

This lecture: Stereo

- Stereo Problem
- Cameras
- Geometry of two views
- Correspondence Search
- Extensions

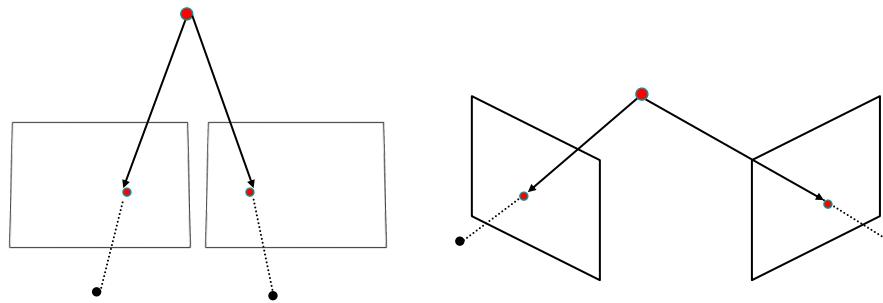
Slide Credits: A. Zisserman, K. Grauman, B. Leibe, S. Seitz, S. Lazebnik, R. Szeliski, M. Pollefeys, K. Grauman, I. Kokkinos

1

1

General Case With Calibrated Cameras

- The two cameras need not have parallel optical axes.



vs.

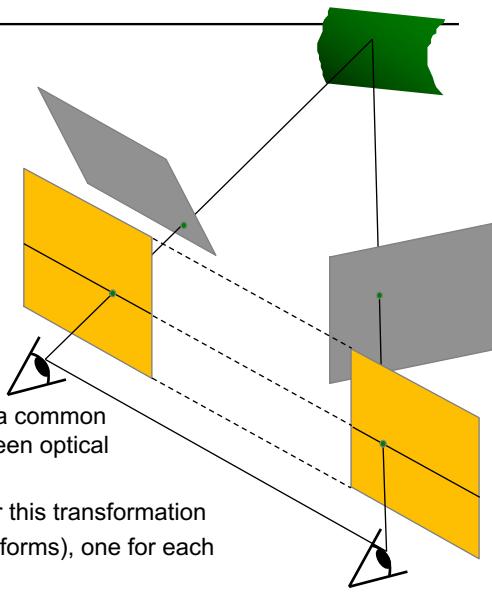
Slide credit: Kristen Grauman, Steve Seitz

2

1

Stereo Image Rectification

- In practice, it is convenient if image scanlines are the epipolar lines.



- **Algorithm**

- Reproject image planes onto a common plane parallel to the line between optical centers
- Pixel motion is horizontal after this transformation
- Two homographies (3×3 transforms), one for each input image reprojection

3

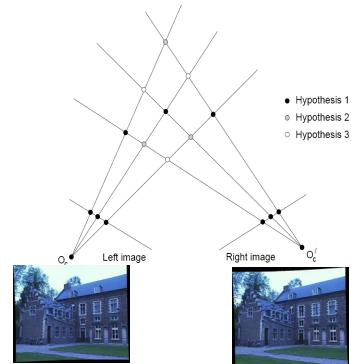
Stereo Image Rectification: Example



4

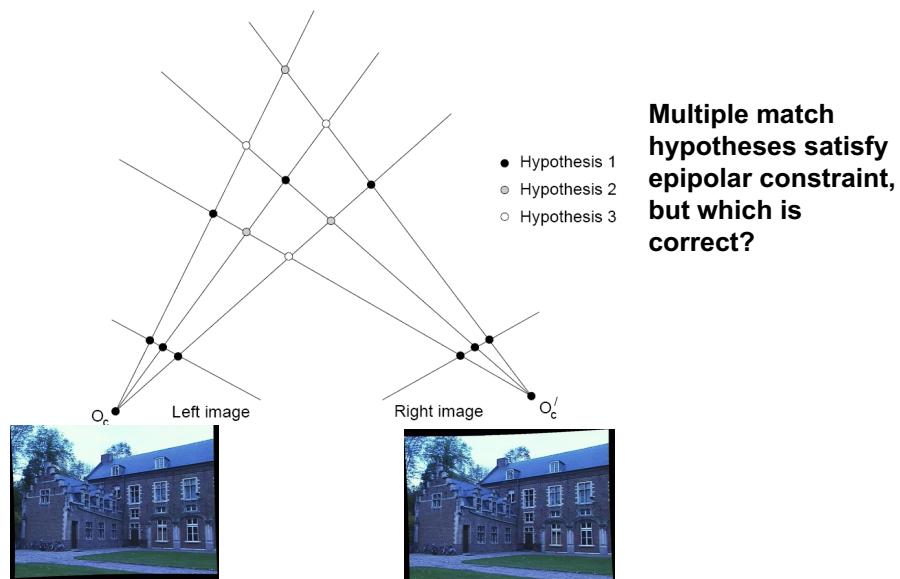
This lecture: Stereo

- Stereo Problem
- Cameras
- Geometry of two views
- Correspondence Search
 - Similarity constraint
 - Additional Constraints
- Extensions



5

Correspondence Problem



6

Problem statement

Given: two images and their associated cameras compute corresponding image points.

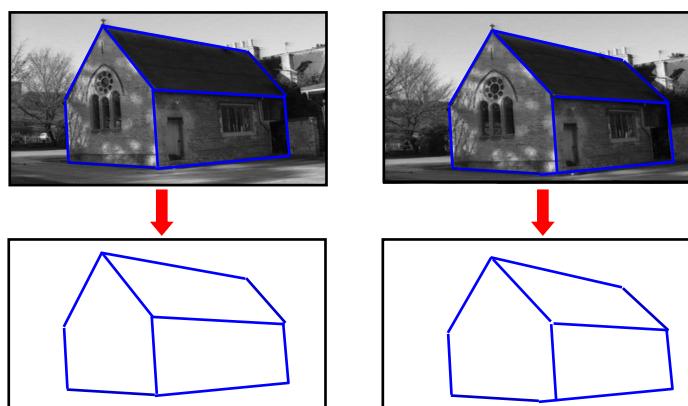
Algorithms may be classified into two types:

