M4-L2-P3

October 1, 2023

1 Problem 6 (5 points)

In this problem, we will investigate kernel selection and regularization strength in support vector regression for a 1-D problem.

Run each cell below, then try out the interactive plot to answer the questions.

```
[]: import numpy as np
     import matplotlib.pyplot as plt
     from sklearn.svm import SVR
     xs = np.array([0.094195, 0.10475, 0.12329, 0.12767, 0.1343, 0.11321, 0.16134, 0.
      416622,0.15704,0.16892,0.1707,0.19564,0.18697,0.20818,0.22071,0.21833,0.
      →23029,0.23398,0.25217,0.25168,0.2538,0.25143,0.27121,0.27319,0.28675,0.
      429971,0.30451,0.32319,0.32141,0.33977,0.35378,0.37053,0.35916,0.36534,0.
      43807,0.38696,0.41073,0.41095,0.41302,0.42177,0.42517,0.43633,0.42191,0.
      45198,0.4606,0.4838,0.4664,0.48132,0.49296,0.51028,0.51747,0.499,0.49948,0.
      →53049,0.53986,0.55444,0.54966,0.56389,0.5544,0.56139,0.58974,0.59864,0.
      459467, 0.6122, 0.61911, 0.62601, 0.63302, 0.63993, 0.65452, 0.64038, 0.67782, 0.
      466911,0.67807,0.68518,0.68705,0.70398,0.72397,0.71793,0.72931,0.76366,0.
      475441,0.73797,0.7741,0.77121,0.77784,0.7816,0.79257,0.80469,0.82256,0.
      482495,0.83913,0.8226,0.84766,0.83838,0.8493,0.89643,0.86783,0.89621,0.
      90823, 0.90054, ])
     ys = np.array([0.51123,0.50881,0.50546,0.50756,0.51653,0.50797,0.49658,0.
      450899,0.50218,0.50242,0.50906,0.50466,0.48063,0.49306,0.48622,0.51558,0.
      450493, 0.48378, 0.518, 0.49348, 0.51459, 0.53657, 0.54106, 0.54207, 0.56463, 0.
      456601, 0.61192, 0.61208, 0.63699, 0.64194, 0.67329, 0.70949, 0.74668, 0.77664, 0.
      482362,0.84736,0.89991,0.91268,0.92689,0.93635,0.94732,0.95202,0.94112,0.
      492713,0.89726,0.88055,0.83289,0.78465,0.75197,0.71588,0.64221,0.58237,0.
      452391,0.45466,0.37946,0.31505,0.25479,0.18915,0.14154,0.084572,0.058735,0.
      4027538,0.013328,0.0098045,0.068816,0.094916,0.10225,0.16912,0.21646,0.
      427493,0.33072,0.40278,0.48282,0.53813,0.63165,0.69685,0.74494,0.8089,0.
      48693,0.89515,0.92841,0.94583,0.93489,0.91862,0.92811,0.90047,0.86258,0.
      485054, 0.82246, 0.83096, 0.78313, 0.74352, 0.71369, 0.69591, 0.65134, 0.65297, 0.
      \leftarrow61356,0.59983,0.57448,0.56923,])
```

