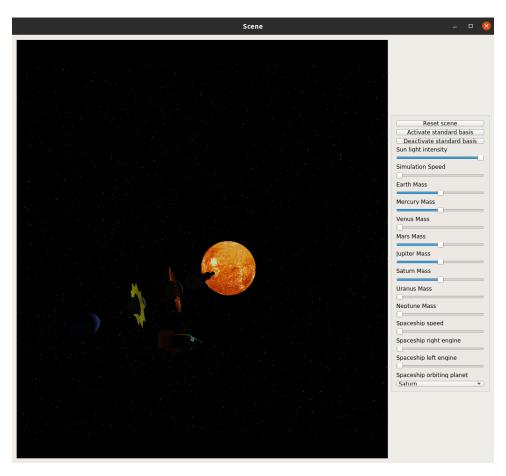


Figure 1: Screenshot of the final product

# 2 Band 4 (40%-50%)

The requirements of band 4 were to create a reasonable complex scene using instancing of different objects, and adding light and material properties to the scene that allow for diffuse and specular lighting. A rough layout of the scene and the objects in it was drawn:

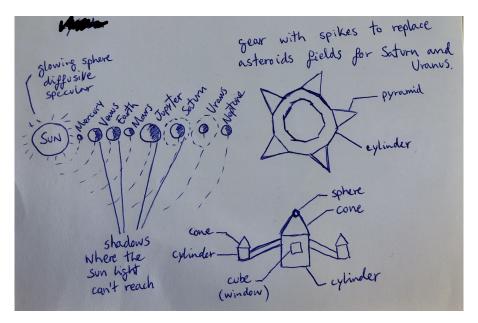


Figure 2: Draft of the complex scene

## 2.1 Basic objects

To make the instantiation of objects easier and in order to build more complex ones, primitive shapes were defined and implemented as described in Table 1.

${f Shape}$	Implementation	Orientation	Description
cube	GL_POLYGON	outside normals	taken from COMP3811 tutorials.
cylinder	GL_POLYGON	outside normals	taken from COMP3811 tutorials.
$_{\mathrm{sphere}}$	gluSphere object	outside normals	quadrics object
$\operatorname{disk}$	gluDisk object	outside normals	quadrics object
cone	GL_POLYGON	outside normals	derived from COMP3811 tutorials cylinder.
pyramid	GL_POLYGON	outside normals	square based pyramid, built within implementation
			of the complex gear object.

Table 1: Basic shapes

The choice for these shapes was decided from the initial design of the scene 2. The Sun is considered to be the light source of the scene, thus the normal vectors of the polygons point outwards. The declarations of the shapes can be found in Figure 3, and the implementation of the new polygons such as the gear (containing pyramids) and the cone is in Figures 4 and 5. Initial instances of the development of the cone and the gear can be seen in Figures 6 and 7.

```
#ifndef A25831C8 51A5 403F B582 7BD4DC518B2A
     #define A25831C8_51A5_403F_B582_7BD4DC518B2A
     #include <GL/gl.h>
     static const float PI = 3.1415926535;
       Lighting values of the materials
     You, 18 hours ago | 1 author (You)
      GLfloat ambient[4];
       GLfloat diffuse[4];
       GLfloat specular[4];
       GLfloat shininess;
                      texture ID to bind
     void cube(const materialStruct* p_front, int flag, GLuint* texID);
     void cylinder(const materialStruct* p front);
47
48
49
50
51
52
53
54
55
56
     void openedCone(const materialStruct* p_front, float r);
                      determines the number of pyramids (spikes) that the gear will have.
     void gear(const materialStruct* p_front, int n_spikes);
     #endif · /* · A25831C8 51A5 403F B582 7BD4DC518B2A ·*/
```

Figure 3: Definitions in utils/Shapes.h

```
void openedCone(const materialStruct* p_front, float r){
           int N
                        = 100;
           int n div
         glMaterialfv(GL_FRONT, GL_AMBIENT, ...
                                                  p front->ambient);
         glMaterialfv(GL_FRONT, GL_DIFFUSE,
                                                   p front->diffuse);
         glMaterialfv(GL FRONT, GL SPECULAR,
glMaterialf(GL_FRONT, GL_SHININESS,
                                                 p_front->specular);
                                                  p front->shininess);
        float x0, x1, y0, y1;
        float z \min = -1;
        float z max = 1;
        float delta z = (z max - z min)/n div;
        for (int i = 0; i < N; i++) {
- for(int i_z = 0; i_z < n_div; i_z++) [
            x0 = cos(2*i*PI/N);
            x1 = \cos(2*(i+1)*PI/N);
             y0 = sin(2*i*PI/N);
             y1 = sin(2*(i+1)*PI/N);
             glBegin(GL_POLYGON);
             glVertex3f(x0,y0,z);
               glNormal3f(x0,y0,0);
             glVertex3f(x1,y1,z);
               glNormal3f(x1,y1,0);
             glVertex3f(r*x1,r*y1,z+delta_z); · · // apply radius to opposite side of cylinder
112
               glNormal3f(x1,y1,0);
             glVertex3f(r*x0,r*y0,z+delta_z); // apply radius to opposite side of cylinder
114
             glNormal3f(x0,y0,0);
116
             glEnd();
119
```

