Data Import

```
In[*]:= SetDirectory[
       "C:/Users/serha/OneDrive/Masaüstü/MyRepo/master_thesis_MMT003/210718_product_diversity
         "1;
In[=]:= Get[".../algoritm_packages/SingleNetworks-algorithm-package-2.wl"]
     (* ?SingleNetworks`* *)
Info |:= datafull = Import[".../data/cgl manipulated 27147 rev1.csv"];
     productionline = "CGL5-inc_sizes";
     stepsizewidth = 22;
     stepsizethickness = 0.1;
     Data for First and Second Half of Complete Data
In[●]:= Dimensions@datafull
Out[*]= { 27 147, 12 }
In[@]:= x = Floor[Length@datafull / 2];
     {a, b} = Range[x, Length@datafull, x];
     data1sthalf = Take[datafull, {1, a}];
     data2ndhalf = Take[datafull, {a + 1, b}];
In[*]:= times = 10;
     picklist1sthalf = Table[
        RandomSample[Range@Length@data1sthalf, Floor@((Length@data1sthalf) * 0.9)], times];
     reduceddata1sthalflist = Table[data1sthalf[[i, All]], {i, picklist1sthalf}];
     picklist2ndhalf = Table[
        RandomSample[Range@Length@data2ndhalf, Floor@((Length@data2ndhalf) * 0.9)], times];
     reduceddata2ndhalflist = Table[data2ndhalf[[i, All]], {i, picklist2ndhalf}];
     picklistfull =
       Table [RandomSample [Range@Length@datafull, Floor@((Length@datafull) * 0.9)], times];
     reduceddatafulllist = Table[datafull[[i, All]], {i, picklistfull}];
     bar chart function
```

```
in[*]:= plotcolumn[modularity_, randommoddegree_,
       randommodcommunity_, zscoredegree_, zscorecommunities_, eZscores_] :=
     Module[{labels, colors, modularityrange, errorBar, errorbars, charts},
       labels = {"Modularity", "Sng. Rnd. Mod.\n Degrees",
         "Sng. Rnd. Mod.\n Degrees & Modules", "Z-score cons. \n Degrees",
         "Z-score cons. \n Degrees & Modules"};
       colors = {{Purple, RGBColor[{0.266122`, 0.486664`, 0.802529`}],
          RGBColor[{0.513417`, 0.72992`, 0.440682`}]}, {RGBColor[
            {0.863512`, 0.670771`, 0.236564`}], RGBColor[{0.857359`, 0.131106`, 0.132128`}]}};
       modularityrange = {0, 0.52};
       errorBar[type_: "Rectangle"][{{x0_, x1_}, {y0_, y1_}}, value_, meta_] := Block[
         {error, mags = QuantityMagnitude[value]}, error = Flatten[QuantityMagnitude[meta]];
         error = If[error === {}, 0, Last[error]];
         {ChartElementData[type][{{x0, x1}, {y0, y1}}, mags, meta],
          {Black, Line[{{(x0 + x1) / 2, y1 - error}, {(x0 + x1) / 2, y1 + error}},
              \{\{1/4(3x0+x1), y1+error\}, \{1/4(x0+3x1), y1+error\}\},
              \{\{1/4(3x0+x1), y1-error\}, \{1/4(x0+3x1), y1-error\}\}\}\}\}\}
       errorbars = {Mean@eZscores[[All, 1]] → StandardDeviation@eZscores[[All, 1]],
         Mean@eZscores[[All, 2]] → StandardDeviation@eZscores[[All, 2]]};
       charts = GraphicsColumn[{BarChart[{modularity, randommoddegree, randommodcommunity},
            ChartStyle → colors[[1]],
            ChartLabels → labels[[{1, 2, 3}]], Frame → True, FrameTicks →
             {{All, None}, {None, {{1, labels[[1]]}, {2, labels[[2]]}, {3, labels[[3]]}}}},
            PlotRange → {{0.5, 3.5}, modularityrange}], GraphicsRow[
            {Show[BarChart[{errorbars[[1]], 0 → 0}, ChartElementFunction → errorBar[],
               ChartStyle \rightarrow colors[[2, 1]], Frame \rightarrow True, PlotRange \rightarrow {{0.5, 1.5}, {-10, 50}},
               FrameTicks \rightarrow {{All, None}, {{{1, labels[[4]]}, {2, labels[[5]]}}, None}}],
              BarChart[{zscoredegree, 0}, ChartStyle → Transparent, Frame → True,
               PlotRange → {\{0.5, 1.5\}, \{-10, 50\}\}, FrameTicks →
                 \{\{All, None\}, \{\{\{1, labels[[4]]\}, \{2, labels[[5]]\}\}, None\}\}\}, AspectRatio \rightarrow 2],
             Show[BarChart[\{0 \rightarrow 0, errorbars[[2]]\}, ChartElementFunction \rightarrow errorBar[],
               ChartStyle \rightarrow colors[[2, 2]], Frame \rightarrow True, PlotRange \rightarrow {{1.5, 2.5}, {-10, 5}},
               FrameTicks \rightarrow {{None, All}, {{{1, labels[[4]]}, {2, labels[[5]]}}, None}}],
              BarChart[{0, zscorecommunities}, ChartStyle → Transparent,
               Frame \rightarrow True, PlotRange \rightarrow {{1.5, 2.5}, {-10, 5}},
               FrameTicks \rightarrow {{None, All}, {{{1, labels[[4]]}, {2, labels[[5]]}}}, None}}],
              AspectRatio → 2]}]}, Spacings → 1]]
```

Investigation of Constraints Impact in Real-life Production Events

Fixed Step Size Networks

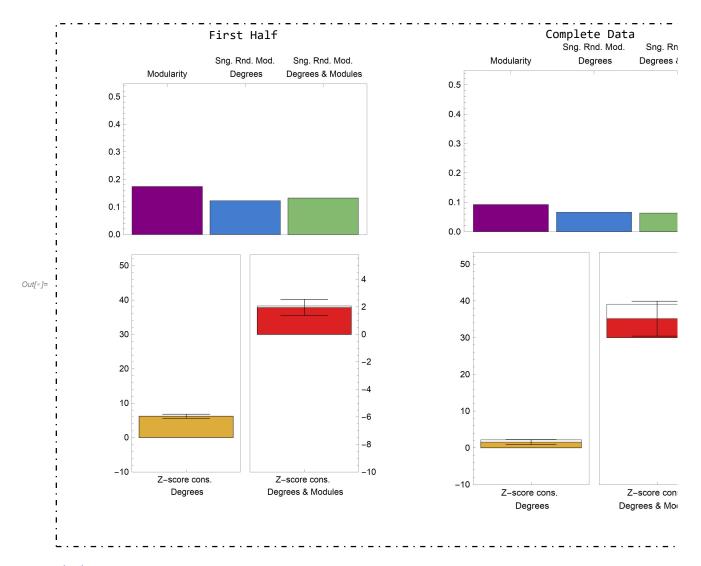
Width Feature

```
log_{ij} = AbsoluteTiming[widthdataFixedstep1 = snetworkdatabinned[9, stepsizewidth, data1sthalf];
      graphsandnodenumbers1 =
       snetworkgraph[widthdataFixedstep1[[1]], widthdataFixedstep1[[2]], 2, 7, 400, Green];
      modularityvalues1 = N@GraphAssortativity[graphsandnodenumbers1[[1]],
         FindGraphCommunities[graphsandnodenumbers1[[1]]], "Normalized" → False];
      singlerandomgraphsdegfxd1 = randomizinggraphdegfxd[graphsandnodenumbers1[[1]]];
      singlerandomerdrenmodularityvalues1 = N@GraphAssortativity[singlerandomgraphsdegfxd1,
         FindGraphCommunities[singlerandomgraphsdegfxd1], "Normalized" -> False];
      singlerandomgraphscomm1 = randomizinggraphmod[graphsandnodenumbers1[[1]]];
      singlerandomcommmodularityvalues1 = N@GraphAssortativity[singlerandomgraphscomm1,
