HW1 Programming Problem 1 (10 points)

You are given 14 temperature measurements from 14 thermocouples in a factory. A model has produced 14 temperature predictions, one for each thermocouple. You must compute the the error vector and MSE between the predicted and measured temperatures via a few methods.

Run the next cell to load the data; then proceed through the notebook.

- y_data is y_i a 14x1 array of temperature measurements (in deg C)
- y_pred is \hat{y} , a 14x1 array of temperature predictions

```
In [ ]: |
        import numpy as np
        np.set_printoptions(precision=4)
        y_{data} = np.array([[20,21,30,30,21,25,38,37,30,22,22,38,20,35]],dtype=np.double).T
        y_pred = np.array([[21,21,31,30,20,28,36,32,31,20,21,39,21,34]],dtype=np.double).T
        print("y_data = \n", y_data)
        print("y_pred = \n", y_pred)
        y_data =
          [[20.]
          [21.]
          [30.]
          [30.]
          [21.]
          [25.]
          [38.]
          [37.]
          [30.]
          [22.]
          [22.]
          [38.]
          [20.]
         [35.]]
        y_pred =
          [[21.]
          [21.]
          [31.]
          [30.]
          [20.]
          [28.]
          [36.]
          [32.]
          [31.]
          [20.]
          [21.]
          [39.]
          [21.]
```

Error vector

[34.]]

First, compute the error vector $y_{err} = y - \hat{y}$. Call the result y_err. It should be 14x1.

You may do this with a loop, or -- better yet -- by simply subtracting the two arrays.

```
In []: # YOUR CODE GOES HERE
# Compute y_err
y_err = y_pred - y_data
print("Size of y_err:", np.shape(y_err))
Size of y_err: (14, 1)
```

Mean squared error (MSE)

Now compute the MSE,

$$MSE = rac{1}{N} \sum_{i=1}^{N} (y_i - \hat{y}_i)^2 = rac{1}{N} \sum_{i=1}^{N} y_{err}^2$$

MSE with Loop

First, compute this quantity by using a for loop to loop through y_err, performing the necessary operations to compute MSE.

Call the result MSE_loop .

Your result should be \approx 3.5714.

```
In []: # YOUR CODE GOES HERE
    # Compute MSE_loop

MSE_loop = 0
N = len(y_err)
for i in range(N):
    MSE_loop += (y_err[i]**2)/N

print("MSE (loop) = ", MSE_loop)

MSE (loop) = [3.5714]
```

MSE by matrix multiplication

Another way to compute the MSE is by recognizing that the sum $\sum_{i=1}^{N}y_{err}^2$ equals the matrix product $y_{err}' \cdot y_{err}$.

Therefore:

$$MSE = rac{1}{N} y_{err}' \cdot y_{err}$$

Compute the MSE this way. Call it MSE_mm, and make sure the result is the same. This is a much more efficient way of computing the MSE in Python.

Note that you can compute the transpose of a 2D array A with A.T, and you can multiply matrices A and B with A @ B.

```
In []: # YOUR CODE GOES HERE
    # Compute MSE_mm
MSE_mm = (y_err.T @ y_err) / N
```

```
print("MSE (matrix multiplication) = ", MSE_mm)
MSE (matrix multiplication) = [[3.5714]]
```

MSE by numpy mean

Now you will compute the MSE once more, but using numpy operations. Use <code>np.mean()</code> to take an average. Compute the square of <code>y_err</code> with either <code>np.square()</code> or <code>y_err</code> * <code>y_err</code>.

Call your MSE_np , and make sure the result is the same. This is also much more efficient than a Python for loop.

```
In []: # YOUR CODE GOES HERE
    # Compute MSE_np
    MSE_np = np.mean(np.square(y_err))

print("MSE (Numpy) = ", MSE_np)
```

MSE (Numpy) = 3.5714285714285716