1. Dense: compute a correspondence at every pixel
2. Sparse: compute correspondences only for features

The methods may be top down or bottom up

7

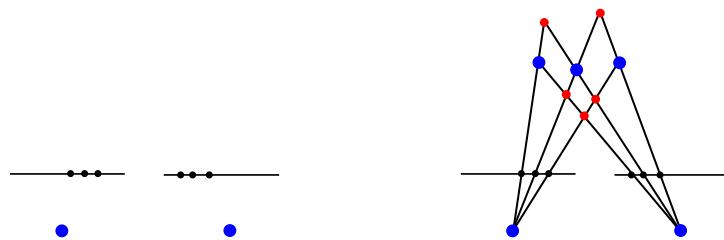
Top down matching



1. Group model (house, windows, etc) independently in each image
2. Match points (vertices) between images

8

Bottom up matching



9

Example image pair – parallel cameras



10

First image



11

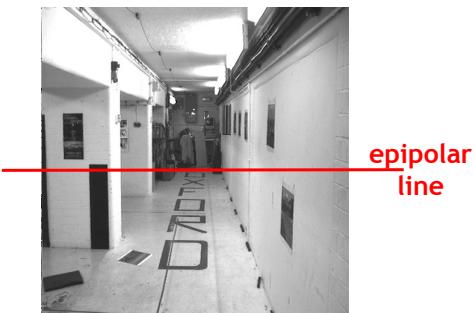
Second image



12

Dense correspondence algorithm

epipolar lines are corresponding rasters

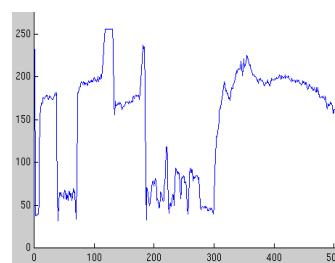
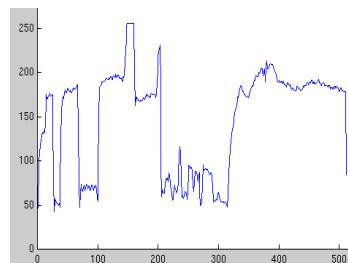


Search problem (geometric constraint): for each point in the left image, the corresponding point in the right image lies on the epipolar line (1D ambiguity)

Disambiguating assumption (photometric constraint): the intensity neighbourhood of corresponding points are similar across images

Measure similarity of neighbourhood intensity by cross-correlation

13

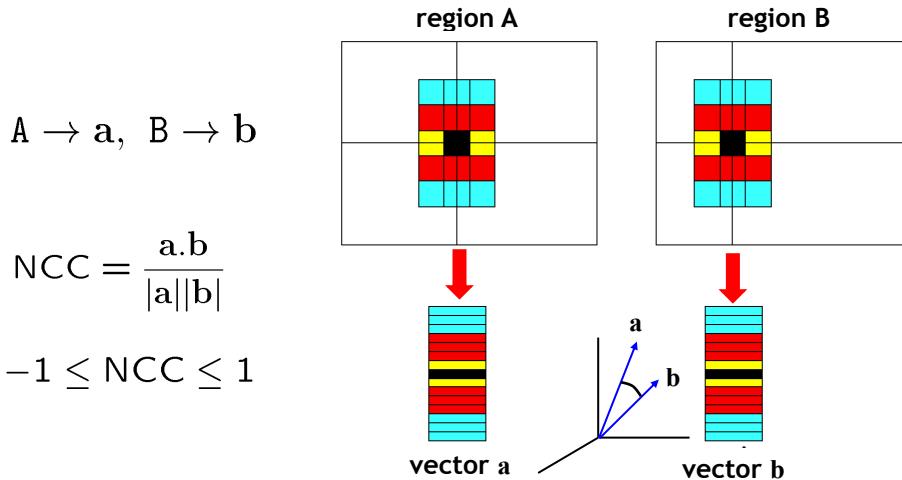


Clear correspondence between intensities, but also noise and ambiguity

14

Normalized Cross Correlation

$$NCC = \frac{\sum_i \sum_j A(i,j)B(i,j)}{\sqrt{\sum_i \sum_j A(i,j)^2} \sqrt{\sum_i \sum_j B(i,j)^2}}$$

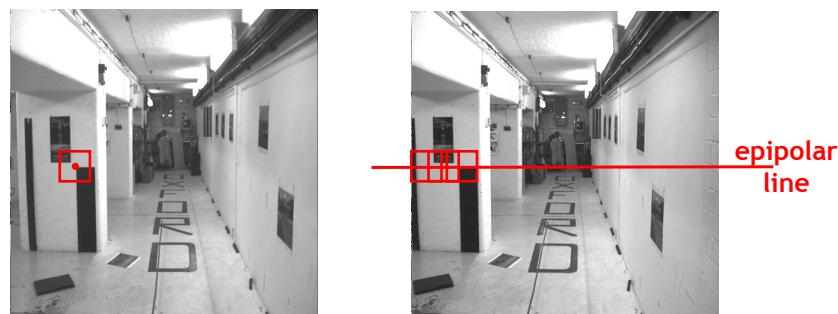


$$NCC = \frac{\mathbf{a} \cdot \mathbf{b}}{|\mathbf{a}| |\mathbf{b}|}$$

$$-1 \leq NCC \leq 1$$

15

Cross-correlation of neighbourhood regions



regions A, B, write as vectors \mathbf{a}, \mathbf{b}

translate so that mean is

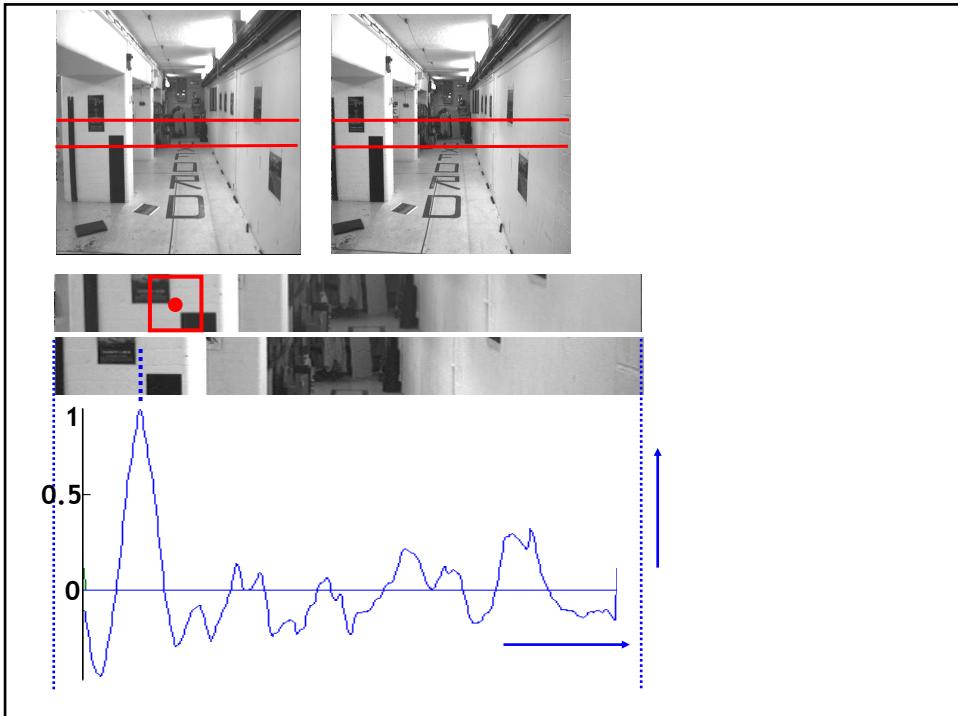
zero

$$\mathbf{a} \rightarrow \mathbf{a} - \langle \mathbf{a} \rangle, \quad \mathbf{b} \rightarrow \mathbf{b} - \langle \mathbf{b} \rangle$$

