Syntactic Parsing

dynamic programming

Syntactic parsing

The task of recognizing a sentence and assigning a syntactic structure to it.

Parse trees are useful in:

- grammar checking
- semantic analysis
- question answering

What books were written by British women authors before 1800?

- need to know the subject is what books
- by-adjunct: British women authors

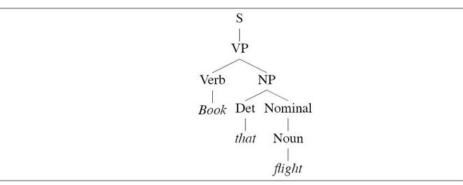
Parsing as Search

Finite-state automata: Recognition algorithms were formalized as search algorithms

- depth-first search
- breadth-first search

In syntactic parsing, we're searching through the space of possible parses and

finding a parse, or all parses.

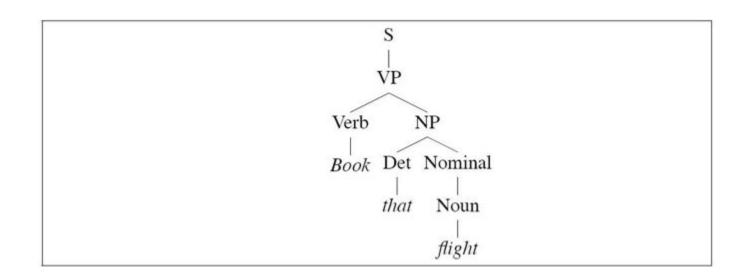


L₁ miniature grammar

Grammar	Lexicon	
$S \rightarrow NP VP$	$Det \rightarrow that \mid this \mid a$	
$S \rightarrow Aux NP VP$	$Noun \rightarrow book \mid flight \mid meal \mid money$	
$S \rightarrow VP$	$Verb \rightarrow book \mid include \mid prefer$	
$NP \rightarrow Pronoun$	$Pronoun \rightarrow I \mid she \mid me$	
NP → Proper-Noun	Proper-Noun → Houston NWA	
$NP \rightarrow Det\ Nominal$	$Aux \rightarrow does$	
Nominal → Noun	$Preposition \rightarrow from \mid to \mid on \mid near \mid through$	
Nominal → Nominal Noun		
$Nominal \rightarrow Nominal PP$		
$VP \rightarrow Verb$		
$VP \rightarrow Verb NP$		
$VP \rightarrow Verb NP PP$		
$VP \rightarrow Verb PP$		
$VP \rightarrow VP PP$		
PP → Preposition NP		

L₁ miniature grammar

Given this grammar, the correct parse for the sentence is



Parsing as Search

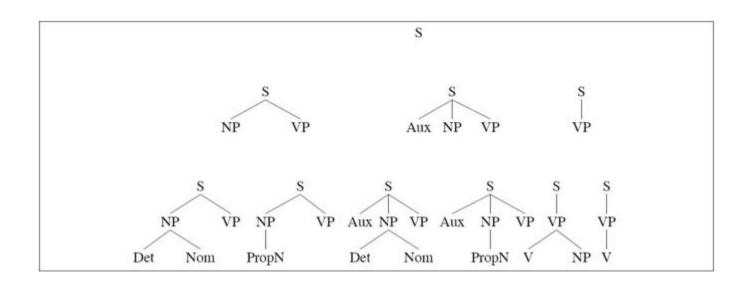
Our goal: Given the grammar, find all the trees whose root is the start symbol S and that cover exactly the words in the input.

Two kinds of constraints:

- Top-down:
 - All parses must begin with S (goal-directed search)
- Bottom-up:
 - All parses must yield the words Book that flight (data-directed search)

Top-down parsing

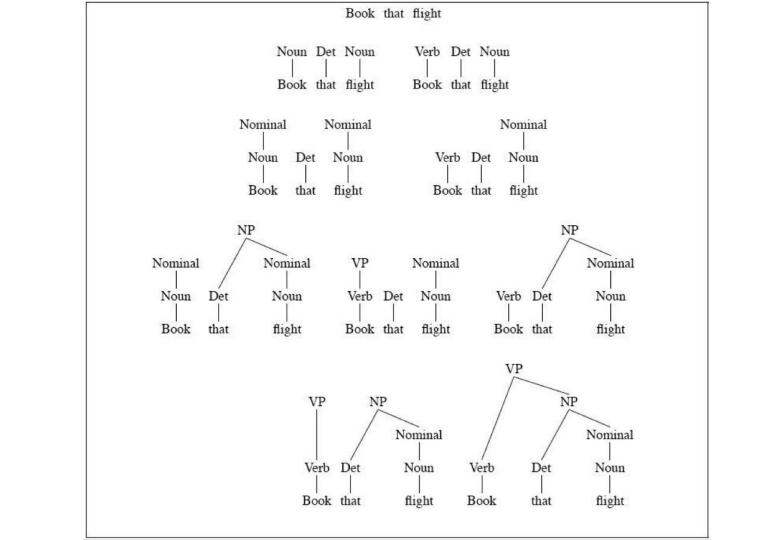
Search for a parse tree by trying to build from the root node S down to the leaves.