         FindGraphCommunities[singlerandomgraphscomm1], "Normalized" -> False];
      Zscoresmodularity1 = zscorefunctionfortwonullmodels[graphsandnodenumbers1[[1]]];
      bucketnode11 = graphsandnodenumbers1[[2]]]
Out[\circ] = \{14.6022, 43\}
m[\cdot] = AbsoluteTiming[widthdataFixedstep2 = snetworkdatabinned[9, stepsizewidth, data2ndhalf];
      graphsandnodenumbers12 =
       snetworkgraph[widthdataFixedstep2[[1]], widthdataFixedstep2[[2]], 2, 7, 400, Green];
      modularityvalues12 = N@GraphAssortativity[graphsandnodenumbers12[[1]],
         FindGraphCommunities[graphsandnodenumbers12[[1]]], "Normalized" → False];
      singlerandomgraphsdegfxd12 = randomizinggraphdegfxd[graphsandnodenumbers12[[1]]];
      singlerandomerdrenmodularityvalues12 = N@GraphAssortativity[singlerandomgraphsdegfxd12,
         FindGraphCommunities[singlerandomgraphsdegfxd12], "Normalized" -> False];
      singlerandomgraphscomm12 = randomizinggraphmod[graphsandnodenumbers12[[1]]];
      singlerandomcommmodularityvalues12 = N@GraphAssortativity[singlerandomgraphscomm12,
         FindGraphCommunities[singlerandomgraphscomm12], "Normalized" -> False];
      Zscoresmodularity12 = zscorefunctionfortwonullmodels[graphsandnodenumbers12[[1]]];
      bucketnode12 = graphsandnodenumbers12[[2]]]
Out[\circ]= {22.5649, 44}
log_{ij} = AbsoluteTiming[widthdataFixedstep3 = snetworkdatabinned[9, stepsizewidth, datafull];
      graphsandnodenumbers13 =
       snetworkgraph[widthdataFixedstep3[[1]], widthdataFixedstep3[[2]], 2, 7, 400, Green];
      modularityvalues13 = N@GraphAssortativity[graphsandnodenumbers13[[1]],
         FindGraphCommunities[graphsandnodenumbers13[[1]]], "Normalized" → False];
      singlerandomgraphsdegfxd13 = randomizinggraphdegfxd[graphsandnodenumbers13[[1]]];
      singlerandomerdrenmodularityvalues13 = N@GraphAssortativity[singlerandomgraphsdegfxd13,
         FindGraphCommunities[singlerandomgraphsdegfxd13], "Normalized" -> False];
      singlerandomgraphscomm13 = randomizinggraphmod[graphsandnodenumbers13[[1]]];
      singlerandomcommmodularityvalues13 = N@GraphAssortativity[singlerandomgraphscomm13,
         FindGraphCommunities[singlerandomgraphscomm13], "Normalized" -> False];
      Zscoresmodularity13 = zscorefunctionfortwonullmodels[graphsandnodenumbers13[[1]]];
      bucketnode13 = graphsandnodenumbers13[[2]]]
Out[\circ] = \{25.5203, 44\}
     Error Bars and Charts
```

```
In[*]:= AbsoluteTiming[ewidthdataFixedstep1 =
       Table[snetworkdatabinned[9, stepsizewidth, i], {i, reduceddata1sthalflist}];
      egraphsandnodenumbers1 = Table[snetworkgraph[ewidthdataFixedstep1[[i, 1]],
         ewidthdataFixedstep1[[i, 2]], 2, 7, 400, Green], {i, Length@reduceddata1sthalflist}];
      emodularityvalues1 = Table[N@GraphAssortativity[egraphsandnodenumbers1[[i, 1]],
          FindGraphCommunities[egraphsandnodenumbers1[[i, 1]]], "Normalized" → False],
        {i, Length@reduceddata1sthalflist}];
      esinglerandomgraphsdegfxd1 = Table[randomizinggraphdegfxd[
         egraphsandnodenumbers1[[i, 1]]], {i, Length@reduceddata1sthalflist}];
      esinglerandomerdrenmodularityvalues1 =
       Table [N@GraphAssortativity[esinglerandomgraphsdegfxd1[[i]],
          FindGraphCommunities[esinglerandomgraphsdegfxd1[[i]]], "Normalized" -> False],
        {i, Length@reduceddata1sthalflist}];
      esinglerandomgraphscomm1 = Table[randomizinggraphmod[egraphsandnodenumbers1[[i, 1]]],
        {i, Length@reduceddata1sthalflist}];
      esinglerandomcommmodularityvalues1 =
       Table [N@GraphAssortativity [esinglerandomgraphscomm1[[i]],
          FindGraphCommunities[esinglerandomgraphscomm1[[i]]], "Normalized" -> False],
        {i, Length@reduceddata1sthalflist}];
      eZscoresmodularity1 = Table[zscorefunctionfortwonullmodels[
         egraphsandnodenumbers1[[i, 1]]], {i, Length@reduceddata1sthalflist}];
      ebucketnode11 = Table[egraphsandnodenumbers1[[i, 2]],
        {i, Length@reduceddata1sthalflist}]]
Outf^{\circ} { 135.619, {42, 43, 43, 43, 43, 43, 41, 43, 41, 43} }
```

```
In[*]:= AbsoluteTiming[ewidthdataFixedstep2 =
       Table[snetworkdatabinned[9, stepsizewidth, i], {i, reduceddata2ndhalflist}];
      egraphsandnodenumbers12 = Table[snetworkgraph[ewidthdataFixedstep2[[i, 1]],
         ewidthdataFixedstep2[[i, 2]], 2, 7, 400, Green], {i, Length@reduceddata2ndhalflist}];
      emodularityvalues12 = Table[N@GraphAssortativity[egraphsandnodenumbers12[[i, 1]],
          FindGraphCommunities[egraphsandnodenumbers12[[i, 1]]], "Normalized" → False],
        {i, Length@reduceddata2ndhalflist}];
      esinglerandomgraphsdegfxd12 = Table[randomizinggraphdegfxd[
         egraphsandnodenumbers12[[i, 1]]], {i, Length@reduceddata2ndhalflist}];
      esinglerandomerdrenmodularityvalues12 =
       Table [N@GraphAssortativity [esinglerandomgraphsdegfxd12 [[i]],
          FindGraphCommunities[esinglerandomgraphsdegfxd12[[i]]], "Normalized" -> False],
        {i, Length@reduceddata2ndhalflist}];
      esinglerandomgraphscomm12 = Table[randomizinggraphmod[egraphsandnodenumbers12[[i, 1]]],
        {i, Length@reduceddata2ndhalflist}];
      esinglerandomcommmodularityvalues12 =
       Table [N@GraphAssortativity [esinglerandomgraphscomm12[[i]],
          FindGraphCommunities[esinglerandomgraphscomm12[[i]]], "Normalized" -> False],