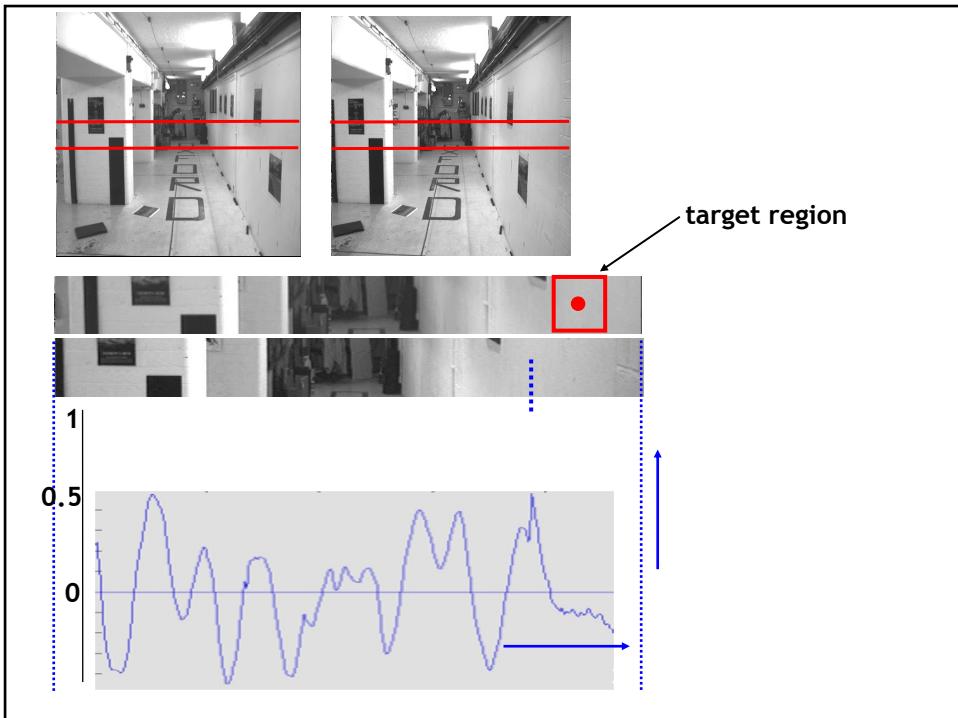
$$\text{cross correlation} = \frac{\mathbf{a} \cdot \mathbf{b}}{|\mathbf{a}| |\mathbf{b}|}$$

Invariant to $I \rightarrow \alpha I + \beta$
(exercise)

16



17

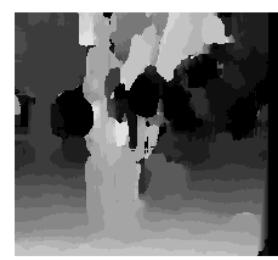


18

Effect of Window Size



$W = 3$



$W = 20$

Want window large enough to have sufficient intensity variation, yet small enough to contain only pixels with about the same disparity.

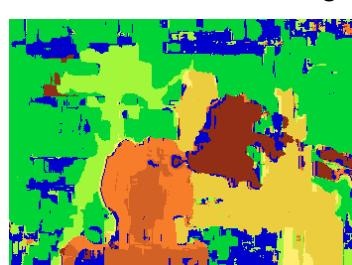
19

Results with window search

Data



Window-based matching



Ground truth

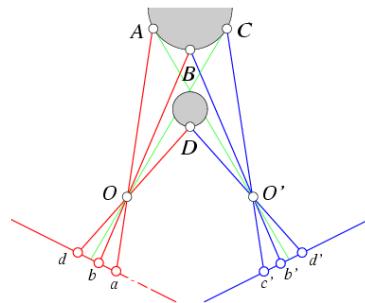


20

10

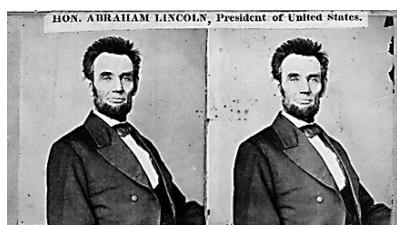
This lecture: Stereo

- Stereo Problem
- Cameras
- Geometry of two views
- Correspondence Search
 - Similarity constraint
 - Additional Constraints
- Extensions



21

Limitations of similarity constraint



Textureless surfaces



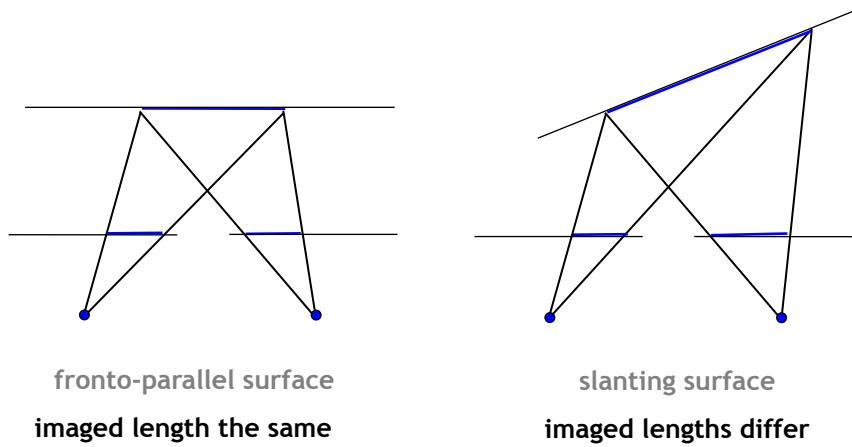
Occlusions, repetition



Specularities

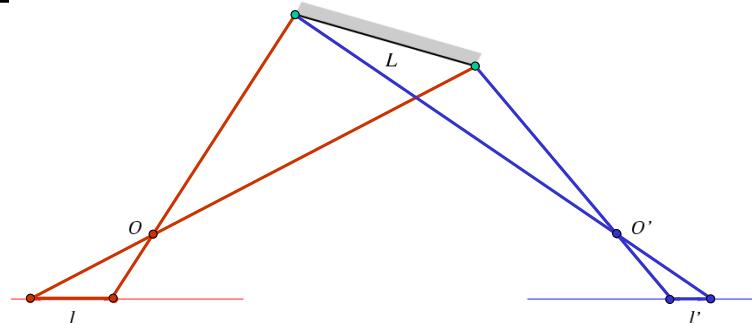
22

Foreshortening effects



23

Correlation Methods: Foreshortening Problems



Solution: add a second pass using disparity estimates to warp the correlation windows, e.g. Devernay and Faugeras (1994).



