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Inferring Harmony from Free Polyphony

Computer Science Tripos – Part II

Clare College

July, 2023

Declaration of originality

I, Judah Daniels of Clare College, being a candidate for Part II of the Computer Science Tripos, hereby declare that this dissertation and the work described in it are my own work, unaided except as may be specified below, and that the dissertation does not contain material that has already been used to any substantial extent for a comparable purpose. I am content for my dissertation to be made available to the students and staff of the University.

Signed Judah Daniels

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Proforma

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Supervisor: Dr Peter Harrison

Original Aims of the Project

Work Completed

All that has been completed appears in this dissertation.

Special Difficulties

None

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Contents

1	Intr	oducti	ion	9
	1.1	Motiva	ation	. 9
	1.2	Relate	ed Work	. 10
2	Pre	paratio	on	11
	2.1	Backg	round Material	. 11
		2.1.1	Proto-voice Model	. 11
		2.1.2	Probabilistic Programming	. 12
		2.1.3	Probabilistic Model of Harmony	. 12
		2.1.4	Heuristic Search Algorithms	. 13
	2.2	Startin	ng Point	. 13
		2.2.1	Relevant courses and experience	. 13
		2.2.2	Existing codebase	. 14
	2.3	Requir	rements Analysis	. 14
	2.4	Softwa	are Engineering Techniques	. 14
		2.4.1	Development model	. 14
		2.4.2	Languages, libraries and tools	. 15
3	Imp	olemen	tation	17
	3.1	Repos	sitory Overview:	. 17
	3.2	Core I	Implementation	. 18
		3.2.1	Heuristic Parser	. 18
		3.2.2	Evaluation Module	. 24
	3.3	Baseli	ne implementation	. 24
		3.3.1	Random Sample Parser	. 24
		3.3.2	Random Choice Search	. 24
	3.4	Extens	sion Implementation	. 25
		3.4.1	Heuristic Design	. 25
		3.4.2	Heuristic Search	. 27
	3.5		g	
4	Eva	luation	n	29
	4.1	Accura	acy	. 29
	4.2		rmance	
	4.3	Heuris	stic Search (Extension)	. 30
	4.4		ss Criteria	

	4.5	Limitations	30
5	Con	aclusions	31
	5.1	Achievements	31
	5.2	Lessons learned	31
	5.3	Future Work	31
Bi	bliog	graphy	31
\mathbf{A}	Add	litional Information	37
В	Pro	ject Proposal	39
	B.1	Abstract	2
	B.2	Substance and Structure	2
		B.2.1 Core: Search	2
		B.2.2 Core: Evaluation	3
		B.2.3 Extension	3
		B.2.4 Overview	3
	B.3	Starting Point	4
	B.4	Success Criteria	4
	B.5	Timetable	6
	B.6	Resources	7
	B.7	Supervisor Information	7

List of Figures

3.1	Path initiliasation	19
3.2	Parse operations	19
3.3	Search state	20
3.4	Unfreeze operation	20
3.5	Enumeration of operations mid parse. Maybe for appendix? This could be	
	much more concise	21
3.6	State Transition diagram	22
3.7	Determine boolean boundary expressions for the freeze operations	23
3.8	Split operation	25

${\bf Acknowledgements}$

Chapter 1

Introduction

This dissertation explores efficient search strategies for parsing a symbolic music data using a musical grammar. We present ... which extends a recent model, addressing problems of intractability by using Heuristic search methods. We will see that that my novel heuristic search algorithm achieves

1.1 Motivation

A piece of music can be described using a sequence of chords, representing a higher level harmonic structure of a piece. There is a small, finite set of chord types, but each chord can be realised on the musical surface in a practically infinite number of ways. Given a score, we wish to infer the underlying chord types. This is often a time consuming and cognitively demanding expert task [21], hence its utility.

The paper Modeling and Inferring Proto-voice Structure in Free Polyphony describes a generative model that encodes the recursive and hierarchical dependencies between notes, giving rise to a grammar-like hierarchical system [7]. This proto-voice model can be used to reduce a piece into a hierarchical structure which encodes an understanding of the tonal/harmonic relations.

Finkensiep suggests in his thesis that the proto-voice model may be an effective way to infer higher level latent entities, such as harmonies or voice leading schemata. Thus in this project I will ask the question: is this parsing model an effective way to annotate harmonies? By 'effective' we are referring to two things:

- Accuracy: can the model successfully emulate how experts annotate harmonic progressions in musical passages?
- Practicality: can the model be used to do this within a reasonable time frame?

