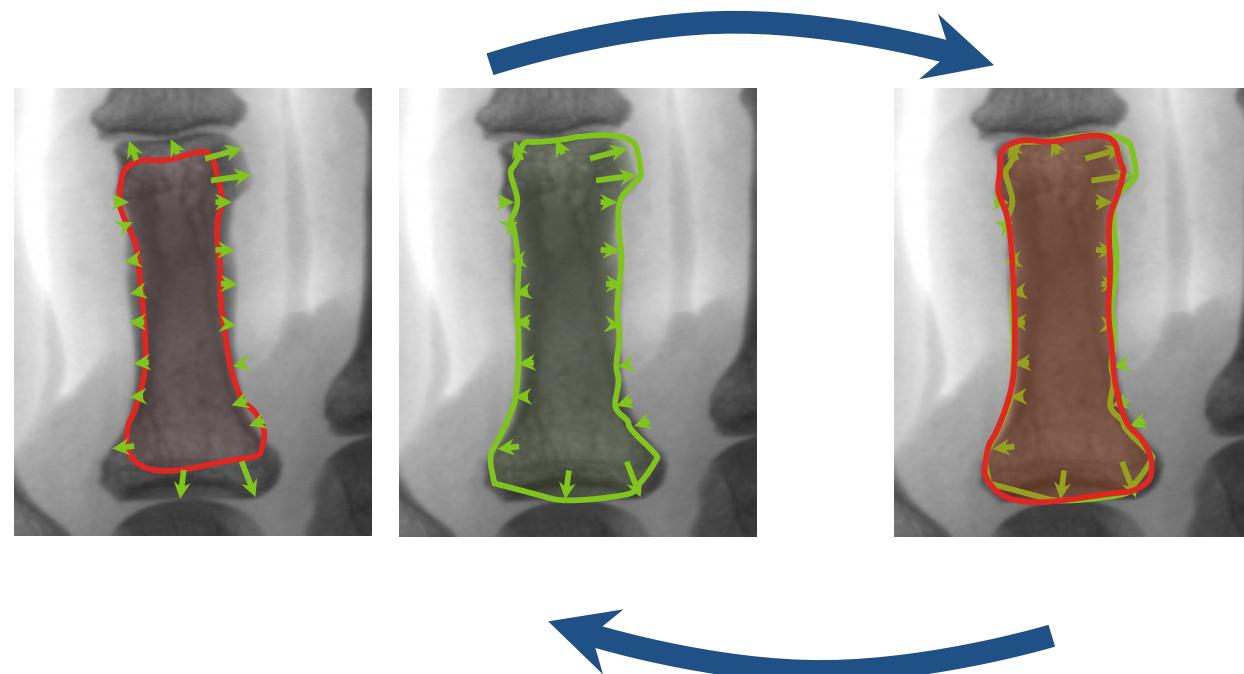
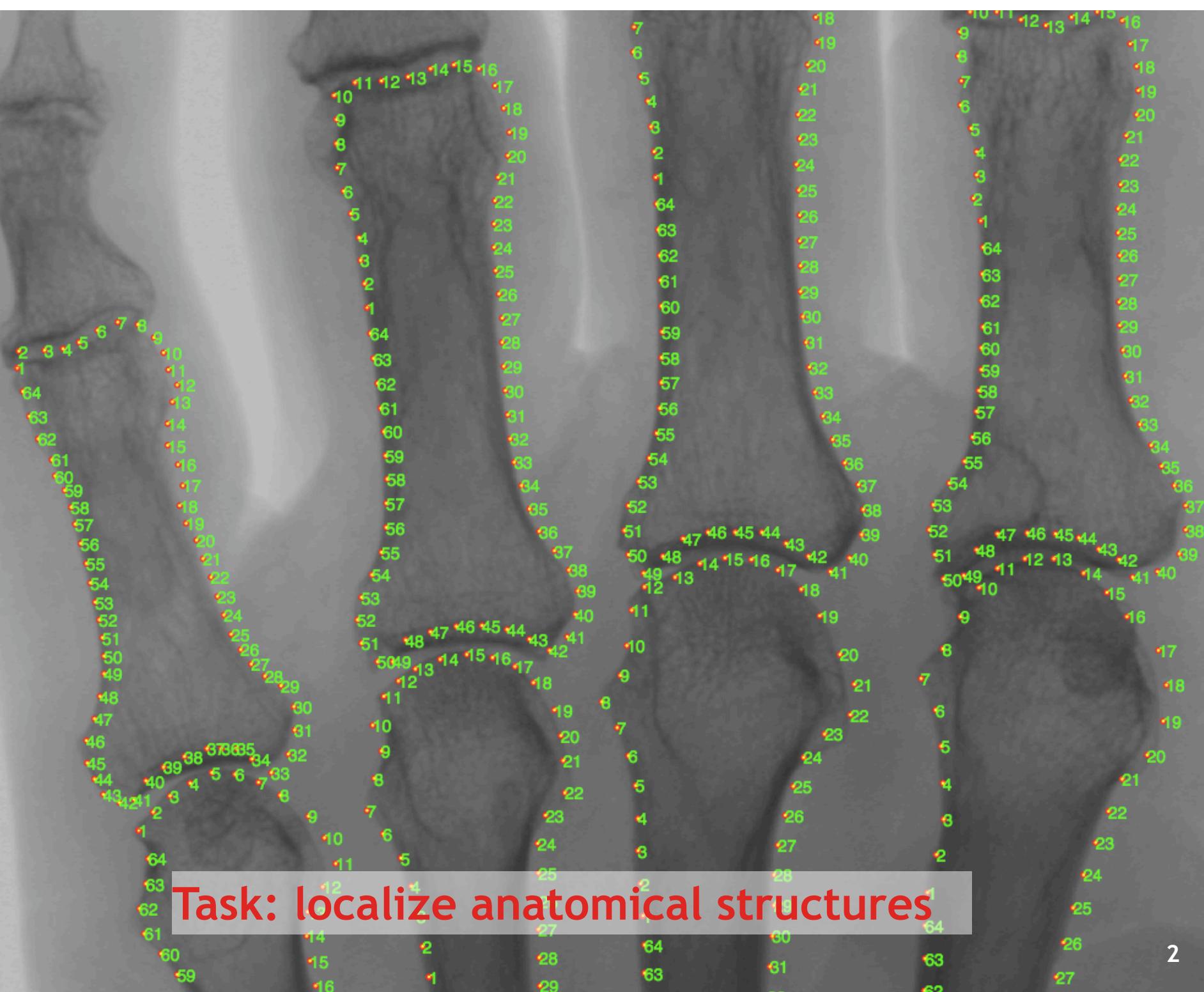


# This lecture: models of shape and texture

- Active Shape Models
- Eigenfaces
- Active Appearance Models

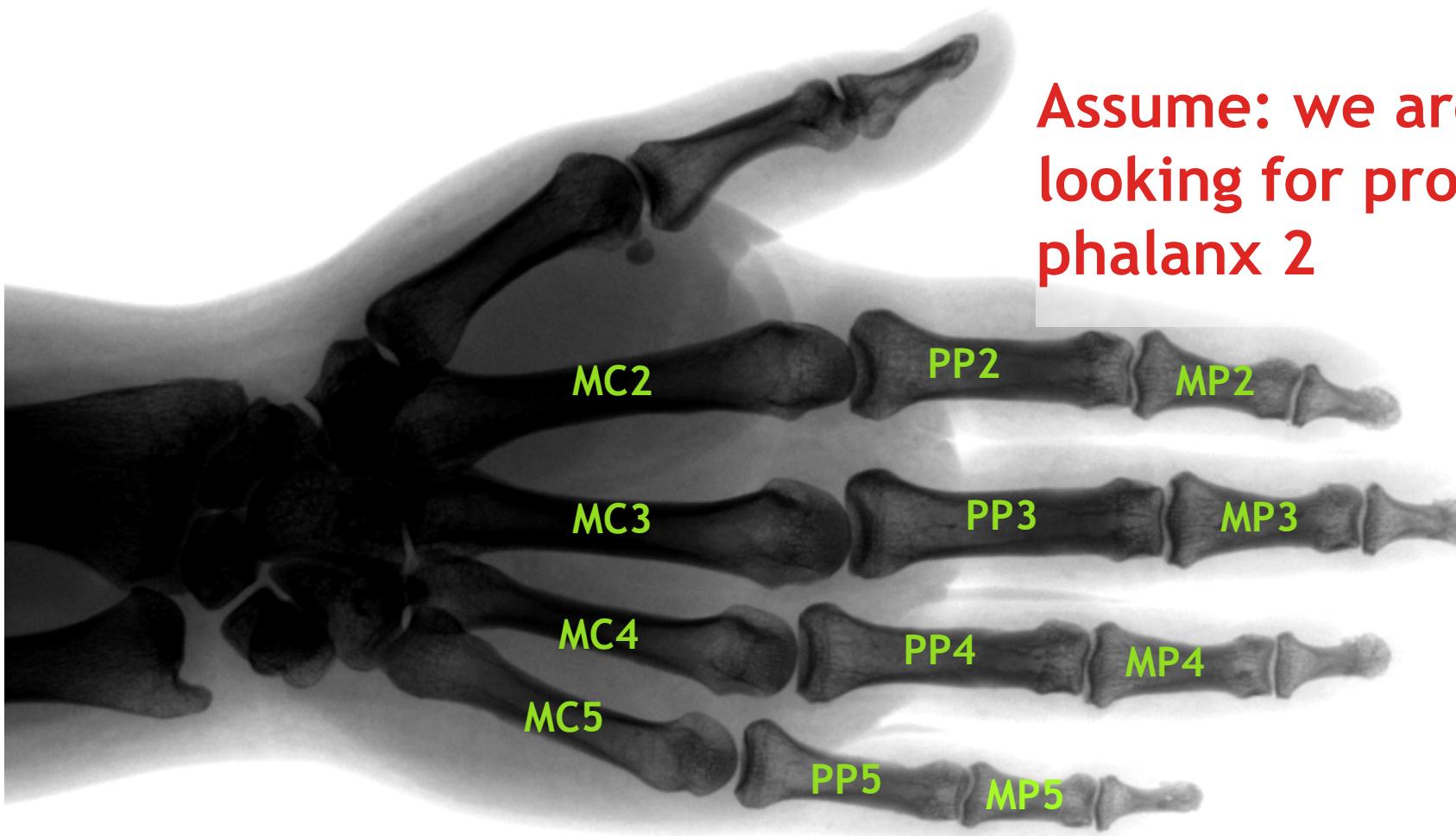




# Task: Analyze a hand radiograph

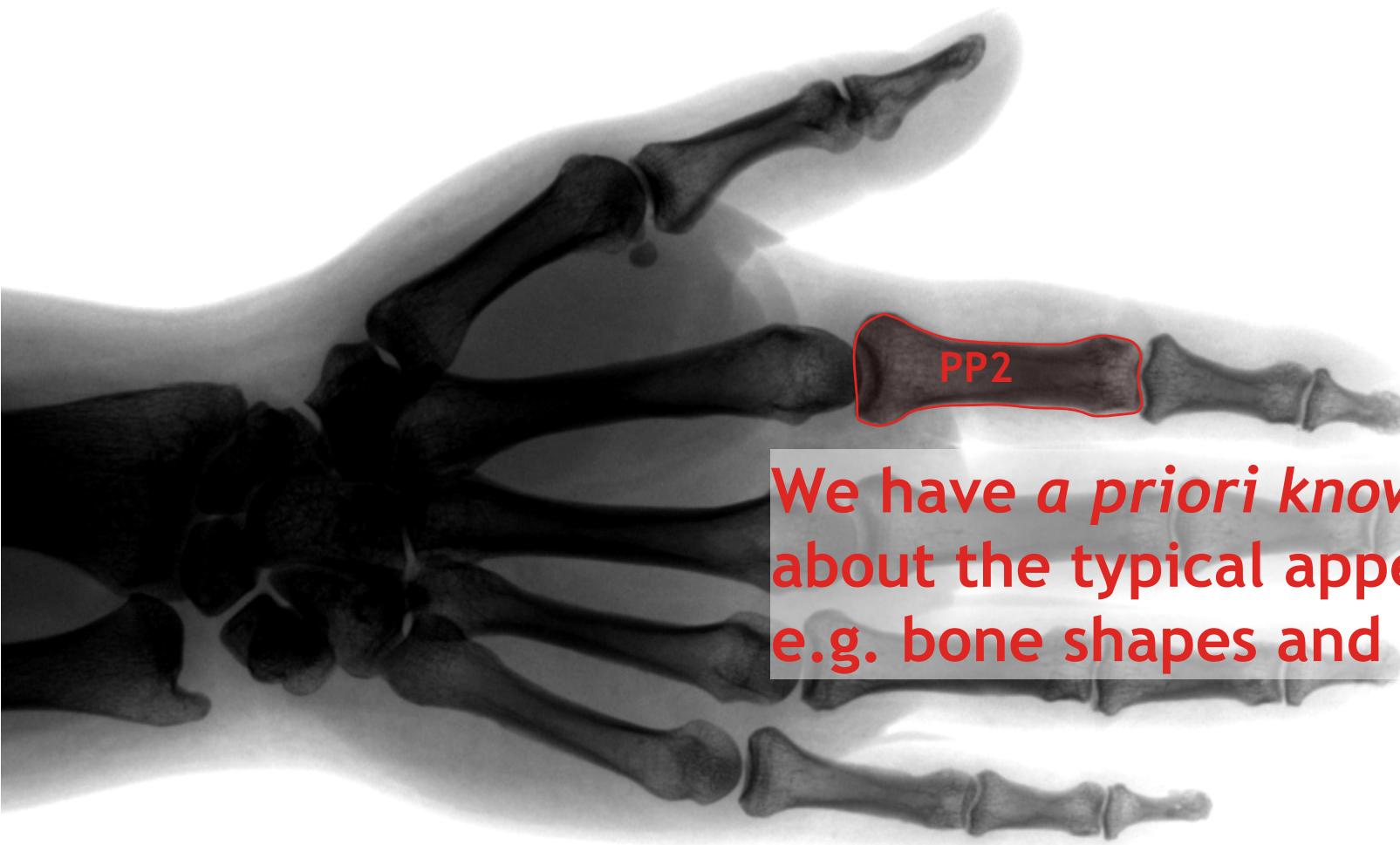


# Task: Analyze a hand radiograph



Assume: we are looking for proximal phalanx 2

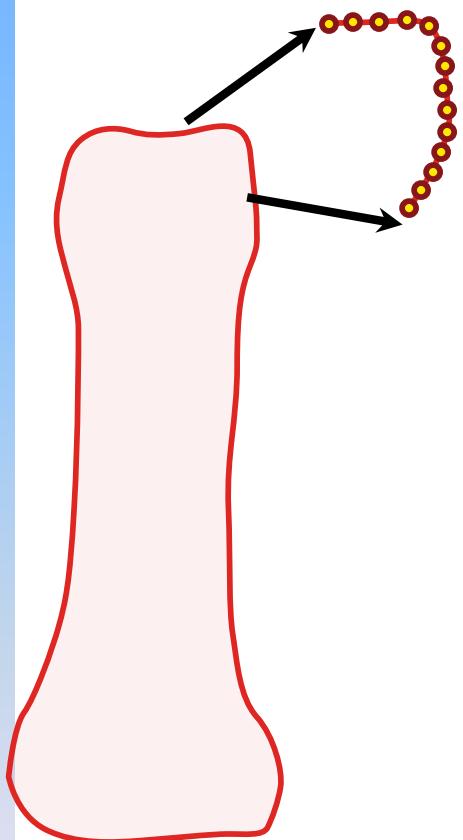
# Analyzing a hand radiograph



We have *a priori* knowledge about the typical appearance:  
e.g. bone shapes and texture

How can we represent this knowledge?  
How can we exploit it?

# How to capture *a priori knowledge*?



**Simple shape representation:** shape consists of a set of points defined by their individual coordinates

- very powerful
- very general
- very unspecific

**Alternative:**

- capture common properties of the bone
- find a representation that is restricted to plausible bones.

# Prior knowledge: first works

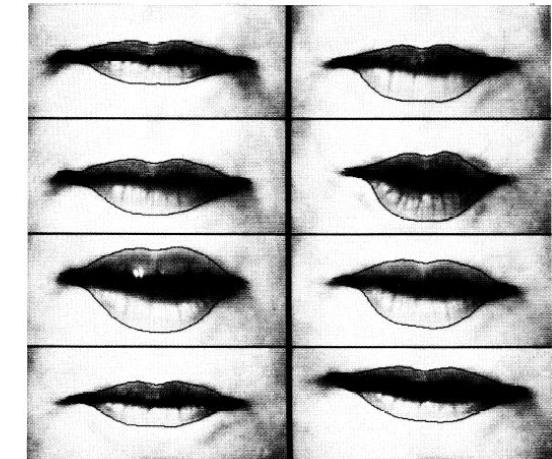
## ➤ Snakes

M. Kass, A. Witkin and  
D. Terzopoulos,  
'Snakes', ICCV 1987,  
IJCV 88

$$\begin{aligned} E_{\text{snake}}^* &= \int_0^1 E_{\text{snake}}(\mathbf{v}(s)) ds \\ &= \int_0^1 E_{\text{int}}(\mathbf{v}(s)) + E_{\text{image}}(\mathbf{v}(s)) \\ &\quad + E_{\text{con}}(\mathbf{v}(s)) ds \end{aligned}$$

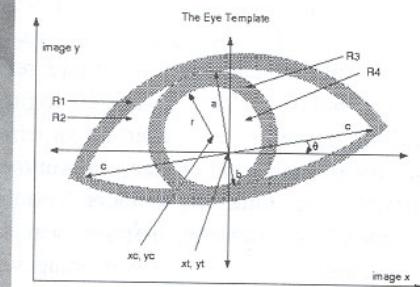
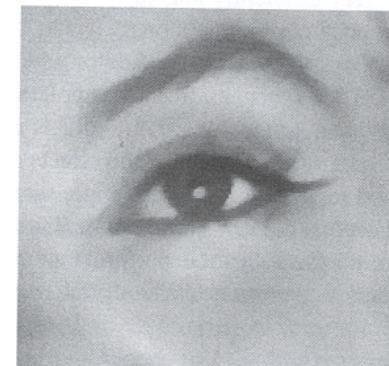
Data-driven

Prior knowledge

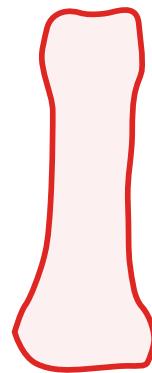


## ➤ Deformable templates

A.L.Yuille, D. Cohen, and P.Hallinan,  
"Feature extraction from faces using  
deformable templates", CVPR 89,  
IJCV 92.



# Current work: Statistical Shape Models



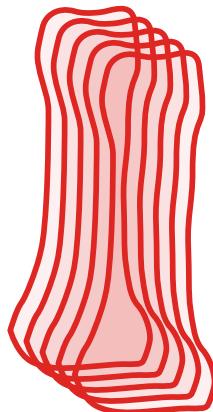
$$\mathbf{x}_i = \begin{pmatrix} x_1 \\ y_1 \\ x_2 \\ y_2 \\ \vdots \\ x_m \\ y_m \end{pmatrix}$$

Each example is represented by a vector containing the coordinates of the landmarks.

**Learning:** Model Acquisition  
**Inference:** Model Fitting

# Model learning

- How can we learn what a bone looks like?