        {i, Length@reduceddata2ndhalflist}];
      eZscoresmodularity12 = Table[zscorefunctionfortwonullmodels[
         egraphsandnodenumbers12[[i, 1]]], {i, Length@reduceddata2ndhalflist}];
      ebucketnode12 = Table[egraphsandnodenumbers12[[i, 2]],
        {i, Length@reduceddata2ndhalflist}]]
```

```
In[@]:= AbsoluteTiming[ewidthdataFixedstep3 =
       Table[snetworkdatabinned[9, stepsizewidth, i], {i, reduceddatafulllist}];
     egraphsandnodenumbers13 = Table[snetworkgraph[ewidthdataFixedstep3[[i, 1]],
         ewidthdataFixedstep3[[i, 2]], 2, 7, 400, Green], {i, Length@reduceddatafulllist}];
     emodularityvalues13 = Table [N@GraphAssortativity [egraphsandnodenumbers13 [[i, 1]],
          FindGraphCommunities[egraphsandnodenumbers13[[i, 1]]],
          "Normalized" → False], {i, Length@reduceddatafulllist}];
     esinglerandomgraphsdegfxd13 = Table[randomizinggraphdegfxd[
         egraphsandnodenumbers13[[i, 1]]], {i, Length@reduceddatafulllist}];
     esinglerandomerdrenmodularityvalues13 =
       Table [N@GraphAssortativity [esinglerandomgraphsdegfxd13 [[i]],
          FindGraphCommunities[esinglerandomgraphsdegfxd13[[i]]],
          "Normalized" -> False], {i, Length@reduceddatafulllist}];
     esinglerandomgraphscomm13 = Table[randomizinggraphmod[egraphsandnodenumbers13[[i, 1]]],
        {i, Length@reduceddatafulllist}];
     esinglerandomcommmodularityvalues13 =
       Table [N@GraphAssortativity [esinglerandomgraphscomm13[[i]],
          FindGraphCommunities[esinglerandomgraphscomm13[[i]]],
          "Normalized" -> False], {i, Length@reduceddatafulllist}];
     eZscoresmodularity13 = Table[zscorefunctionfortwonullmodels[
         egraphsandnodenumbers13[[i, 1]]], {i, Length@reduceddatafulllist}];
     ebucketnode13 = Table[egraphsandnodenumbers13[[i, 2]], {i, Length@reduceddatafulllist}]]
Imfe := emodvalues1 = {emodularityvalues1, emodularityvalues12, emodularityvalues13};
    eZscores1 = {eZscoresmodularity1, eZscoresmodularity12, eZscoresmodularity13};
    Export["error_bar_values/" <> productionline <> "-modularity_values1.mx", emodvalues1];
    Export["error_bar_values/" <> productionline <> "-zscores1.mx", eZscores1];
In[*]: (*emodvalues1=Import["error_bar_values/CCM5-modularity_values1.mx"];
    eZscores1=Import["error_bar_values/CCM5-zscores1.mx"];*)
Info ]:= set11 = plotcolumn[modularityvalues1,
        singlerandomerdrenmodularityvalues1, singlerandomcommmodularityvalues1,
        Zscoresmodularity1[[1]], Zscoresmodularity1[[2]], eZscores1[[1]]];
    set12 = plotcolumn[modularityvalues12, singlerandomerdrenmodularityvalues12,
        singlerandomcommmodularityvalues12, Zscoresmodularity12[[1]],
        Zscoresmodularity12[[2]], eZscores1[[2]]];
    set13 = plotcolumn[modularityvalues13, singlerandomerdrenmodularityvalues13,
        singlerandomcommmodularityvalues13, Zscoresmodularity13[[1]],
        Zscoresmodularity13[[2]], eZscores1[[3]]];
    Legended[Framed[GraphicsRow[{set11, Magnify[set13, 1.03], set12}, ImageSize → 1093],
       FrameMargins → 5, FrameStyle → DotDashed], {Placed["First Half", {0.155, 0.99}],
       Placed["Complete Data", {0.505, 0.99}], Placed["Second Half", {0.86, 0.99}]]]
```



Thickness Feature

```
/// /:= AbsoluteTiming[
      thicknessdataFixedstep1 = snetworkdatabinned[10, stepsizethickness, data1sthalf];
      graphsandnodenumbers2 = snetworkgraph[thicknessdataFixedstep1[[1]],
        thicknessdataFixedstep1[[2]], 2, 7, 400, Green];
      modularityvalues2 = N@GraphAssortativity[graphsandnodenumbers2[[1]],
         FindGraphCommunities[graphsandnodenumbers2[[1]]], "Normalized" → False];
      singlerandomgraphsdegfxd2 = randomizinggraphdegfxd[graphsandnodenumbers2[[1]]];
      singlerandomerdrenmodularityvalues2 = N@GraphAssortativity[singlerandomgraphsdegfxd2,
         FindGraphCommunities[singlerandomgraphsdegfxd2], "Normalized" -> False];
      singlerandomgraphscomm2 = randomizinggraphmod[graphsandnodenumbers2[[1]]];
      singlerandomcommmodularityvalues2 = N@GraphAssortativity[singlerandomgraphscomm2,
         FindGraphCommunities[singlerandomgraphscomm2], "Normalized" -> False];
      Zscoresmodularity2 = zscorefunctionfortwonullmodels[graphsandnodenumbers2[[1]]];
      bucketnode21 = graphsandnodenumbers2[[2]]]
Out[\circ] = \{11.2698, 28\}
```

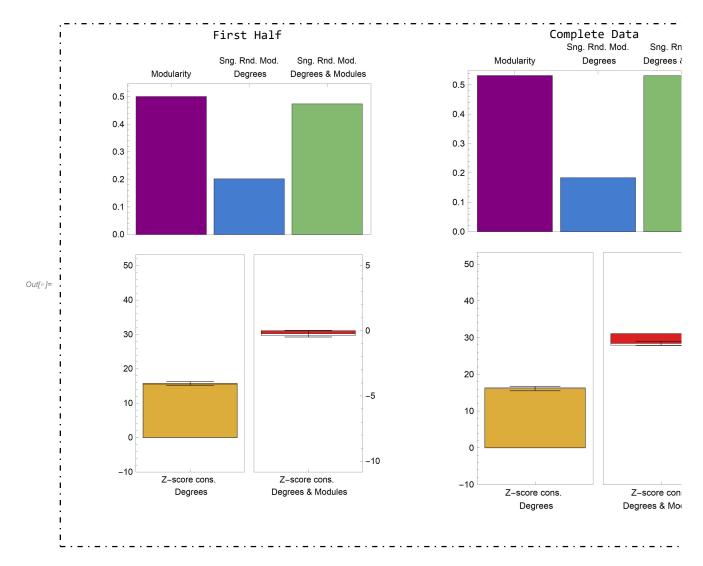
```
In[@]:= AbsoluteTiming[
      thicknessdataFixedstep2 = snetworkdatabinned[10, stepsizethickness, data2ndhalf];
      graphsandnodenumbers22 = snetworkgraph[thicknessdataFixedstep2[[1]],
        thicknessdataFixedstep2[[2]], 2, 7, 400, Green];
      modularityvalues22 = N@GraphAssortativity[graphsandnodenumbers22[[1]],
         FindGraphCommunities[graphsandnodenumbers22[[1]]], "Normalized" → False];
      singlerandomgraphsdegfxd22 = randomizinggraphdegfxd[graphsandnodenumbers22[[1]]];
      singlerandomerdrenmodularityvalues22 = N@GraphAssortativity[singlerandomgraphsdegfxd22,
         FindGraphCommunities[singlerandomgraphsdegfxd22], "Normalized" -> False];
      singlerandomgraphscomm22 = randomizinggraphmod[graphsandnodenumbers22[[1]]];
      singlerandomcommmodularityvalues22 = N@GraphAssortativity[singlerandomgraphscomm22,
         FindGraphCommunities[singlerandomgraphscomm22], "Normalized" -> False];