While the original model could in theory be used to generate harmonic annotations, its exhaustive search strategy would be prohibitively time-consuming in practice for any but the shortest musical extracts; one half measure can have over 100,000 valid derivations [6]. My approach will be to explore the use of heuristic search algorithms to solve this problem.

1.2 Related Work

First grammar/rule-based systems [23] [37], optimisation algorithms [27] and supervised learning approaches making use of large datasets [26] [24] [21].

Distinction to be drawn between approaches that take segmented or non-segmented pieces. Some models make use of a joint segmentation and labelling approach [21]...

More general heuristic search techniques for huge search spaces.

Chapter 2

Preparation

In this chapter, I present the work which was undertaken before the code was written. After a brief description of my starting point, I provide an exposition of the Proto-voice Model which forms the foundation of this project. Subsequently, I discuss probabilistic programming and Bayesian inference, including a probabilistic model of harmony. Finally, I describe the software engineering techniques and principles used throughout the project.

2.1 Background Material

2.1.1 Proto-voice Model

TODO: Brief description of what notes are, what is a piece of music, introduce relevant musical terminology (Score, note, protovoice, repetition, neighbor/ornament(choose one?)). Conflict of meaning with root-note (generative operation) and root note (musical terminology). What are the main assumptions/information we need to know in order to understand the proto-voice model?

TODO: Motivation of the model as a generative model on the note level, describing the piece as a DAG (Directed Acyclic Graph). What is a proto-voice exactly?

The proto-voice model is characterised by 3 primitive generative operations on notes.

- Repetitions
- Neighbor notes
- Passing notes

Operations with two notes are represented by edge replacement.

$$p_1 \to p_2 \implies p_1 \to c \to p_2$$

Proto-voice Operations

To model simulataneity of notes we introduce slices, which are multisets of pitches, representing segments of a piece where a group of notes are heard.

Diagram showing a slice + a diagram showing a higher level slices, grouping an arpegiation.

A slice m is defined as a multiset of pitches.

A transition $t = (s_l, e, s_r)$ relates two slices with a configuration of edges $e = (e_{reg}, e_{pass})$, a set of regular edges (repetition or neighbor), and a set of passing edges.

Outer operations (Diagram of all three operations):

Split:

$$t \to t_l' s' t_r'$$

Spread:

$$t_l \ s \ t_r \rightarrow t_l' \ s_l' \ t_m' \ s_r' \ t_r'$$

Freeze:

$$t \to t$$

Proto-voice harmony

How do we get from a proto-voice (partial)derivation to a harmonic inference?

Explain what harmony is, and how the proto-voice model allows us to capture harmony. Elaboration of the introduction.

What assumptions are needed for a protovoice derivation to be able to describe harmonic entities? These shape heuristic design.

2.1.2 Probabilistic Programming

Provide an explanation of all the concepts I learned and used in this project. Techniques such as marginalisation, joint distributions, bayes rule etc. Probabilistic programming is the combination model definitions and statistical inference algorithms for computing the conditional distribution of inputs (chords) that could have given rise to the observed output (score). We are making the assumption that the score is a realisation of the latent harmonic entities.

Dirchelet distributions Beta distribution Multinomiall distribution Normal Distribution

Inference as model \rightarrow data \rightarrow prob distribution \rightarrow chord guess

2.1.3 Probabilistic Model of Harmony

Outline of the probabilistic model of harmony, describing the parts that are relevant for harmonic annotations. This section allows the reader to understand the evaluation and heuristic modules.

Describe how the parameters were attained

Then describe how to go from the parameters to chord, chordtone and ornamentation distributions

Parameters:

pHarmonies: \mathbb{N}^{n_c}

pChordtones: \mathbb{N}^{n_c}

pOrnaments: \mathbb{N}^{n_c}

Chordtypes, $C = \{M, m, Mm7, om, o7, mm7, \%7, MM7, +, Ger, It, Fr, mM7, +7\}$

 $\vec{\chi}' \sim \text{Dirchlet(pHarmonies}, n_c)$

$$\vec{\chi} = \mathbb{E}(\vec{X}_i) = \frac{\alpha_i}{\sum_j \alpha_j}$$

Chord:

$$c \sim \text{Categorical}(\vec{\chi})$$

Single chordtone distribution. We want to find P(p|c,ct) probability of the pitch given the chord, and that the note is a chordtone:

$$\vec{\phi}'_{ct} \sim \text{Dirchlet}(pChordtones, n_p) \implies \vec{\phi}$$

For each of these parameters we use the MLE to get our probability distribution.

$$\vec{\phi}_{ct} = \text{MLE}(\vec{\phi}'_{ct})$$

$$\vec{\phi}_{or} = \text{MLE}(\vec{\phi}'_{or})$$

$$\vec{\chi} = \text{MLE}(\vec{\chi}')$$

Then for each chord tone,

$$p_{ct} \sim \text{Categorical}(\vec{\phi}_{ct})$$

$$p_{or} \sim \text{Categorical}(\vec{\phi}_{or})$$

We get the distribution of likelihoods for each pitch.

