

```
BeginPackage["SingleNetworks`"];
```

```
snetworkdatasingleintimewindows::usage = "description.";
snetworkgraphsinglenodes::usage = "description.";
snetworkdatabinned::usage = "description.";
snetworkdatafxdbucket::usage = "description.";
snetworkdatabinnedintimewindows::usage = "description.";
snetworkdatafxdbucketintimewindows::usage = "description.";
snetworkgraph::usage = "description.";
correlationfunction::usage = "description.";
randomnessfunction::usage = "description.";
GirvanNewmanmodularity::usage = "description.";
randomizedgraphamongcommunities::usage = "description.";
randomnessfunctionformodularity::usage = "description.";
randomnessfunctionformodularityonnullmodel::usage = "description.";
randomnessfunctionformodularitytwonullmodel::usage = "description.";
randomnessvaluesformodularitytwonullmodel::usage = "description.";
```

```
Begin["`Private`"];
```

```
Clear[snetworkdatasingleintimewindows]
snetworkdatasingleintimewindows[feature_, datadimension_] := Module[{rawaim, pos, aim, campaig
rawaim = Table[Symbol["data"]][[i]][[All, feature]], {i, Range@datadimension}];
pos = Table[Partition[Flatten@Table[Position[k, i], {i, {"NA", 0}}], 1], {k, rawaim}];
aim = Table[Delete[i[[1]], i[[2]]], {i, MapThread[{#1, #2} &, {rawaim, pos}]}];
campaign = Table[Delete[Symbol["data"]][[i[[1]]]][[All, 2]], i[[2]],
{i, MapThread[{#1, #2} &, {Range@datadimension, pos}]}];
seri = Table[Delete[Symbol["data"]][[i[[1]]]][[All, 1]], i[[2]],
{i, MapThread[{#1, #2} &, {Range@datadimension, pos}]}];
{aim, campaign, seri}]
```

```

Clear[snetworkgraphsinglenodes]
snetworkgraphsinglenodes[aim_,campaign_,vertexsize_,vertexlabelsize_,imagesize_,vertexcolor_] := Module[{binningmembers,aimbaskets,singlesupportvalues,pairs,pairsupportvalues,liftvalues,allmatricelements,likelypairs,binarymatrix,graph},
binningmembers=Sort[DeleteDuplicates[aim]];
aimbaskets=Table[DeleteDuplicates[i],{i,Values@GroupBy[Thread[{aim,campaign}],Last->First]},1];
singlesupportvalues=Table[N[Count[Table[MemberQ[i,j],{i,aimbaskets}],True]/Length[aimbaskets]],{j,binningmembers}];
pairs=Subsets[binningmembers,{2}];
pairsupportvalues=Table[N[Count[Table[SubsetQ[i,j],{i,aimbaskets}],True]/Length[aimbaskets]],{j,pairs}];
liftvalues=pairsupportvalues/(DeleteCases[Flatten@UpperTriangularize[Table[singlesupportvalues[[j]]*singlesupportvalues[[k]],{j,Length[binningmembers]},{k,Length[binningmembers]}],1]);
allmatricelements=Sort[Join[pairs,Reverse[pairs,2],Table[{i,i},{i,binningmembers}]]];
likelypairs=Extract[pairs,Position[liftvalues,x_/;>1]];
binarymatrix=ArrayReshape[Table[If[j==True,1,0],{j,Table[MemberQ[likelypairs,i],{i,allmatricelements}]}],{Length@binningmembers,Length@binningmembers}];
graph=AdjacencyGraph[binarymatrix,{GraphLayout->Automatic,DirectedEdges->False,EdgeShapeFunction->"Line",VertexSize->vertexsize,VertexStyle->vertexcolor,VertexLabelStyle->Directive[Black,Italic,vertexlabelsize],VertexLabels->Flatten[MapThread[{#1->Placed[#2,Center]}&,{Range[1,Dimensions[binarymatrix][[1]]},binningmembers}]}],ImageSize->imagesize];{graph,Length@binningmembers}]

```

```

Clear[snetworkdatabinned]
snetworkdatabinned[feature_,step_,data_] := Module[{rawaim,pos,aim,campaign,seri,min,max,binningamount,binning},
rawaim=data[[All,feature]];
pos=Partition[Flatten@Table[Position[rawaim,i],{i,{"NA",0}}],1];
aim=Delete[rawaim,pos];
campaign=Delete[data[[All,2]],pos];
seri=Delete[data[[All,1]],pos];
min=Floor[Min[Sort[DeleteDuplicates[aim]]],0.1];
max=Ceiling[Max[Sort[DeleteDuplicates[aim]]]+step];
binningamount=Length[DeleteCases[BinLists[aim,{min,max,step}],{}]];
binning=Table[Catch[Do[If[IntervalMemberQ[Interval[i],aim[[j]]]==True,Throw[i]],{i,Partition[Range[min,max,step],2,1]}]],{j,Length[aim]}];
aim=DeleteCases[binning,Null];
{aim,campaign,seri}]