Bottom-up parsing

The earliest known parsing algorithm and is used in **shift-reduce parsers** common for programming languages. (Yngve 1955)

- Start with the POS and try to apply rules bottom-up until you reach an S.
- Any false starts that cannot be continued up are terminated.



Top-down vs. Bottom-up parsing

Top-down strategy:

- Never wastes time exploring trees that cannot result in an S.
- Never explores subtrees that cannot find a place in some S-rooted tree.

Bottom-up strategy:

Wildly generates trees that may have no hope of fitting in an S-rooted tree.

Top-down vs. Bottom-up parsing

Top-down strategy:

- Spends considerable time on S-trees that are inconsistent with the input.
- Generates trees before even examining the input.

Bottom-up strategy:

Never suggests trees that are not at least locally grounded in the input.

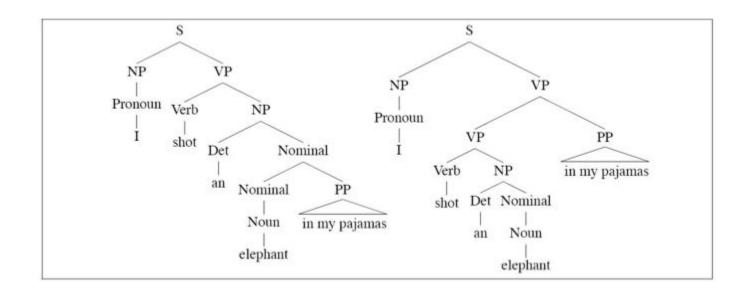
We have seen POS ambiguity (book can be a verb or a noun)

Structural ambiguity is when a grammar assigns **more than one possible parse** to a sentence.

One morning I shot an elephant in my pajamas.

How he got into my pajamas I don't know.

Attachment ambiguity: *Elephant in my pajamas* or *shot in my pajamas*?



Adverbial phrase attachment ambiguity:

We saw the **Eiffel Tower flying to Paris**.

We saw the Eiffel Tower flying to Paris.

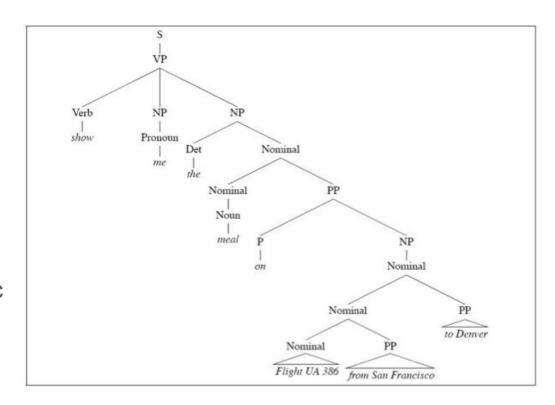
Coordination ambiguity:

```
[old [men and women]] // both are old
[old men] and [women] // only the men are old
```

14 parses for this sentence!

- $VP \rightarrow VP PP$
- Nominal → Nominal PP

The number of parses grow **exponentially**, at the same rate as the number of parenthesizations of arithmetic expressions.



President Kennedy today pushed aside other White House business to devote all his time and attention to working on the Berlin crisis address he will deliver tomorrow night to the American people over nationwide television and radio.

Dynamic programming parsing

Both top-down and bottom-up parsing require that we explore all possible parse trees in parallel.

We can use the efficient state space search algorithms that we saw for FSA

- Depth-first search
- Breadth-first search
- or any sort of agenda-based approach where an agenda can tell us what trees to consider next.

Unfortunately this leads to a lot of duplicate effort.

Det Nominal Nominal Det Noun Nominal. PP flight... Noun NP from Indianapolis... flight False starts of a top-Det Nominal down depth-first left-toright backtracking Nominal to Houston ... parser. Nominal PP Noun from Indianapolis NP flight Nominal Det Nominal PP on TWA Nominal to Houston Nominal PP Noun from Indianapolis flight

NP

Dynamic programming parsing

Systematically fill in tables of solutions to sub-problems. When complete, the table contains the solution to all the sub-problems needed to solve the problem as a whole.

In parsing, solutions to sub-problems are going to be **subtrees for each potential constituent** in the input.

These subtrees then are *looked up* and not re-parsed.

CKY parsing

Also known as the Cocke-Kasami-Younger algorithm.

One requirement: The grammar must be in **Chomsky normal form (CNF)** (Chomsky, 1963).

A grammar is in CNF if

- it is ←free
- each production is either of the form A → B C or A → a for some terminal a.

These grammars are binary branching.