2.1.4 Heuristic Search Algorithms

Provide an outline of the heuristic search paradigm with a formalisation.

Provide a brief overview of different techniques that are used to prune the search space that might be relevant.

2.2 Starting Point

2.2.1 Relevant courses and experience

Haskell I was introduced to Haskell during an internship during the summer before starting this project (July to August 2022). This project is an excuse to learn the language.

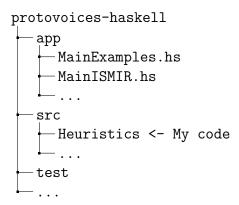
Python I have experience coding in Python.

IB Formal Models of Language, Artificial Intelligence.

2.2.2 Existing codebase

NOTE: I need to restructure the codebase to reflect the different modules more clearly. This will help with the flow to the dissertation.

The following describes the protovoices-haskell repository, and where my code contribution will lie:



2.3 Requirements Analysis

Table of main components with a dependency and risk analysis

Table 2.1: Overview of main deliverables along with a risk analysis

ID	Delieverable	Priority	Risk
core1	Evaluation Module	High	Low
core2	End to End Pipeline	High	Medium
core3	Parser	High	Medium
base1	Random Choice search	High	Low
base2	Random Sample	High	Low
ext1	Heuristic Search 1	Medium	High
ext2	Heuristic Search 2	Medium	High

Short description of where the risk lies.

Pertt chart showing the dependencies between different modules

2.4 Software Engineering Techniques

Justified and documented selection of suitable tools; good engineering approach.

2.4.1 Development model

Usig the dependency and risk analysis above, I created this gantt chart, and totally stuck to it(100% didn't wait until now to get the end-to-end pipeline fully running, and spend most of the time in an extension rabbit hole.. We live and we learn).

Include Gantt chart.

Table 2.2: Languages, libraries and tools

Tool	Purpose	License
Haskell	Main language	
GHC	Compiling and profiling to inspect time performance and memory usage	GPL-3.0+
Haskell-Musicology		•••
Dimcat		
Python		
Numpy		
Pandas		
MS3		
Musescore 3		
Protovoice Annotation Tool		
Git	Version Control, Continuous Integration	

2.4.2 Languages, libraries and tools

The chapter will also cite any new programming languages and systems which had to be learnt

Chapter 3

Implementation

3.1 Repository Overview:

Table 3.1: Repository Overview

File/Folder	Description	LOC
protovoices-haskell/	Root directory	2272
	s, HeuristicSearch.hs Core Implementation (Section x)	470
RandomChoiceSearch	n.hs, RandomSampleParser.hs Baseline Implementation (Section x)	121
Heuristics.hs, PBF	HModel.hs Extension Implementation (Section x)	383
FileHandling.hs	Utilities	188
app/ MainFullParse.hs	Entry Point	431
harmonic-inference		
experiments/ preprocess.ipynb dcml_params.json inputs/		115
test/	Unit Tests (Section x)	611

The following describes an overview of the project repository:

3.2 Core Implementation

3.2.1 Heuristic Parser

This is not a descriptive name. Think of a new name to describe the implementation of the search space of partial reductions. We use the outer representation of structure and outer operations. This is an abstraction.

Parsing Operations

Piece represented by an alternating list of slices and transitions, this is called a path. Define path formally. inductive definitions. dont need the Nothing: just Path trans slice. Transition can be frozen or unfrozen, and boundary or non boundary. Boundary is represented by vertical line, frozen is represented by two lines.

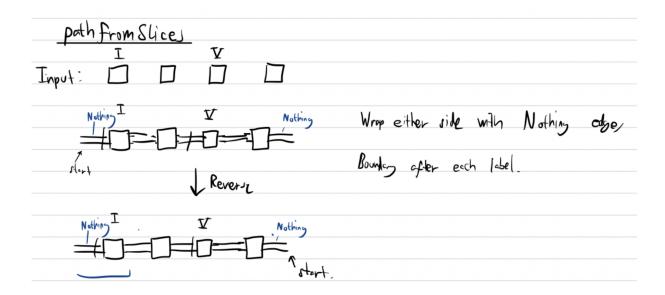


Figure 3.1: Path initiliasation

Definition 3.2.1 (Path). A path is an alternating sequence of an two types of elements, in our case transitions and slices. Definition: Haskell code block or mathematical definition?