```

```

Clear[snetworkdatafxdbucket]
snetworkdatafxdbucket[feature_, nodenumber_, data_] := Module[{rawaim, pos, aim,
campaign, seri, bucketsize, aimlabeled, aimpartitioned, bins, repetitivesreport, repetitives,
labelgeneration, binsrearranged, aimbinned},
rawaim = data[[All, feature]];
pos = Partition[Flatten@Table[Position[rawaim, i], {i, {"NA", 0}}], 1];
aim = Delete[rawaim, pos];
campaign = Delete[data[[All, 2]], pos];
seri = Delete[data[[All, 1]], pos];
bucketsize = Ceiling[(N@Dimensions@aim)/nodenumber];
aimlabeled = Thread[Range@Length@aim -> aim];
aimpartitioned = Partition[Normal@Sort@Association@aimlabeled, UpTo@bucketsize];
bins = Table[MinMax[i], {i, Values@aimpartitioned}];
repetitivesreport = DeleteCases[Tally@bins, x_ /; x[[2]] == 1];
repetitives = repetitivesreport[[All, 1]];

labelgeneration[x_] := Table[{repetitives[x] [[1]] + i*repetitives[x] [[1]]
/ (2*10^(RealDigits@repetitives[x] [[1]] + 1) [[2]]), repetitives[x] [[2]] +
i*repetitives[x] [[2]] / (2*10^(RealDigits@repetitives[x] [[2]] + 1) [[2]])},
{i, Range@repetitivesreport[x] [[2]]}];

binsrearranged = ReplacePart[bins, Flatten[Table[MapThread[#1 -> #2 &,
{Flatten@Position[bins, repetitives[g]], labelgeneration[g]}],
{g, Range@Length@repetitives}], 1]];

aimbinned = Values@Sort[Flatten[Table[aimpartitioned[[i]] /.
Dispatch@Table[Values@aimpartitioned[[i]] [[j]] -> binsrearranged[[i]],
{j, Length@aimpartitioned[[i]]}], {i, Length@aimpartitioned}], 1], #1[[1]] < #2[[1]] &];
{aimbinned, campaign, seri}]

```

```

Clear[snetworkdatabinnedintimewindows]
snetworkdatabinnedintimewindows[data_,feature_,step_,datadimension_] := Module[{rawaim,pos,
campaign,seri,min,max,binningamount,binning},
rawaim=Table[data[[i]][[All,feature]],{i,Range@datadimension}];
pos=Table[Partition[Flatten@Table[Position[k,i],{i,{"NA",0}}],1],{k,rawaim}];
aim=Table[Delete[i[[1]],i[[2]]],{i,MapThread[{#1,#2}&,{rawaim,pos}}]};
campaign=Table[Delete[data[[i[[1]]]][[All,2]],i[[2]]],
{i,MapThread[{#1,#2}&,{Range@datadimension,pos}}]};
seri=Table[Delete[data[[i[[1]]]][[All,1]],i[[2]]],
{i,MapThread[{#1,#2}&,{Range@datadimension,pos}}]};
min=Table[Floor[Min[Sort[DeleteDuplicates[i]]],0.1],{i,aim}];
max=Table[Ceiling[Max[Sort[DeleteDuplicates[i]]]+step,{i,aim}];
binningamount=Table[Length[DeleteCases[BinLists[i[[1]],{i[[2]],i[[3]],step}],{}]],
{i,MapThread[{#1,#2,#3}&,{aim,min,max}}]};
binning=Table[Table[Catch[Do[If[IntervalMemberQ[Interval[i],(k[[1]])[[j]]]==True,Throw
{i,Partition[Range[k[[2]],k[[3]],step],2,1]}]],{j,Length[k[[1]]]}],{k,MapThread[{#1,#2
{aim,min,max}}]};
aim=Table[DeleteCases[i,Null],{i,binning}];
{aim,campaign,seri}]