CNF conversion

Assuming *ϵ*-freeness, deal with the following cases:

- RHS mixes terminals and nonterminals
 - \circ Replace INF \rightarrow to VP with INF \rightarrow TO VP and TO \rightarrow to
- RHS is a single nonterminal (unit production / unary rule)
 - o if $A \rightarrow ... \rightarrow B$ and $B \rightarrow \gamma$ then we add $A \rightarrow \gamma$ and discard the intervening unary rules
- RHS is more than 2 nonterminals (N-ary rule)
 - \circ A \to B C γ then introduce A \to X₁ γ and X₁ \to B C and keep iterating

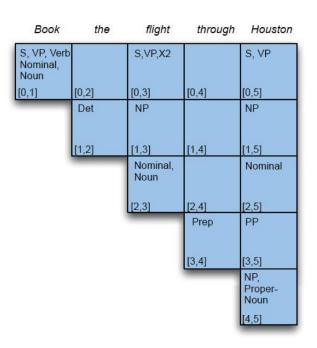
\mathscr{L}_1 Grammar	\mathscr{L}_1 in CNF
$S \rightarrow NP VP$	$S \rightarrow NP VP$
$S \rightarrow Aux NP VP$	$S \rightarrow XI VP$
	$XI \rightarrow Aux NP$
$S \rightarrow VP$	$S \rightarrow book \mid include \mid prefer$
	$S \rightarrow Verb NP$
	$S \rightarrow X2 PP$
	$S \rightarrow Verb PP$
	$S \rightarrow VPPP$
$NP \rightarrow Pronoun$	$NP \rightarrow I \mid she \mid me$
$NP \rightarrow Proper-Noun$	$NP \rightarrow TWA \mid Houston$
$NP \rightarrow Det Nominal$	$NP \rightarrow Det Nominal$
Nominal → Noun	$Nominal \rightarrow book \mid flight \mid meal \mid money$
Nominal → Nominal Noun	Nominal → Nominal Noun
$Nominal \rightarrow Nominal PP$	$Nominal \rightarrow Nominal PP$
$VP \rightarrow Verb$	$VP \rightarrow book \mid include \mid prefer$
$VP \rightarrow Verb NP$	$VP \rightarrow Verb NP$
$VP \rightarrow Verb NP PP$	$VP \rightarrow X2 PP$
	$X2 \rightarrow Verb NP$
$VP \rightarrow Verb PP$	$VP \rightarrow Verb PP$
$VP \rightarrow VP PP$	$VP \rightarrow VP PP$
PP → Preposition NP	$PP \rightarrow Preposition NP$

In dynamic programming parsing, our "solutions to sub-problems" are going to be subtrees for each *potential* constituent in the input.

₀ Book ₁ that ₂ flight ₃

All possible constituent spans:

- 0 Book 1
- 1 that 2
- 2 flight 3
- Book that 2
- that 2 flight 3
- Book 1 that 2 flight 3



We can use the upper-triangular portion of an $(n+1) \times (n+1)$ matrix to represent all constituents that span i through j of the input.

In any tree, each node above the POS level will have exactly two children. Why?

Therefore each constituent span must have a corresponding position k, i < k < j where it can be split into two constituents.

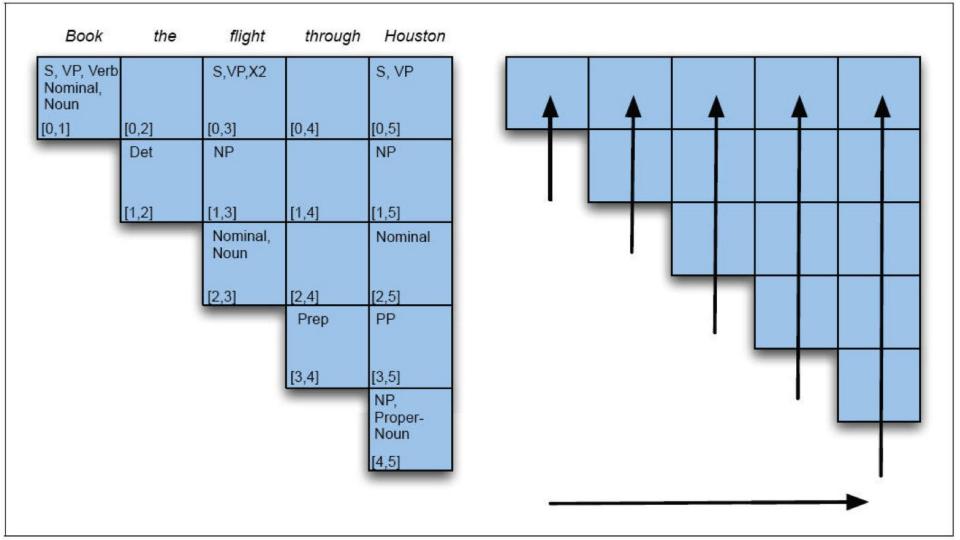
$$_{i}A_{j} \rightarrow _{i}B_{k}C_{j}$$

Our task is simply to fill the parse table in the right way.

We will proceed in a bottom-up fashion, forming constituents for [i, j] out of already filled constituents of [i, k] and [k, j] considering all possible k such that i < k < j.