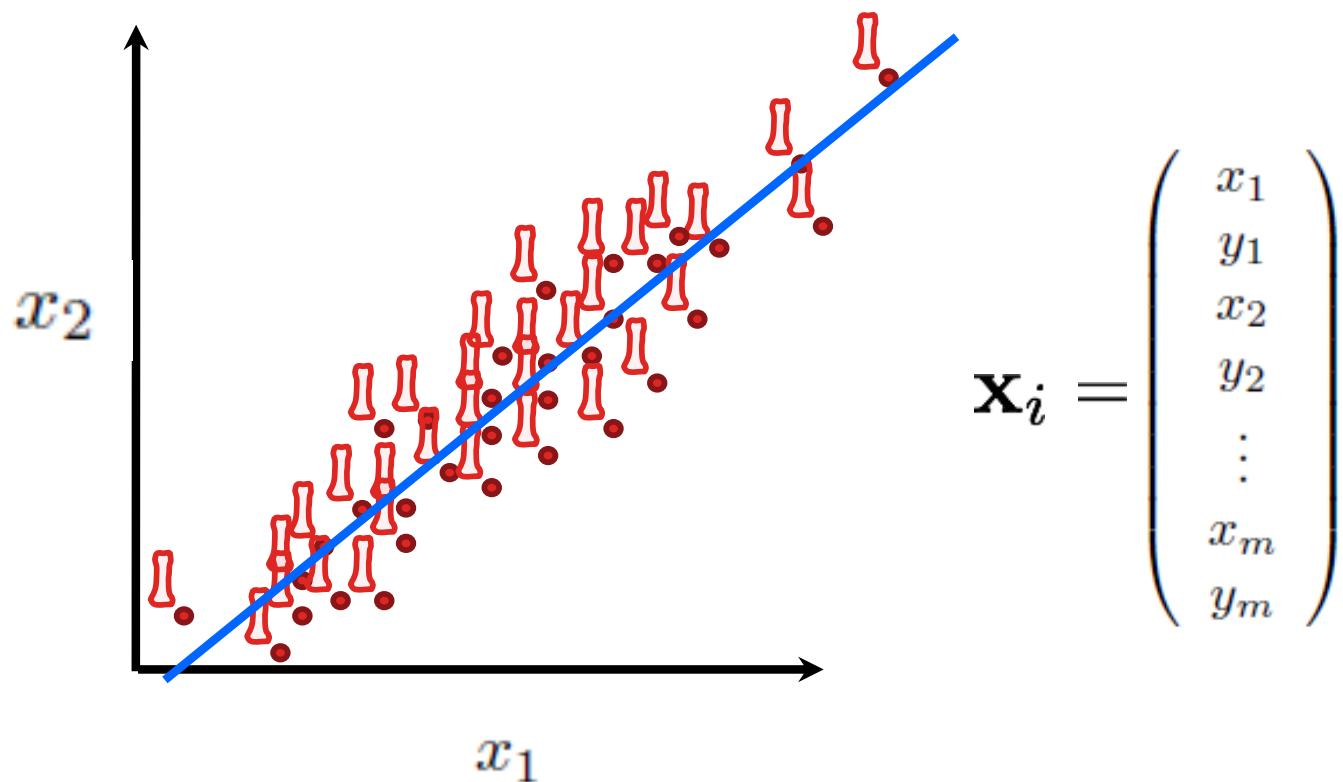


$\{\mathbf{x}_1, \dots, \mathbf{x}_n\}$  To build a statistical model of the data we need many examples.

- Objectives:
  - Expressiveness (model can account for all bones)
  - Compactness (as simple as possible)
- Method: Principal Components Analysis (PCA)

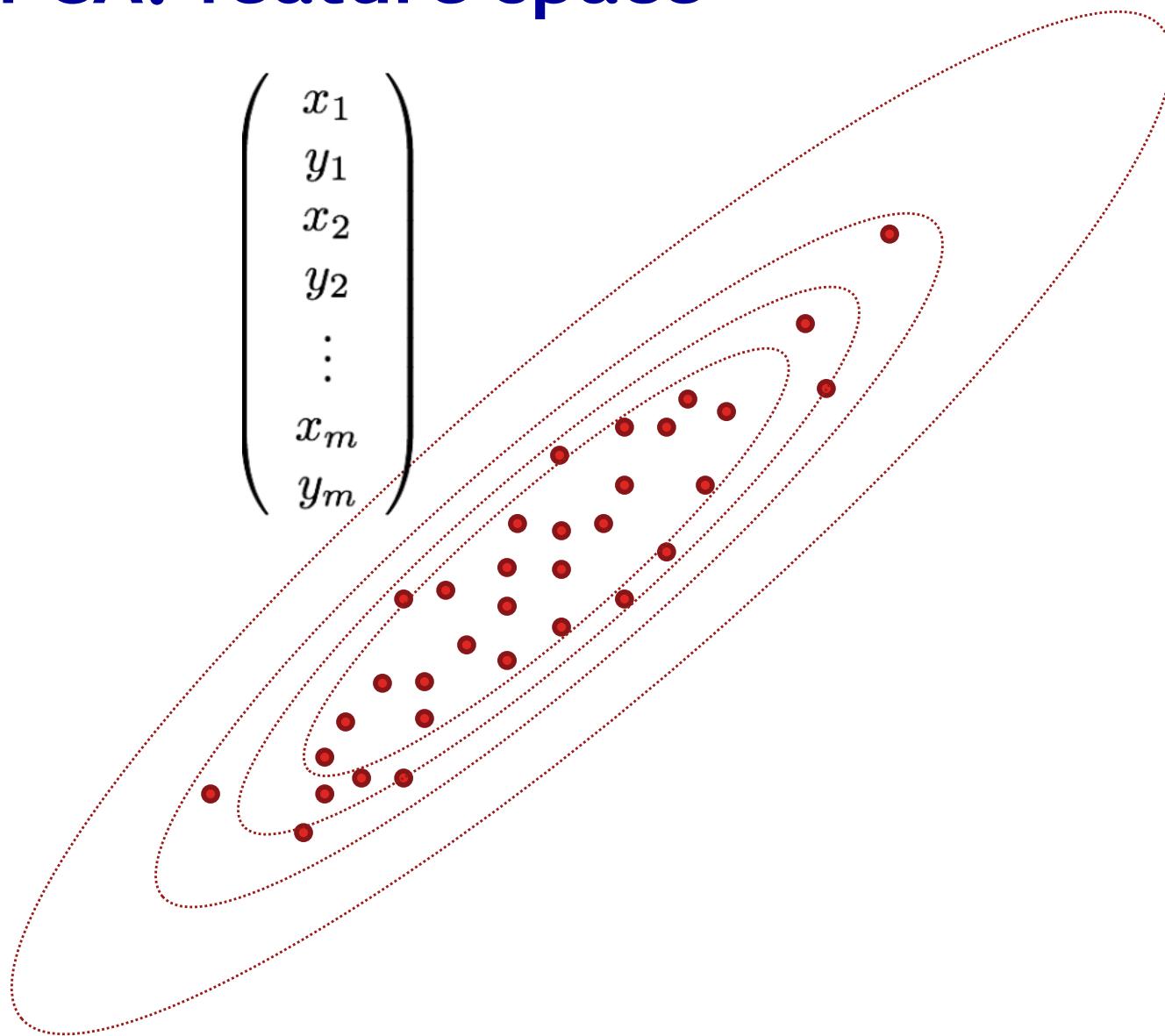
# The space of all bone shapes

- Bone shapes: vectors in  $R^{2m}$



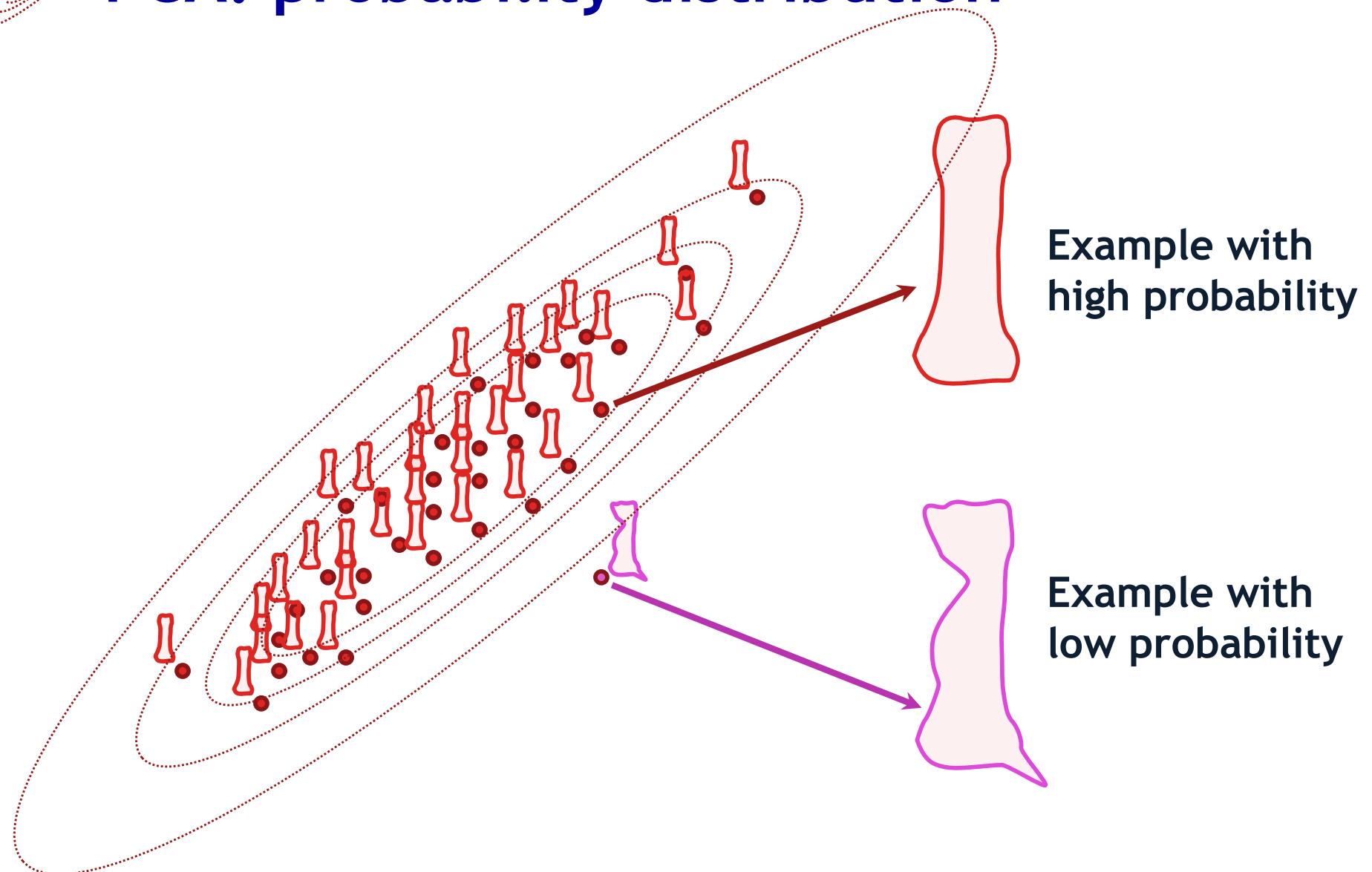
- Goal: project data onto a low-dimensional linear subspace that best explains their variation.

# PCA: feature space

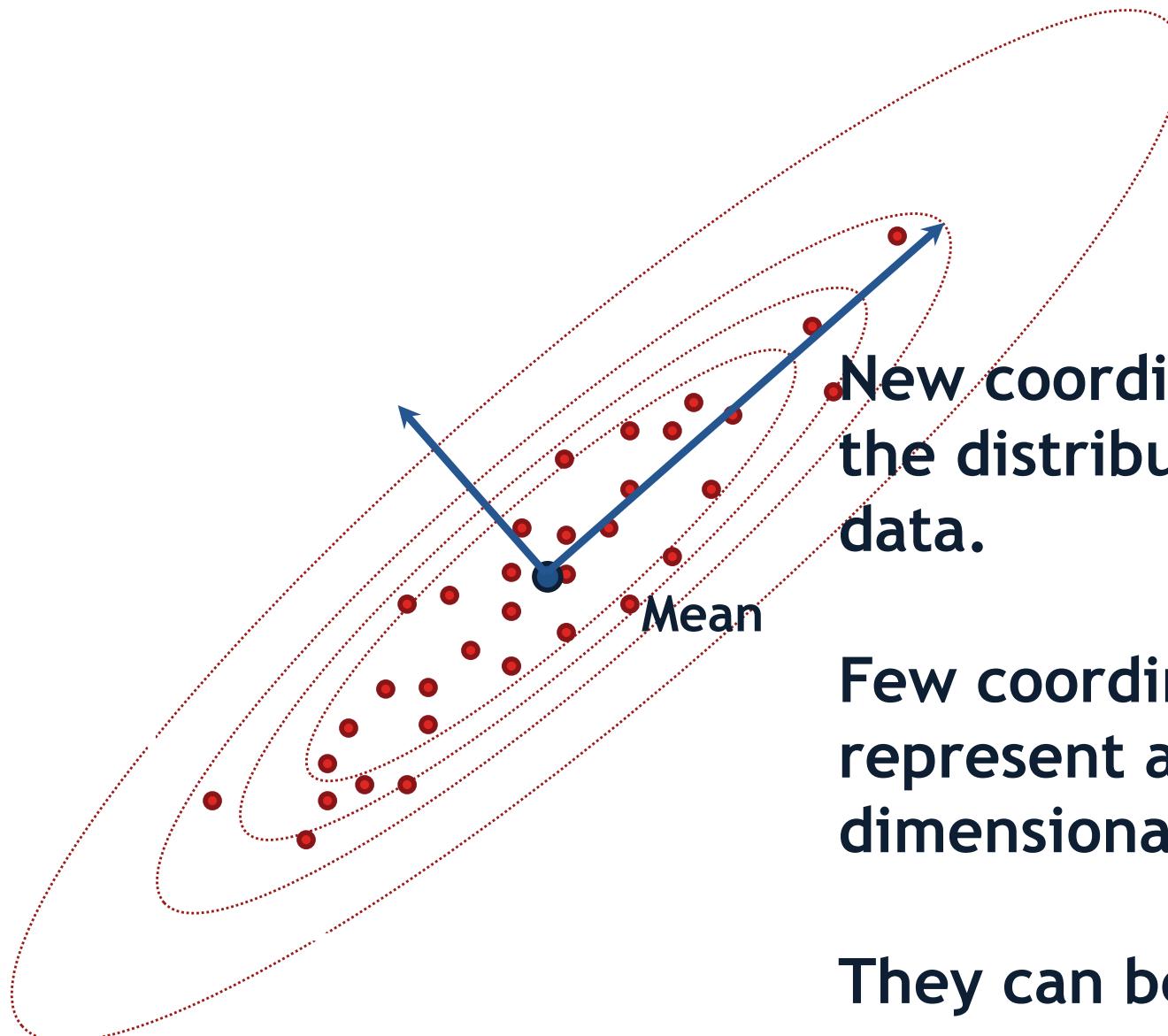




# PCA: probability distribution



# New subspace: 'better' coordinate system



New coordinates reflect  
the distribution of the  
data.

Few coordinates suffice to  
represent a high  
dimensional vector

They can be viewed as  
parameters of a model

# Principal Component Analysis

- Given: N data points  $x_1, \dots, x_N$  in  $\mathbb{R}^d$
- We want to find a new set of features that are linear combinations of original ones:

$$u(x_i) = u^T(x_i - \mu)$$

( $\mu$ : mean of data points)

- What unit vector  $u$  in  $\mathbb{R}^d$  captures the most variance of the data?

# Principal Component Analysis

- Variance of projection on  $\mathbf{u}$ :

$$\begin{aligned} \text{var}(u) &= \frac{1}{N} \sum_{i=1}^N \mathbf{u}^T (\mathbf{x}_i - \mu)(\mathbf{u}^T (\mathbf{x}_i - \mu))^T \\ &\quad \text{Projection of data point} \end{aligned}$$

$$= \mathbf{u}^T \left[ \sum_{i=1}^N (\mathbf{x}_i - \mu)(\mathbf{x}_i - \mu)^T \right] \mathbf{u}$$

$$\begin{aligned} &\quad \text{Covariance matrix of data} \\ &= \mathbf{u}^T \Sigma \mathbf{u} \end{aligned}$$

**Direction: Unit norm vector**

The direction that maximizes the variance: the eigenvector associated with the largest eigenvalue of  $\Sigma$

# Principal component analysis

- The direction that captures the maximum covariance of the data is the eigenvector corresponding to the largest eigenvalue of the data covariance matrix
- Furthermore, the top  $k$  orthogonal directions that capture the most variance of the data are the  $k$  eigenvectors corresponding to the  $k$  largest eigenvalues

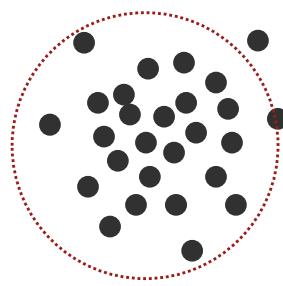
# Covariance matrix reminder

- Covariance matrix:

$$\Sigma_{i,j} = E((x_i - E(x_i))(x_j - E(x_j)))$$

$$\hat{\Sigma}_{i,j} = \frac{1}{N-1} \left[ \sum_{i=1}^N (\mathbf{x}_i - \mu)(\mathbf{x}_i - \mu)^T \right] \quad \mu = \frac{1}{N} \sum_{i=1}^N \mathbf{x}_i$$

- Uncorrelated coordinates: diagonal covariance

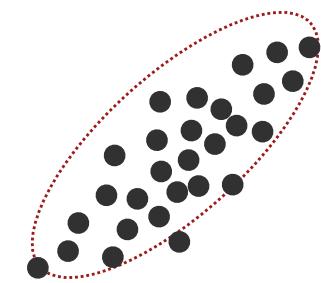


$$\Sigma = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$

Height, Income



$$\Sigma = \begin{pmatrix} 4 & 0 \\ 0 & 0.5 \end{pmatrix}$$

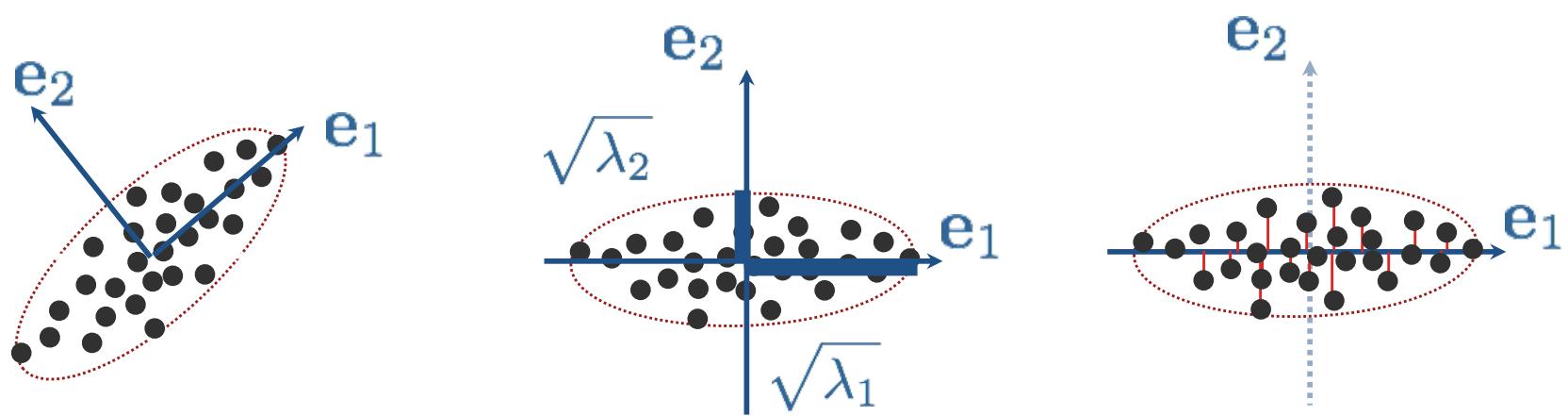


$$\Sigma = \begin{pmatrix} 2.45 & 1.2 \\ 1.2 & 2.1 \end{pmatrix}$$

Height, Weight

# PCA: decorrelation of random variables

- PCA: projection onto eigenvectors of covariance matrix



$$\Sigma = \begin{pmatrix} 2.45 & 1.2 \\ 1.2 & 2.1 \end{pmatrix} \quad \begin{pmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{pmatrix}$$