Our goal is to reduce the piece into a partial redution by appluying operations until we have one slice per segment. Diagram of this state. This means we have one group of notes per segment, and this group of notes should represent the harmony of the segment.

We parse by applying the inverse of the generative operations, right to left. Unsplit, Unspread, Unfreeze.

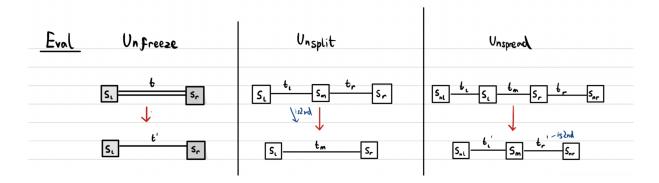


Figure 3.2: Parse operations

State Space

This is how we define the search. We start at the right, the end of the piece. We have a pointer to the current node, and all preceding slices are open and subsequent slices are frozen. Open Slices can be reduced, but only to the point that there is one slice in a segment. We keep track of the operations performed as it (1). allows us to the draw out the derivation for the partial reduction at the end, and (2). it is used later for calculate a cost for each operation for the heuristic search.

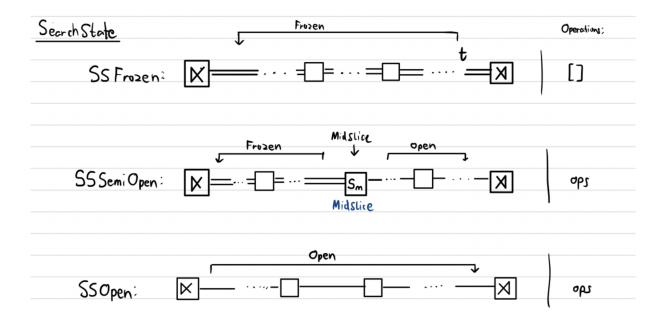


Figure 3.3: Search state

Enumerating State transitions

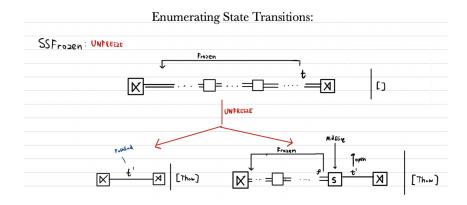


Figure 3.4: Unfreeze operation

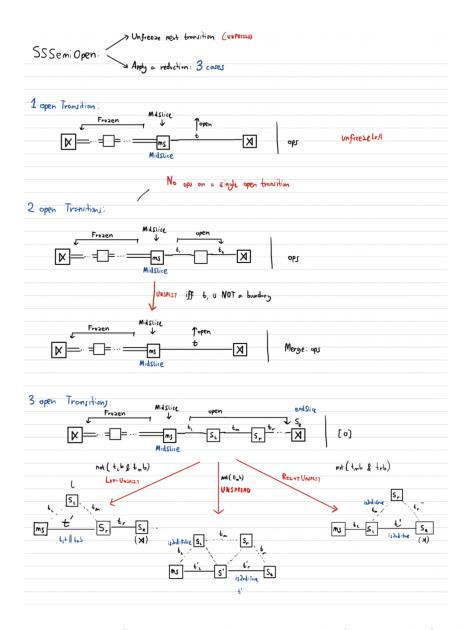


Figure 3.5: Enumeration of operations mid parse. Maybe for appendix? This could be much more concise.