Reprinted from "Computing Differential Properties of 3D Shapes from Stereopsis without 3D Models," by F. Devernay and O. Faugeras, Proc. IEEE Conf. on Computer Vision and Pattern Recognition (1994). © 1994 IEEE.

24

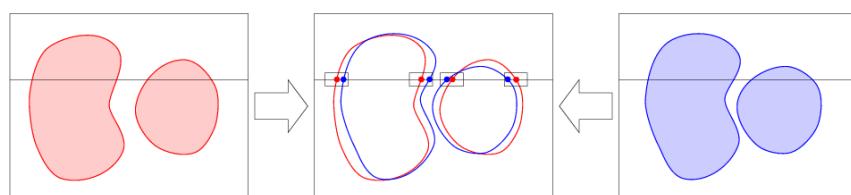
Feature based approaches

- Instead of trying to match every single pixel in the left image to its mate in the right image we could simply extract features such as edges in the left images and look for matches for those features only

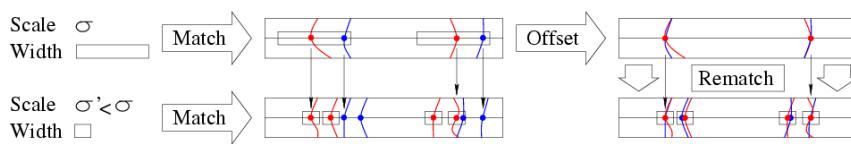
25

Multi-Scale Edge Matching (Marr, Poggio and Grimson, 1979-81)

Matching zero-crossings at a single scale



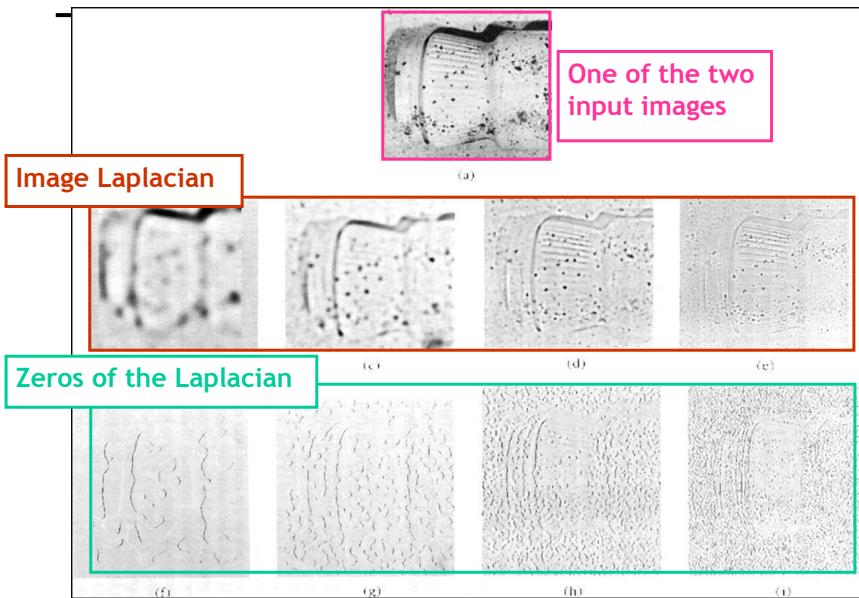
Matching zero-crossings at multiple scales



- Edges are found by repeatedly smoothing the image and detecting the zero crossings of the second derivative (Laplacian).
- Matches at coarse scales are used to offset the search for matches at fine scales (equivalent to eye movements).

26

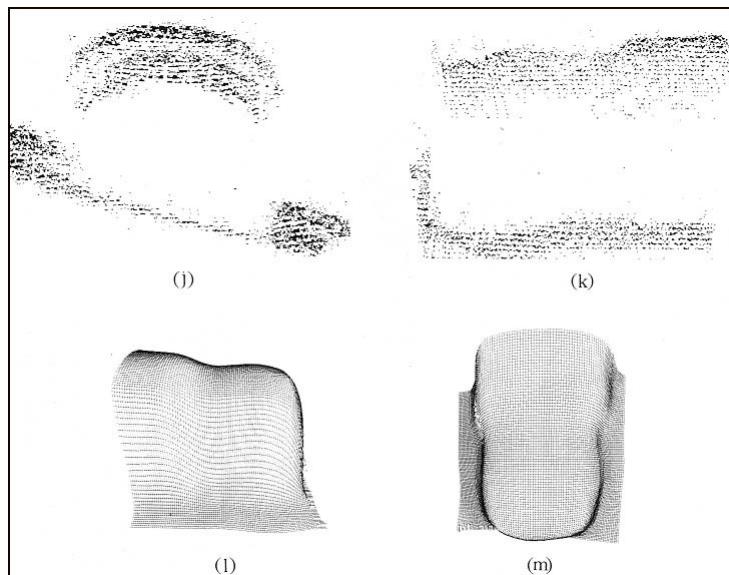
Multi-Scale Edge Matching (Marr, Poggio and Grimson, 1979-81)



Reprinted from Vision: A Computational Investigation into the Human Representation and Processing of Visual Information by David Marr.
© 1982 by David Marr. Reprinted by permission of Henry Holt and Company, LLC.

27

Multi-Scale Edge Matching (Marr, Poggio and Grimson, 1979-81)



Reprinted from Vision: A Computational Investigation into the Human Representation and Processing of Visual Information by David Marr.
© 1982 by David Marr. Reprinted by permission of Henry Holt and Company, LLC.