Figure 4: openedCone() implementation, utils/Shapes.cpp

```
float z_max = ··1.; ··// depth ·1.0 · max float r = 1.5 · · · · // radius
        float delta_z = (z_max - - z_min)/n_div;
     glBegin(GL_POLYGON);
close for (int i_z = 0; i_z < n_div; i_z++){
close = cos(2*i*PI/N);</pre>
            x1 = \cos(2*(i+1)*PI/N);
            x2 = r*cos(2*i*PI/N);
            x3 = r*cos(2*(i+1)*PI/N);
y0 = sin(2*i*PI/N);
            y1 = sin(2*(i+1)*PI/N);
            y3 = r*sin(2*(i+1)*PI/N);
            glVertex3f(x0,y0,0);
                                       glNormal3f(x0,y0,0);
            glVertex3f(x2,y2,0);
                                       glNormal3f(x2,y2,0);
            glVertex3f(x2,y2,0.5);
                                      glNormal3f(x2,y2,0.5);
            glVertex3f(x0,y0,0.5);
                                      glNormal3f(x0,y0,0.5);
            glVertex3f(x2,y2,0);
                                       glNormal3f(x2,y2,0);
            glVertex3f(x3,y3,0);
                                       glNormal3f(x3,y3,0);
            glVertex3f(x3,y3,0.5);
                                       glNormal3f(x3,y3,0.5);
            glVertex3f(x2,y2,0.5);
                                       glNormal3f(x2,y2,0.5);
            glVertex3f(x3,y3,0);
                                       glNormal3f(x3,y3,0);
                                      glNormal3f(x1,y1,0);
glNormal3f(x1,y1,0.5);
            glVertex3f(x1,y1,0);
            glVertex3f(x1,y1,0.5);
            glVertex3f(x3,y3,0.5);
                                      glNormal3f(x3,y3,0.5);
                                       glNormal3f(x1,y1,0);
            glVertex3f(x1,y1,0);
            glVertex3f(x0,y0,0);
                                       glNormal3f(x0,y0,0);
            glVertex3f(x1,y1,0.5); glNormal3f(x1,y1,0.5);
            glVertex3f(x0,y0,0.5); glNormal3f(x0,y0,0.5);
            if (1%2==0)
              x0 = x2; // old x2
x1 = x3; // old x3
              x2 = 2.*cos(2*i*PI/N);
x3 = 2.*cos(2*(i+0.5)*PI/N);
              y1 = y3;
y2 = 2.*sin(2*i*PI/N);
y3 = 2.*sin(2*(i+0.5)*PI/N);
187
              glVertex3f(x0,y0,0);
                                         glNormal3f(x0,y0,0);
              glVertex3f(x2,y2,z);
                                         glNormal3f(x2,y2,0);
              glVertex3f(x2,y2,z); glNormal3f(x2,y2,0.5);
              glVertex3f(x0,y0,0.5); glNormal3f(x0,y0,0.5);
              glVertex3f(x2,y2,z);
                                         glNormal3f(x2,y2,0);
              glVertex3f(x2,y2,z); glNormal3f(x2,y2,0.5);
              glVertex3f(x3,y3,z);
                                         glNormal3f(x3,y3,0);
              glVertex3f(x1,y1,0);
                                         glNormal3f(x1,y1,0);
              glVertex3f(x1,y1,0.5); glNormal3f(x1,y1,0.5);
              glVertex3f(x3,y3,z); -glNormal3f(x3,y3,0.5);
              glVertex3f(x1,y1,0);
                                         glNormal3f(x1,y1,0);
              glVertex3f(x0,y0,0);
                                         glNormal3f(x0,y0,0);
                                         glNormal3f(x1,y1,0.5);
              glVertex3f(x1,y1,0.5);
              glVertex3f(x0,y0,0.5); glNormal3f(x0,y0,0.5);
     glEnd();
```

Figure 5: gear() implementation in utils/Shapes.cpp. Top part of the function initialises variables and materials properties.

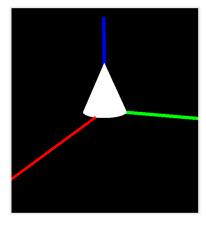


Figure 6: Instance of a cone object (early implementation)

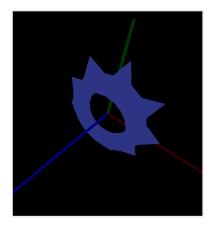


Figure 7: Instance of a gear object (early implementation)

# 2.2 Complex scene

The complex scene was built with instances of the basic shapes defined in Table 1. the scene is comprised of a centered star, the Sun, and eight planets: Mercury, Venus, Earth, Mars, Jupiter, Saturn, Uranus and Neptune. An initial stage of the scene development is shown in Figure 8. Planets were obtained from the result of applying their corresponding textures to each gluSphere() object.



Figure 8: Solar system early stage

A spaceship, shown in Figures 9 and 10, was created from the basic shapes with the mission to carry Marc and Markus around the different planets. The ring with spikes (gear() in Figures 3 and 5) that simulates the fields of asteroids of Saturn and Neptune is shown in Figure 11. The solar system scene is contained within a cubemap of stars which defines an infinite space background, Figure 12 shows the rendered background.



Figure 9: Spaceship front



Figure 10: Spaceship back



Figure 11: Saturn's ring

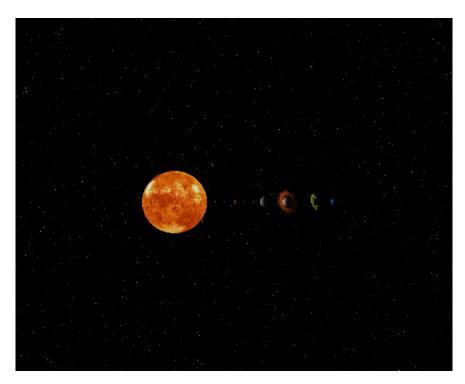


Figure 12: Solar system within a cubemap simulating other stars away

Materials are defined in 20 of type materialStruct (declared in 3) to be applied to the complex shapes to generate the ambient, diffuse, specular and shiny lighting properties of each of the objects.

The following subsections give a more detailed explanation of the transformations that the objects in the scene involve.

#### 2.2.1 Planets

Each planet is an instance of gluSphere() with its correspondent planet texture, each planet with GLU\_SMOOTH gluQuadricNormals normals. The sun is in the center of the standard basis, the rest of the planets are transformed in order from closest to furthest according to their distances from the Sun, on the positive x direction in the start of the simulation. Each planet, including the Sun, has its own rotation around the up vector, which is the y-axis. drawPlanet() (defined in Figure 16) instantiates a planet in the scene with the given parameters to calculate their orbit, mass, momentum, radius of sphere and their texture ID. Each planet is of type PlanetWidget which is declared in PlanetWidget.h and defined in Figure 13.

#### 2.2.2 Spaceship

An instance of a cylinder() (Figure 3) is used with yellowPlastic material properties as the main body of the craft. It has a instance of an openedCone() (Figure 3) with cyanPlastic material properties on top of the cylinder. The openedCone instance is instantiated such that one of the polygon's opposite ends has a different radius to the other end. Therefore, in this case, it is an opened cone such that a gluSphere() object can fit at the end of the polygon to create the tip of the craft. The bottom of the cylinder is covered by a gluDisk() instance with ruby material properties. The spaceship is comprised of two engines placed on opposite sides, each of them is built by a cylinder() instance with a openedCone instance on top with brassMaterials and cyanPlastic material properties respectively. Both openedCone instances are created with a very small radius by their top end such that they look as if they were a cone. The bottom of each of the engines is covered by an instance of gluDisk() with material properties polishedCopper. Both engines are joined to the main body of the spaceship through scaled cube() instances that result in rectangles. The drawSpaceship() function declared in Figure 14 with an extense declaration in Spaceship.cpp instantiates

the spaceship in the scene. Part of its declaration can be seen in Figure 38 that shows the transformations, rotations, and basic objects by which the right engine is comprised of.