Dimensionality  
reduction by using  
only leading  
eigenvectors



## PCA: step by step

1. Compute the empirical mean and subtract it from the data, and compute empirical covariance matrix
2. Compute eigenvalue decomposition of the covariance matrix resulting in

$$\Lambda, E \quad \Sigma = E\Lambda E^T$$

3. Retain only the k eigenvectors with highest corresponding eigenvalues.



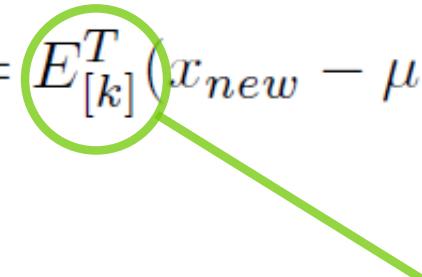
# PCA: step by step

4. Given a new input vector

$$x_{new} \in R^m$$

5. project it into the eigenspace

$$b_{new} = E_{[k]}^T (x_{new} - \mu) \in R^k$$

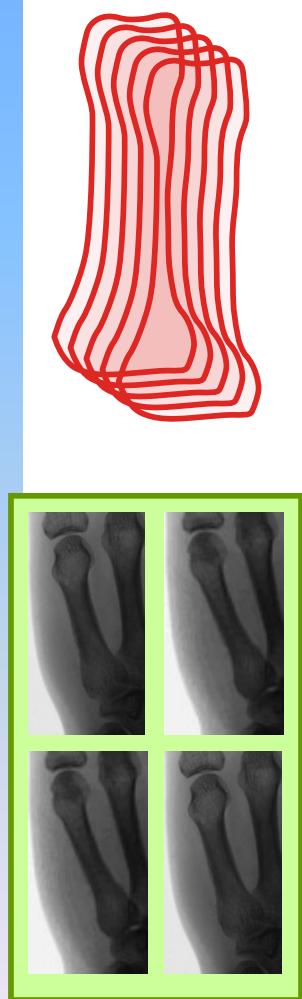


Only first k  
eigenvectors

6. resulting in the coefficient vector or parameter vector

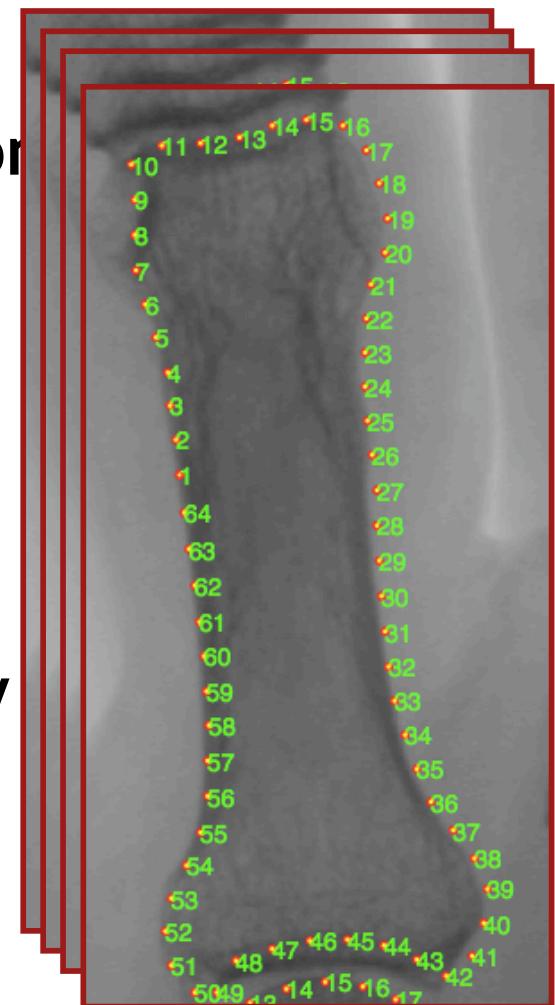
$$b_{new}$$

# Using PCA to model shape

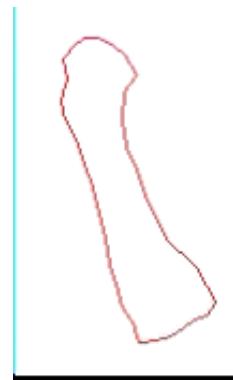
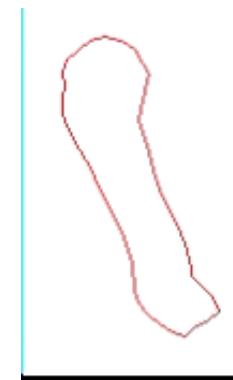
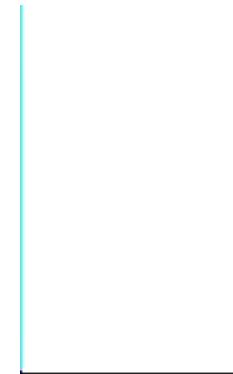
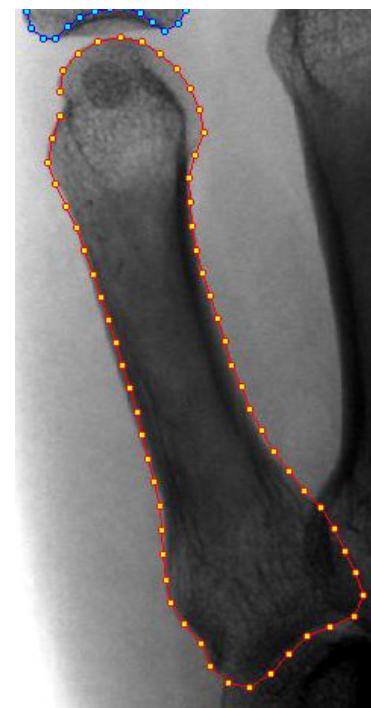
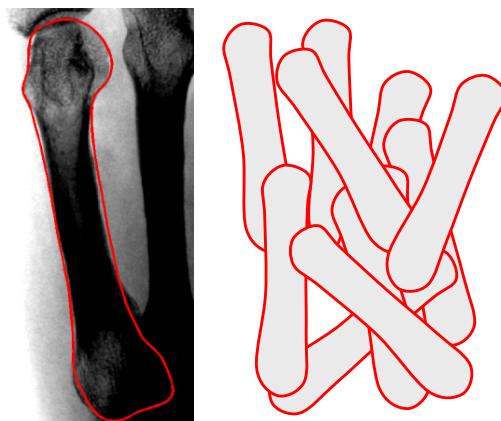


# Active shape models (ASM)

- A set of training examples (images)
- A set of landmarks, that are present on all images
- Build a statistical model of shape variation (PCA)
- Build a statistical model of the local texture (PCA)
- Use the model for the search in a new image



# ASM: model building

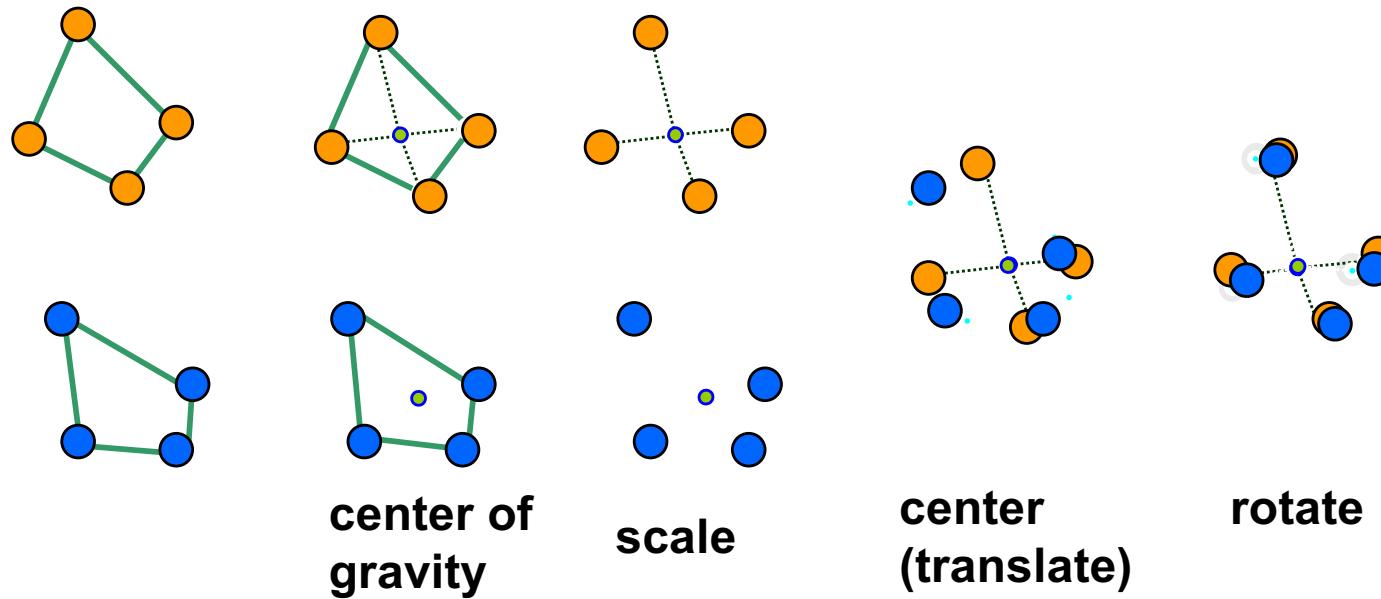


- shape
- texture
- orientation
- scale
- position

pose

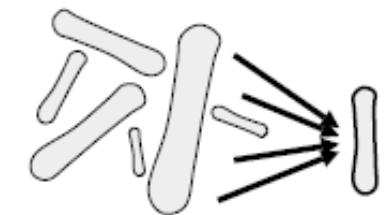
$$\mathbf{x}_i \in \mathbb{R}^{2m}$$

# ASM: alignment of examples



- The alignment removes rotation, scale and translation differences
- Minimizes Procrustes distance

# ASM: alignment of examples

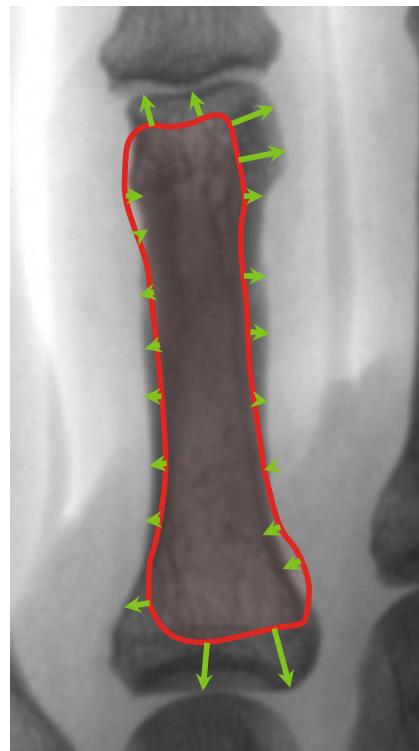


- Center all training shapes  $\mathbf{x}_i$
- Choose one example  $\mathbf{x}_j$  as initial mean shape  $\mathbf{x}_{mean}$  and scale  $|\mathbf{x}_{mean}| = 1$
- Align all shapes  $\mathbf{x}_i$  to  $\mathbf{x}_{mean}$  by minimizing the Procrustes distance
- Recalculate the mean shape  $\mathbf{x}_{mean}$  from the aligned set.
- Iterate until the mean shape converges

# ASM: shape model

- Given: a set of aligned shapes  $\{\mathbf{x}_1, \dots, \mathbf{x}_n\}$
- Perform PCA on the set of shapes, resulting in a set of Eigenvectors and corresponding Eigenvalues  $\mathbf{E} = (\mathbf{e}_1, \dots, \mathbf{e}_m)$   
 $\Lambda = (\lambda_1, \dots, \lambda_m)$
- Each shape can be reconstructed by  
$$\mathbf{x} = \mathbf{E}\mathbf{b} + \mathbf{m}_{mean}$$

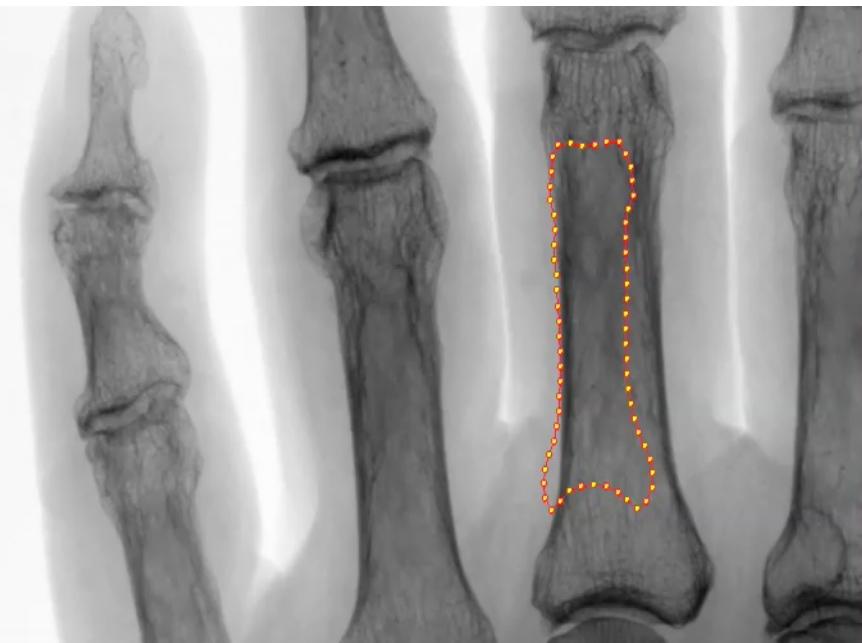
# ASM search



# ASM search: shape

- Update the instance according to shape model and pose
- Initialize  $\mathbf{b} = 0$
- Generate model pose instance  $\mathbf{x}' = \mathbf{E}\mathbf{b} + \mathbf{m}_{mean}$
- Find pose parameters to map  $\mathbf{x}'$  to  $\mathbf{x}$
- Project  $\mathbf{x}$  into the model coordinates
- Update model parameters  $\mathbf{b}$  to match  $\mathbf{x}$
- Apply constraints  $|b_i| < 3\sqrt{\lambda_i}$

# ASM search

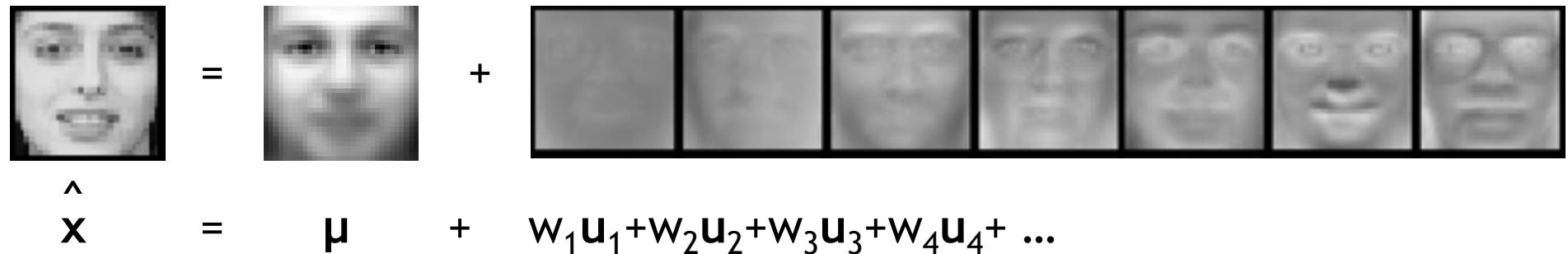


# Modelling the appearance

- To perform a search with the shape model, we have to capture the appearance, too.
  - Local appearance at the landmark positions:  
**Active shape model (ASM)**
  - Appearance of the enclosed texture  
**Active appearance model (AAM)**

# This lecture: models of shape and texture

- Active Shape Models
- Eigenfaces
- Active Appearance Models
- Class Projects

$$\hat{x} = \mu + w_1u_1 + w_2u_2 + w_3u_3 + w_4u_4 + \dots$$
The diagram illustrates the decomposition of a face image into a mean face and principal components. On the left, a grayscale portrait of a smiling man is shown. To its right is an equals sign. Next is a smaller version of the same face, representing the mean face ( $\mu$ ). To the right of the mean face is a plus sign. To the right of the plus sign is a vertical stack of seven grayscale images. The first six images are narrow strips representing the principal components (eigenfaces), and the seventh image is a wider strip representing the residual error or the difference between the original face and the reconstructed mean plus components.