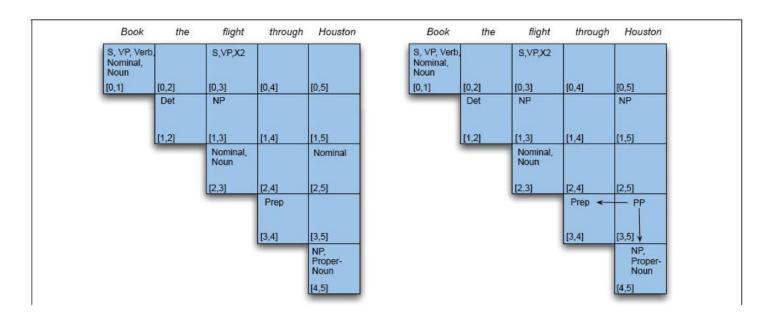


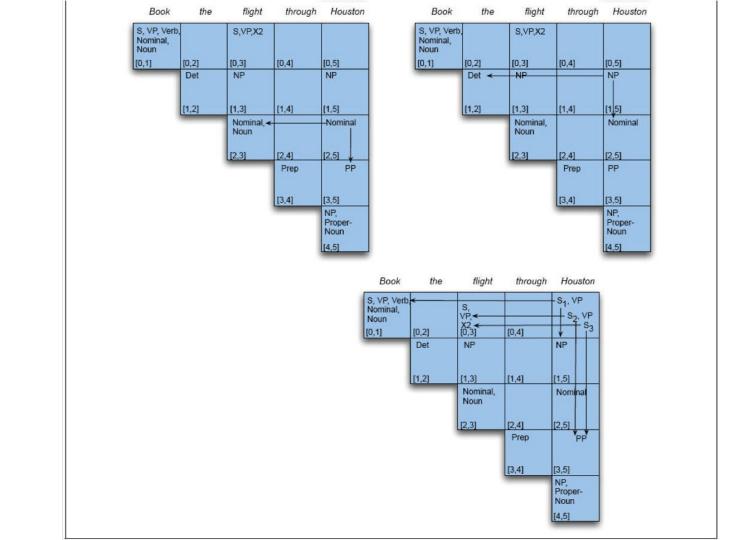
Book	the	flight	through	Houston
S, VP, Verb Nominal, Noun		S,VP,X2		S, VP
[0,1]	[0,2]	[0,3]	[0,4]	[0,5]
	Det	NP		NP
	[1,2]	[1,3]	[1,4]	[1,5]
		Nominal, Noun		Nominal
		[2,3]	[2,4]	[2,5]
		45,5	Prep	PP
			[3,4]	[3,5]
				NP, Proper- Noun
				[4,5]



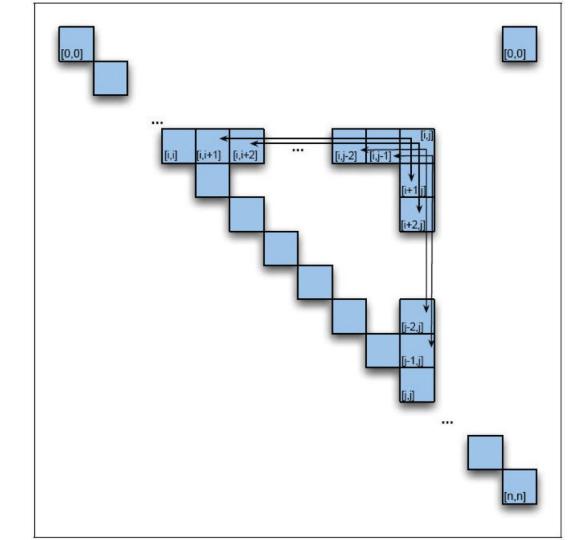
```
function CKY-PARSE(words, grammar) returns table
  for j \leftarrow from 1 to LENGTH(words) do
     table[j-1,j] \leftarrow \{A \mid A \rightarrow words[j] \in grammar\}
     for i \leftarrow from j-2 downto 0 do
          for k \leftarrow i+1 to j-1 do
              table[i,j] \leftarrow table[i,j] \cup
                           \{A \mid A \rightarrow BC \in grammar,
                                B \in table[i,k],
                                C \in table[k, j]
```

After the word *Houston* is read, this is how we fill the 5 cells in the corresponding column.





All the ways to fill the [i, j]th cell in the CKY table.



CKY parsing

This algorithm builds a <u>set of nonterminals</u> that can span [i, j] of the input.

In this way, it is a **recognizer**, not a parser. When it discovers an S for the [0, N] span of the input, it recognizes the sentence as being **parseable**.

CKY parsing

If we want a parser (that will return <u>all possible parses</u> of a sentence) we must make changes to the algorithm:

- Every nonterminal in a cell has two pointers to the constituents from which it was derived
- Allow for multiple versions of the same nonterminal to be entered into one cell of the table.

Statistical Parsing

Probabilistic CKY

Statistical parsing

We will see that it is possible to build probabilistic models of syntactic knowledge and use some of this probabilistic knowledge in efficient probabilistic parsers.