### 2.2.3 Gear

Saturn and Neptune have asteroid fields which in this project were simulated by "gears with spikes", instanced by gear() in 5. Saturn's ring shown in Figure 11 with material properties polishedCopper is comprised of a cylinder with a top layer of pyramids (Figure 5, lines 173-207), these were implemented within gear() function. In the other hand, Neptune's gear has material properties yellowPlastic. The rings are translated to their planet's coordinates and have a radius larger than their the planet that they orbit. The chosen materials might not match the colour of the planet, but they respond to lighting conditions with vibrant colours that catch our eyes.

# 2.2.4 Background

A cubemap of 6 textures is loaded by loadCubemap() and rendered by renderCubemap (Figure 15), both declared in (declared in SolarSystemWidget.cpp). A single instance of renderCubemap() shown in Figure 12 renders a cubemap which is scaled to contain the solar system. The textures of the cubemap represent an infinite amount of bright stars, without any light properties attributed to it.

Textures for the planets and for the cubemap were obtained from [2]

```
#include <GL/glu.h>
#include *"PlanetWidget.h"

// constructor

PlanetWidget::PlanetWidget(QWidget *parent, GLuint texID, double mass, double radius, for the planetwidget(QWidget *pose, double *momentum, into i)

Constructor

Construc
```

Figure 13: PlanetWidget class defined in PlanetWidget.cpp

Figure 14: Definitions of spaceship in Spaceship.h

```
void SolarSystemWidget::renderCubemap()
                                      glPushMatrix();
                                      \verb|glScalef(9.,9.,9.)|; \cdots // \cdot \verb|scale| \cdot \verb|it+to+make| \cdot \verb|it+the+background+of+the+scene|
 503
                                                 glBindTexture(GL TEXTURE CUBE MAP, texIDcube);
                                                 glBegin(GL_QUADS);
                                               glTexCoord3f(~0.5f,~-0.5f,~0.5f); glVertex3f(~0.5f,~-0.5f,~0.5f); glTexCoord3f(~0.5f,~-0.5f,~-0.5f); glTexCoord3f(~0.5f,~-0.5f,~-0.5f); glVertex3f(~0.5f,~-0.5f,~-0.5f); glTexCoord3f(~0.5f,~0.5f,~-0.5f); glVertex3f(~0.5f,~0.5f,~-0.5f);
                                              glEnd();
                                      ·//·Render the left quad
glBegin(GL_QUADS);
                                              glTexCoord3f(~-0.5f,~0.5f,~0.5f~); glVertex3f(~-0.5f,~0.5f,~0.5f~);
                                               glTexCoord3f( -0.5f, -0.5f, -0.5f); glVertex3f( -0.5f, -0.5f, -0.5f); glTexCoord3f( -0.5f, -0.5f, -0.5f); glVertex3f( -0.5f, -0.5f, -0.5f); glTexCoord3f( -0.5f, -0.5f, -0.5f); glVertex3f( -0.5f, -0.5f, -0.5f);
                                       glEnd();
                                       // Render the top quad
                                      glBegin(GL QUADS);
                                              glTexCoord3f( -0.5f, -0.5f, -0.5f ); glVertex3f( -0.5f, -0.5f, -0.5f ); glTexCoord3f( -0.5f, -0.5f, -0.5f ); glVertex3f( -0.5f, -0.5f, -0.5f ); glTexCoord3f( -0.5f, -0.5f, -0.5f ); glVertex3f( -0.5f, -0.5f, -0.5f ); glVertex3f( -0.5f, -0.5f, -0.5f ); glVertex3f( -0.5f, -0.5f, -0.5f );
                                      glEnd();
                                      glBegin(GL QUADS);
                                                 glTexCoord3f( -0.5f, -0.5f, -0.5f ); glVertex3f( -0.5f, -0.5f, -0.5f );
                                                 glTexCoord3f( -0.5f, -0.5f, -0.5f ); glVertex3f( -0.5f, -0.5f, -0.5f );
                                               glTexCoord3f(~0.5f,~0.5f,~0.5f); glVertex3f(~0.5f,~0.5f,~0.5f); glTexCoord3f(~0.5f,~0.5f,~0.5f,~0.5f);
                                      glEnd();
                                      glBegin(GL QUADS);
535
                                               glTexCoord3f( - 0.5f, - -0.5f, - --0.5f ); glVertex3f( - 0.5f, --0.5f, --0.5f );
                                               glTexCoord3f( -0.5f, -0.5f, glTexCoord3f( -0.5f, -0
                                                                                                                                                                                                    --0.5f ); glVertex3f( --0.5f, --0.5f, -0.5f, );

--0.5f ); glVertex3f( --0.5f, -0.5f, --0.5f );

--0.5f ); glVertex3f( --0.5f, -0.5f, --0.5f );
                                      glEnd();
                                                glBegin(GL QUADS);
                                               glTexCoord3f( 0.5f, -0.5f, glTexCoord3f( -0.5f, -0.5f, glTexCoord3f( -0.5f, -0.
                                                                                                                                                                                                     0.5f ); glVertex3f( 0.5f, -0.5f, 0.5f );
0.5f ); glVertex3f( -0.5f, -0.5f, 0.5f );
                                                                                                                                                                                                     0.5f ); glVertex3f( -0.5f, -0.5f, -0.5f );
                                                 glTexCoord3f(-0.5f,-0.5f,-0.5f); glVertex3f(-0.5f,-0.5f,-0.5f);
                                                 glEnd();
                                       glPopMatrix();
```