28

Correspondence

- Since stereo matching is an ill-posed problem global constraints are often employed
- These constraints effectively represent prior knowledge about the scenes

29

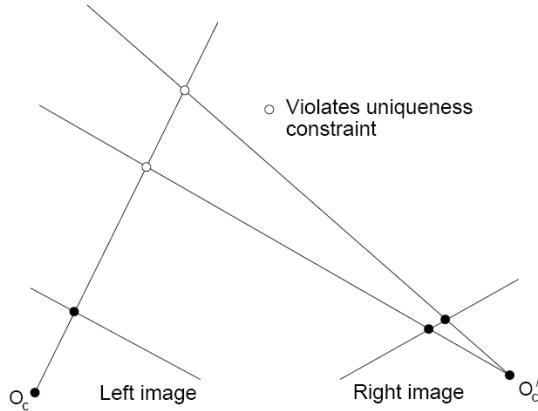
Correspondence Problem

- To find matches in the image pair, we will assume
 - Most scene points visible from both views
 - Image regions for the matches are similar in appearance
- Additional constraints!

30

Uniqueness

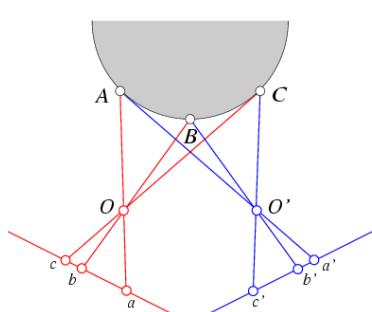
- For opaque objects, up to one match in right image for every point in left image



31

Non-Local Constraints

- Uniqueness
 - For any point in one image, there should be at most one matching point in the other image
- Ordering
 - Corresponding points should be in the same order in both views

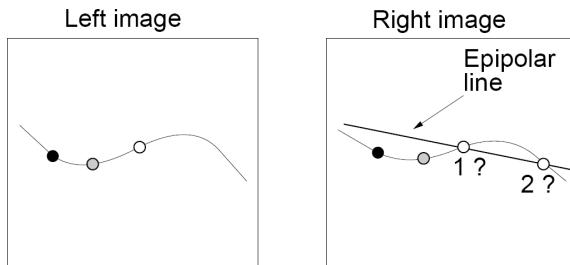


Ordering constraint may not always hold

32

Disparity Gradient

- Assume piecewise continuous surface, so want disparity estimates to be locally smooth



Given matches \bullet and \circ , point \circ in the left image must match point 1 in the right image. Point 2 would exceed the disparity gradient limit.

33

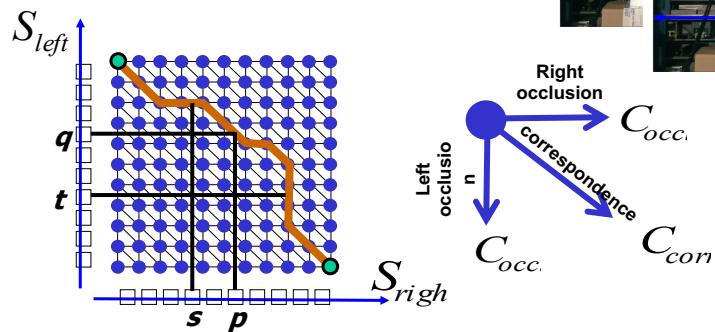
Scanline Stereo

- Try to coherently match pixels on the entire scanline
- Different scanlines are still optimized independently



34

“Shortest Path” for Scanline Stereo



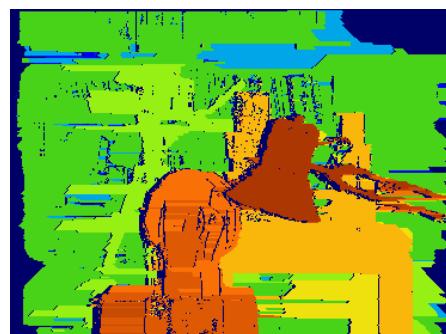
Can be implemented with dynamic programming

35 [Ohta & Kanade '85, Cox et al. '96]

35

Coherent Stereo on 2D Grid

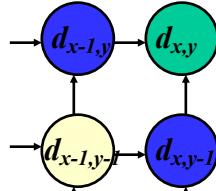
- Scanline stereo generates streaking artifacts



36

Dynamic Programming

- Can we apply this trick in 2D as well?



- No: $d_{x,y-1}$ and $d_{x-1,y}$ may depend on different values of $d_{x-1,y-1}$
- ⇒ Can't use dynamic programming to find spatially coherent disparities/ correspondences on a 2D grid!
- ⇒ But... we will later see methods for performing
37 inference on 2D Markov Random Fields.

37

Stereo Matching as Energy Minimization



MAP estimate of disparity image D : $P(D | I_1, I_2) \propto P(I_1, I_2 | D)P(D)$

$$-\log P(D | I_1, I_2) \propto -\log P(I_1, I_2 | D) - \log P(D)$$

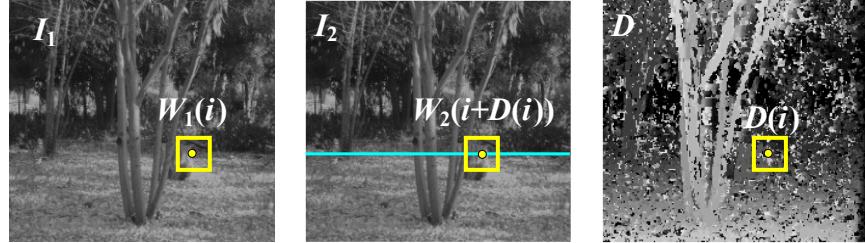
$$E = \alpha E_{\text{data}}(I_1, I_2, D) + \beta E_{\text{smooth}}(D)$$

$$E_{\text{data}} = \sum_i (W_1(i) - W_2(i + D(i)))^2 \quad 38$$

$$E_{\text{smooth}} = \sum_{\text{neighbors } i,j} \rho(D(i) - D(j))$$

38

Stereo Matching as Energy Minimization



$$E = \alpha E_{\text{data}}(I_1, I_2, D) + \beta E_{\text{smooth}}(D)$$

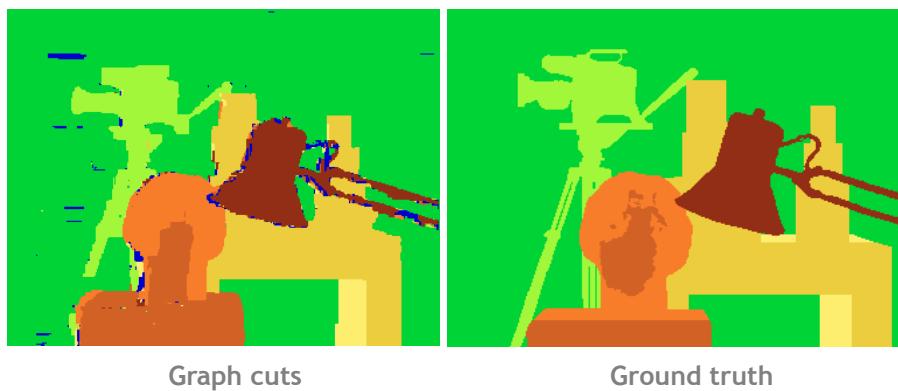
$$E_{\text{data}} = \sum_i (W_1(i) - W_2(i + D(i)))^2$$

$$E_{\text{smooth}} = \sum_{\text{neighbors } i,j} \rho(D(i) - D(j))$$

- Energy functions of this form can be minimized using *Graph Cuts*.