      Zscoresmodularity22 = zscorefunctionfortwonullmodels[graphsandnodenumbers22[[1]]];
      bucketnode22 = graphsandnodenumbers22[[2]]]
Out[\circ] = \{14.2695, 26\}
In[@]:= AbsoluteTiming[
      thicknessdataFixedstep3 = snetworkdatabinned[10, stepsizethickness, datafull];
      graphsandnodenumbers23 = snetworkgraph[thicknessdataFixedstep3[[1]],
        thicknessdataFixedstep3[[2]], 2, 7, 400, Green];
      modularityvalues23 = N@GraphAssortativity[graphsandnodenumbers23[[1]],
         FindGraphCommunities[graphsandnodenumbers23[[1]]], "Normalized" → False];
      singlerandomgraphsdegfxd23 = randomizinggraphdegfxd[graphsandnodenumbers23[[1]]];
      singlerandomerdrenmodularityvalues23 = N@GraphAssortativity[singlerandomgraphsdegfxd23,
         FindGraphCommunities[singlerandomgraphsdegfxd23], "Normalized" -> False];
      singlerandomgraphscomm23 = randomizinggraphmod[graphsandnodenumbers23[[1]]];
      singlerandomcommmodularityvalues23 = N@GraphAssortativity[singlerandomgraphscomm23,
         FindGraphCommunities[singlerandomgraphscomm23], "Normalized" -> False];
      Zscoresmodularity23 = zscorefunctionfortwonullmodels[graphsandnodenumbers23[[1]]];
      bucketnode23 = graphsandnodenumbers23[[2]]]
Out[@] = \{18.2687, 28\}
```

Error Bars and Charts

```
In[*]:= AbsoluteTiming[ethicknessdataFixedstep1 =
      Table[snetworkdatabinned[10, stepsizethickness, i], {i, reduceddata1sthalflist}];
     egraphsandnodenumbers2 = Table[snetworkgraph[ethicknessdataFixedstep1[[i, 1]],
         ethicknessdataFixedstep1[[i, 2]], 2, 7, 400, Green],
        {i, Length@reduceddata1sthalflist}];
     emodularityvalues2 = Table[N@GraphAssortativity[egraphsandnodenumbers2[[i, 1]],
          FindGraphCommunities[egraphsandnodenumbers2[[i, 1]]], "Normalized" → False],
        {i, Length@reduceddata1sthalflist}];
     esinglerandomgraphsdegfxd2 = Table[randomizinggraphdegfxd[
         egraphsandnodenumbers2[[i, 1]]], {i, Length@reduceddata1sthalflist}];
     esinglerandomerdrenmodularityvalues2 =
      Table [N@GraphAssortativity[esinglerandomgraphsdegfxd2[[i]],
          FindGraphCommunities[esinglerandomgraphsdegfxd2[[i]]], "Normalized" -> False],
        {i, Length@reduceddata1sthalflist}];
     esinglerandomgraphscomm2 = Table[randomizinggraphmod[egraphsandnodenumbers2[[i, 1]]],
        {i, Length@reduceddata1sthalflist}];
     esinglerandomcommmodularityvalues2 =
      Table [N@GraphAssortativity [esinglerandomgraphscomm2[[i]],
          FindGraphCommunities[esinglerandomgraphscomm2[[i]]], "Normalized" -> False],
        {i, Length@reduceddata1sthalflist}];
     eZscoresmodularity2 = Table[zscorefunctionfortwonullmodels[
         egraphsandnodenumbers2[[i, 1]]], {i, Length@reduceddata1sthalflist}];
     ebucketnode21 = Table[egraphsandnodenumbers2[[i, 2]],
        {i, Length@reduceddata1sthalflist}]]
```

```
In[*]:= AbsoluteTiming[ethicknessdataFixedstep2 =
       Table[snetworkdatabinned[10, stepsizethickness, i], {i, reduceddata2ndhalflist}];
      egraphsandnodenumbers22 = Table[snetworkgraph[ethicknessdataFixedstep2[[i, 1]],
         ethicknessdataFixedstep2[[i, 2]], 2, 7, 400, Green],
        {i, Length@reduceddata2ndhalflist}];
      emodularityvalues22 = Table [N@GraphAssortativity [egraphsandnodenumbers22 [ [i, 1] ],
          FindGraphCommunities[egraphsandnodenumbers22[[i, 1]]], "Normalized" → False],
        {i, Length@reduceddata2ndhalflist}];
      esinglerandomgraphsdegfxd22 = Table[randomizinggraphdegfxd[
         egraphsandnodenumbers22[[i, 1]]], {i, Length@reduceddata2ndhalflist}];
      esinglerandomerdrenmodularityvalues22 =
       Table [N@GraphAssortativity[esinglerandomgraphsdegfxd22[[i]],
          FindGraphCommunities[esinglerandomgraphsdegfxd22[[i]]], "Normalized" -> False],
        {i, Length@reduceddata2ndhalflist}];
      esinglerandomgraphscomm22 = Table[randomizinggraphmod[egraphsandnodenumbers22[[i, 1]]],
        {i, Length@reduceddata2ndhalflist}];
      esinglerandomcommmodularityvalues22 =
       Table [N@GraphAssortativity[esinglerandomgraphscomm22[[i]],
          FindGraphCommunities[esinglerandomgraphscomm22[[i]]], "Normalized" -> False],
        {i, Length@reduceddata2ndhalflist}];
      eZscoresmodularity22 = Table[zscorefunctionfortwonullmodels[
         egraphsandnodenumbers22[[i, 1]]], {i, Length@reduceddata2ndhalflist}];
      ebucketnode22 = Table[egraphsandnodenumbers22[[i, 2]],
        {i, Length@reduceddata2ndhalflist}]]
Out[\circ] = \{149.217, \{26, 26, 26, 26, 26, 26, 25, 26, 25, 26\}\}
```

```
In[*]:= AbsoluteTiming[ethicknessdataFixedstep3 =
       Table[snetworkdatabinned[10, stepsizethickness, i], {i, reduceddatafulllist}];
      egraphsandnodenumbers23 =
       Table[snetworkgraph[ethicknessdataFixedstep3[[i, 1]], ethicknessdataFixedstep3[[i, 2]],
         2, 7, 400, Green], {i, Length@reduceddatafulllist}];
      emodularityvalues23 = Table[N@GraphAssortativity[egraphsandnodenumbers23[[i, 1]],
          FindGraphCommunities[egraphsandnodenumbers23[[i, 1]]],
          "Normalized" → False], {i, Length@reduceddatafulllist}];
      esinglerandomgraphsdegfxd23 = Table[randomizinggraphdegfxd[
         egraphsandnodenumbers23[[i, 1]]], {i, Length@reduceddatafulllist}];