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$\text{\circ}070707,0.080808,0.090909,0.10101,0.11111,0.12121,0.13131,0.14141,0.15152,0.}$
      416162,0.17172,0.18182,0.19192,0.20202,0.21212,0.22222,0.23232,0.24242,0.
      425253,0.26263,0.27273,0.28283,0.29293,0.30303,0.31313,0.32323,0.33333,0.
      -34343,0.35354,0.36364,0.37374,0.38384,0.39394,0.40404,0.41414,0.42424,0.
      43434,0.44444,0.45455,0.46465,0.47475,0.48485,0.49495,0.50505,0.51515,0.
      $52525,0.53535,0.54545,0.55556,0.56566,0.57576,0.58586,0.59596,0.60606,0.
      →61616,0.62626,0.63636,0.64646,0.65657,0.66667,0.67677,0.68687,0.69697,0.
      470707,0.71717,0.72727,0.73737,0.74747,0.75758,0.76768,0.77778,0.78788,0.
      479798,0.80808,0.81818,0.82828,0.83838,0.84848,0.85859,0.86869,0.87879,0.
      48889,0.89899,0.90909,0.91919,0.92929,0.93939,0.94949,0.9596,0.9697,0.9798,0.
      ⇔9899,1.0,])
     y = np.array([0.46193, 0.47566, 0.48699, 0.49609, 0.50315, 0.50836, 0.51189, 0.
      451393,0.51467,0.51428,0.51294,0.51085,0.50818,0.50512,0.50186,0.49856,0.
      49542,0.49263,0.49035,0.48878,0.4881,0.4885,0.49015,0.49323,0.49794,0.
      $50446,0.51298,0.52376,0.53706,0.55316,0.57231,0.59478,0.62084,0.65075,0.
      468477,0.72317,0.76529,0.80864,0.85051,0.88819,0.91898,0.94015,0.94917,0.
      494553,0.93,0.90339,0.86651,0.82017,0.76518,0.70233,0.63243,0.5563,0.47475,0.
      438966, 0.3049, 0.22456, 0.15274, 0.093526, 0.051005, 0.028929, 0.027469, 0.044659, 0.
      4078502,0.127,0.18816,0.25999,0.34048,0.42761,0.51845,0.60913,0.69574,0.
      477438,0.84113,0.89208,0.92416,0.93858,0.93795,0.92487,0.90197,0.87185,0.
      483712,0.80039,0.76426,0.73054,0.69893,0.66883,0.63963,0.61072,0.5815,0.
      $\sqrt{55136}, 0.51968, 0.48587, 0.44931, 0.40939, 0.36551, 0.31706, 0.26344, 0.20402, 0.
      \hookrightarrow13821,0.065402,])
[]: %matplotlib inline
     from ipywidgets import interact, interactive, fixed, interact_manual, Layout, __
      →FloatSlider, Dropdown
     def plotting_function(kernel, log_C, log_epsilon):
         C = np.power(10.,log C)
         epsilon = np.power(10.,log_epsilon)
         model = SVR(kernel=kernel,C=C,epsilon=epsilon)
         model.fit(xs.reshape(-1,1),ys)
         xfit = np.linspace(0,1,200)
         yfit = model.predict(xfit.reshape(-1,1))
         plt.figure(figsize=(12,7))
         plt.scatter(xs,ys,s=10,c="k",label="Data")
         plt.plot(xfit,yfit,linewidth=3, label="SVR")
         plt.plot(x_gt,y_gt,"--",label="Ground Truth")
         title = f"Kernel: {kernel}, C = {C:.1e}, eps = {epsilon:.1e}"
         plt.legend(loc="lower left")
         plt.xlabel("$x 1$")
```

x gt = np.array([0.0,0.010101,0.020202,0.030303,0.040404,0.050505,0.060606,0.

```
plt.ylabel("$y$")
    plt.title(title)
    plt.show()
slider1 = FloatSlider(
    value=0,
   min=-5,
   \max=5,
    step=.5,
    description='C',
    disabled=False,
    continuous_update=True,
    orientation='horizontal',
    readout=False,
   layout = Layout(width='550px')
)
slider2 = FloatSlider(
   value=-1,
   min=-7,
   \max=-1,
    step=.5,
    description='epsilon',
    disabled=False,
    continuous_update=True,
    orientation='horizontal',
    readout=False,
    layout = Layout(width='550px')
)
dropdown = Dropdown(
    options=['linear', 'rbf', 'sigmoid'],
    value='linear',
    description='kernel',
    disabled=False,
interactive_plot = interactive(
   plotting_function,
    kernel = dropdown,
    log_C = slider1,
    log_epsilon = slider2
output = interactive_plot.children[-1]
output.layout.height = '500px'
```

interactive_plot

[]: interactive(children=(Dropdown(description='kernel', options=('linear', 'rbf', 'sigmoid'), value='linear'), Fl...

1.1 Questions

- 1. Which kernel produced the best fit overall? (Assume this kernel for subsequent questions.)

 Linear produced the best overall fit
- 2. As 'C' increases, does model performance on in-sample data generally improve or worsen? It generally improves until a certain point where it starts to overfit
- 3. As 'C' increases, does model performance on out-of-sample data (on the intervals [0.0, 0.1] and [0.9, 1.0]) generally improve or worsen?
 - It doesn't necessarily improve all that much past a certain point but compared to very low C values it does imporve.
- 4. What 'C' value would you recommend for this kernel?
 - I would recommend a C value of 3,200 because it has a good balance of fitting the inner data well while also not overfitting too much
- 5. What 'epsilon' value would you recommend?
 - I would recommend an epsilon of 3.2e-5.