# Face Recognition Problem



# Face Recognition Problem



[Sinha and Poggio 2002]

# Challenges: Image Variability

Short Term

Expression



Pose



Illumination

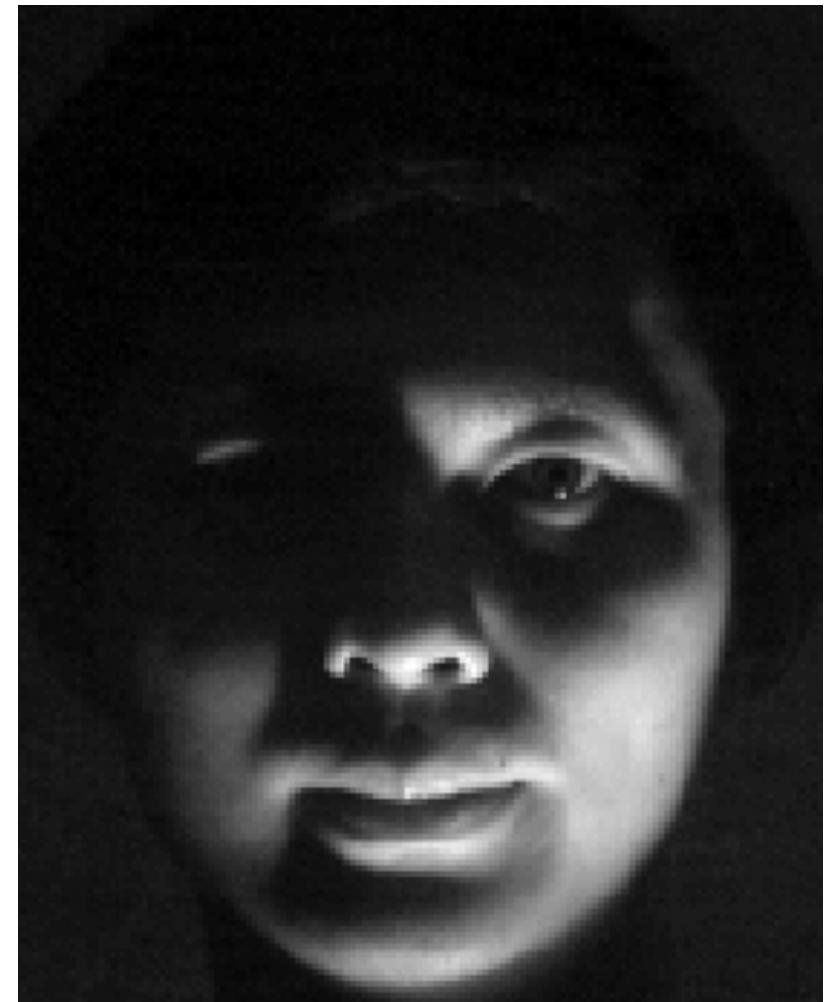
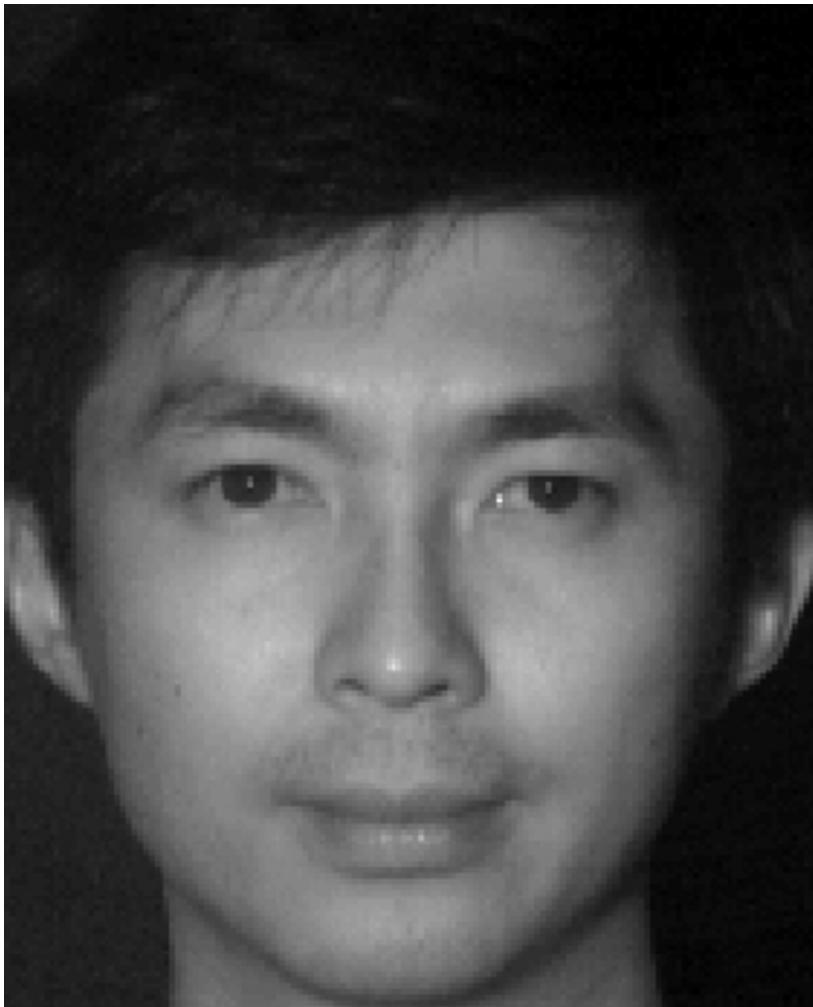


Long Term

- Facial Hair
- Makeup
- Eyewear

- Hairstyle
- Piercings
- Aging

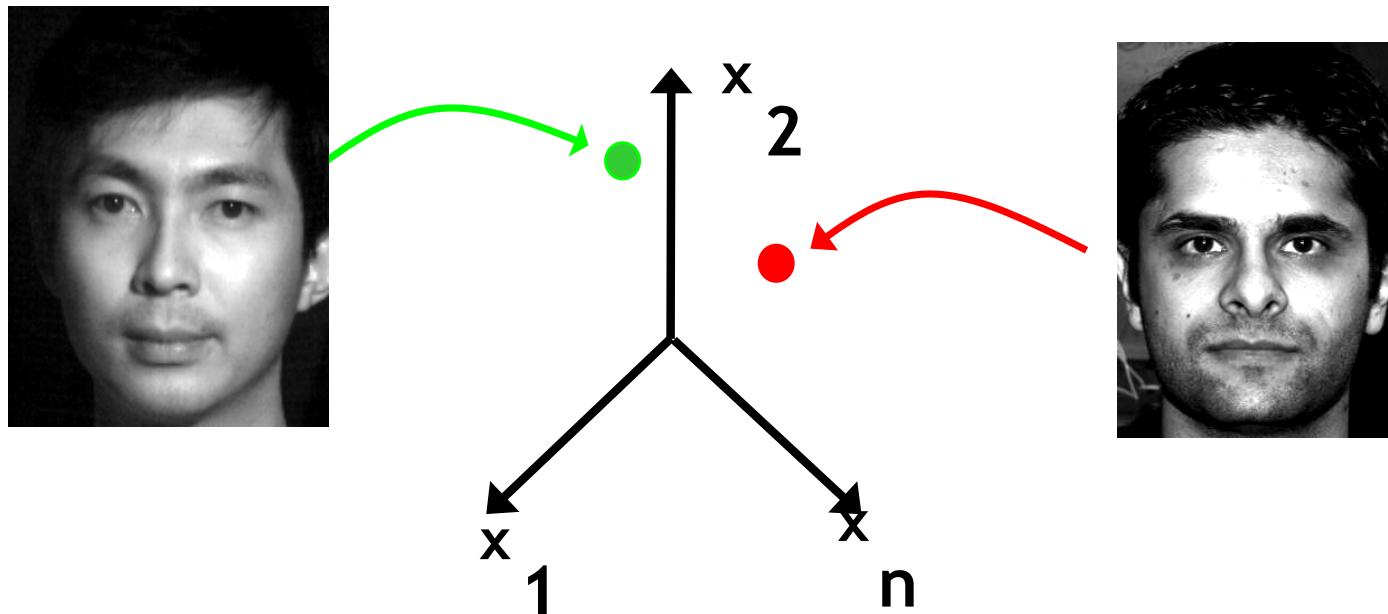
# Invariance Problem



# Invariance Problem

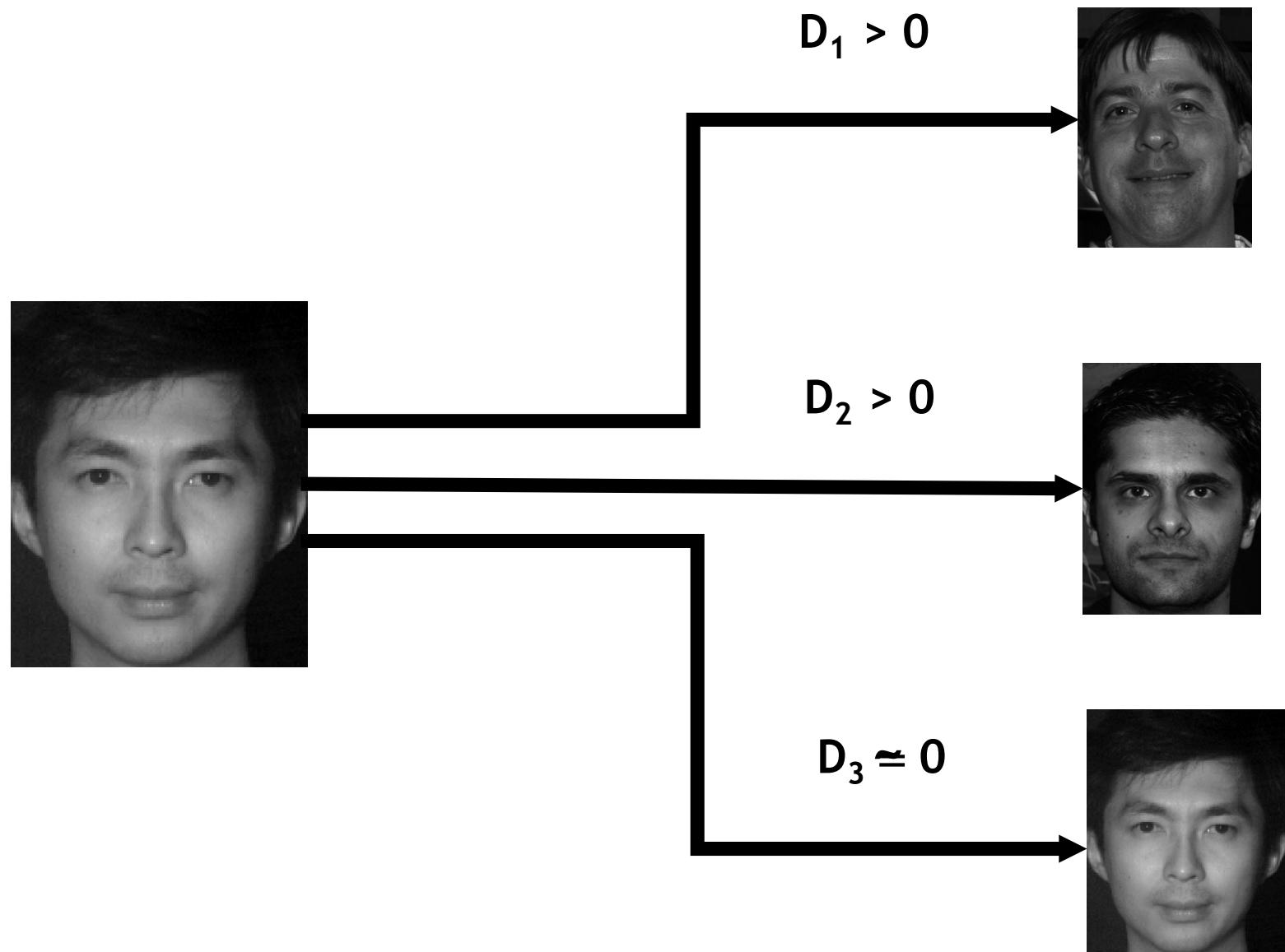


# Images as Points in Euclidean Space

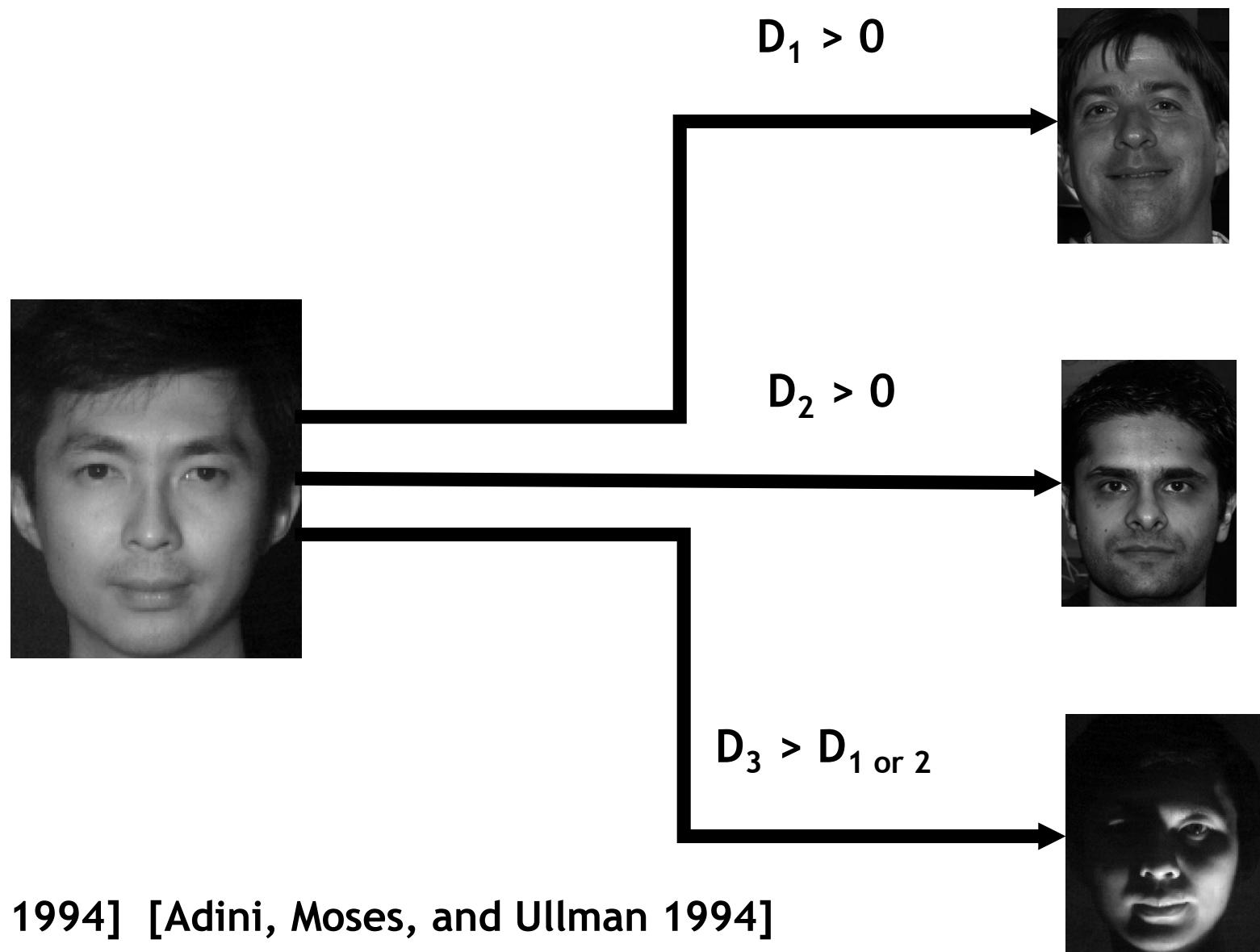


- Let an  $n$ -pixel image to be a point in an  $n$ -D space,  $x \in \mathbb{R}^n$ .
- Each pixel value is a coordinate of  $x$ .

# Face Recognition: Euclidean Distances



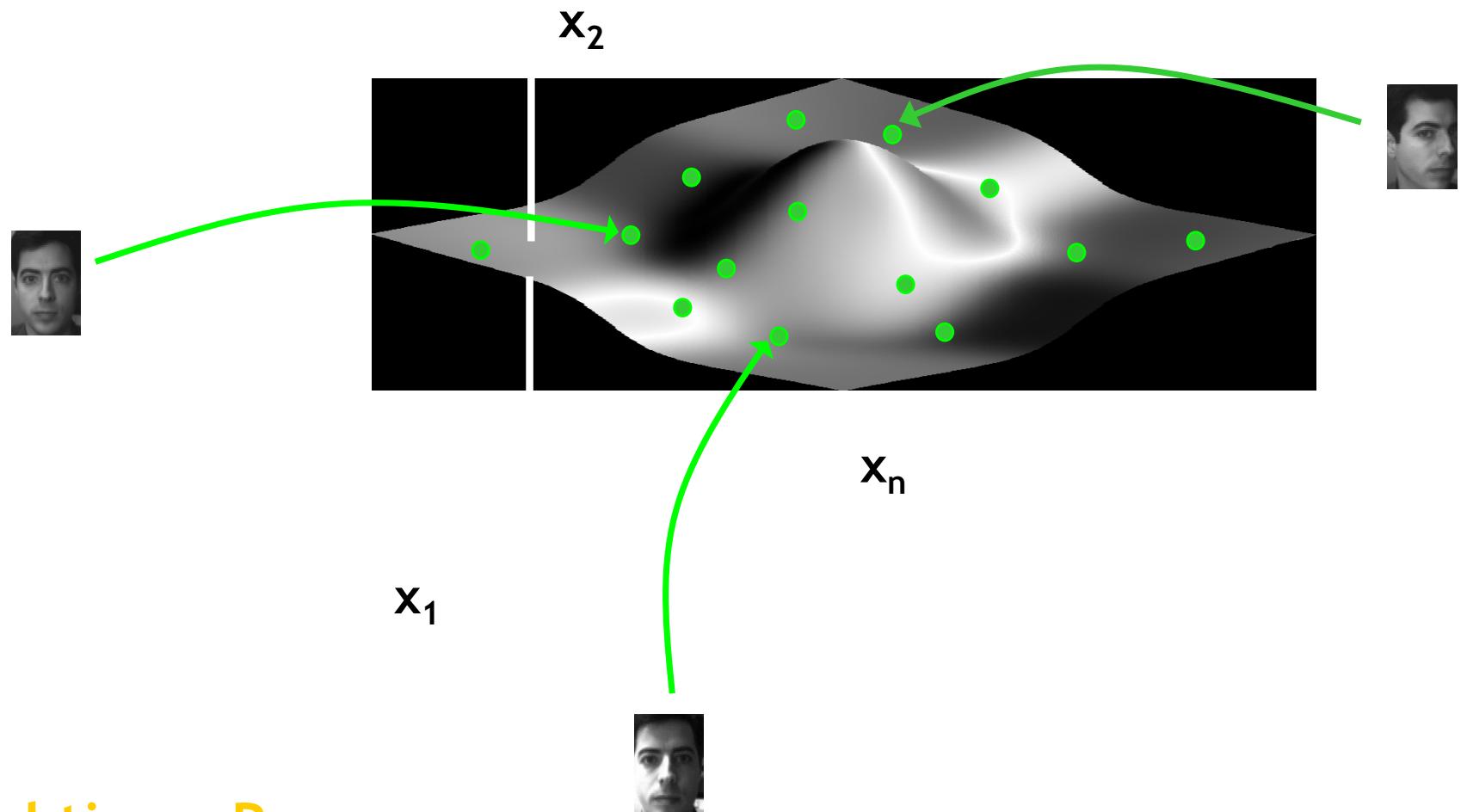
# Face Recognition: Euclidean Distances



# Nearest Neighbor Classifier

- Variations on distance function (e.g.  $L_1$ , robust distances)
- Multiple templates per class- perhaps many training images per class.
- Expensive to compute  $k$  distances, especially when each image is big ( $N$  dimensional).
- May not generalize well to unseen examples.
- Some solutions:
  - Bayesian classification
  - Dimensionality reduction

# Image Variability: Appearance Manifolds

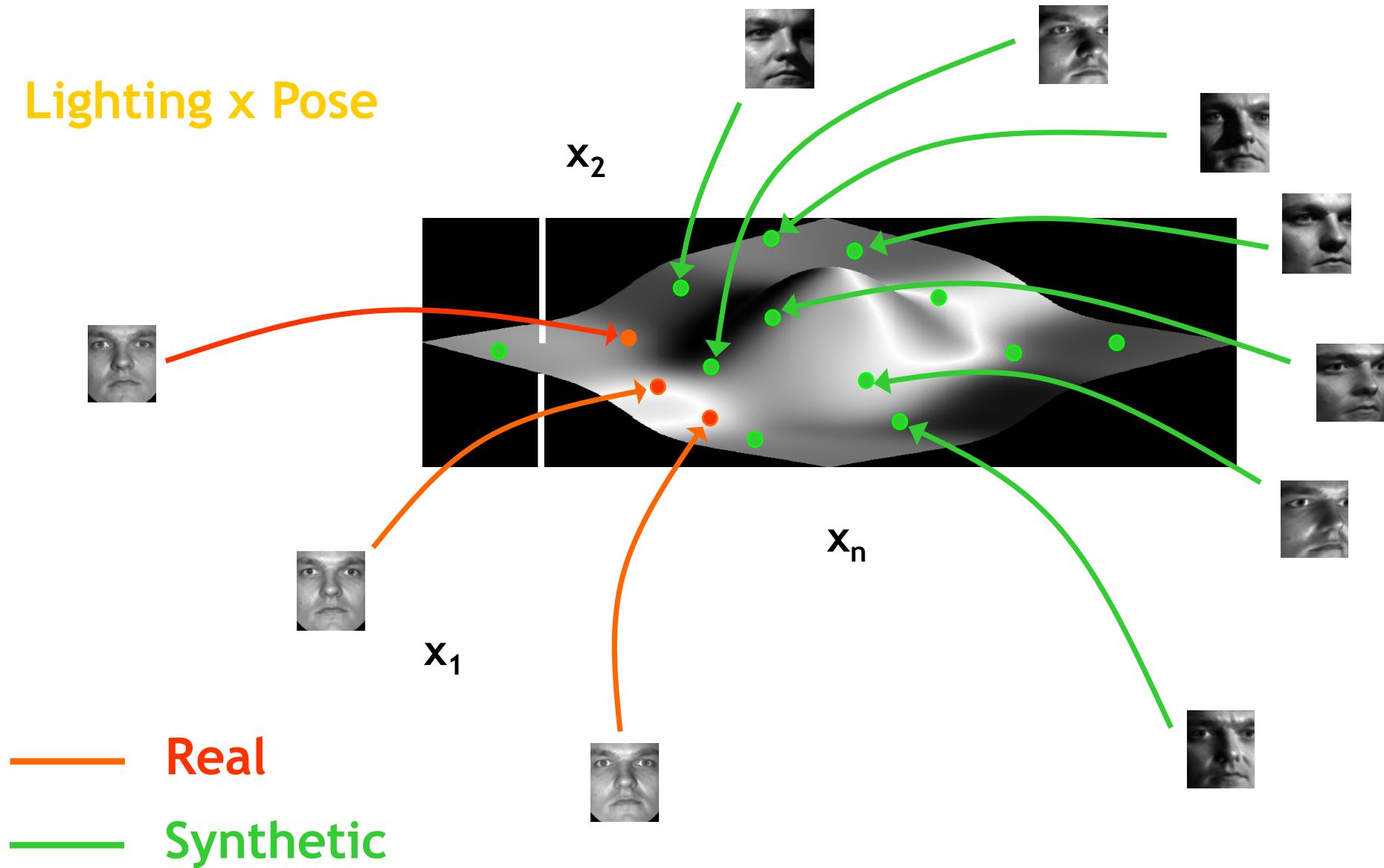


Lighting x Pose

[Murase and Nayar 1993]

# Image Variability: From Few to Many

Lighting x Pose



[Georghiades, Belhumeur, and Kriegman 1999]

# **Modeling Image Variability**

**Can we model illumination and pose variability in images of a face?**

**Yes, if we can determine the shape and texture of the face. But how?**

# Appearance modelling for faces

- When viewed as vectors of pixel values, face images are extremely high-dimensional
  - $100 \times 100$  image = 10,000 dimensions
- Very few vectors correspond to valid face images



- Original coordinates are not revealing about face properties
- We want to model the subspace of face images
- Same story as shape modelling....