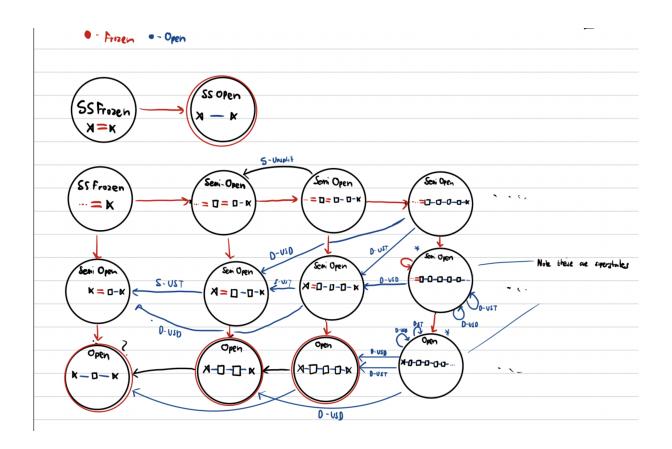


Figure 3.6: State Transition diagram

In the state transition diagram (Figure 3.6), we see all the possible parse states (Is this actually useful? Maybe for appendix). This was useful for me as it helps to conceptualise how the full parse actually works. The dimensions of this digramm of the search state depends on the length of the piece, and the size of each segment. We can see that there is a process of moving to the right to unfreeze transitions, and moving towards the left during reduction operations. Perhaps some simplification of the diagram would be useful. This transition diagram does not consider segment boundaries.

sdfsdfs sdf

Boundary handling

It is important that we don't reduce to an empty segment, because that would mean we've lost all information about the segment, and would not be able to make a harmonic inference. In order to prohibit this, we add additional constraints to the parse operations for each operation based on the boolean boundary value of all involved transitions.

We use karnaugh maps to determine the boolean expression for these constraints.

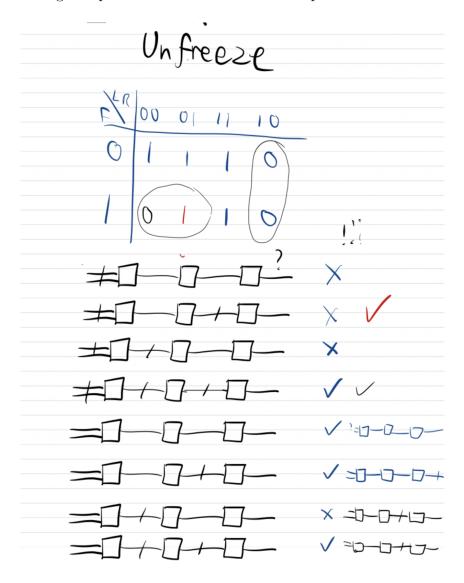


Figure 3.7: Determine boolean boundary expressions for the freeze operations

Could show other maps in the appendix.

3.2.2 Evaluation Module

We need to know exactly what we are trying to achieve before we can understand the baseline and extention implementations.

Probabilistic Model of Harmony

When evaluating using the protovoice model: we assume that we result in only chord tones for each segment. Thus we can use the chord tone probabilities to evaluate the prediction.

When just using a random sample, we have to assume that there is a mixture model of chord tones and ornaments. We can use the learnt parameters to determine the distribution.

These two measures of likelihoods are comparable as they are drawn from the same distributions.

We also need to infer chord labels. We can simply choose the chord that is most likely according to our model.

This gives us two key metrics, likelihood and accuracy.

Could also use a more sophisticated notion of accuracy, using a chord similarity function [13]. The mir_eval package provides a plethora of metrics to compare chord label predictions [30].

3.3 Baseline implementation

3.3.1 Random Sample Parser

As a crude baseline we develop two algorithms based on randomly sampling notes for each segment to infer the chord label.

The pure random sample algorithm simply samples random notes for each segment, and uses those to guess the chord label. This doesn't even consider the notes of the piece, so it's really bad, but provides a useful reference.

The per segment sample algorithm samples notes from each segment. Could just sample a random number of notes from each segment, or just use all the notes in the segment to predict the most likely chord label. This is reminiscent of using a key-profile model [34] to find local keys.

3.3.2 Random Choice Search

Now we use our implementation of the protovoice parser, but just do a random walk in the tree of partial reductions. By comparing this against the random ample parser, we can get an idea of the utility of the model. We show that this works surprisingly well.

3.4 Extension Implementation

3.4.1 Heuristic Design

First the full piece heuristic parse

Problem of very large slices.

Segment by segment heuristic parse - avoids the problem, but is slightly hacky. Can we incorprate our knowledge regarding the relative proportion of chord tones and ornaments. Should we allow duplicates of notes in slices? Perhaps we should favour spreads more.

Always consider a certain number of slices and spreads.

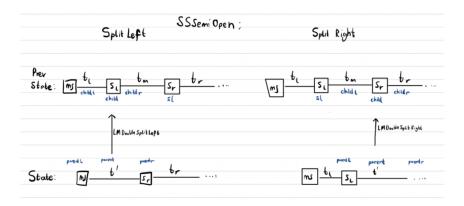


Figure 3.8: Split operation

Scoring Unsplit Operations

Consider the Split rule:

$$t \to t'_l \ s' \ t'_r$$

During a split, each edge in the transition and each node in an adjacent slice can be elaborated by one or more inner operations. These new edges can be discarded or kept to form the new edge of t'_l and t'_r .