Figure 15: Cubemap texture mapping in renderCubemap() function declaration in SolarSystemWidget.cpp

```
void SolarSystemWidget::drawPlanet(PlanetWidget* planet)
         GLfloat mat emission[] = {0.8, 0.8, 0.8, 0.0};
         glPushAttrib(GL LIGHTING BIT);
         if (planet == sun)
           glMaterialfv(GL_FRONT, GL_EMISSION, mat_emission);
         PlanetWidget* planet_to_orbit;
         if (planetIndex == 0)
          planet to orbit = mercury;
         else if (planetIndex == 1)
          planet to orbit = venus;
         else if (planetIndex == 2)
         planet_to_orbit = earth;
         else if (planetIndex == 3)
          planet_to_orbit = mars;
         else if (planetIndex == 4)
          planet_to_orbit = jupyter;
         else if (planetIndex == 5)
          planet to orbit = saturn;
         else if (planetIndex == 6)
          planet to orbit = uranus;
         else if (planetIndex == 7)
          planet_to_orbit = neptune;
          \textbf{if} \cdot (\textbf{planet} \cdot == \cdot \textbf{earth}) \cdot \cdot \cdot \cdot / / \cdot \textbf{reder} \cdot \textbf{spaceship} \cdot \textbf{once} \cdot \textbf{per} \cdot \textbf{frame}, \cdot \textbf{that's} \cdot \textbf{why} \cdot \textbf{we} \cdot \textbf{make} \cdot \textbf{this} \cdot \textbf{check} 
           glDisable(GL TEXTURE 2D);
           glPushMatrix();
           glTranslatef(planet to orbit-> pose[0],planet to orbit-> pose[1],planet to orbit-> pose[2]);
           glPushMatrix();
           qlRotatef(spaceshipSpeed* time, 1.,0.,0.);
           glTranslatef(0., 1.5, 0.);
           glRotatef(1*_time, 0.,0.,1.);
glScalef(0.2, 0.2, 0.2);
           drawSpaceship(texID, time sinewave, left engine deg, right engine deg);
           glPopMatrix();
           glPopMatrix();
           glEnable(GL TEXTURE 2D);
         //-update-planet's-orbit-according-to-their-gravitational-force-to-the-rest-of-the-bodies
         updatePlanetOrbit(planet);
         glTranslatef(planet-> pose[0],planet-> pose[1],planet-> pose[2]);
477
478 |
         glRotatef(0.5* time, 0.f, 1.f, 0.f);
         GLUquadric *qobj = gluNewQuadric();
         gluQuadricTexture(qobj, GL_TRUE);
         gluQuadricNormals(qobj, GLU_SM00TH); // One normal is generated for every vertex of a quadric
         gluQuadricDrawStyle(qobj, GLU_FILL);
         glRotatef(-90, 1.0, 0.0, 0.0); // correct orientation for planet's textures
         glBindTexture( GL_TEXTURE_2D, texID[planet->_texID] );
         gluSphere(qobj, planet->_radius, 200, 200);
         gluDeleteQuadric(gobj);
         glPopAttrib();
```

Figure 16: drawPlanet() defined in SolarSystemWidget.cpp

# 2.3 Materials and lighting



Figure 17: Perspective view of complex scene, diffuse light only



Figure 18: Perspective view of complex scene, ambient light only

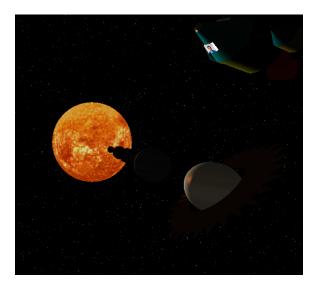


Figure 19: Perspective view of complex scene, diffuse and specular

Only six materials of type materialStruct (Figure 3) are defined in Figure 20 that represent the materials used in the complex objects described above.

In terms of lighting conditions,

- the background does not show any sign of lighting, only ambient light applies to it, Figure 21.
- the sun is a glowing sphere, this effect is acquired with the light property GL\_EMISSION which is set in drawPlanet() (Figure 16).
- The scene contains only GL\_LIGHTO which is placed in the center of the scene, i.e. within the Sun. GL\_LIGHTO is assigned GL\_DIFFUSE and GL\_SPECULAR OpenGL light properties shown in Figure 21. The GL\_POSITION of GL\_LIGHTO creates the sense of day and night on the planet's surfaces. The back faces of the planets are not illuminated, creating a shadow which defines the night.
- Ambient light is set as a global lighting property (Figure 21) calling OpenGL's function glLightModelfv() with property GL\_LIGHT\_MODEL\_AMBIENT.

The results from enabling GL\_LIGHTO with the light properties described above can be seen in the Figures from 17 to 19. Different online sources were visited to better understand lighting in OpenGL [7, 8, 9].

```
#define B0B6A216 C18B 40CC ABB7 B5BB23BDB9E6
#include "utils/Shapes.h"
static materialStruct brassMaterials = {
    ·{·0.33,·0.22,·0.03,·1.0},
·{·0.78,·0.57,·0.11,·1.0},
    { 0.99, 0.91, 0.81, 1.0},
    27.8
static materialStruct whiteShinyMaterials = {
    100.0
static materialStruct yellowPlastic = {
    {0.0f,0.0f,0.0f,1.0f},
    {0.5f,0.5f,0.0f,1.0f },
    {0.60f,0.60f,0.50f,1.0f},
    12.0f};
static materialStruct ruby = {
   { 0.1745f, 0.01175f, 0.01175f, 0.55f }, {0.61424f, 0.04136f, 0.04136f, 0.55f },
    {0.727811f, 0.626959f, 0.626959f, 0.55f},
    76.8f};
static materialStruct cyanPlastic = {
    {0.0f,0.1f,0.06f ,1.0f},
    {0.0f,0.50980392f,0.50980392f,1.0f},
    {0.50196078f,0.50196078f,0.50196078f,1.0f},
    32.0f};
static materialStruct polishedCopper = {
    {0.2295f, 0.08825f, 0.0275f, 1.0f},
    {0.5508f, 0.2118f, 0.066f, 1.0f},
    {0.580594f, 0.223257f, 0.0695701f, 1.0f},
    51.2f};
```

Figure 20: Definitions in utils/Materials.h

```
void SolarSystemWidget::createSolarSystem()
  glDisable(GL_TEXTURE_CUBE_MAP);
 if (rotate)
    glRotatef(2 * qRadiansToDegrees(angle), objSpaceRotAxis[0], objSpaceRotAxis[1], objSpaceRotAxis[2]);
 /// Zoom in and out of the scene
glScalef(1 - scrollDelta/160, 1 - scrollDelta/160, 1 - scrollDelta/160);
 GLfloat dif[] = {sunlightIntensity, sunlightIntensity, sunlightIntensity, 1.};
GLfloat spec[] = {0.8, 0.8, 0.8, 1.};
 // global ambient light values
float ambientLevel[] = { 0.15, 0.15, 0.15, 1. };
glLightModelfv( GL_LIGHT_MODEL_AMBIENT, ambientLevel );
 glEnable(GL_LIGHTING);
 glPushMatrix();
    glPushMatrix();
      GLfloat-centerLight[] = {0., 0., 0.};
glLightfv(GL_LIGHT0, GL_POSITION, centerLight);
glLightfv(GL_LIGHT0, GL_DIFFUSE, dif);
glLightfv(GL_LIGHT0, GL_SPECULAR, spec);
glEnable(GL_LIGHT0); //set lighting conditions for the scene
       drawPlanet(sun);
    glPopMatrix();
    glPushMatrix();
      drawPlanet(mercury);
    glPopMatrix();
    glPushMatrix();
      drawPlanet(venus);
    glPopMatrix();
    glPushMatrix();
      drawPlanet(earth);
    glPopMatrix();
    glPushMatrix();
      drawPlanet(mars);
    glPopMatrix();
    glPushMatrix();
- drawPlanet(jupyter);
    glPopMatrix();
    glPushMatrix();
      drawPlanet(saturn);
    glPopMatrix();
    glPushMatrix();
      drawPlanet(uranus);
    glPopMatrix();
    glPushMatrix();
      drawPlanet(neptune);
    glPopMatrix();
    glDisable(GL_TEXTURE_2D);
    glPushAttrib(GL_LIGHTING_BIT);
       glPushMatrix();
         glTranslatef(saturn->_pose[0], saturn->_pose[1], saturn->_pose[2]);
         glRotatef(-90, 1.0, 0.0, 0.0);
glRotatef(0.5*_time, 0.5f, 1.f, 0.5f);
         glScalef(0.35,0.35,0.1);
         gear(&polishedCopper, 60);
       glPopMatrix();
    glPopAttrib();
```