      esinglerandomerdrenmodularityvalues23 =
       Table [N@GraphAssortativity[esinglerandomgraphsdegfxd23[[i]],
          FindGraphCommunities[esinglerandomgraphsdegfxd23[[i]]],
          "Normalized" -> False], {i, Length@reduceddatafulllist}];
      esinglerandomgraphscomm23 = Table[randomizinggraphmod[egraphsandnodenumbers23[[i, 1]]],
        {i, Length@reduceddatafulllist}];
      esinglerandomcommmodularityvalues23 =
       Table [N@GraphAssortativity [esinglerandomgraphscomm23[[i]],
          FindGraphCommunities[esinglerandomgraphscomm23[[i]]],
          "Normalized" -> False], {i, Length@reduceddatafulllist}];
      eZscoresmodularity23 = Table[zscorefunctionfortwonullmodels[
         egraphsandnodenumbers23[[i, 1]]], {i, Length@reduceddatafulllist}];
      ebucketnode23 = Table[egraphsandnodenumbers23[[i, 2]], {i, Length@reduceddatafulllist}]]
Outf^{\circ} { 137.541, {27, 28, 28, 28, 28, 28, 28, 28, 28, 28} }
<code>ln[*]:= emodvalues2 = {emodularityvalues2, emodularityvalues23};</code>
     eZscores2 = {eZscoresmodularity2, eZscoresmodularity23};
     Export["error_bar_values/" <> productionline <> "-modularity_values2.mx", emodvalues2];
     Export["error_bar_values/" <> productionline <> "-zscores2.mx", eZscores2];
Info := (* emodvalues2=Import["error_bar_values/CCM5-modularity_values2.mx"];
     eZscores2=Import["error_bar_values/CCM5-zscores2.mx"];*)
In[@]:= set21 = plotcolumn[modularityvalues2,
        singlerandomerdrenmodularityvalues2, singlerandomcommmodularityvalues2,
        Zscoresmodularity2[[1]], Zscoresmodularity2[[2]], eZscores2[[1]]];
    set22 = plotcolumn[modularityvalues22, singlerandomerdrenmodularityvalues22,
        singlerandomcommmodularityvalues22, Zscoresmodularity22[[1]],
        Zscoresmodularity22[[2]], eZscores2[[2]]];
    set23 = plotcolumn[modularityvalues23, singlerandomerdrenmodularityvalues23,
        singlerandomcommmodularityvalues23, Zscoresmodularity23[[1]],
        Zscoresmodularity23[[2]], eZscores2[[3]]];
     Legended[Framed[GraphicsRow[{set21, Magnify[set23, 1.03], set22}, ImageSize → 1093],
       FrameMargins → 5, FrameStyle → DotDashed], {Placed["First Half", {0.155, 0.99}],
       Placed["Complete Data", {0.505, 0.99}], Placed["Second Half", {0.86, 0.99}]}]
```



Fixed Bucket Size Networks

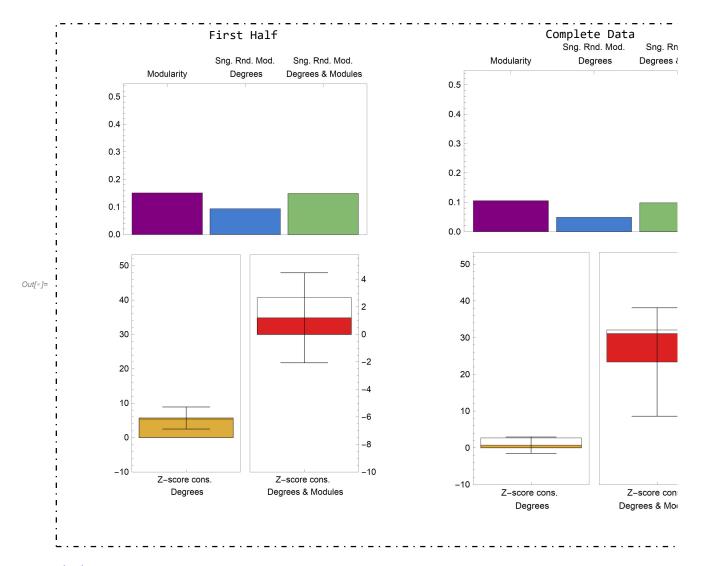
Width Feature

```
In[@]:= AbsoluteTiming[
     widthdataFixedbucket1 = snetworkdatafxdbucket[9, bucketnode11, data1sthalf];
     graphsandnodenumbers3 = snetworkgraph[widthdataFixedbucket1[[1]],
        widthdataFixedbucket1[[2]], 2, 7, 400, Green];
     modularityvalues3 = N@GraphAssortativity[graphsandnodenumbers3[[1]],
         FindGraphCommunities[graphsandnodenumbers3[[1]]], "Normalized" → False];
     singlerandomgraphsdegfxd3 = randomizinggraphdegfxd[graphsandnodenumbers3[[1]]];
     singlerandomerdrenmodularityvalues3 = N@GraphAssortativity[singlerandomgraphsdegfxd3,
         FindGraphCommunities[singlerandomgraphsdegfxd3], "Normalized" -> False];
     singlerandomgraphscomm3 = randomizinggraphmod[graphsandnodenumbers3[[1]]];
     singlerandomcommmodularityvalues3 = N@GraphAssortativity[singlerandomgraphscomm3,
         FindGraphCommunities[singlerandomgraphscomm3], "Normalized" -> False];
     Zscoresmodularity3 = zscorefunctionfortwonullmodels[graphsandnodenumbers3[[1]]];]
```

```
Out[*]= {13.8327, Null}
In[*]:= bucketsize11 = widthdataFixedbucket1[[4]]
Out[*]= { 316 }
In[*]:= AbsoluteTiming[
      widthdataFixedbucket2 = snetworkdatafxdbucket[9, bucketnode12, data2ndhalf];
      graphsandnodenumbers32 = snetworkgraph[widthdataFixedbucket2[[1]],
        widthdataFixedbucket2[[2]], 2, 7, 400, Green];
      modularityvalues32 = N@GraphAssortativity[graphsandnodenumbers32[[1]],
         FindGraphCommunities[graphsandnodenumbers32[[1]]], "Normalized" → False];
      singlerandomgraphsdegfxd32 = randomizinggraphdegfxd[graphsandnodenumbers32[[1]]];
      singlerandomerdrenmodularityvalues32 = N@GraphAssortativity[singlerandomgraphsdegfxd32,
         FindGraphCommunities[singlerandomgraphsdegfxd32], "Normalized" -> False];
      singlerandomgraphscomm32 = randomizinggraphmod[graphsandnodenumbers32[[1]]];
      singlerandomcommmodularityvalues32 = N@GraphAssortativity[singlerandomgraphscomm32,
         FindGraphCommunities[singlerandomgraphscomm32], "Normalized" -> False];
      Zscoresmodularity32 = zscorefunctionfortwonullmodels[graphsandnodenumbers32[[1]]];]
Out[*]= {18.2675, Null}
In[*]:= bucketsize12 = widthdataFixedbucket2[[4]]
Out[*]= { 309 }
Info := AbsoluteTiming [widthdataFixedbucket3 = snetworkdatafxdbucket [9, bucketnode13, datafull];
      graphsandnodenumbers33 = snetworkgraph[
        widthdataFixedbucket3[[1]], widthdataFixedbucket3[[2]], 2, 7, 400, Green];
      modularityvalues33 = N@GraphAssortativity[graphsandnodenumbers33[[1]],
         FindGraphCommunities[graphsandnodenumbers33[[1]]], "Normalized" → False];
      singlerandomgraphsdegfxd33 = randomizinggraphdegfxd[graphsandnodenumbers33[[1]]];
      singlerandomerdrenmodularityvalues33 = N@GraphAssortativity[singlerandomgraphsdegfxd33,
         FindGraphCommunities[singlerandomgraphsdegfxd33], "Normalized" -> False];
      singlerandomgraphscomm33 = randomizinggraphmod[graphsandnodenumbers33[[1]]];