39

Graph Cuts Results



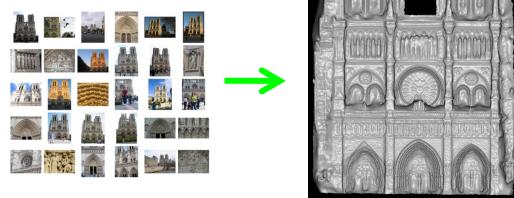
[Y. Boykov, O. Veksler, and R. Zabih, Fast Approximate Energy Minimization via Graph Cuts, PAMI 2001.](#)

40

40

This lecture: Stereo

- Stereo Problem
- Cameras
- Geometry of two views
- Correspondence Search
 - Similarity constraint
 - Additional Constraints
- Extensions

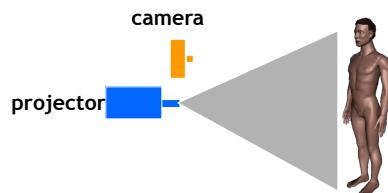


41

Active stereo with structured light



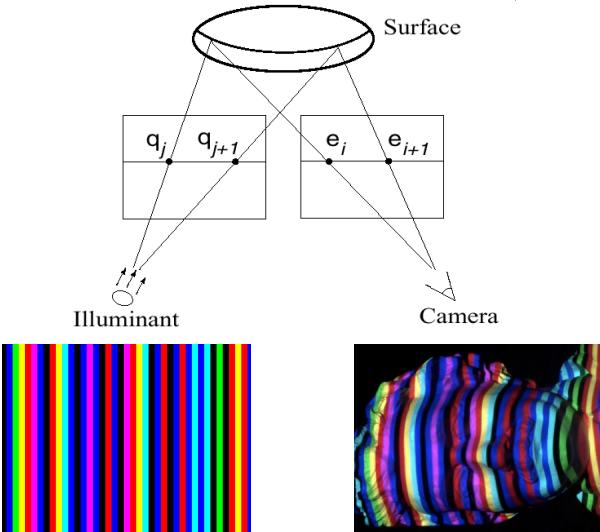
- Project “structured” light patterns onto the object
 - simplifies the correspondence problem
 - Allows us to use only one camera



L. Zhang, B. Curless, and S. M. Seitz. [Rapid Shape Acquisition Using Color Structured Light and Multi-pass Dynamic Programming](#). 3DPVT 2002

42

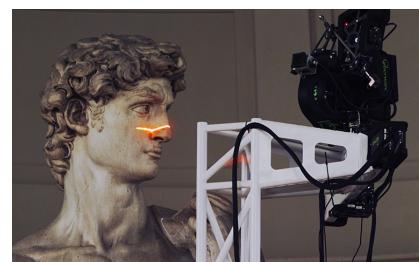
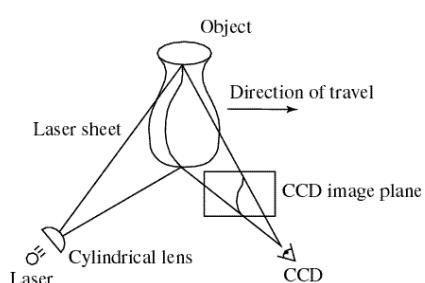
Active stereo with structured light



L. Zhang, B. Curless, and S. M. Seitz. [Rapid Shape Acquisition Using Color Structured Light and Multi-pass Dynamic Programming](#). 3DPVT 2002

43

Laser scanning



Digital Michelangelo Project
<http://graphics.stanford.edu/projects/mich/>

- Optical triangulation
 - Project a single stripe of laser light
 - Scan it across the surface of the object
 - This is a very precise version of structured light scanning

Source: S. Seitz

44

Laser scanned models



The Digital Michelangelo Project, Levoy et al.

Source: S. Seitz

45

Laser sca

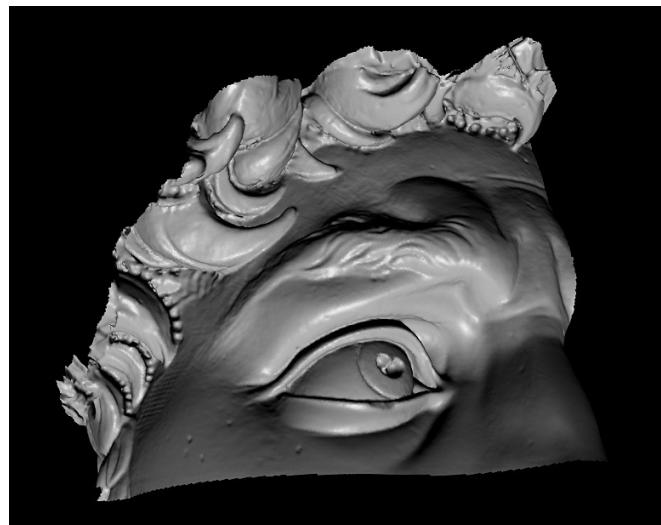


The Digital Michelangelo Project, Levoy et al.