Figure 21: createSolarSystem() function declaration in SolarSystemWidget.cpp

# 3 Band 3 (50%-60%)

Band 3 requires to contain at least one element of user interaction.

# 3.1 User interaction

Name	Type	Values	Description
Reset Scene	QPushButton	None	Reset the scene to its ini-
			tial state
Activate standard basis	QPushButton	None	Activates standard basis
			(used for debugging)
Activate standard basis	QPushButton	None	Deactivate standard basis
			(used for debugging)
Sun light intensity	QSlider	range(-10,10)	Magnitude of diffuse from
			Sun (GL_LIGHTO)
Simulation speed	QSlider	range(0,100)	Accelerates the orbit speed
			of each of the planet
			around the Sun
Earth Mass	QSlider	range(10,30)	Earth Mass slider that af-
			fects simulation orbits
Mercury Mass	QSlider	range(10,30)	Mercury Mass slider that
			affects simulation orbits
Venus Mass	QSlider	range(10,30)	Venus Mass slider that af-
			fects simulation orbits
Mars Mass	QSlider	range(10,30)	Mars Mass slider that af-
			fects simulation orbits
Jupiter Mass	QSlider	range(10,30)	Jupiter Mass slider that af-
			fects simulation orbits
Saturn Mass	QSlider	range(10,30)	Saturn Mass slider that af-
			fects simulation orbits
Neptune Mass	QSlider	range(10,30)	Neptune Mass slider that
			affects simulation orbits
Spaceship orbiting planet	QComboBox	Planets in the system	Select planet for the space-
			ship to orbit
Spaceship right engine	QSlider	range(10,3600)	Rotates the position of the
			right engine
Spaceship left engine	QSlider	range(10,3600)	Rotates the position of the
			right engine
Spaceship speed	QSlider	range(10,100)	Accelerates the space-
			ship's orbit around Saturn
Scroll wheel zoom	QWheelEvent	None	Zooms in and out of the
			scene
Arcball camera (mouse drag)	QMouseEvent	None	Mouse interacts with
			the scene by pressing
			and releasing to update
			MODELVIEW matrix to a
			different perspective.

Table 2: Qt user interface, tabulated

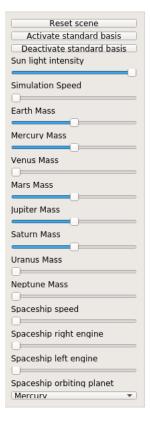


Figure 22: Qt user interface, actual

User interfaces provided through Qt (Table 2 and Figure 22) allow users interact with simulation through a different set of actions such as the light intensity of the Sun in the solar system, the mass of each of the planets conforming the solar system can be adjusted, the simulation speed for all the orbits of the planets, the spaceship speed orbiting around any planet, the planet that the spaceship orbits, right and left engines positions, and there also exists a "Reset scene" button to reset the values of the scene to default.

The second and third buttons are dedicated to activate and deactivate the standard coordinate axes. This was used during the development of the scene to debug position related issues.

Zoom in and out of the scene was implemented to allow the user to change perspective by re-scaling the scene, Figure 23. An "arcball camera" was implemented to translate and rotate around the center of the scene as shown in Figure 24, using QMouseEvent pressing and releasing events (Figure 25) to update the MODELVIEW matrix of the scene (updateModelViewMatrix() and calculateArcBallVector() in Figure 26). These two mouse interactive interfaces facilitate the user to have a better 3D experience in the simulation.

To better understand what the "arcball camera" is, there are helpful online sources [4, 5, 6] that I visited.

Signals from SceneWindow.cpp of each widget are connected to public slots functions in SolarSystemWidget.cpp to update the state of SolarySystemWidget QGLWidget object. The setup for a few signal instances and their connections is shown in Figures from 27 to 29.

```
760  void SolarSystemWidget::wheelEvent(QWheelEvent * event) {
761  | · · · · scrollDelta += · · event -> delta() · / · 120;
762  }
```

Figure 23: Declaration of wheelScrollEvent() in SolarSystemWidget.cpp

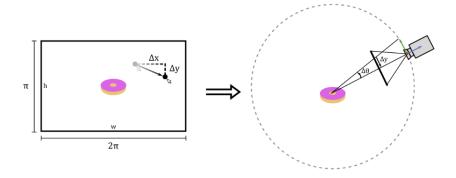


Figure 24: Visual representation of the implemented the "arcball" camera (Image from [6)]

Figure 25:  ${\tt QMouseEvent}$  events dragging mouse movement simulation

```
void SolarSystemWidget::mouseMoveEvent(QMouseEvent **event){
110
        if(event->buttons() && Qt::LeftButton)
111
112
113
114
           xEnd = event->x();
115
           yEnd = event->y();
           updateModelViewMatrix();
116
117
118
         xStart = event->x();
         yStart = event->y();
      void SolarSystemWidget::updateModelViewMatrix()
        QVector3D v = calculateArcBallVector(xStart, yStart); // from the mouse
        QVector3D u = calculateArcBallVector(xEnd, yEnd);
128
        angle = std::acos(std::min(1.0f, QVector3D::dotProduct(v, u))); // min to avoid acos to give us values > 1
        rotAxis = QVector3D::crossProduct(v,u); // axis that we will rotate about
133
134
        float current_matrix[16];
135
        glGetFloatv(GL_MODELVIEW_MATRIX, current_matrix); // get current MODELVIEW matrix
        mRotate = QMatrix4x4(current matrix);
        QMatrix4x4 eye20bjSpaceMat = mRotate;
139
        // Returns the result of transforming point according to matrix, with the matrix applied pre-point
        objSpaceRotAxis = eye20bjSpaceMat * rotAxis;
        xStart = xEnd:
144
        yStart = yEnd;
      QVector3D SolarSystemWidget::calculateArcBallVector(int x, int y)
148
149
        QVector3D pt_ndc = QVector3D(2.0 * x / mWidth - 1.0, 2.0 * y / mHeight - 1.0 , 0);
        pt ndc.setY(pt ndc.y() * -1);
        compute z-coordinates by executing pythagoras theorem with two conditions:
159
        float z = pt ndc.x() * pt ndc.x() + pt ndc.y() * pt ndc.y();
161
        if(z <= 1.0)
           pt_ndc.setZ(std::sqrt(1.0 -- z));
164
           pt ndc.normalize();
166
        return pt ndc;
```