      singlerandomcommmodularityvalues33 = N@GraphAssortativity[singlerandomgraphscomm33,
         FindGraphCommunities[singlerandomgraphscomm33], "Normalized" -> False];
      Zscoresmodularity33 = zscorefunctionfortwonullmodels[graphsandnodenumbers33[[1]]];]
Out[\circ] = \{20.0812, Null\}
In[@]:= bucketsize13 = widthdataFixedbucket3[[4]]
Out[*]= {617}
     Error Bars and Charts
```

```
ln[*]:= AbsoluteTiming[ewidthdataFixedbucket1 = Table[snetworkdatafxdbucket[9, i[[1]], i[[2]]],
        {i, MapThread[{#1, #2} &, {ebucketnode11, reduceddata1sthalflist}]}];
      egraphsandnodenumbers3 = Table[snetworkgraph[ewidthdataFixedbucket1[[i, 1]],
         ewidthdataFixedbucket1[[i, 2]], 2, 7, 400, Green],
        {i, Length@reduceddata1sthalflist}];
      emodularityvalues3 = Table[N@GraphAssortativity[egraphsandnodenumbers3[[i, 1]],
          FindGraphCommunities[egraphsandnodenumbers3[[i, 1]]], "Normalized" → False],
        {i, Length@reduceddata1sthalflist}];
      esinglerandomgraphsdegfxd3 = Table[randomizinggraphdegfxd[
         egraphsandnodenumbers3[[i, 1]]], {i, Length@reduceddata1sthalflist}];
      esinglerandomerdrenmodularityvalues3 =
       Table [N@GraphAssortativity [esinglerandomgraphsdegfxd3[[i]],
          FindGraphCommunities[esinglerandomgraphsdegfxd3[[i]]], "Normalized" -> False],
        {i, Length@reduceddata1sthalflist}];
      esinglerandomgraphscomm3 = Table[randomizinggraphmod[egraphsandnodenumbers3[[i, 1]]],
        {i, Length@reduceddata1sthalflist}];
      esinglerandomcommmodularityvalues3 =
       Table [N@GraphAssortativity [esinglerandomgraphscomm3[[i]],
          FindGraphCommunities[esinglerandomgraphscomm3[[i]]], "Normalized" -> False],
        {i, Length@reduceddata1sthalflist}];
      eZscoresmodularity3 = Table[zscorefunctionfortwonullmodels[
         egraphsandnodenumbers3[[i, 1]]], {i, Length@reduceddata1sthalflist}];]
Out[*]= {142.285, Null}
l_{n[e]}:= AbsoluteTiming[ewidthdataFixedbucket2 = Table[snetworkdatafxdbucket[9, i[[1]], i[[2]]],
        {i, MapThread[{#1, #2} &, {ebucketnode12, reduceddata2ndhalflist}]}];
      egraphsandnodenumbers32 = Table[snetworkgraph[ewidthdataFixedbucket2[[i, 1]],
         ewidthdataFixedbucket2[[i, 2]], 2, 7, 400, Green],
        {i, Length@reduceddata2ndhalflist}];
      emodularityvalues32 = Table[N@GraphAssortativity[egraphsandnodenumbers32[[i, 1]],
          FindGraphCommunities[egraphsandnodenumbers32[[i, 1]]], "Normalized" → False],
        {i, Length@reduceddata2ndhalflist}];
      esinglerandomgraphsdegfxd32 = Table[randomizinggraphdegfxd[
         egraphsandnodenumbers32[[i, 1]]], {i, Length@reduceddata2ndhalflist}];
      esinglerandomerdrenmodularityvalues32 =
       Table [N@GraphAssortativity[esinglerandomgraphsdegfxd32[[i]],
          FindGraphCommunities[esinglerandomgraphsdegfxd32[[i]]], "Normalized" -> False],
        {i, Length@reduceddata2ndhalflist}];
      esinglerandomgraphscomm32 = Table[randomizinggraphmod[egraphsandnodenumbers32[[i, 1]]],
        {i, Length@reduceddata2ndhalflist}];
      esinglerandomcommmodularityvalues32 =
       Table [N@GraphAssortativity[esinglerandomgraphscomm32[[i]],
          FindGraphCommunities[esinglerandomgraphscomm32[[i]]], "Normalized" -> False],
        {i, Length@reduceddata2ndhalflist}];
      eZscoresmodularity32 = Table[zscorefunctionfortwonullmodels[
         egraphsandnodenumbers32[[i, 1]]], {i, Length@reduceddata2ndhalflist}];]
```

```
Out[*]= { 267.815, Null }
In[*]:= AbsoluteTiming[ewidthdataFixedbucket3 = Table[snetworkdatafxdbucket[9, i[[1]], i[[2]]],
        {i, MapThread[{#1, #2} &, {ebucketnode13, reduceddatafulllist}]}];
      egraphsandnodenumbers33 = Table[snetworkgraph[ewidthdataFixedbucket3[[i, 1]],
         ewidthdataFixedbucket3[[i, 2]], 2, 7, 400, Green], {i, Length@reduceddatafulllist}];
      emodularityvalues33 = Table[N@GraphAssortativity[egraphsandnodenumbers33[[i, 1]],
          FindGraphCommunities[egraphsandnodenumbers33[[i, 1]]],
          "Normalized" → False], {i, Length@reduceddatafulllist}];
      esinglerandomgraphsdegfxd33 = Table[randomizinggraphdegfxd[
         egraphsandnodenumbers33[[i, 1]]], {i, Length@reduceddatafulllist}];
      esinglerandomerdrenmodularityvalues33 =
       Table [N@GraphAssortativity[esinglerandomgraphsdegfxd33[[i]],
          FindGraphCommunities[esinglerandomgraphsdegfxd33[[i]]],
           "Normalized" -> False], {i, Length@reduceddatafulllist}];
      esinglerandomgraphscomm33 = Table[randomizinggraphmod[egraphsandnodenumbers33[[i, 1]]],
        {i, Length@reduceddatafulllist}];
      esinglerandomcommmodularityvalues33 =
       Table [N@GraphAssortativity [esinglerandomgraphscomm33[[i]],
          FindGraphCommunities[esinglerandomgraphscomm33[[i]]],
           "Normalized" -> False], {i, Length@reduceddatafulllist}];
      eZscoresmodularity33 = Table[zscorefunctionfortwonullmodels[
         egraphsandnodenumbers33[[i, 1]]], {i, Length@reduceddatafulllist}];]
Out[*]= { 368.134, Null }
Infer: emodvalues3 = {emodularityvalues3, emodularityvalues32, emodularityvalues33};
     eZscores3 = {eZscoresmodularity3, eZscoresmodularity32, eZscoresmodularity33};
     Export["error_bar_values/" <> productionline <> "-modularity_values3.mx", emodvalues3];