Why probabilistic?

- Disambiguation: Deal with syntactic ambiguity (attachment/coordination ambiguity) in a principled way and resolve them by choosing the most probable interpretation.
- Language modeling: Define a probability distribution over sentences that is better than n-grams (accounting for longer range dependencies)

A PCFG differs from a CFG by augmenting each rule with a conditional probability

$$A \rightarrow \beta [p]$$

Here p expresses the probability that A will be expanded to the sequence β

$$P(A \rightarrow \beta)$$
 or $P(A \rightarrow \beta \mid A)$ or $P(RHS \mid LHS)$

Thus, we have a probability distribution for every nonterminal LHS

$$\sum_{\beta} P(A \to \beta) = 1$$

Grammar		Lexicon
$S \rightarrow NP VP$	[.80]	$Det \to that [.10] \mid a [.30] \mid the [.60]$
$S \rightarrow Aux NP VP$	[.15]	$Noun \rightarrow book [.10] \mid flight [.30]$
$S \rightarrow VP$	[.05]	meal [.15] money [.05]
NP → Pronoun	[.35]	flights [.40] dinner [.10]
NP → Proper-Noun	[.30]	$Verb \rightarrow book [.30] \mid include [.30]$
NP → Det Nominal	[.20]	prefer; [.40]
$NP \rightarrow Nominal$	[.15]	$Pronoun \rightarrow I[.40] \mid she[.05]$
Nominal → Noun	[.75]	me [.15] you [.40]
Nominal → Nominal Noun	[.20]	$Proper-Noun \rightarrow Houston$ [.60]
$Nominal \rightarrow Nominal PP$	[.05]	NWA [.40]
$VP \rightarrow Verb$	[.35]	$Aux \rightarrow does [.60] \mid can [40]$
$VP \rightarrow Verb NP$	[.20]	$Preposition \rightarrow from [.30] \mid to [.30]$
$VP \rightarrow Verb NP PP$	[.10]	on [.20] near [.15]
$VP \rightarrow Verb PP$	[.15]	through [.05]
$VP \rightarrow Verb NP NP$	[.05]	
$VP \rightarrow VP PP$	[.15]	
PP → Preposition NP	[1.0]	

A probabilistic CFG is defined as follows (Booth, 1969)

```
N a set of non-terminal symbols (or variables)

\Sigma a set of terminal symbols (disjoint from N)

R a set of rules or productions, each of the form A \to \beta [p], where A is a non-terminal,

\beta is a string of symbols from the infinite set of strings (\Sigma \cup N)*, and p is a number between 0 and 1 expressing P(\beta|A)

S a designated start symbol
```

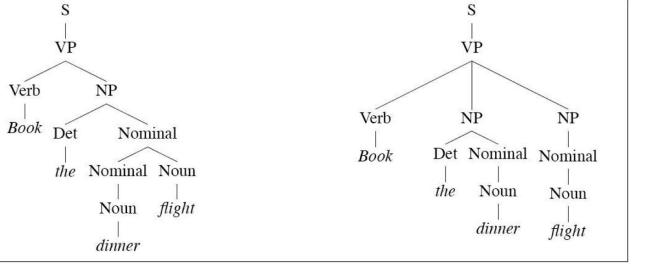
How are PCFGs used?

- They are used to estimate the probability of a parse tree (disambiguation)
- They are used to estimate the probability of a sentence or a constituent (language modeling)

Disambiguation: A PCFG assigns a probability to each parse tree T of a sentence.

The probability of a parse tree is defined as the product of the probabilities of all the n rules used to expand each of the n non-terminal nodes (each rule is of the form LHS $_i \rightarrow RHS_i$)

$$P(T,S) = \prod_{i=1}^{n} P(RHS_i|LHS_i)$$



Rules		P	Rules		ıles	P	
S	\rightarrow	VP	.05	S	\rightarrow	VP	.05
VP	\rightarrow	Verb NP	.20	VP	\rightarrow	Verb NP NP	.10
NP	\rightarrow	Det Nominal	.20	NP	\rightarrow	Det Nominal	.20
Nominal	\longrightarrow	Nominal Noun	.20	NP	\rightarrow	Nominal	.15
Nominal	\rightarrow	Noun	.75	Nominal	\rightarrow	Noun	.75
				Nominal	\rightarrow	Noun	.75
Verb	\rightarrow	book	.30	Verb	\longrightarrow	book	.30
Det	\rightarrow	the	.60	Det	\rightarrow	the	.60
Noun	\rightarrow	dinner	.10	Noun	\longrightarrow	dinner	.10
Noun	\rightarrow	flights	.40	Noun	\rightarrow	flights	.40

Why does it make sense to pick the tree with the highest probability?