Figure 26: "arcball" camera functions that update the modelview matrix with respect to mouse dragging interaction

```
void SceneWindow::createHorizontalGroupBox()
   horizontalGroupBox = new QGroupBox(tr(""),this);
   horizontalGroupBox->setMinimumSize(112, 612);
   horizontalGroupBox->setMaximumSize(212, 612);
   QVBoxLayout * *layout = new QVBoxLayout(this);
   buttonR = new QPushButton(tr("Reset scene"));
   layout->addWidget(buttonR);
   activateBasis = new QPushButton(tr("Activate standard basis"));
   layout->addWidget(activateBasis);
   deactivateBasis = new QPushButton(tr("Deactivate standard basis"));
   layout->addWidget(deactivateBasis);
   Sunlight = new QSlider(Qt::Horizontal);
   Sunlight->setMinimum(-10);
   Sunlight->setMaximum(10);
   Sunlight->setValue(10);
   OrbitSpeed = new QSlider(Qt::Horizontal);
   OrbitSpeed->setMinimum(0);
   OrbitSpeed->setMaximum(100);
   OrbitSpeed->setValue(0);
   EarthSlider = new QSlider(Qt::Horizontal);
   EarthSlider->setMinimum(10);
   EarthSlider->setMaximum(30);
   EarthSlider->setValue(20);
```

Figure 27: creation of a QGroupBox declaration in SceneWindow.cpp where some interactive widgets are instantiated

Figure 28: QComboBox instantiated and other interactive widgets added to instance of QGroupBox layout shown in Figure 27

```
pTimer = new QTimer;
               pTimer->start(10);
          connect(pTimer, SIGNAL(timeout()), solarSystemWidget, SLOT(updateAngle()));
           // orbit speed or simulation speed
          connect(OrbitSpeed, SIGNAL(valueChanged(int)), solarSystemWidget, SLOT(updateOrbitSpeed(int)));
          connect(Sunlight, SIGNAL(valueChanged(int)), solarSystemWidget, SLOT(updateSunLight(int)));
          connect(buttonR, SIGNAL(released()), solarSystemWidget, SLOT(resetOrbitValues()));
connect(buttonR, SIGNAL(released()), this, SLOT(resetAllSliders()));
           // standard basis activation for debuging purposes
          connect(activateBasis, SIGNAL(released()), solarSystemWidget, SLOT(activateStandardBasis()));
connect(deactivateBasis, SIGNAL(released()), solarSystemWidget, SLOT(deactivateStandardBasis()));
41
           // planets mass sliders
          connect(EarthSlider, SIGNAL(valueChanged(int)), solarSystemWidget, SLOT(updatePlanetEarthMass(int)));
          connect(mercurySlider, SIGNAL(valueChanged(int)), solarSystemWidget, SLOT(updatePlanetMercuryMass(int)));
          connect(venusSlider, SIGNAL(valueChanged(int)), solarSystemWidget, SLOT(updatePlanetVenusMass(int)));
connect(marsSlider, SIGNAL(valueChanged(int)), solarSystemWidget, SLOT(updatePlanetMarsMass(int)));
          connect(jupyterSlider, SIGNAL(valueChanged(int)), solarSystemWidget, SLOT(updatePlanetJupyterMass(int)));
          connect(saturnSlider, SIGNAL(valueChanged(int)), solarSystemWidget, SLOT(updatePlanetSaturnMass(int)));
          connect (uranus Slider, SIGNAL (value Changed (int)), solar System Widget, SLOT (update Planet Uranus Mass (int))); \\
          connect(neptuneSlider, SIGNAL(valueChanged(int)), solarSystemWidget, SLOT(updatePlanetNeptuneMass(int)));
          connect(spaceship, SIGNAL(valueChanged(int)), solarSystemWidget, SLOT(updateSpaceshipSpeed(int)));
          connect(right_engine, SIGNAL(valueChanged(int)), solarSystemWidget, SLOT(updateSpaceship_rightEngine(int)));
          connect(left engine, SIGNAL(valueChanged(int)), solarSystemWidget, SLOT(updateSpaceship leftEngine(int)));
           // spaceship planet to orbit
          connect(spaceship panetOrbit, SIGNAL(currentIndexChanged(int)), solarSystemWidget, SLOT(setPlanetIndex(int)));
```

Figure 29: Signal's connection to slots in SceneWindow.cpp

# 4 Band 2 (60%-70%)

Band 2 requires to have at least one element of animation, one convex object constructed from polygons and texture mapping.

#### 4.1 Animation

Animation is created through constant updates to the MODELVIEW matrices in the scene over time. The widget QTimer from SceneWindow QWidget updates the scene targeting 100 frames per second. On every second, the orbit of each of the planets, rings around Saturn and Neptune, orbit of spaceship and propulsion of spaceship animation are updated to simulate movement.

In this planetary simulation, two different movement animations were implemented and they are described below.

#### 4.1.1 Orbit

The orbit of each of the planets around the sun was achieved with the gravitational force function (2). The real gravitational constant,

$$G = 6.67408 \times 10^{-11} \tag{1}$$

was not used, and instead it was given a value of 1.0. The formula 2 considers the masses between two planetary bodies and their distance. For each planet in the solar system, including the sun, their gravitational forces are calculated to update their momentum and their position respectively in their rotation around the Sun. Implementation of equation 2 is shown in Figure 30.

Momentum defines the velocity per mass. If we increase the mass of a body and not the momentum, the heavier body will travel less distance because it has less velocity per mass. Momentum is defined for every planet to be

- momentum is static in the x direction,
- constant momentum in the y direction, and
- increasing momentum in the z direction.

The application of momentum to each planet is shown in updatePlanetOrbit() in Figure 31.

Notice that the sun has a mass of 1000.0 so that it remains in the center of the system, with constant momentum (0,0,0).