     Export["error_bar_values/" <> productionline <> "-zscores3.mx", eZscores3];
In[*]:= (* emodvalues3=Import["error bar values/CCM5-modularity values3.mx"];
     eZscores3=Import["error_bar_values/CCM5-zscores3.mx"]; *)
In[@]:= set31 = plotcolumn[modularityvalues3,
        singlerandomerdrenmodularityvalues3, singlerandomcommmodularityvalues3,
        Zscoresmodularity3[[1]], Zscoresmodularity3[[2]], eZscores3[[1]]];
     set32 = plotcolumn[modularityvalues32, singlerandomerdrenmodularityvalues32,
        singlerandomcommmodularityvalues32, Zscoresmodularity32[[1]],
        Zscoresmodularity32[[2]], eZscores3[[2]]];
     set33 = plotcolumn[modularityvalues33, singlerandomerdrenmodularityvalues33,
        singlerandomcommmodularityvalues33, Zscoresmodularity33[[1]],
        Zscoresmodularity33[[2]], eZscores3[[3]]];
     Legended[Framed[GraphicsRow[{set31, Magnify[set33, 1.03], set32}, ImageSize → 1093],
       FrameMargins → 5, FrameStyle → DotDashed], {Placed["First Half", {0.155, 0.99}],
       Placed["Complete Data", {0.505, 0.99}], Placed["Second Half", {0.86, 0.99}]]]
```



Thickness Feature

```
In[*]:= AbsoluteTiming[
      thicknessdataFixedbucket1 = snetworkdatafxdbucket[10, bucketnode21, data1sthalf];
      graphsandnodenumbers4 = snetworkgraph[thicknessdataFixedbucket1[[1]],
        thicknessdataFixedbucket1[[2]], 2, 7, 400, Green];
      modularityvalues4 = N@GraphAssortativity[graphsandnodenumbers4[[1]],
         FindGraphCommunities[graphsandnodenumbers4[[1]]], "Normalized" → False];
      singlerandomgraphsdegfxd4 = randomizinggraphdegfxd[graphsandnodenumbers4[[1]]];
      singlerandomerdrenmodularityvalues4 = N@GraphAssortativity[singlerandomgraphsdegfxd4,
         FindGraphCommunities[singlerandomgraphsdegfxd4], "Normalized" -> False];
      singlerandomgraphscomm4 = randomizinggraphmod[graphsandnodenumbers4[[1]]];
      singlerandomcommmodularityvalues4 = N@GraphAssortativity[singlerandomgraphscomm4,
         FindGraphCommunities[singlerandomgraphscomm4], "Normalized" -> False];
      Zscoresmodularity4 = zscorefunctionfortwonullmodels[graphsandnodenumbers4[[1]]];]
Out[ \circ ] = \{ 29.9691, Null \}
```

```
In[*]:= bucketsize21 = thicknessdataFixedbucket1[[4]]
Out[*]= {485}
In[*]:= AbsoluteTiming[
      thicknessdataFixedbucket2 = snetworkdatafxdbucket[10, bucketnode22, data2ndhalf];
      graphsandnodenumbers42 = snetworkgraph[thicknessdataFixedbucket2[[1]],
        thicknessdataFixedbucket2[[2]], 2, 7, 400, Green];
      modularityvalues42 = N@GraphAssortativity[graphsandnodenumbers42[[1]],
         FindGraphCommunities[graphsandnodenumbers42[[1]]], "Normalized" → False];
      singlerandomgraphsdegfxd42 = randomizinggraphdegfxd[graphsandnodenumbers42[[1]]];
      singlerandomerdrenmodularityvalues42 = N@GraphAssortativity[singlerandomgraphsdegfxd42,
         FindGraphCommunities[singlerandomgraphsdegfxd42], "Normalized" -> False];
      singlerandomgraphscomm42 = randomizinggraphmod[graphsandnodenumbers42[[1]]];
      singlerandomcommmodularityvalues42 = N@GraphAssortativity[singlerandomgraphscomm42,
         FindGraphCommunities[singlerandomgraphscomm42], "Normalized" -> False];
      Zscoresmodularity42 = zscorefunctionfortwonullmodels[graphsandnodenumbers42[[1]]];]
Out[@] = \{28.6945, Null\}
In[*]:= bucketsize22 = thicknessdataFixedbucket2[[4]]
Out[*]= { 523 }
In[@]:= AbsoluteTiming[
      thicknessdataFixedbucket3 = snetworkdatafxdbucket[10, bucketnode23, datafull];
      graphsandnodenumbers43 = snetworkgraph[thicknessdataFixedbucket3[[1]],
        thicknessdataFixedbucket3[[2]], 2, 7, 400, Green];
      modularityvalues43 = N@GraphAssortativity[graphsandnodenumbers43[[1]],
         FindGraphCommunities[graphsandnodenumbers43[[1]]], "Normalized" → False];
      singlerandomgraphsdegfxd43 = randomizinggraphdegfxd[graphsandnodenumbers43[[1]]];
      singlerandomerdrenmodularityvalues43 = N@GraphAssortativity[singlerandomgraphsdegfxd43,
         FindGraphCommunities[singlerandomgraphsdegfxd43], "Normalized" -> False];
      singlerandomgraphscomm43 = randomizinggraphmod[graphsandnodenumbers43[[1]]];
      singlerandomcommmodularityvalues43 = N@GraphAssortativity[singlerandomgraphscomm43,
         FindGraphCommunities[singlerandomgraphscomm43], "Normalized" -> False];
      Zscoresmodularity43 = zscorefunctionfortwonullmodels[graphsandnodenumbers43[[1]]];]
Out[*]= {33.0375, Null}
In[*]:= bucketsize23 = thicknessdataFixedbucket3[[4]]
Out[ • ]= { 970 }
     Error Bars and Charts
```

```
In[@]:= AbsoluteTiming[
      ethicknessdataFixedbucket1 = Table[snetworkdatafxdbucket[10, i[[1]], i[[2]]],
        {i, MapThread[{#1, #2} &, {ebucketnode21, reduceddata1sthalflist}]}];
      egraphsandnodenumbers4 = Table[snetworkgraph[ethicknessdataFixedbucket1[[i, 1]],
         ethicknessdataFixedbucket1[[i, 2]], 2, 7, 400, Green],
        {i, Length@reduceddata1sthalflist}];
      emodularityvalues4 = Table[N@GraphAssortativity[egraphsandnodenumbers4[[i, 1]],
          FindGraphCommunities[egraphsandnodenumbers4[[i, 1]]], "Normalized" → False],
        {i, Length@reduceddata1sthalflist}];
      esinglerandomgraphsdegfxd4 = Table[randomizinggraphdegfxd[
         egraphsandnodenumbers4[[i, 1]]], {i, Length@reduceddata1sthalflist}];
      esinglerandomerdrenmodularityvalues4 =