$$T^*$$
 = $\underset{T \text{ s.t. } S = \text{yield}(T)}{\operatorname{argmax}_{T \text{ s.t. } S = \text{yield}(T)}} P(T|S)$
= $\underset{T \text{ s.t. } S = \text{yield}(T)}{\operatorname{argmax}_{T \text{ s.t. } S = \text{yield}(T)}} \frac{P(S|T)P(T)}{P(S)}$
= $\underset{T \text{ s.t. } S = \text{yield}(T)}{\operatorname{argmax}_{T \text{ s.t. } S = \text{yield}(T)}} P(T)$

Language modeling: A PCFG defines a probability distribution over sentences

$$P(S) = \sum_{\substack{T \text{ s.t. } S = \text{yield}(T)}} P(T, S)$$

$$= \sum_{\substack{T \text{ s.t. } S = \text{yield}(T)}} P(T)$$

It can model long range dependencies better than n-grams

the contract ended with a loss of 7 cents after trading as low as 9 cents

Probabilistic CKY

Our probabilistic parsing objective is to produce the most likely parse T for a given sentence S

$$T^* = \operatorname{argmax}_{T \text{ s.t. } S = \operatorname{yield}(T)} P(T)$$

First described by Ney (1991).

Probabilistic CKY

As with deterministic CKY, assume that our probabilistic grammar is in CNF.

 \rightarrow Each production is either of the form $A \rightarrow B C$ or $A \rightarrow a$ for some terminal a.

In deterministic CKY each cell **table[i,j]** contained a set of constituents that could span the input words from i to j

In probabilistic CKY each cell **table[i,j,A]** is the maximum probability of a constituent A that spans words i through j.

```
function PROBABILISTIC-CKY(words, grammar) returns most probable parse and its probability for j \leftarrow from 1 to LENGTH(words) do
```

for all $\{A \mid A \rightarrow words[j] \in grammar\}$ $table[j-1,j,A] \leftarrow P(A \rightarrow words[j])$

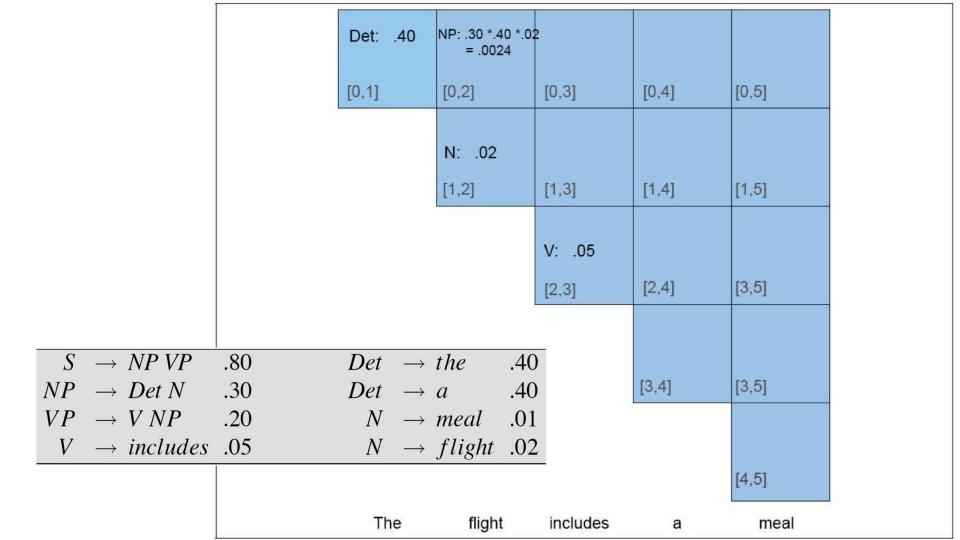
for $i \leftarrow$ from j-2 downto 0 do for $k \leftarrow i+1$ to j-1 do

for all $\{A \mid A \rightarrow BC \in grammar,$ and table[i,k,B] > 0

and table[i,k,B] > 0 and table[k,j,C] > 0 }

if $(table[i,j,A] < P(A \rightarrow BC) \times table[i,k,B] \times table[k,j,C])$ then $table[i,j,A] \leftarrow P(A \rightarrow BC) \times table[i,k,B] \times table[k,j,C]$ $back[i,j,A] \leftarrow \{k,B,C\}$

return BUILD_TREE(back[1, LENGTH(words), S]), table[1, LENGTH(words), S]



Learning with PCFG

The simplest way: Use the **Penn Treebank**, a collection of parse trees in English, Chinese and other languages.

$$P(\alpha \to \beta | \alpha) = \frac{\text{Count}(\alpha \to \beta)}{\sum_{\gamma} \text{Count}(\alpha \to \gamma)} = \frac{\text{Count}(\alpha \to \beta)}{\text{Count}(\alpha)}$$

Unsupervised learning is also an option. The **Inside Outside algorithm** (Lari and Young, 1990) is an instance of the expectation maximization framework and a generalization of the Forward Backward algorithm that we used for unsupervised learning of HMMs.