The spaceship can orbit any planet selected by the user, and its orbit is calculated by a call to glRotatef() in the x direction by spaceshipSpeed\*\_time (Figure 16, line 464) degrees.

$$\vec{F}_g = G \frac{m_1 m_2}{|\vec{r}|^2} \hat{r} \tag{2}$$

The use of these physics formulas was decided from online sources from where I obtained information regarding how they work and their use [12].

Figure 30: Declaration of gforce() function equivalent to equation 2 in SolarSystemWidget.cpp

```
oid SolarSystemWidget::updatePlanetOrbit(PlanetWidget* p1)
             float dt = speedInc; ....// simulation speed controller
             std::vector<PlanetWidget*> planets{sun, mercury, venus, earth, mars, jupyter, saturn, uranus, neptune}
                  if (p1 == p2){
                        planets.erase(planets.begin()+i);
            double** _gforce = new double* [(int)planets.size()];
  _gforce[0] = gforce(p1, planets.at(0));
  _gforce[1] = gforce(p1, planets.at(1));
  _gforce[2] = gforce(p1, planets.at(2));
  _aforce[3] = aforce(p1, planets.at(2));
560
561
562
563
564
             _gforce[3] = gforce(p1, planets.at(3));
             _gforce[4] = gforce(p1, planets.at(4));
              _gforce[5] = gforce(p1, planets.at(5));
              _gforce[6] = gforce(p1, planets.at(6));
              __gforce[7] = gforce(p1, planets.at(7));
569
570
571
             double* gforce_sum = addVectors(_gforce, sizeof(_gforce));
             p1->_forceVector[0] = gforce_sum[0];
             pl->_forceVector[1] = gforce_sum[1];
             pl->_forceVector[2] = gforce_sum[2];
             p1-> momentum[0] = p1-> momentum[0] + p1-> forceVector[0] * dt;
p1-> momentum[1] = p1-> momentum[1] + p1-> forceVector[1] * dt;
p1-> momentum[2] = p1-> momentum[2] + p1-> forceVector[2] * dt;
             p1-> pose[0] = p1-> pose[0] + p1-> momentum[0] / p1-> mass*dt;
             pl-> pose[1] = pl-> pose[1] + pl-> momentum[1] / pl-> mass*dt; pl-> pose[2] = pl-> pose[2] + pl-> momentum[2] / pl-> mass*dt;
```

Figure 31: Function that updates the orbit of each planet using gravitational force and momentum, declared in SolarSystemWidget.cpp

#### 4.1.2 Oscillation

Sine waves are used to animate the propulsion medium of the spaceship. By using the sine wave equation 3 below, the sine wave used is defined with a wave length value of 2 ( $\lambda=2$ ) and an amplitude of 0.5. Initially, one wave length is drawn between intervals -1 and 1. The intervals where the wave length is calculated are incremented by 0.1 every frame by the argument \_time\_sinewave passed to drawSpaceship() call in function drawPlanet(), line 468 in Figure 16. Therefore, applying an increasing translation (Figure 32, line 38) on every frame along the positive z axis, results in the animation of the sine wave oscillating. The implementation of the sine wave with the parameters explained above is shown in Figure 32, and it is drawn by OpenGL using GL\_POINTS with ruby material properties.

$$y = A * sin(k * x), k = 2\pi/\lambda \tag{3}$$

where A is the amplitude and k is the wave length.

Visual representations of the orbit and the oscillation animations can be seen from Figures 33 to 35. Although, it is suggested to see it by running the code or watching the videos ??.

```
glPushMatrix();
      glTranslatef(0.,0.,-1.);
        float wave length = 2;
        float amplitude = 0.5;
        float inc = 0.05;
        glPointSize(26);
        glTranslatef(0.,0, time sinewave);
        glBegin(GL POINTS);
             for(x=-1+_time_sinewave;x<=1+_time_sinewave;x+=inc)
              k = 2 \cdot * \cdot M PI \cdot / \cdot wave length;
              y = amplitude * sin(k * x);
              glVertex3f(0, y, -x);
              glVertex3f(0.2, y, -x);
              glVertex3f(-0.2, y, -x);
              glVertex3f(0, y+0.2, -x);
              glVertex3f(0.2, y+0.2, -x);
              glVertex3f(-0.2, y+0.2, -x);
        glEnd();
    glPopMatrix();
 glPopAttrib();
glPopMatrix();
```

Figure 32: Implementation of sine wave animation in the rear of the spaceship



Figure 33: Planets orbiting the Sun





Figure 34: sine wave function simulating movement attached to rocket

Figure 35: sine wave function simulating movement attached to rocket (different perspective)

### 4.2 Convex objects

The construction of the spaceship is made up of basic convex shapes, as well as the asteroid rings.

### 4.3 Texture mapping

As mentioned before, each planet in the scene has its own texture. Texture loading is done by loadTextures() function (Figure 37). The open source library used to read the textures is FreeImage [10]. The implementation of texture mapping is done by either calls to glBindTexture() or to glTexCoord3f() to store texture coordinates for the polygon being constructed. For example, instances of cube() (Figure 3) map the entire image (if texture is flagged) to the front face of the polygon with calls to glTexCoord3f() with texture values between 0 and 1.

Similarly to how the the textures of the planets are loaded by loadTextures(), the textures defining the cubemap are loaded in a similar way by loadCubemap() function in SolarSystemWidget. Although, in this case binding to GL\_TEXTURE\_CUBE\_MAP. To maintain the order in which the texture faces of the cube are loaded, OpenGL sets a texture target parameter to each texture of the cubemap at loading time. GL\_TEXTURE\_CUBE\_MAP\_POSITIVE\_X is the beginning of an OpenGL enum which is composed of:

Texture target	Orientation
GL_TEXTURE_CUBE_MAP_POSITIVE_X	Right
GL_TEXTURE_CUBE_MAP_NEGATIVE_X	Left
GL_TEXTURE_CUBE_MAP_POSITIVE_Y	Тор
GL_TEXTURE_CUBE_MAP_NEGATIVE_Y	Bottom
GL_TEXTURE_CUBE_MAP_POSITIVE_Z	Back
GL_TEXTURE_CUBE_MAP_NEGATIVE_Z	Front

Figure 36: Table describing 6 special texture targets for targeting a face of the cubemap. Table from [9]

Since we use an array to store the cubemap textures, we can loop through them linearly incrementing by 1 and calling glTexImage2D() with its correspondent texture target. Additionally, the textures names are defined in cubemapTextures[6] array (SolarSystemWidget.h) in the same order that OpenGL tags each face of the cube map.

The render function of the cubemap takes each loaded texture and maps it to the corresponding face of the cube, this is shown in Figure 15, where calls to glTexCoord3f() are performed to do the mapping.