# Eigenfaces: Key idea

- Assume that most face images lie on a low-dimensional subspace determined by the first  $k$  ( $k < d$ ) directions of maximum variance
- Use PCA to determine the vectors or “eigenfaces”  $u_1, \dots, u_k$  that span that subspace
- Represent all face images in the dataset as linear combinations of eigenfaces
- Same idea as shapes

# Eigenfaces example

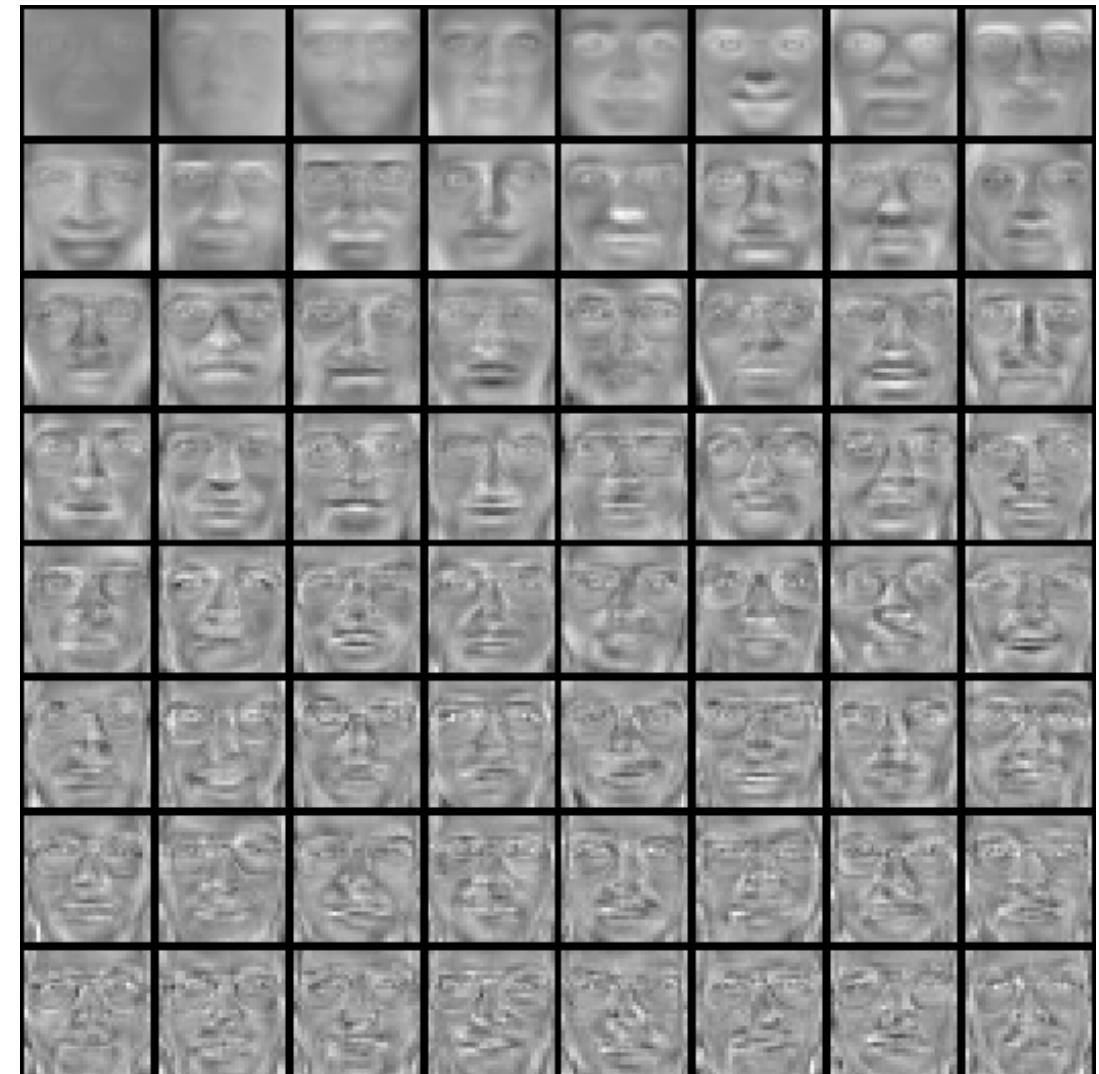
- Training images
- $\mathbf{x}_1, \dots, \mathbf{x}_N$



# Eigenfaces example

Top eigenvectors:  $u_1, \dots, u_k$

Mean:  $\mu$



# Eigenfaces example

Principal component (eigenvector)  $u_k$



$\mu + 3\sigma_k u_k$



$\mu - 3\sigma_k u_k$



# Eigenfaces example

- Face  $x$  in “face space” coordinates:



$$\begin{aligned} \mathbf{x} &\rightarrow [\mathbf{u}_1^T(\mathbf{x} - \boldsymbol{\mu}), \dots, \mathbf{u}_k^T(\mathbf{x} - \boldsymbol{\mu})] \\ &= w_1, \dots, w_k \end{aligned}$$

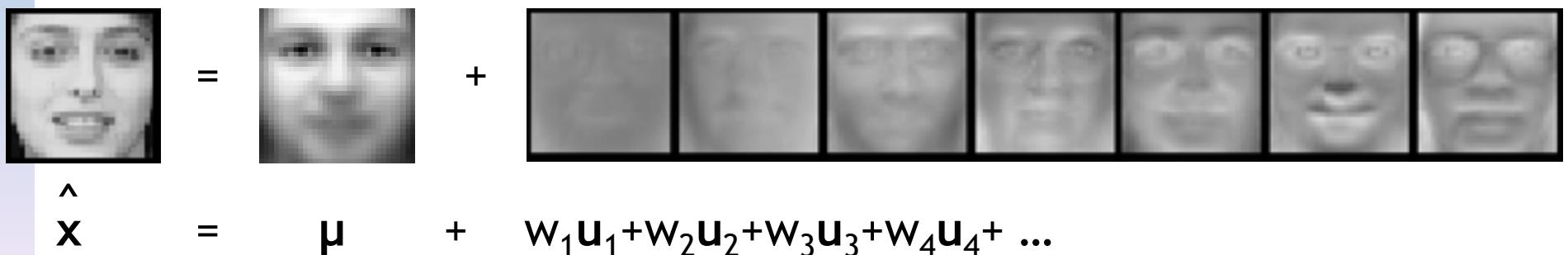
# Eigenfaces example

- Face  $x$  in “face space” coordinates:



$$\begin{aligned} \mathbf{x} &\rightarrow [\mathbf{u}_1^T(\mathbf{x} - \mu), \dots, \mathbf{u}_k^T(\mathbf{x} - \mu)] \\ &= w_1, \dots, w_k \end{aligned}$$

- Reconstruction:

$$\begin{aligned} \hat{\mathbf{x}} &= \hat{\mu} + \sum_{i=1}^k w_i \mathbf{u}_i \\ \hat{\mathbf{x}} &= \hat{\mu} + w_1 \mathbf{u}_1 + w_2 \mathbf{u}_2 + w_3 \mathbf{u}_3 + w_4 \mathbf{u}_4 + \dots \end{aligned}$$


# Recognition with eigenfaces

- Process labeled training images:
  - Find mean  $\mu$  and covariance matrix  $\Sigma$
  - Find  $k$  principal components (eigenvectors of  $\Sigma$ )  $u_1, \dots, u_k$
  - Project each training image  $x_i$  onto subspace spanned by principal components:  
$$(w_{i1}, \dots, w_{ik}) = (u_1^T(x_i - \mu), \dots, u_k^T(x_i - \mu))$$
- Given novel image  $x$ :
  - Project onto subspace:  
$$(w_1, \dots, w_k) = (u_1^T(x - \mu), \dots, u_k^T(x - \mu))$$
  - Check reconstruction error  $x - \hat{x}$  to determine whether image is really a face
  - Classify as closest training face in  $k$ -dimensional subspace

# Challenges addressed by Eigenfaces

Short Term

Expression



Pose



Illumination



Long Term

- Facial Hair
- Makeup
- Eyewear

- Hairstyle
- Piercings
- Aging

# Limitations

- Global appearance method: not robust to misalignment, background variation



### Offline Training Phase:

Input a set  $I$  of  $M$  labeled training images and produce a basis set  $B$  and a vector of coefficients for each image.

$I = \{I_1, I_2, \dots, I_M\}$  is the set of training images. (input)

$B = \{F_1, F_2, \dots, F_m\}$  is the set of basis vectors. (output)

$A_j = [a_{j1}, a_{j2}, \dots, a_{jm}]$  is the vector of coefficients for image  $I_j$ . (output)

1.  $I_{mean} = mean(I)$ .
2.  $\Phi = \{\Phi_i | \Phi_i = I_i - I_{mean}\}$ , the set of difference images
3.  $\Sigma_\Phi$  = the covariance matrix obtained from  $\Phi$ .
4. Use the principal components method to compute eigenvectors and eigenvalues of  $\Sigma_\Phi$ . (see text)

5. Construct the vector  $\mathbf{B}$  as the basis set by selecting the most significant  $m$  eigenvectors; start from the largest eigenvalue and continue in decreasing order of the eigenvalues to select the corresponding eigenvectors.
6. Represent each training image  $I_j$  by a linear combination of the basis vectors:  
$$I_j^m = a_{j1}F_1 + a_{j2}F_2 + \dots + a_{jm}F_m$$

#### Online Recognition Phase:

Input the set of basis vectors  $B$ , the database of coefficient sets  $\{A_j\}$ , and a test image  $I_u$ . Output the class label of  $I_u$ .

1. Compute vector of coefficients  $A_u = [a_{u1}, a_{u2}, \dots, a_{um}]$  for  $I_u$ ;
2. Find the  $h$  nearest neighbors of vector  $A_u$  in the set  $\{A_j\}$ ;
3. Decide the class of  $I_u$  from the labels of the  $h$  nearest neighbors (possibly reject in case neighbors are far or inconsistent in labels);

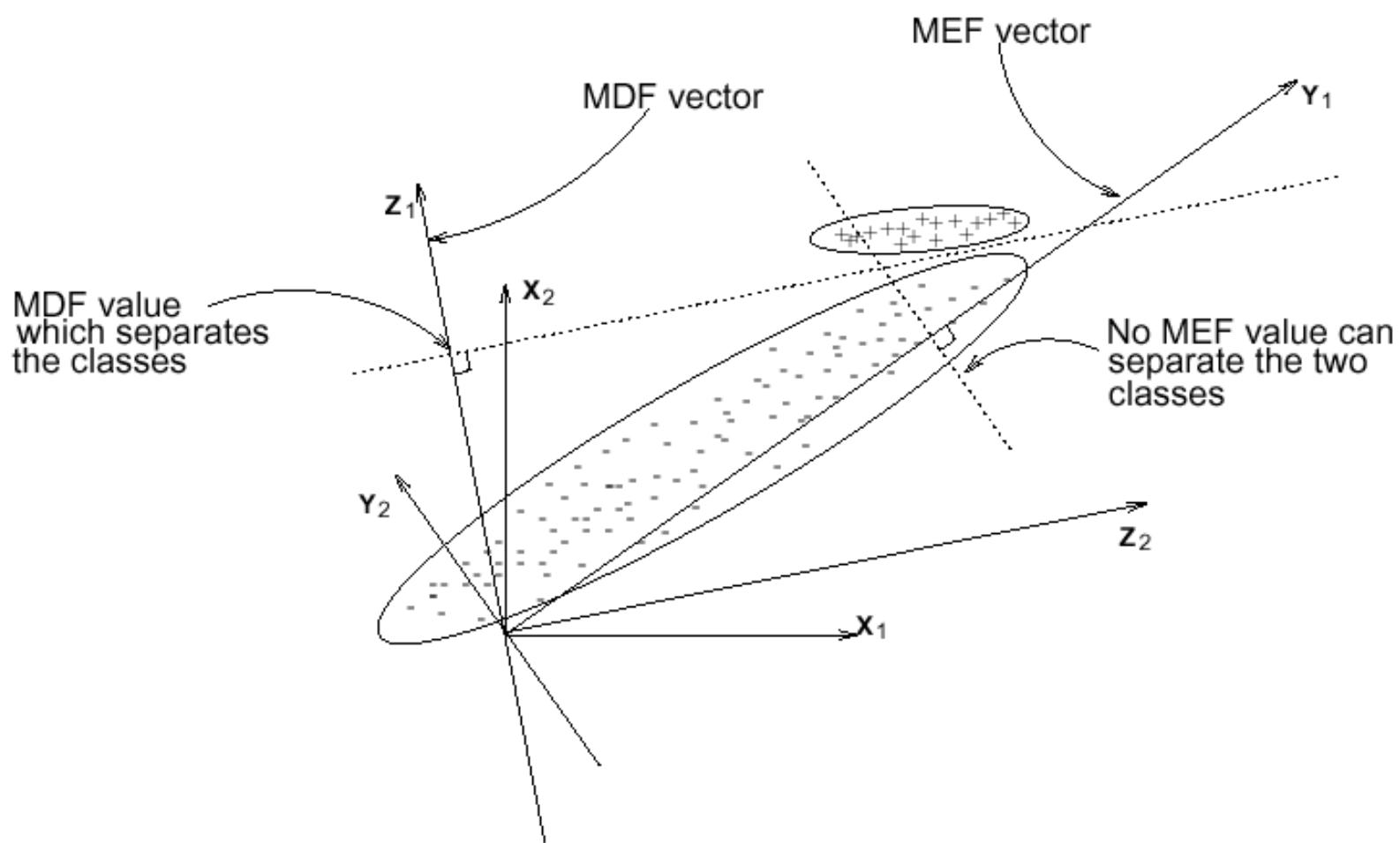


Figure 14.40: The most expressive features determined by the eigenvectors of the scatter matrix represent the data well, but may not represent the differences between classes well. Discriminant analysis can be used to find subspaces that emphasize differences between classes. (Figure contributed by J. Swets and J. Weng.)

# Linear Discriminant Analysis

- We wish to choose linear functions of the features that allow good discrimination.
  - Assume class-conditional covariances are the same
  - Want linear feature that maximises the spread of class means for a fixed within-class variance

**Algorithm 22.6:** Canonical variates identifies a collection of linear features that separating the classes as well as possible.

Assume that we have a set of data items of  $g$  different classes. There are  $n_k$  items in each class, and a data item from the  $k$ 'th class is  $\mathbf{x}_{k,i}$ , for  $i \in \{1, \dots, n_k\}$ . The  $j$ 'th class has mean  $\boldsymbol{\mu}_j$ . We assume that there are  $p$  features (i.e. that the  $\mathbf{x}_i$  are  $p$ -dimensional vectors).