The notes in the child slice s can either have edges connected to the left neighboring slice or right neighbouring slice, or both. I.e for each note in the child slice, it can be a an ornmentation of a previous note, subsequent note, both, or repetition of prev note, subsequent note etc. So we consider the chord tone profiles of the involved slices.

We first guess the chord type each parent slice.

$$\theta_l = \underset{c \in C}{argmax} P(s_l|c) , \quad \theta_r = \underset{c \in C}{argmax} P(s_r|c)'$$

We now consider each edge individually, considering their likelihoods based on the proabilistic model of harmony along with theoretical assumptions.

Single Sided Operations

• Right Neighbour (Left Neighbour anagolously)

$$x \implies x \to n , x, n \in P$$

$$x \sim \text{Categorical}(\sigma_{ct}^{\theta_l})$$

$$n \sim \text{Categorical}(\sigma_{or}^{\theta_r})$$

Find

$$P(x, n \mid \theta_l)$$

• Right Repeat (Left Repeat anagolously)

$$x \implies x \to x , x \in P$$

$$x \sim \text{Categorical}(\sigma_{ct}^{\theta_l})$$

Find

$$P(x \mid \theta_l)$$

Two Sided Operations

- Root Note: This operation is only done once in the original model. In our case we do not need to consider due to segment boundaries.
- Full Repeat:

$$x \implies x \to n , x, n \in P$$

$$x \sim \text{Categorical}(\sigma_{ct}^{\theta_l})$$

$$n \sim \text{Categorical}(\sigma_{or}^{\theta_r})$$

Find

$$P(x, n \mid \theta_l)$$

• Left Repeat of Right:

$$x \to y \implies x \to y' \to y$$

 $y \sim \text{Categorical}(\sigma_{ct}^{\theta_l})$

Find

$$P(y \mid \theta_l)$$

• Full Neighbour:

$$x_1 \to x_2 \implies x_1 \to n \to x_2, x \in P$$

Find

$$P(\mid \theta_l, \theta_r)$$

3.5. TESTING 27

Scoring Unspread Operations

Consider the Spread rule:

$$t_l s_r \to t_l' s_l t_m' s_r t_r'$$

We make the assumption that s, s_l , & s_r are all realisations of the same chord. This lines up with the music theoretical basis for this operation in the model(justify).

Thus we find the most likely chord (optional extension: marginalise over all chords)

$$\theta = \operatorname*{argmax}_{c \in C} P(s|c)$$

When then measure the extent to which the parent slics match this chord.

$$p(s_l, s_r | \theta)$$

We can calculate $p(s_l|\theta)$ and $p(s_r|\theta)$ using the multinomial distribution probability density function as described in the preparation chapter.

Scoring Unfreeze Operations

We assign 0 cost to unfreeze operations. This means we need to be careful about ensure that we don't just unfreeze the entire piece immediately. Careful construction of the search algorithm can ensure this. More later.

Full state evalutation

We need to combine all of these in a fair way. Also the distinction between splits and spreads need to be considered, as they are different operations, the calculations of likelihood may cause an imbalance.

3.4.2 Heuristic Search

Step 2: Relax the heuristic search in order to reduce runtime/lower complexity.

In the case that there are 85,000,000 options, perhaps we should sample the options rather than evaluating all of them.

This version of heuristic search should be able to parse full pieces (hopefully), so can be used to compare with the baselines on an entire corpus.

3.5 Testing

Show unit tests, and examples of the test/development cycle for the heuristic search development

Chapter 4

Evaluation

In this chapter, I provide qualitative and quantitative evaluations of the work completed. I then provide and interpret evidence to show that the success criteria were met.

The main questions to answer are as follows:

- Can the proto-voice model be used to accurately infer chord labels?
- Can the proto-voice model be used to practically infer chord labels?
- How well my heuristic search algorithms infer chord labels?

4.1 Accuracy

Things to note

- The fact that segmentation is known ahead of time provides a great deal of information [10]
- So we can use comparisons between the random sample from each segment algorithm and the random parse algorithm to see if the use of the grammar provides an advantage over just sampling the notes directly, without looking at relations between notes.
- Then we want a heuristic search algorithm that considers each option exhaustively and finds the best local option. This is too computationally expensive to be used for whole pieces.
- Given there can be millions of possible next states in the search, we need to look at different strategies to avoid searching through them all. E.g just sample states.
- Sensitivity Analysis for the heuristic search is useful for the evaluation. Explore how robust it is to handcrafted attacks/ different types of passages.
- Could evaluate by segments instead of pieces.