       Table [N@GraphAssortativity[esinglerandomgraphsdegfxd4[[i]],
          FindGraphCommunities[esinglerandomgraphsdegfxd4[[i]]], "Normalized" -> False],
        {i, Length@reduceddata1sthalflist}];
      esinglerandomgraphscomm4 = Table[randomizinggraphmod[egraphsandnodenumbers4[[i, 1]]],
        {i, Length@reduceddata1sthalflist}];
      esinglerandomcommmodularityvalues4 =
       Table [N@GraphAssortativity [esinglerandomgraphscomm4[[i]],
          FindGraphCommunities[esinglerandomgraphscomm4[[i]]], "Normalized" -> False],
        {i, Length@reduceddata1sthalflist}];
      eZscoresmodularity4 = Table[zscorefunctionfortwonullmodels[
         egraphsandnodenumbers4[[i, 1]]], {i, Length@reduceddata1sthalflist}];]
Out[*]= { 204.245, Null }
```

```
In[@]:= AbsoluteTiming[
      ethicknessdataFixedbucket2 = Table[snetworkdatafxdbucket[10, i[[1]], i[[2]]],
        {i, MapThread[{#1, #2} &, {ebucketnode22, reduceddata2ndhalflist}]}];
      egraphsandnodenumbers42 = Table[snetworkgraph[ethicknessdataFixedbucket2[[i, 1]],
         ethicknessdataFixedbucket2[[i, 2]], 2, 7, 400, Green],
        {i, Length@reduceddata2ndhalflist}];
      emodularityvalues42 = Table [N@GraphAssortativity [egraphsandnodenumbers42 [ [i, 1] ],
          FindGraphCommunities[egraphsandnodenumbers42[[i, 1]]], "Normalized" → False],
        {i, Length@reduceddata2ndhalflist}];
      esinglerandomgraphsdegfxd42 = Table[randomizinggraphdegfxd[
         egraphsandnodenumbers42[[i, 1]]], {i, Length@reduceddata2ndhalflist}];
      esinglerandomerdrenmodularityvalues42 =
       Table [N@GraphAssortativity[esinglerandomgraphsdegfxd42[[i]],
          FindGraphCommunities[esinglerandomgraphsdegfxd42[[i]]], "Normalized" -> False],
        {i, Length@reduceddata2ndhalflist}];
      esinglerandomgraphscomm42 = Table[randomizinggraphmod[egraphsandnodenumbers42[[i, 1]]],
        {i, Length@reduceddata2ndhalflist}];
      esinglerandomcommmodularityvalues42 =
       Table [N@GraphAssortativity [esinglerandomgraphscomm42[[i]],
          FindGraphCommunities[esinglerandomgraphscomm42[[i]]], "Normalized" -> False],
        {i, Length@reduceddata2ndhalflist}];
      eZscoresmodularity42 = Table[zscorefunctionfortwonullmodels[
         egraphsandnodenumbers42[[i, 1]]], {i, Length@reduceddata2ndhalflist}];]
Out[\circ] = \{250.325, Null\}
```

```
In[@]:= AbsoluteTiming[
      ethicknessdataFixedbucket3 = Table[snetworkdatafxdbucket[10, i[[1]], i[[2]]],
        {i, MapThread[{#1, #2} &, {ebucketnode23, reduceddatafulllist}]}];
      egraphsandnodenumbers43 = Table[snetworkgraph[ethicknessdataFixedbucket3[[i, 1]],
         ethicknessdataFixedbucket3[[i, 2]], 2, 7, 400, Green],
        {i, Length@reduceddatafulllist}];
      emodularityvalues43 = Table[N@GraphAssortativity[egraphsandnodenumbers43[[i, 1]],
          FindGraphCommunities[egraphsandnodenumbers43[[i, 1]]],
           "Normalized" → False], {i, Length@reduceddatafulllist}];
      esinglerandomgraphsdegfxd43 = Table[randomizinggraphdegfxd[
         egraphsandnodenumbers43[[i, 1]]], {i, Length@reduceddatafulllist}];
      esinglerandomerdrenmodularityvalues43 =
       Table [N@GraphAssortativity[esinglerandomgraphsdegfxd43[[i]],
          FindGraphCommunities[esinglerandomgraphsdegfxd43[[i]]],
           "Normalized" -> False], {i, Length@reduceddatafulllist}];
      esinglerandomgraphscomm43 = Table[randomizinggraphmod[egraphsandnodenumbers43[[i, 1]]],
        {i, Length@reduceddatafulllist}];
      esinglerandomcommmodularityvalues43 =
       Table [N@GraphAssortativity [esinglerandomgraphscomm43[[i]],
          FindGraphCommunities[esinglerandomgraphscomm43[[i]]],
           "Normalized" -> False], {i, Length@reduceddatafulllist}];
      eZscoresmodularity43 = Table[zscorefunctionfortwonullmodels[
         egraphsandnodenumbers43[[i, 1]]], {i, Length@reduceddatafulllist}];]
Out[\circ] = \{301.612, Null\}
In[*]:= emodvalues4 = {emodularityvalues4, emodularityvalues42, emodularityvalues43};
     eZscores4 = {eZscoresmodularity4, eZscoresmodularity42, eZscoresmodularity43};
     Export["error_bar_values/" <> productionline <> "-modularity_values4.mx", emodvalues4];
     Export["error_bar_values/" <> productionline <> "-zscores4.mx", eZscores4];
Info := (* emodvalues4=Import["error_bar_values/CCM5-modularity_values4.mx"];
     eZscores4=Import["error_bar_values/CCM5-zscores4.mx"]; *)
In[@]:= set41 = plotcolumn[modularityvalues4,
        singlerandomerdrenmodularityvalues4, singlerandomcommmodularityvalues4,
        Zscoresmodularity4[[1]], Zscoresmodularity4[[2]], eZscores4[[1]]];
    set42 = plotcolumn[modularityvalues42, singlerandomerdrenmodularityvalues42,
        singlerandomcommmodularityvalues42, Zscoresmodularity42[[1]],
        Zscoresmodularity42[[2]], eZscores4[[2]]];
    set43 = plotcolumn[modularityvalues43, singlerandomerdrenmodularityvalues43,
        singlerandomcommmodularityvalues43, Zscoresmodularity43[[1]],
        Zscoresmodularity43[[2]], eZscores4[[3]]];
     Legended[Framed[GraphicsRow[{set41, Magnify[set43, 1.03], set42}, ImageSize → 1093],
       FrameMargins → 5, FrameStyle → DotDashed], {Placed["First Half", {0.155, 0.99}],
       Placed["Complete Data", {0.505, 0.99}], Placed["Second Half", {0.86, 0.99}]}]
```