Write  $\overline{\boldsymbol{\mu}}$  for the mean of the class means, i.e.

$$\overline{\boldsymbol{\mu}} = \frac{1}{g} \sum_{j=1}^g \boldsymbol{\mu}_j$$

Write

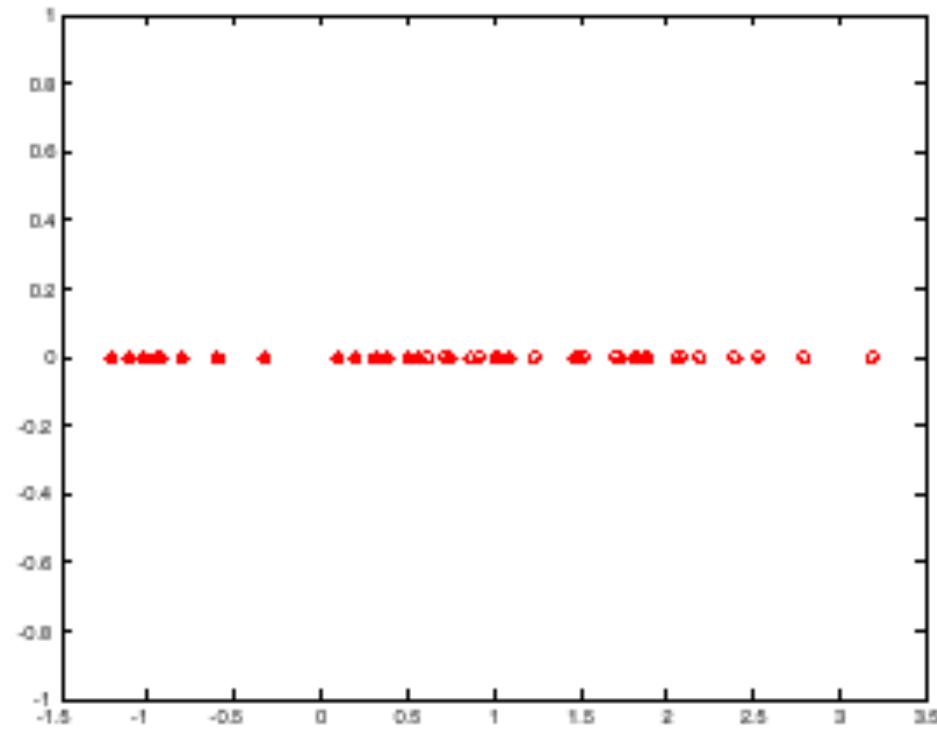
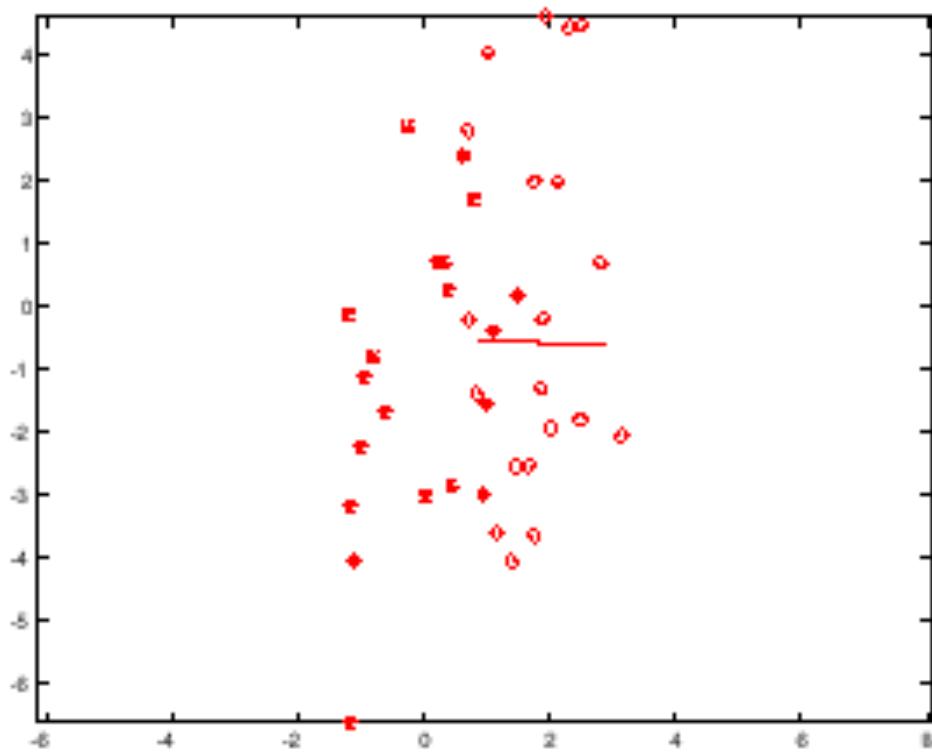
$$\mathcal{B} = \frac{1}{g-1} \sum_{j=1}^g (\boldsymbol{\mu}_j - \overline{\boldsymbol{\mu}})(\boldsymbol{\mu}_j - \overline{\boldsymbol{\mu}})^T$$

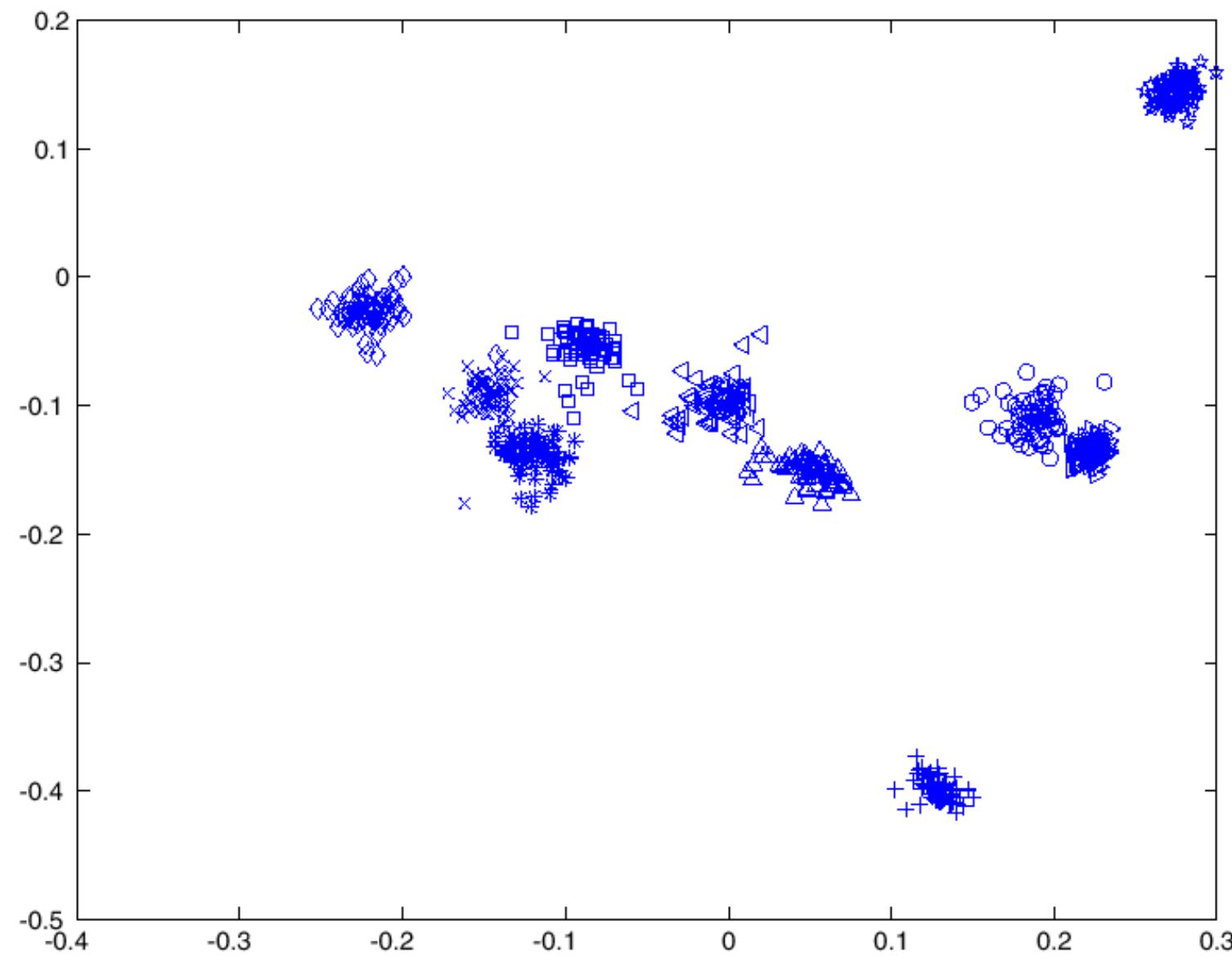
Assume that each class has the same covariance  $\Sigma$ , which is either known or estimated as

$$\Sigma = \frac{1}{N-1} \sum_{c=1}^g \left\{ \sum_{i=1}^{n_c} (\mathbf{x}_{c,i} - \boldsymbol{\mu}_c)(\mathbf{x}_{c,i} - \boldsymbol{\mu}_c)^T \right\}$$

The unit eigenvectors of  $\Sigma^{-1}\mathcal{B}$  — which we write as  $\mathbf{v}_1, \mathbf{v}_2, \dots, \mathbf{v}_d$ , where the order is given by the size of the eigenvalue and  $\mathbf{v}_1$  has the largest eigenvalue — give a set of features with the following property:

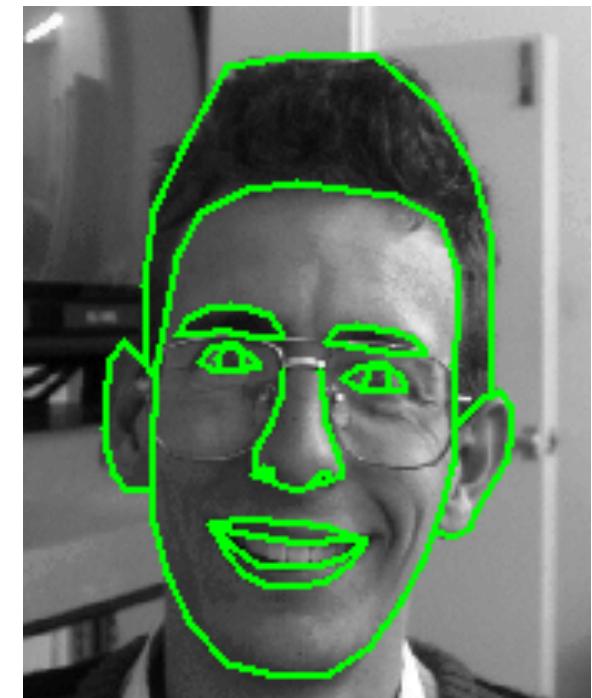
- Projection onto the basis  $\{\mathbf{v}_1, \dots, \mathbf{v}_k\}$  gives the  $k$ -dimensional set of linear features that best separates the class means.





# This lecture: models of shape and texture

- Active Shape Models
- Eigenfaces
- **Active Appearance Models**
- Class Projects



# Challenges: Image Variability

Short Term

Expression



Pose



Illumination

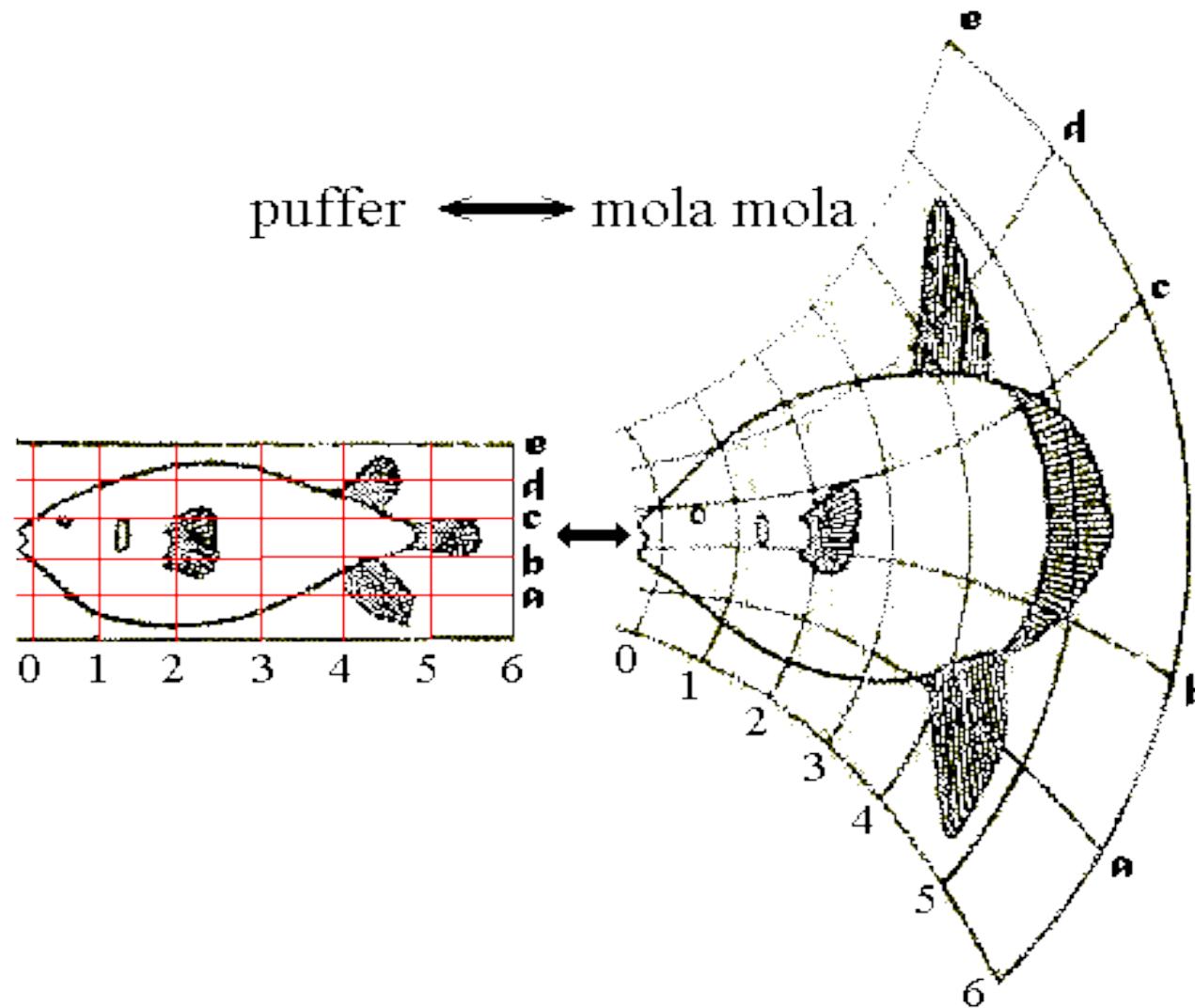


Long Term

- Facial Hair
- Makeup
- Eyewear

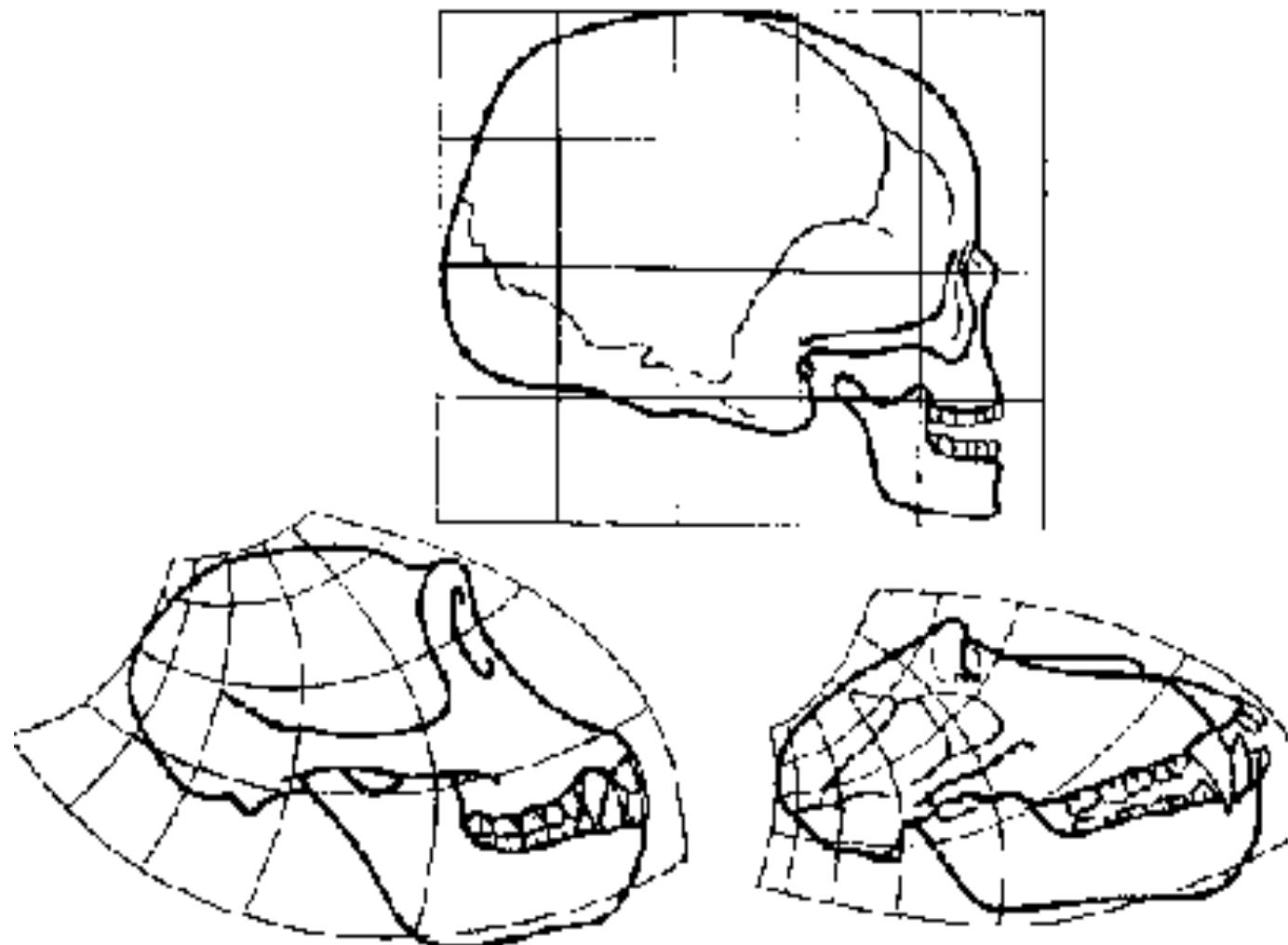
- Hairstyle
- Piercings
- Aging

# Modelling Shape Variability via Deformations



D'Arcy Thompson, “On Growth and Form” (1917)

# Modelling Shape Variability via Deformations



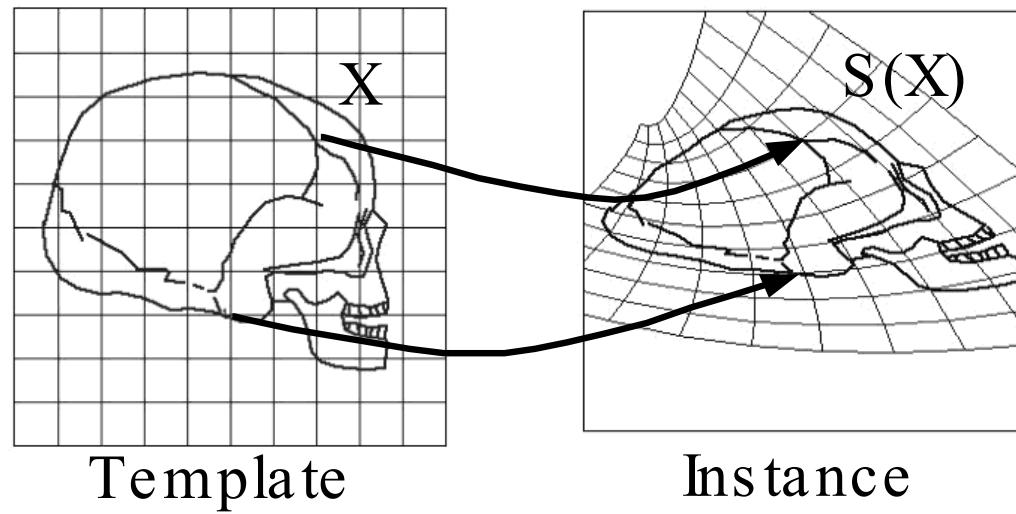
Skulls of a human, a chimpanzee and a baboon  
and transformations between them

D'Arcy Thompson, "On Growth and Form" (1917)

# Active Appearance Models

- *Apearance = Shape + Texture*
- *Shape:* deformation from ‘template’ domain to instance domain

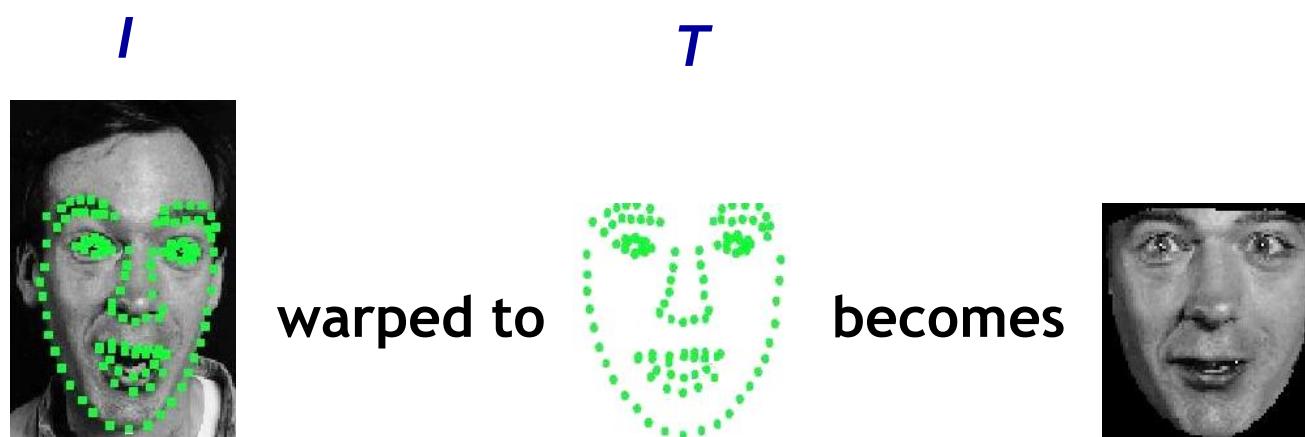
$$I(S(x)) = T(x)$$



- *Texture:* intensity (or color) patch of an image in the template domain.