- 4.2 Performance
- 4.3 Heuristic Search (Extension)
- 4.4 Success Criteria
- 4.5 Limitations

Chapter 5

Conclusions

In this chapter, I first discuss the success achieved by the project then offer a reflection on lessons learned. Finally, I consider the directions in which there is potential for future work.

- 5.1 Achievements
- 5.2 Lessons learned
- 5.3 Future Work

[?]

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36 BIBLIOGRAPHY

Appendix A Additional Information

Appendix B
 Project Proposal

Inferring Harmony from Free Polyphony

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March 28, 2023

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B.1 Abstract

A piece of music can be described using a sequence of chords, representing a higher level harmonic structure of a piece. There is a small, finite set of chord types, but each chord can be realised on the musical surface in a practically infinite number of ways. Given a score, we wish to infer the underlying chord types.

The paper Modeling and Inferring Proto-voice Structure in Free Polyphony describes a generative model that encodes the recursive and hierarchical dependencies between notes, giving rise to a grammar-like hierarchical system [?]. This proto-voice model can be used to reduce a piece into a hierarchical structure which encodes an understanding of the tonal/harmonic relations of a piece.

Christoph Finkensiep suggests in his paper that the proto-voice model may be an effective way to infer higher level latent entities, such as harmonies or voice leading schemata. Thus in this project I will ask the question: is this parsing model an effective way to annotate harmonies? By 'effective' we are referring to two things:

- Accuracy: can the model successfully emulate how experts annotate harmonic progressions in musical passages?
- Practicality: can the model be used to do this within a reasonable time frame?

While the original model could in theory be used to generate harmonic annotations, its exhaustive search strategy would be prohibitively time-consuming in practice for any but the shortest musical extracts; one half measure can have over 100,000 valid derivations [?]. My approach will be to explore the use of heuristic search algorithms to solve this problem.

B.2 Substance and Structure

B.2.1 Core: Search

The core of this project is essentially a search problem characterised as follows:

- The state space S is the set of all possible partial reductions of a piece along with each reduction step that has been done so far.
- We have an initial state $s_o \in S$, which is the empty reduction, corresponding to the unreduced surface of the piece. The score is represented as a sequence of slices grouping notes that sound simultaneously. We are also given the segmentation of the original chord labels that we wish to retrieve.
- We have a set of actions, A modelled by a function $action: A \times S \to S$. These actions correspond to a single reduction step.
 - The reduction steps are the inverses of the operations defined by the generative proto-voice model.
- Finally we have a goal test, $goal: S \to \{true, false\}$ which is true iff the partial reduction s has exactly one slice per segment of the input.

- This means the partial reduction s contains a sequence of slices which start and end positions corresponding to the segmentation of the piece.
- At the first stage, this will be implemented using a random graph search algorithm, picking each action randomly, according to precomputed distributions.

B.2.2 Core: Evaluation

The second core task is to create an evaluation module that iterates over the test dataset, and evaluates the partial reduction computed by the search algorithm above. This will be done by comparing the outputs to ground truth annotations from the Annotated Beethoven Corpus.

In order to do this I will make use of the statistical harmony model from Finkensiep's thesis, *The Structure of Free Polyphony* [?]. This model provides a way of mapping between the slices that the algorithm generates and the chords in the ground truth. This can be used to empirically measure how closely the slices match the expert annotations.

B.2.3 Extension

Once the base search implementation and evaluation module have been completed, the search problem will be tackled by heuristic search methods, with different heuristics to be trialled and evaluated against each other. The heuristics will make use of the chord profiles from Finkensiep's statistical harmony model discussed above. These profiles relate note choices to the underlying harmony. Hence the heuristics may include:

- How the chord types relate to the pitches used.
- How the chord types relate which notes are used as ornamentation, and the degree of ornamentation.
- Contextual information about neighboring slices

B.2.4 Overview

The main work packages are as follows:

Preliminary Reading – Familiarise myself with the proto-voice model, and read up on similar models and their implementations. Study heuristic search algorithms.

Dataset Preparation – Pre-process the Annotated Beethoven Corpus into a suitable representation for my algorithm.

Basic Search – Implement a basic random search algorithm that takes in surface and segmentations, and outputting the sequence of slices matching the segmentations.

Evaluation Module – Implement an evaluation module to evaluate the output from the search algorithm.

End-to-end pipeline – Implement a full pipeline from the data to the evaluation that can be used to compare different reductions.