Source: S. Seitz

46

Laser scanned models

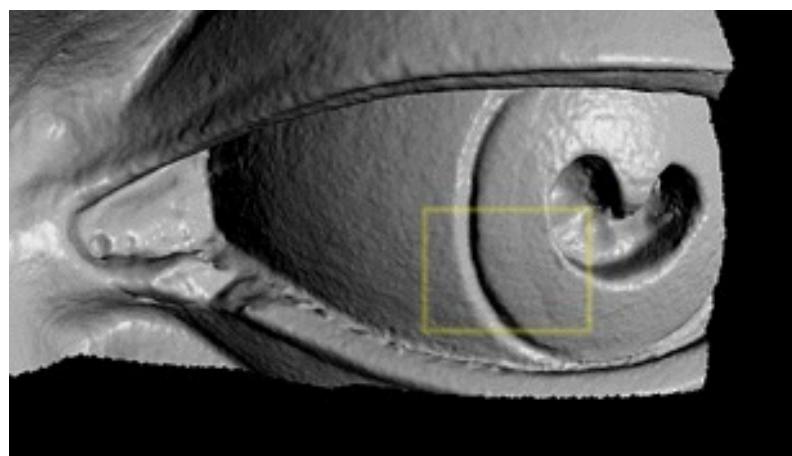


The Digital Michelangelo Project, Levoy et al.

Source: S. Seitz

47

Laser scanned models

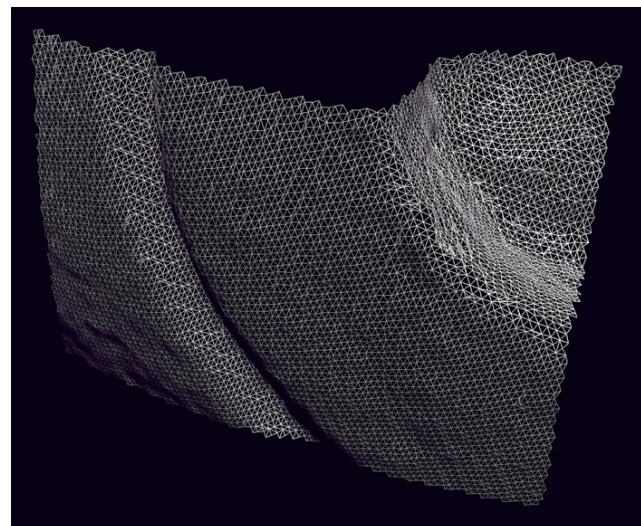


The Digital Michelangelo Project, Levoy et al.

Source: S. Seitz

48

Laser scanned models



The Digital Michelangelo Project, Levoy et al.

Source: S. Seitz

49

Real-time stereo



Nomad robot searches for meteorites in Antarctica
<http://www.frc.ri.cmu.edu/projects/meteorobot/index.html>

- Used for robot navigation (and other tasks)
 - Several software-based real-time stereo techniques have been developed (most based on simple discrete search)

50

50

Stereo reconstruction pipeline

- Steps

- Calibrate cameras
- Rectify images
- Compute disparity
- Estimate depth

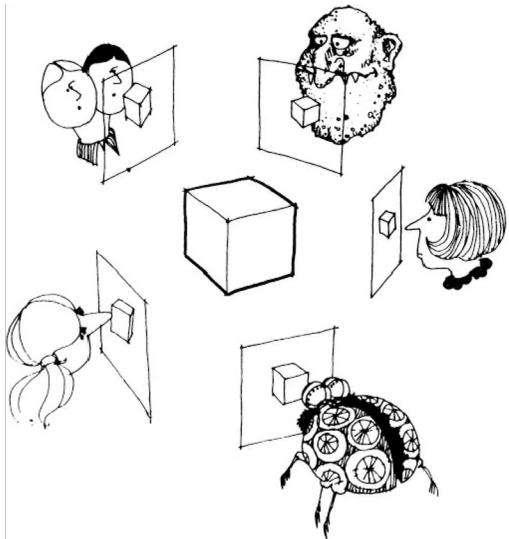
What will cause errors?

- Camera calibration errors
- Poor image resolution
- Occlusions
- Violations of brightness constancy (specular reflections)
- Large motions
- Low-contrast image regions

51

51

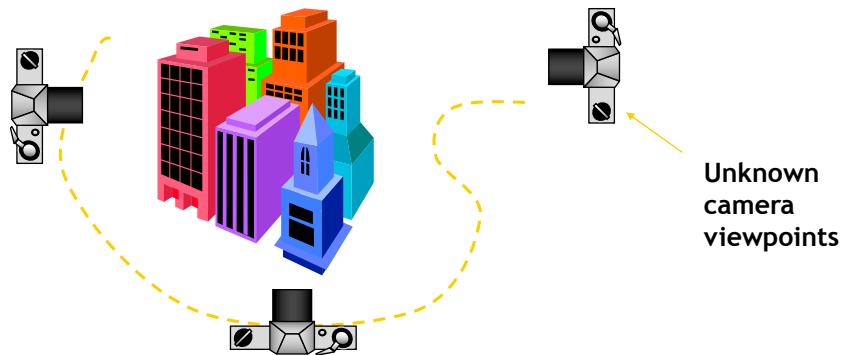
Multi-view stereo ?



52

52

Later in this class: structure from motion



Recover both 3D shape and camera motion
Huge importance for robotics

53

53

Structure from motion + the internet



Input photographs

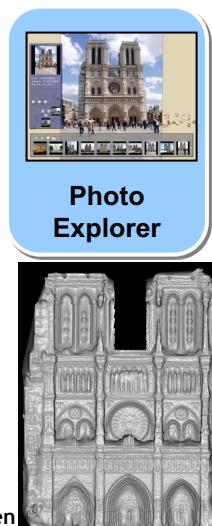
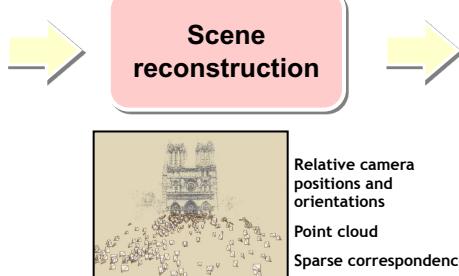


Photo Explorer

Photo Tourism: Exploring Photo Collections in 3D, Noah Snavely, Steven

Seitz, Richard Szeliski, SIGGRAPH 2006

Multi-View Stereo for Community Photo Collections [Michael Goesele](#), [Noah Snavely](#), [Brian Curless](#), [Hugues Hoppe](#), [Steven M. Seitz](#), ICCV 2007

54

Something to play with:

- **Finding Paths through the World's Photos**
 - <http://phototour.cs.washington.edu/findingpaths/>
 - <http://www.youtube.com/watch?v=gLLzV5qeKyk&fmt=18>
- **Navigating the world's photographs**
 - Google Tech Talk:
 - <http://video.google.com/videoplay?docid=-5778605234686979545>