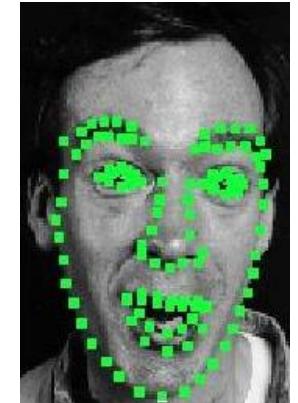
# Shape-free texture

- An attempt to eliminate texture variation due to shape
- Given instance  $I$  and a reference “template”  $T$  we warp our image so that points of  $I$  move into the corresponding points of  $T$

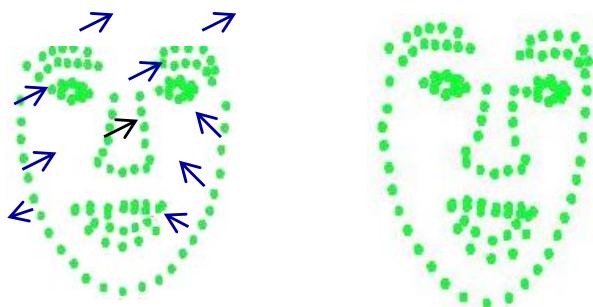


# AAM training

- Training set: annotated grayscale images



Shape: displacements  
from mean shape



PCA

Optional:  
Interpolate to recover  
dense deformation field

Model of shape

Texture (shape-free)

PCA



Model of texture

# Active Appearance Models

**Shape:**

$$\mathcal{S}(\mathbf{x}; \mathbf{s}) = \sum_i \mathbf{s}_i S_i(\mathbf{x}),$$

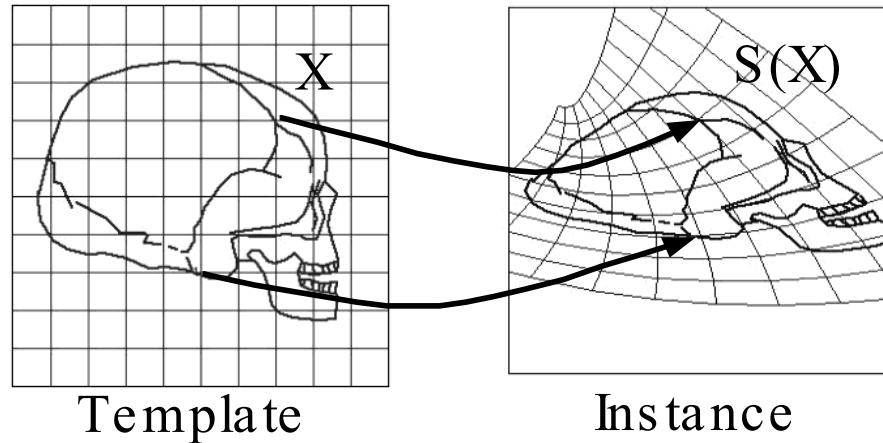
**Appearance:**

$$\mathcal{T}(\mathbf{x}; \mathbf{t}) = \sum_i \mathbf{t}_i T_i(\mathbf{x})$$

**Synthesis:**

$$I(\mathcal{S}(\mathbf{x}; \mathbf{s})) \simeq \mathcal{T}(\mathbf{x}; \mathbf{t})$$

$$I(\mathcal{S}(\mathbf{x})) = \mathcal{T}(\mathbf{x})$$



# AAM model

- Shape Eigenvectors



- Texture Eigenvectors



# Playing with the Parameters

- 3 s.d. ----- + 3 s.d.



First two modes of shape variation

- 3 s.d. ----- + 3 s.d.



First two modes of gray-level variation



First four  
modes of  
appearance  
variation

# Active Appearance Model fitting

Given:

- 1) an appearance model,
- 2) a new image,
- 3) a starting approximation

Find:

the best matching  
synthetic image

- **Minimize reconstruction error**

$$E(\mathbf{s}, \mathbf{t}) = \sum_{\mathbf{x}} [I(\mathcal{S}(\mathbf{x}; \mathbf{s})) - \mathcal{T}(\mathbf{x}; \mathbf{t})]^2$$

- **How?**
  - Alternate between estimating  $\mathbf{s}$  and  $\mathbf{t}$
- **For  $\mathbf{t}$ :** projection of deformed image  $I(\mathcal{S}(\mathbf{x}; \mathbf{s}))$  onto PCA basis
- **For  $\mathbf{s}$ ?**

# AAM parameter estimation: shape

- Iterative scheme (Newton-Raphson minimization)

$$E(\mathbf{s}, \mathbf{t}) = \sum_{\mathbf{x}} [I(\mathcal{S}(\mathbf{x}; \mathbf{s})) - \mathcal{T}(\mathbf{x}; \mathbf{t})]^2$$

$$E(\mathbf{s} + \Delta \mathbf{s}, \mathbf{t}) = E(\mathbf{s}, \mathbf{t}) + \mathcal{J}\Delta \mathbf{s} + \frac{1}{2} \Delta \mathbf{s}^T \mathcal{H} \Delta \mathbf{s}$$

$$\Delta \mathbf{s}^* = -\mathcal{J}\mathcal{H}^{-1} \quad \mathbf{s}' = \mathbf{s} - \mathcal{J}\mathcal{H}^{-1}$$

$$I(S(\mathbf{x}; \mathbf{s} + \Delta \mathbf{s})) \simeq I(S(\mathbf{x}; \mathbf{s})) + \sum_{i=1}^{N_S} \frac{dI}{d\mathbf{s}_i}(\mathbf{x}; \mathbf{s}) \Delta \mathbf{s}_i$$

$$\frac{dI}{d\mathbf{s}_i}(\mathbf{x}; \mathbf{s}) = \frac{\partial I(S(\mathbf{x}; \mathbf{s}))}{\partial x} \frac{\partial S_x}{\partial \mathbf{s}_i} + \frac{\partial I(S(\mathbf{x}; \mathbf{s}))}{\partial y} \frac{\partial S_y}{\partial \mathbf{s}_i},$$

$$\mathcal{J}_i = \sum_x [I(S(\mathbf{x}, \mathbf{s})) - T(\mathbf{x}, \mathbf{t})] \frac{dI}{d\mathbf{s}_i}(x) \quad \mathcal{H}_{i,j} = \sum_x \frac{dI}{d\mathbf{s}_i}(x) \frac{dI}{d\mathbf{s}_j}(x)$$

# Active Appearance Model Search (Results)



# Model fitting + Image segmentation

- AAM fitting

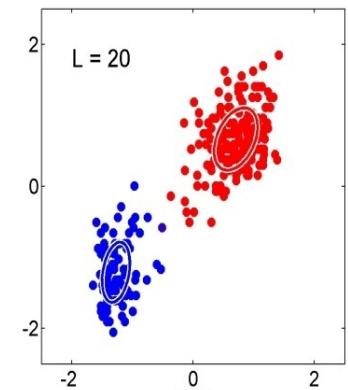


- Variational Segmentation



# Model fitting + Image segmentation

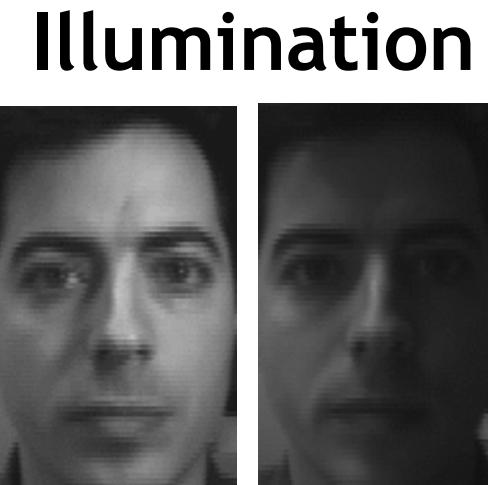
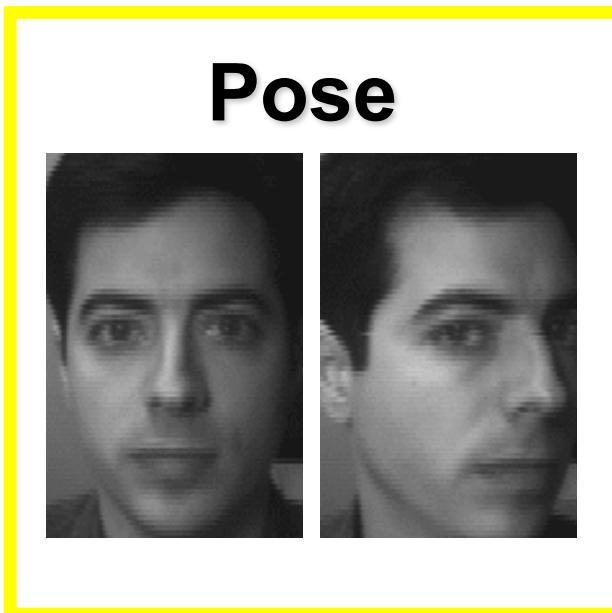
- **EM formulation**
  - **E-step: Assign data to models**
  - **M-step: Estimate model parameters**
- **Joint segmentation & recognition**
  - **E-step: segmentation**
  - **M-step: deformable model fitting**



# Challenges: Image Variability



Short Term



Long Term

- Facial Hair
- Makeup
- Eyewear

- Hairstyle
- Piercings
- Aging

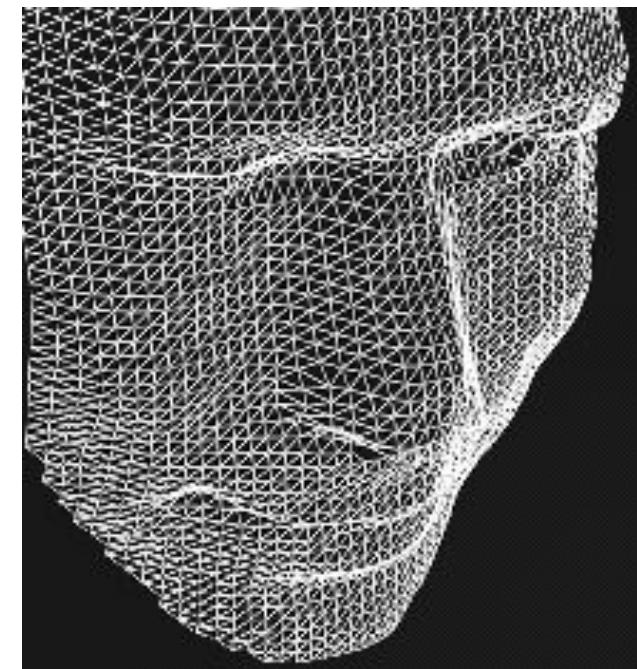
# Modeling Image Variability: 3-D Faces

Laser Range Scanners

Stereo Cameras

Structured Light

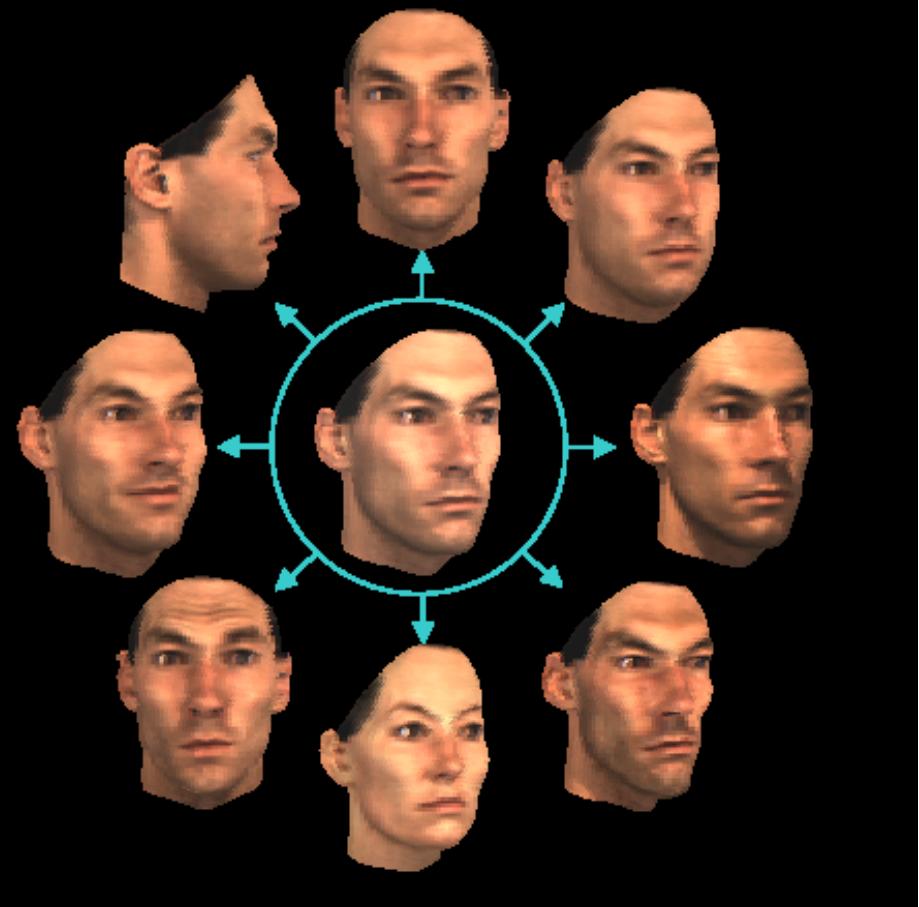
Photometric Stereo



# What can we do with 3d shape?

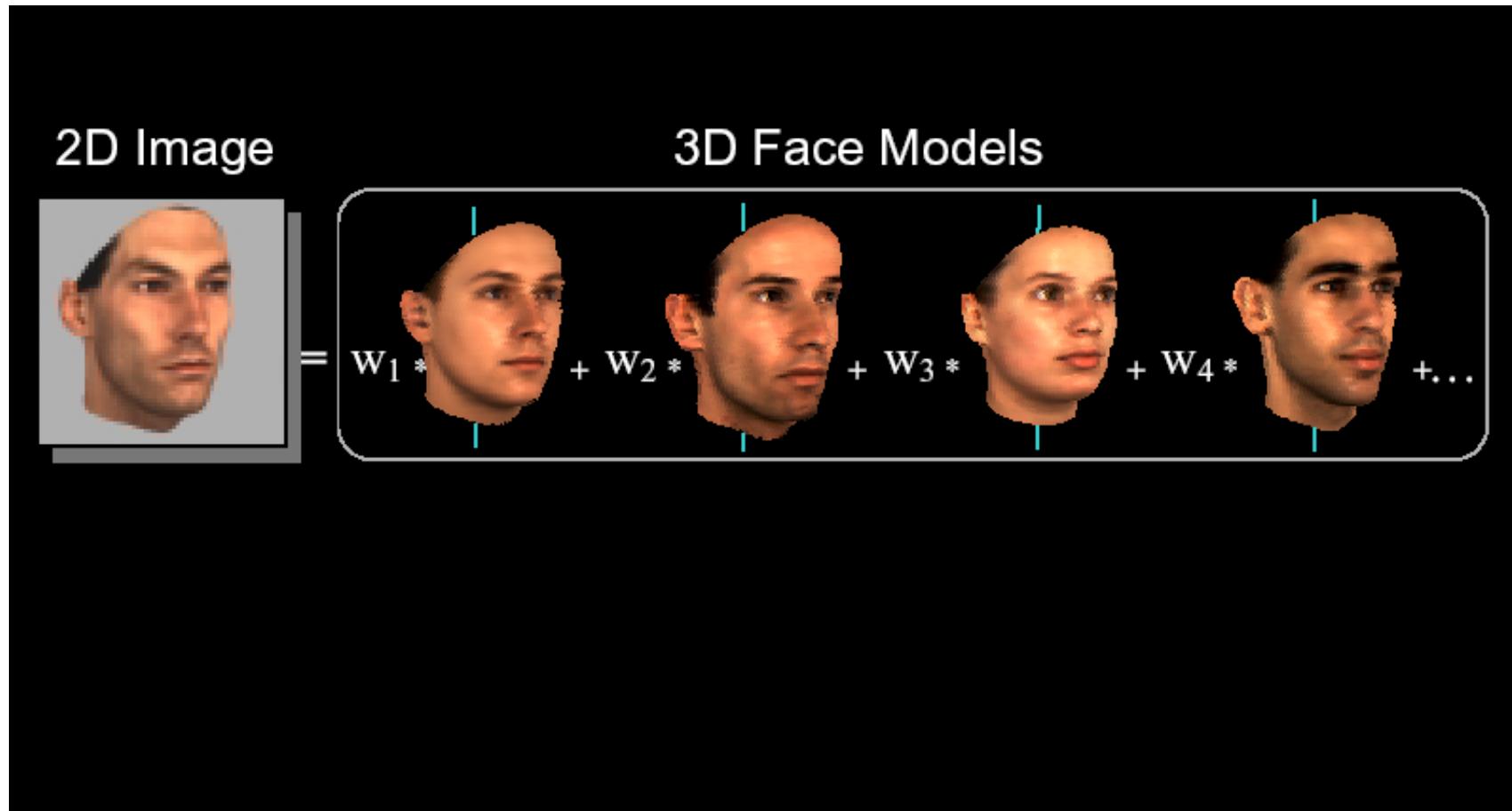
From a single image

- Novel views
- Novel expressions
- Synthesis of siblings
- Change of illumination
- Variations of body weight