The images markus.ppm, Marc\_Dekamps.ppm.ppm were used as passengers on board of the spaceship seen through the windows. The texture Mercatorprojection.ppm was applied to the Earth gluSphere() instance.

Before learning how to read textures with FreeImage, I went through some tutorials [7] where they give examples on how to load and apply textures in OpenGL.

```
void SolarSystemWidget::loadTextures()
        glGenTextures( nTex, texID ); ..// Get the texture object IDs.
        for (int i=0; i<nTex; i++)[]
iData[i] = 0;
            FREE_IMAGE_FORMAT format = FreeImage_GetFIFFromFilename(textures[i]);
            if (format == FIF_UNKNOWN) {
               printf("Unknown file type for texture image file %s\n", textures[i]);
            FIBITMAP* bitmap = FreeImage_Load(format, textures[i], 0);
            if (!bitmap) {
               ///printf("Cannot load file image %s\nSTB Reason: %s\n", textures[i], stbi_failure_reason());
printf("Cannot load file image %s. \n", textures[i]);
               printf("Textures %s successfully loaded. \n", textures[i]);
            FIBITMAP* bitmap2 = FreeImage ConvertTo24Bits(bitmap); // convert to RGB format
845
              bitmap2 = FreeImage Rotate(bitmap2, 180);
            FreeImage_Unload(bitmap);
            iData[i] = FreeImage GetBits(bitmap2);
            width[i] = FreeImage GetWidth(bitmap2);
            height[i] = FreeImage_GetHeight(bitmap2);
            if (iData[i]) {
                int format; // The format of the color data in memory, depends on platform.
                   format = GL BGR;
                glTexImage2D(GL_TEXTURE_2D, 0, GL_RGBA, width[i], height[i], 0, format,
               else {
                printf("Failed to get texture data from %s\n", textures[i]);
```

Figure 37: Function that reads and loads the textures to bind them by OpenGL

# 5 Band 1 (70%-100%)

Band 1 requires the scene to contain an object that requires hierarchical modelling and displays motion in some of its parts. User interaction with this model is available through the user interface.

### 5.1 Hierarchical modelling

The space ship required hierarchical modelling since it is made up of the main body (cylinder and cone) and two side rocket engines (Figures 9 and 10). The body and the engines can be drawn as children of the craft instance with their pose dependent on the parent.

Animation of the spaceship shows that it can orbit around any planet at the desired speed by the user, while each of its engines can be set to point to a different position without affecting the orbit of the planet as a result of hierarchical modelling. Figure 38 shows the structure, in particular, of the right engine which calls glRotatef() with the argument float deg set by the user through the Qt user interface (spaceship right engine QSlider in Figure 2). The hierarchical model of the spaceship is defined in Spaceship.cpp, due to its length only code block that defines the right engine is shown below.

```
void right_engine(float deg)
 glPushMatrix();
 glRotatef(deg, 1.0, 0, 0);
 glPushMatrix();
    // materials of gludisk right engine bottom
   materialStruct* rightEngine = &polishedCopper;
   glMaterialfv(GL_FRONT, GL_AMBIENT,
glMaterialfv(GL_FRONT, GL_DIFFUSE,
                                            rightEngine->ambient):
                                            rightEngine->diffuse);
   glMaterialfv(GL FRONT, GL SPECULAR,
                                            rightEngine->specular);
   glMaterialf(GL FRONT, GL SHININESS,
                                            rightEngine->shininess);
   glTranslatef(-1.8, 0., -0.6);
   GLUquadric * *qobjR = * gluNewQuadric();
   gluQuadricNormals(qobjR, GLU_SMOOTH);
   gluQuadricDrawStyle(qobjR, GLU FILL);
   gluDisk(qobjR, 0, 0.4, 200, 200);
   gluDeleteQuadric(qobjR);
 glPopMatrix();
 glPushMatrix();
   glPushAttrib(GL LIGHTING BIT);
     glTranslatef(-1.8, 0., -0.2);
     glScalef(0.4,0.4,0.4);
     cylinder(&brassMaterials);
     glTranslatef(0.,0.,1.0);
     openedCone(&cyanPlastic, 0.01);
   glPopAttrib();
 glPopMatrix();
 glPopMatrix();
```

Figure 38: Hierarchical implementation of the right engine of the spaceship in Spaceship.cpp

The implementations of renderCubemap() and createSolarSystem() might also make use or hierarchical modelling, where the former contains the solar system within a cube, and the latter creates a complex scene out of basic shapes.

# 5.2 User interaction

Users can interact with the spaceship hierarchical model by setting the spaceship right and left engine sliders to rotate in the x direction, and changing the planet of orbit in the drop down menu, outlined in 3. The animation of the propulsion engine in the rear on the craft is explained in 4.1.

# 6 Conclusion

All in all, I have been able to create my own solar system even though its parameters might not be well tuned for a good simulation. However, I believe that I have met the requirements of the project, which made me learn how to use the huge state machine that OpenGL is. It was interesting to simulate the targeted system using real world physics formulas, texturing polygons, creating new polygons for the scene, applying lighting properties and programming an immersive user interface.

### 6.1 Source code instructions

To run the application from source, enter the following commands from the project directory in a terminal:

```
cd src/include/
unzip FreeImage3180.zip
cd FreeImage
make -f Makefile.fip
cd ../../
qmake or qmake-qt5
make
./Scene
```

### 6.2 Video demonstrations

The testing of the scene through feng-linux/gpu result in low frame rate performance. Links to videos running the scene at higher frame rate here:

• https://www.youtube.com/watch?v=OrLoSbXruZY

# 7 References

- 1. This report was written using https://github.com/spookycouch/comp3811\_cg/blob/master/doc/report.pdf as a template for the sections to cover.
- 2. https://www.solarsystemscope.com/textures/
- 3. http://titan.csit.rmit.edu.au/~e20068/teaching/i3dg&a/2016/tute-2.html
- 4. https://en.wikibooks.org/wiki/OpenGL\_Programming/Modern\_OpenGL\_Tutorial\_Arcball
- 5. http://courses.cms.caltech.edu/cs171/assignments/hw3/hw3-notes/notes-hw3.html
- 6. https://asliceofrendering.com/camera/2019/11/30/ArcballCamera/
- 7. https://math.hws.edu/graphicsbook/
- 8. http://www.glprogramming.com/red/
- 9. https://learnopengl.com/
- 10. http://graphics.stanford.edu/courses/cs148-10-summer/docs/FreeImage3131.pdf
- 11. http://www.it.hiof.no/~borres/j3d/explain/light/p-materials.html
- 12. https://www.youtube.com/watch?v=4ycpvtIio-o