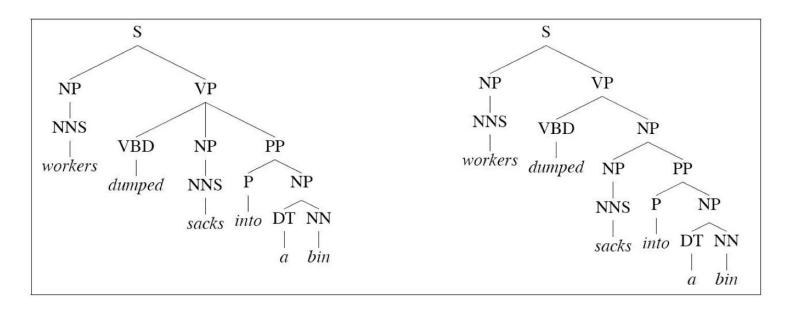
Poor independence assumptions: PCFGs assume that rule expansions are independent (that's why the probabilities are multiplied).

Fact: Subject-NPs are much more likely to be pronouns than object-NPs.

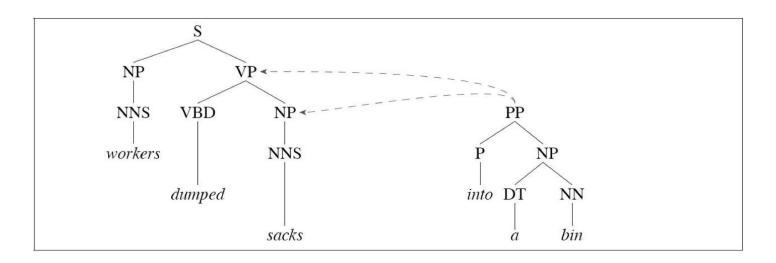
	S .	Non-Pronoun
Subject	91%	9%
Subject Object	34%	66%

But PCFGs are context-free therefore they don't allow a rule probability to be conditioned on surrounding context.

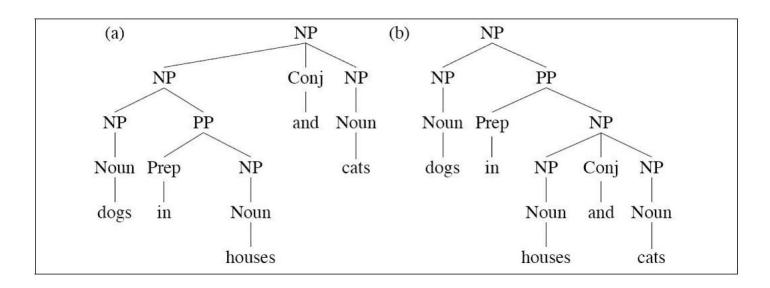
Lack of lexical conditioning: PCFGs do not model syntactic facts about specific words.



Lack of lexical conditioning: PCFGs do not model syntactic facts about specific words.



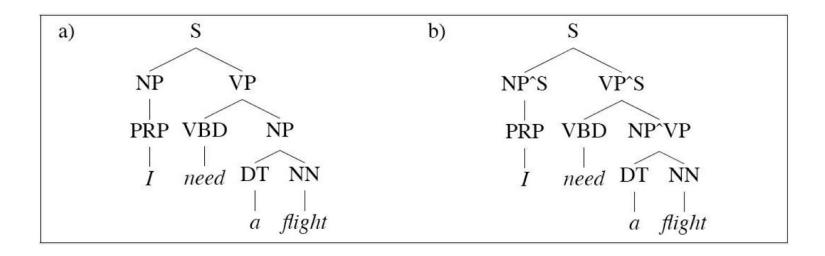
Lack of lexical conditioning: PCFGs do not model syntactic facts about specific words.



Solutions to problems with PCFGs

Nonterminal splitting: $NP_{subject} \rightarrow PRP$ and $NP_{object} \rightarrow PRP$

Parent annotation is one way to achieve this:



Solutions to problems with PCFGs

Nonterminal splitting: $NP_{subject} \rightarrow PRP$ and $NP_{object} \rightarrow PRP$

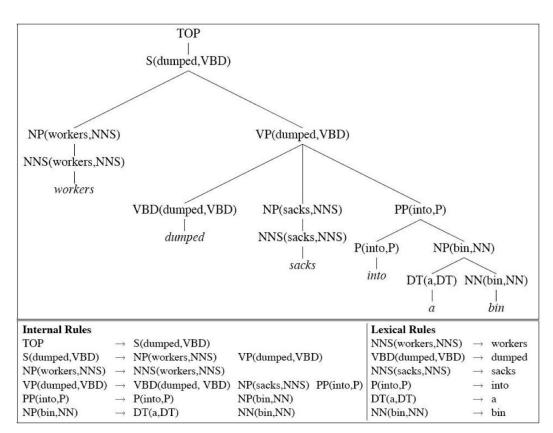
Expectation maximization is another way: The **Split-and-Merge parser** (Petrov et al. 2006) starts with an X-bar grammar and searches for optimal splits and merges of nonterminals that maximize the likelihood of the training set treebank.