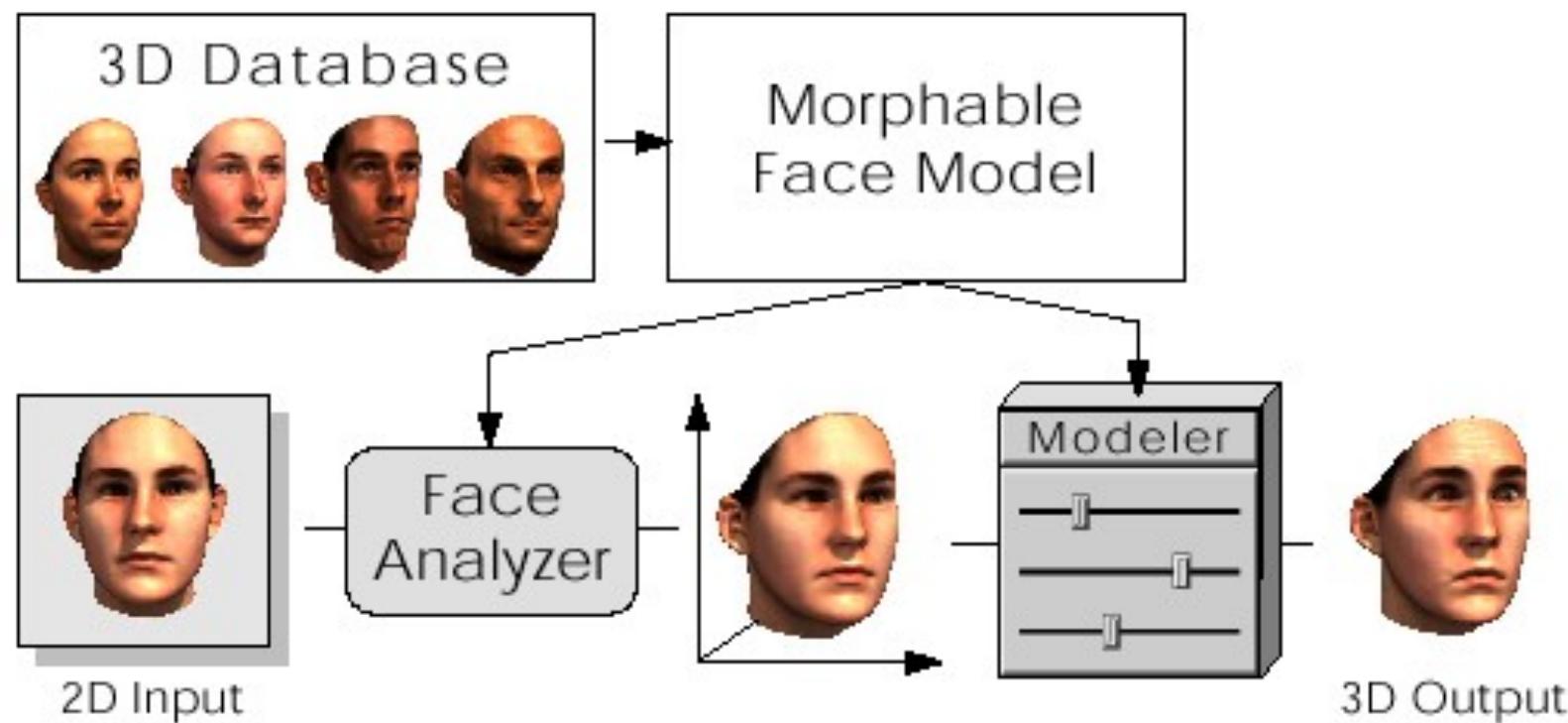
[Blanz and Vetter 1999, 2003]

# Building a Morphable Face Model



[Blanz and Vetter 1999, 2003]

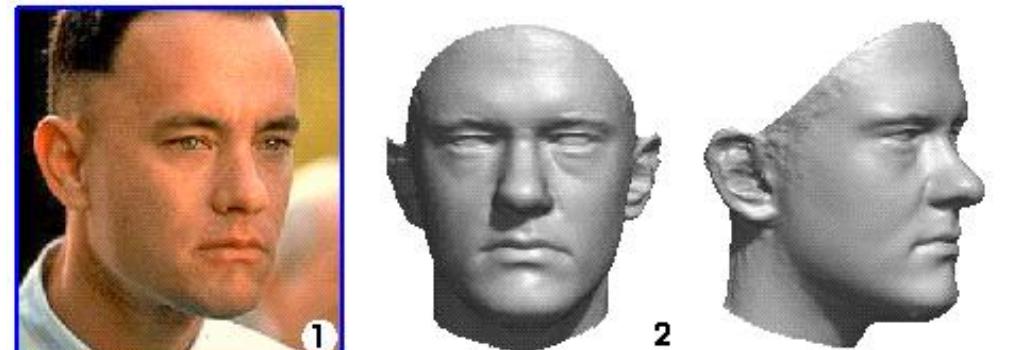
# 3-D Morphable Models



[Blanz and Vetter 1999, 2003]

# 3D Morphable models

Recover Shape



Synthesize new views



Synthesize new expressions

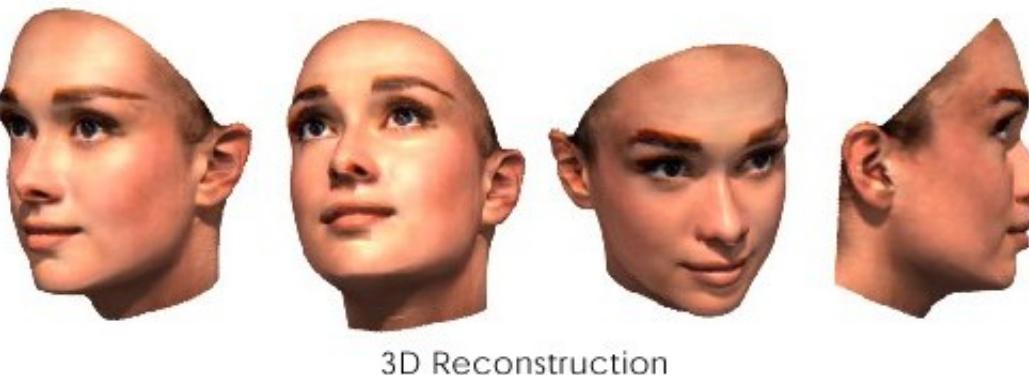


# 3-D Morphable Models fitting

- **Rough manual initialization**
- **Gradient descent to minimize reconstruction error functional**

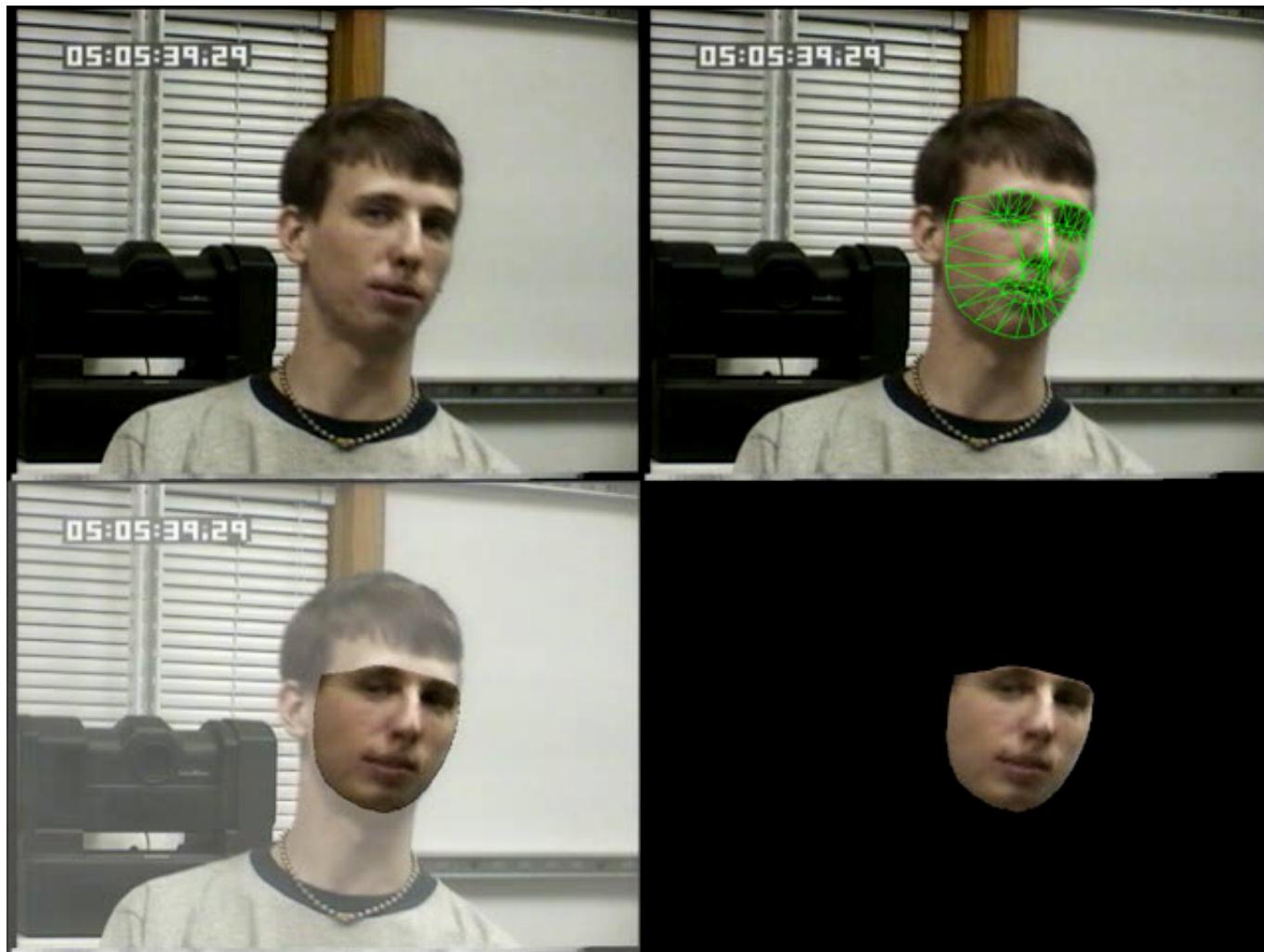


- **And then**



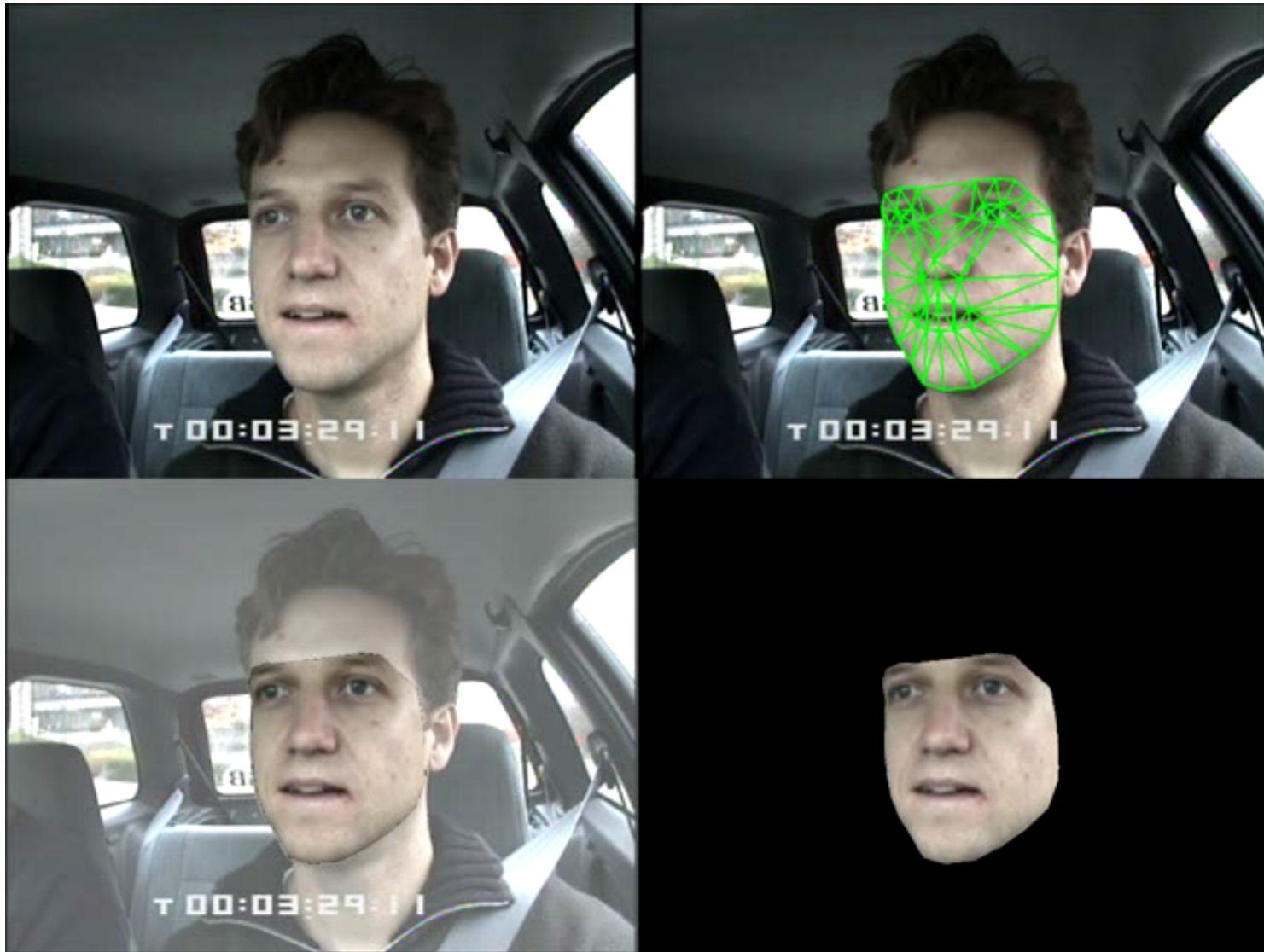
3D Reconstruction

# 3D AAM for face tracking



CMU group: I. Matthews, S. Baker, R. Gross  
(230 Frames per second)

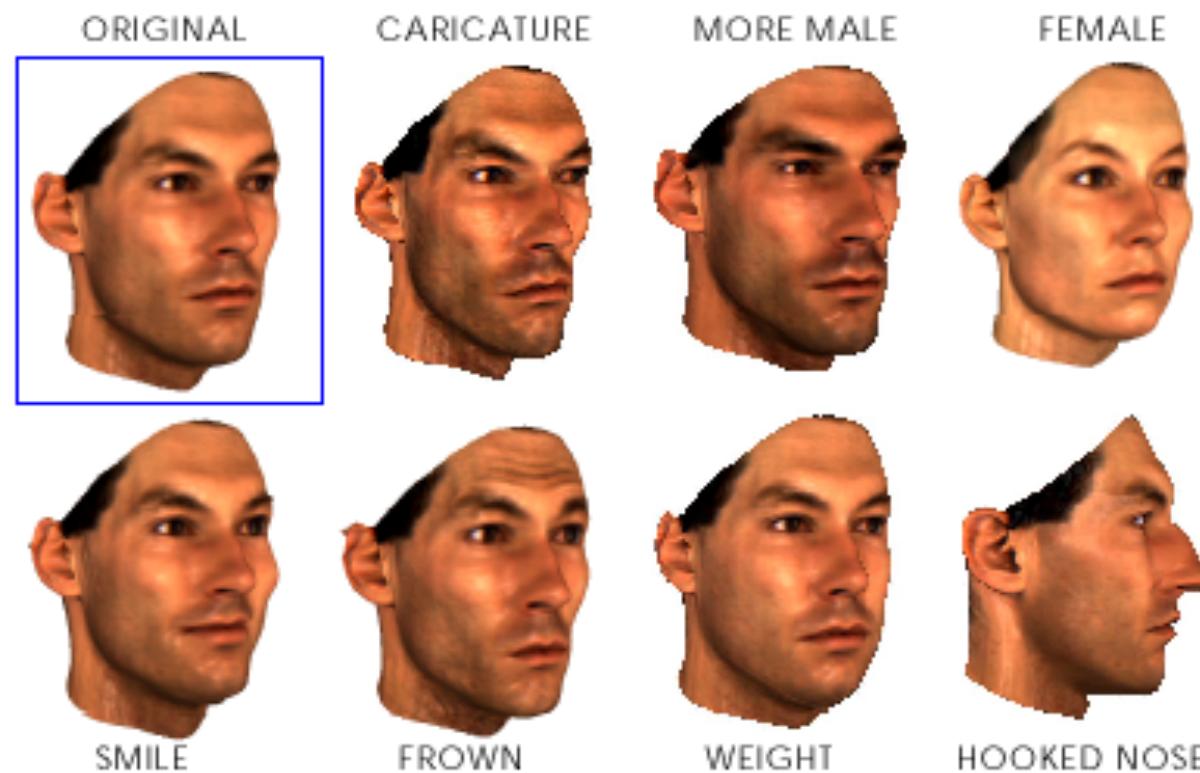
# 3D AAM for face tracking



# Playing with Facial Attributes

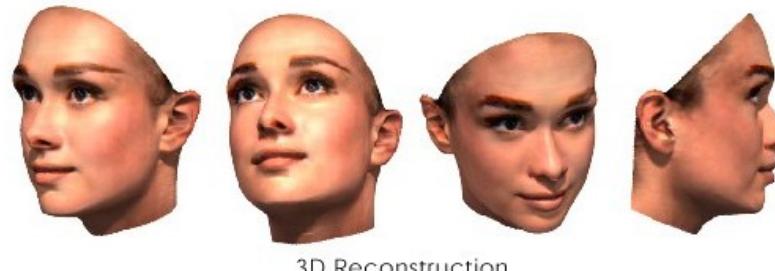
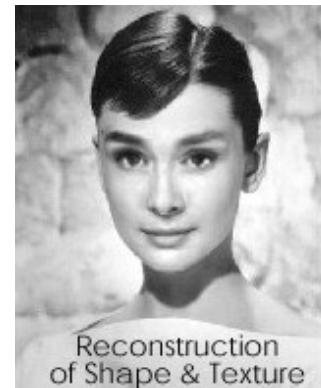
Several classes of attributes are modeled:

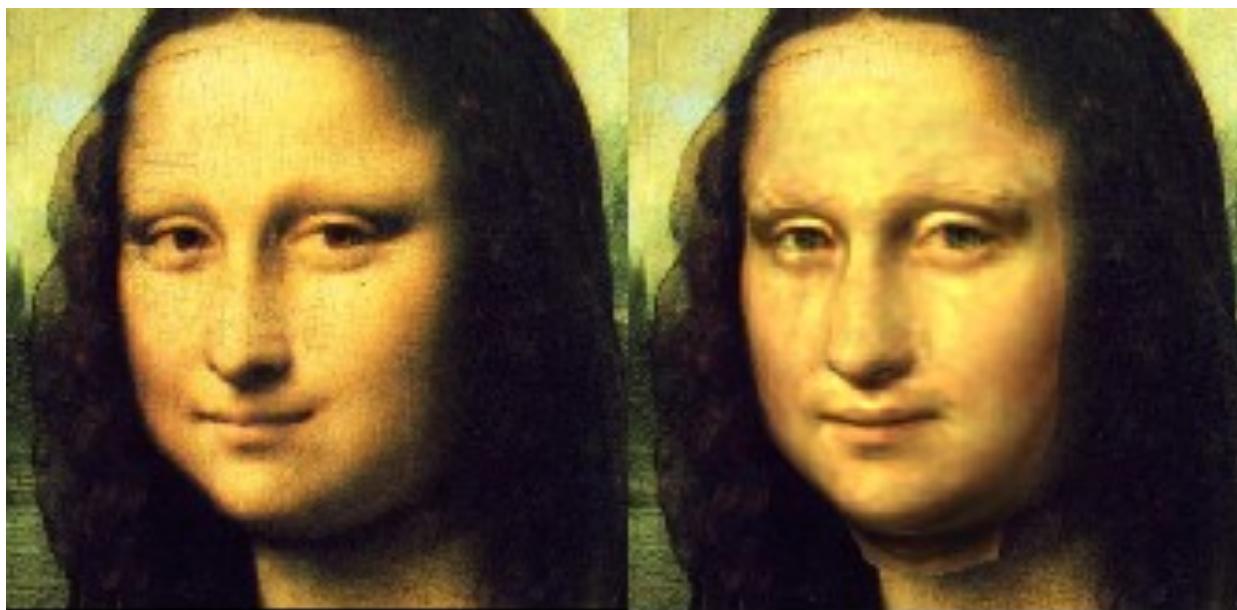
- Facial expressions (smile, frown)
- Individual characteristics (double chin, hooked nose, ‘maleness’ )
- Distinctiveness



# Manipulating Facial Attributes via Deformations

- For each face in the database, two scans are recorded:  $S_{neutral}$ , and  $S_{expression}$ .
- The difference vector  $\Delta S = S_{expression} - S_{neutral}$  is saved and later on simply added to the 3D reconstruction of the input image.





# A Morphable Model for the Synthesis of 3D Faces

Volker Blanz & Thomas Vetter

MPI for Biological Cybernetics  
Tübingen, Germany