Heuristic Design – Extension – Trial different heuristics and evaluate their performance against each other.

Dissertation – I intend to work on the dissertation throughout the duration of the project. I will then focus on completing and polishing the project upon completion.

B.3 Starting Point

The following describes existing code and languages that will be used for this project:

Haskell – I will be using Haskell for this project as it is used in the proto-voice implementation. It must be noted that my experience with Haskell is limited, as I was first introduced to it via an internship this summer (July to August 2022).

Python – Python will be used for data handling. I have experience coding in Python.

Prior Research - Over the summer I have been reading the literature on computational models of music, as well as various parsing algorithms such as semi-ring parsing [?], and the CYK algorithm, which is used in the implementation of the proto-voice model.

Protovoices-Haskell – The paper *Modeling and Inferring Proto-Voice Structure in Free Polyphony* [?] includes an implementation of the proto-voice model in Haskell. A fork of this repository will form the basis of my project. This repository includes as parsing module which will be used to perform the actions in the search space of partial reductions. There is module that can exhaustively enumerate reductions of a piece, but this is infeasible in practice due to the blowup of the derivation forest.

MS3 – This is a library for parsing MuseScore Files and manipulating labels [?], which I will use as part of the data processing pipeline.

ABC – The *Annotated Beethoven Corpus* [?] contains analyses of all Beethoven string quartets composed between 1800 and 1826), encoded in a human and machine readable format. This will be used as a dataset for this project.

B.4 Success Criteria

This project will be deemed a success if I complete the following tasks:

- Develop a baseline search algorithm that uses the proto-voice model to output a partial reduction of a piece of music up to the chord labels.
- Create an evaluation module that can take the output of the search algorithm and quantitatively evaluate its accuracy against the ground truth annotations by providing a score based on a statistical harmony model.
- Extension: Develop one or more search algorithms that use additional heuristics to inform the search, and compare the accuracy with the baseline algorithm.

B.5 Timetable

Time frame	Work	Evidence
Michaelmas (Oct 4 to Dec 2)		
Oct 14 to Oct 24	Oct 14: Final proposal deadline. Preparation work: familiarise myself with the dataset and the protovoice model implementation. Work on manipulating reductions using the proto-voice parser provided by the paper.	None
Oct 24 to Nov 7	Dataset preparation and handling.	Plot useful metrics about the dataset us- ing Haskell
Nov 7 to Nov 21	Random Search implementation	None
Nov 21 to Dec 5	Evaluation Module. Continue with search implementation.	Evaluate a manually created derivation and plot results
Vacation (Dec 3 to Jan 16)		
Dec 5 to Dec 11	Evaluate performance of random search. Begin to work on extensions	Plot results
Dec 10 to Dec 21	Trial different heuristics. Implement an end-to-end pipeline from input to evaluation.	None
Dec 21 to Dec 27	None	None
Dec 27 to Jan 10	Continue trialing and evaluating heuristics	Fulfill success criterion: At least one heuristic technique gives better performance than random search.
Lent (Jan 17 to Mar 17)		
Jan 4 to Jan 20	Buffer Period to help keep on track	None
Jan 20 to Feb 3	Feb 3: Progress Report Deadline. Write progress report and prepare presentation. Write draft Evalua- tion chapter	Progress Report (approx. 1 page)
Feb 3 to Feb 17	Prepare presentation.	Feb 8 – 15: Progress Report presentation
Feb 17 to Mar 3	Feb 17: How to write a Dissertation briefing. Write draft Introduction and Preparation chapters. Incorporate feedback on Evaluation chap-	Send draft Introduc- tion and Preparation chapter to supervisor

B.6. RESOURCES 7

B.6 Resources

I plan to use my own laptop for development: MacBook Pro 16-inch, M1 Max, 32GB Ram, 1TB SSD, 24-core GPU.

All code will be stored on a GitHub repository, which will guarantee protection from data loss. I will easily be able to switch to using university provided computers upon hardware/software failure.

The project will be built upon work that has been done in the DCML (Digital cognitive musicology lab) based in EPFL. The files are in their Github repository, and I have been granted permission to access their in-house datasets of score annotations, as well as software packages which are used to handle the data.

B.7 Supervisor Information

Peter Harrison, head of Centre for Music and Science at Cambridge, has agreed to supervise me for this. We have agreed on a timetable for supervisions for this year. I am also working with Christoph Finkensiep, a PHD student at the DCML, and originator of the proto-voice model. Professor Larry Paulson has agreed to be the representative university teaching officer.