55

55

Fundamental Matrix + Dense correspondence

The Visual Turing Test for Scene Reconstruction Supplementary Video

Qi Shan⁺ Riley Adams⁺ Brian Curless⁺
Yasutaka Furukawa^{*} Steve Seitz^{++*}

⁺University of Washington ^{*}Google

3DV 2013

56

SIFT + Fundamental Matrix + RANSAC

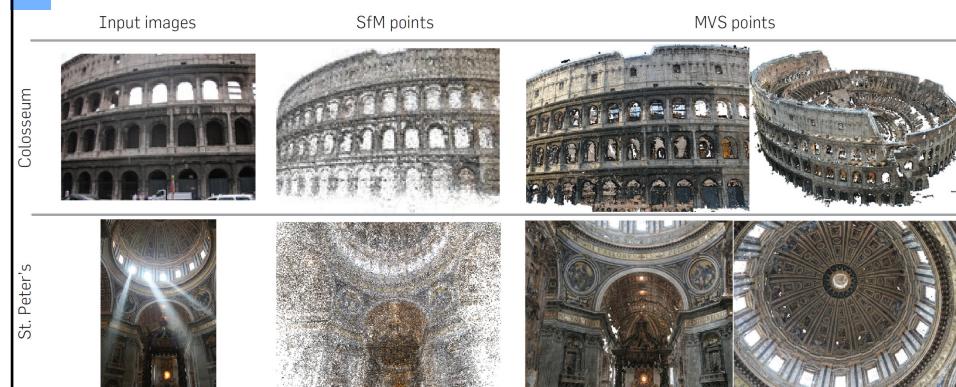
Despite their scale invariance and robustness to appearance changes, SIFT features are *local* and do not contain any global information about the image or about the location of other features in the image. Thus feature matching based on SIFT features is still prone to errors. However, since we assume that we are dealing with rigid scenes, there are strong geometric constraints on the locations of the matching features and these constraints can be used to clean up the matches. In particular, when a rigid scene is imaged by two pinhole cameras, there exists a 3×3 matrix F , the *Fundamental matrix*, such that corresponding points x_j^T and x_k (represented in homogeneous coordinates) in two images j and k satisfy¹⁰:

$$x_j^T F x_k = 0. \quad (3)$$

A common way to impose this constraint is to use a greedy randomized algorithm to generate suitably chosen random estimates of F and choose the one that has the largest support among the matches, i.e., the one for which the most matches satisfy (3). This algorithm is called Random Sample Consensus (RANSAC)⁶ and is used in many computer vision problems.

57

Sparse to Dense Correspondence



58

Unsupervised Monocular Depth Estimation with Left-Right Consistency

Clément Godard¹

Oisin Mac Aodha²
Brostow¹

Gabriel J.

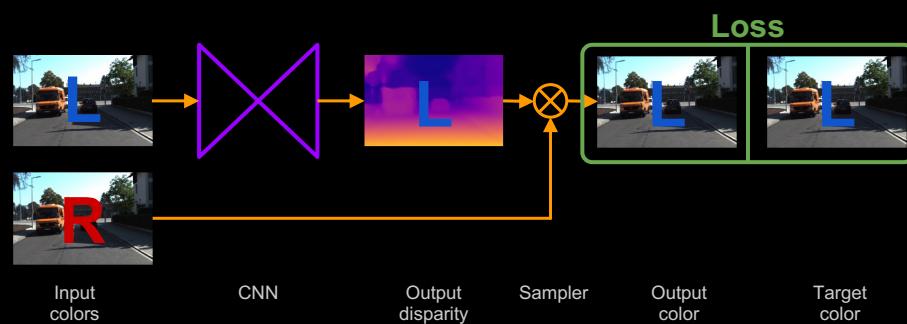
¹University College London

²Caltech



59

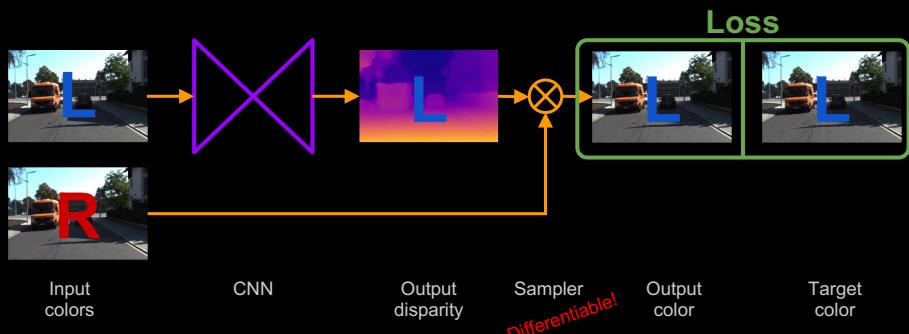
Unsupervised depth estimation - Concept



60

60

Unsupervised depth estimation - Baseline



Spatial transformer networks, Jaderberg et al. [NIPS 15]

61

61

Input



62

62

31

Baseline



63

63

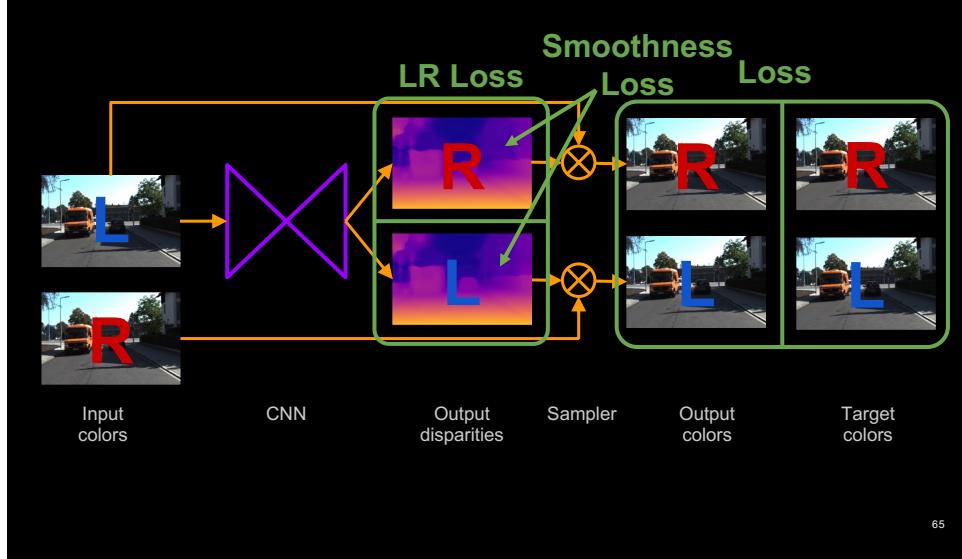
Our method



64

64

Unsupervised depth estimation - Our method



65

65