Solutions to problems with PCFGs

Lexicalized PCFG:

 $VP(dumped) \rightarrow$

VP(dumped) NP(sacks) PP(into)



Evaluating parsers

PARSEVAL: Measure how much the constituents in the hypothesis parse tree look like the constituents in a gold-standard parse (Black et al, 1991).

Labeled precision: Percentage of constituents predicted that are correct.

Labeled recall: Percentage of gold standard constituents that are predicted correctly.

Cross-brackets: The number of constituents for which the system parse has ((A B) C) but the gold-standard has (A (B C)).

Evaluating parsers

The state-of-the-art parser performance on the Penn treebank is around 90% recall, 90% precision and about 1% cross-bracketed constituents per sentence.

<u>Evalb:</u> The publicly available implementation of PARSEVAL (Sekine and Collins, 1997).

Many NLP tasks do not require whole parse trees for all inputs. For example, in named-entity recognition we might only care about noun phrases.

Chunking: The task of identifying and classifying the non-overlapping segments of a sentence that constitute the basic (non-recursive) phrases, e.g. NP, VP, ADJP, PP.

 $[N_P]$ The morning flight $[N_P]$ from $[N_P]$ Denver $[N_P]$ has arrived

- 1. Find the extents of the chunks
- Label the discovered chunks

In general not all words have to fall in some chunk. Often we only care about Base-NP constituents.

 $[N_{\rm NP}]$ The morning flight] from $[N_{\rm NP}]$ Denver] has arrived

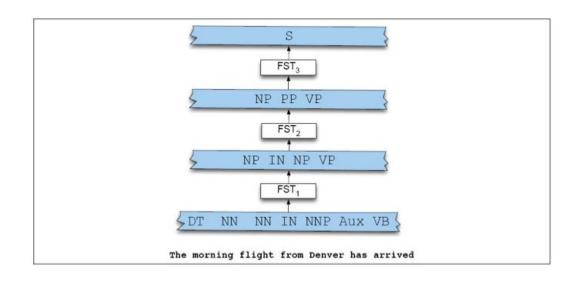
Base-NP constituents are NP constituents that do not contain other NPs.

[NP The morning flight Denver] has arrived

Chunk are non-recursive, therefore they can be modeled using FSTs.

- NP \rightarrow (DT) NN* NN
- \bullet NP \rightarrow NNP
- $VP \rightarrow VB$
- VP → Aux VB
- PP → IN NP
- $S \rightarrow PP^* NP PP^* VP PP^*$

Turn each rule into FST

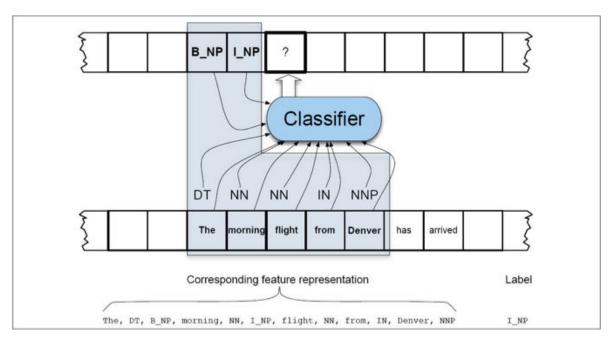


Machine learning approach: Treat chunking as a sequence classification task (like POS tagging) and train on an annotated training set.

IOB tagging: Introduce tags to represent the beginning (B) and internal (I) parts of each chunks, as well as those elements of the input that are outside (O) any chunk.

The	morning	flight	from	Denver	has	arrived
B _{NP}	I _{NP}	I _{NP}	0	B _{NP}	О	О

At this point any sequence classification technique that we have already seen will work.



Partial parsing evaluation

Word-by-word accuracy metric of POS tagging is not appropriate anymore.

Precision: The percentage of system-provided chunks that were correct (correct = both the boundaries and the label is right).

Recall: The percentage of chunks in the data that were correctly identified by the system.

$$\begin{aligned} & \operatorname{Precision} = \frac{\operatorname{tp}}{\operatorname{tp} + \operatorname{fp}} \\ & \operatorname{Recall} = \frac{\operatorname{tp}}{\operatorname{tp} + \operatorname{fn}} \end{aligned}$$

Partial parsing evaluation

F-measure is a way to combine precision and recall.

$$F_{\beta} = \frac{(\beta^2 + 1)PR}{\beta^2 P + R}$$

The β parameter weights the importance of recall and precision: $\beta > 1$ favors recall, $\beta < 1$ favors precision.

$$F_1 = \frac{2PR}{P+R}$$

Partial parsing evaluation

Most machine learning systems using chunks such as below achieve F-measures in the .92 to .94 range.

Label	Category	Proportion (%)	Example
NP	Noun Phrase	51	The most frequently cancelled flight
VP	Verb Phrase	20	may not arrive
PP	Prepositional Phrase	20	to Houston
ADVP	Adverbial Phrase	4	earlier
SBAR	Subordinate Clause	2	that
ADJP	Adjective Phrase	2	late