```

```

Clear[snetworkdatafxdbucketintimewindows]
snetworkdatafxdbucketintimewindows[data_,feature_,nodenumber_,datadimension_] := Module[{r
pos,aim,campaign,seri,bucketsize,aimlabeled,aimpartitioned,bins,repetitivesreport,repeti
labelgeneration,binsrearranged,aimbinned},
rawaim=Table[data[[i]][[All,feature]],{i,Range@datadimension}];
pos=Table[Partition[Flatten@Table[Position[k,i],{i,{"NA",0}},1],{k,rawaim}];
aim=Table[Delete[i[[1]],i[[2]]],{i,MapThread[{#1,#2}&,{rawaim,pos}}];
campaign=Table[Delete[data[[i[[1]]]][[All,2]],i[[2]]],
{i,MapThread[{#1,#2}&,{Range@datadimension,pos}}];
seri=Table[Delete[data[[i[[1]]]][[All,1]],i[[2]]],
{i,MapThread[{#1,#2}&,{Range@datadimension,pos}}];
bucketsize=Table[Ceiling@N@Dimensions@i/nodenumber,{i,aim}];
aimlabeled=Table[Thread[Range@Length@i->i],{i,aim}];
aimpartitioned=Table[Partition[Normal@Sort@Association@i[[1]],UpTo@i[[2]]],
{i,MapThread[{#1,#2}&,{aimlabeled,bucketsize}}];
bins=Table[Table[MinMax[i],{i,Values@k}],{k,aimpartitioned}];
repetitivesreport=Table[DeleteCases[Tally@i,x_/;x[[2]]==1],{i,bins}];
repetitives=Table[i[[All,1]],{i,repetitivesreport}];

labelgeneration[x_,dim_] := Table[{repetitives[[dim]][[x]][[1]]+i*repetitives[[dim]][[x]
/(2*10^(RealDigits@repetitives[[dim]][[x]][[1]]+1)[[2]]),repetitives[[dim]][[x]][[2]]
i*repetitives[[dim]][[x]][[2]]/(2*10^(RealDigits@repetitives[[dim]][[x]][[2]]+1)[[2]]
{i,Range@repetitivesreport[[dim]][[x]][[2]]}];

binsrearranged=Table[ReplacePart[bins[[o]],Flatten[Table[MapThread[#1->#2&,
{Flatten@Position[bins[[o]],repetitives[[o]][[g]]},labelgeneration[g,o]],
{g,Range@Length@repetitives[[o]]},1]],{o,Range@datadimension}];

aimbinned=Table[Values@Sort[Flatten[Table[aimpartitioned[[k]][[i]]/.
Dispatch@Table[Values@aimpartitioned[[k]][[i]][[j]]->binsrearranged[[k]][[i]],
{j,Length@aimpartitioned[[k]][[i]]},{i,Length@aimpartitioned[[k]]},1],#1[[1]]<#2[[1]
{k,Range@datadimension}];{aimbinned,campaign,seri}]

```

```

Clear[snetworkgraph]
snetworkgraph[aim_,campaign_,vertexsize_,vertexlabelsize_,imagesize_,vertexcolor_] := Module[
  binningmembers, aimbaskets, singlesupportvalues, pairs, pairsupportvalues, liftvalues,
  allmatricelements, likelypairs, binarymatrix, graph},
  binningmembers = Sort[DeleteDuplicates[aim]];
  aimbaskets = Table[DeleteDuplicates[i], {i, Values@GroupBy[Thread[{aim, campaign}], Last -> First]}];
  singlesupportvalues = Table[N[Count[Table[MemberQ[i, j], {i, aimbaskets}],
    True]/Length[aimbaskets]], {j, binningmembers}];
  pairs = Subsets[binningmembers, {2}];
  pairsupportvalues = Table[N[Count[Table[SubsetQ[i, j], {i, aimbaskets}], True]/
    Length[aimbaskets]], {j, pairs}];
  liftvalues = pairsupportvalues / (DeleteCases[Flatten@UpperTriangularize[Table[singlesupport
    [[j]] * singlesupportvalues[[k]], {j, Length[binningmembers]}, {k, Length[binningmembers]}], 1
  allmatricelements = Sort[Join[pairs, Reverse[pairs, 2], Table[{i, i}, {i, binningmembers}]]];
  likelypairs = Extract[pairs, Position[liftvalues, x_ /; x > 1]];
  binarymatrix = ArrayReshape[Table[If[j == True, 1, 0], {j, Table[MemberQ[likelypairs, i],
    {i, allmatricelements}]}], {Length@binningmembers, Length@binningmembers}];
  graph = AdjacencyGraph[binarymatrix, {GraphLayout -> Automatic, DirectedEdges -> False,
    EdgeShapeFunction -> "Line", VertexSize -> vertexsize, VertexStyle -> vertexcolor,
    VertexLabelStyle -> Directive[Black, Italic, vertexlabelsize], VertexLabels -> Flatten[MapThread[
    {#1 -> Placed[#2, Center]} &, {Range[1, Dimensions[binarymatrix][[1]]}, Table[StringRiffle[i, "
    {i, binningmembers}]]}], ImageSize -> imagesize]; {graph, Length@binningmembers}]

```

```

Clear[correlationfunction]
correlationfunction[network_, choice_] := Module[{De, CC, BC, DeBC, CCBC, out},
  De = VertexDegree[network];
  CC = LocalClusteringCoefficient[network];
  BC = BetweennessCentrality[network];
  DeBC = Which[choice == 1, SpearmanRho[De, BC], choice == 2, Correlation[De, BC], choice == 3,
    Kendall1Tau[[De, BC]]];
  CCBC = Which[choice == 1, SpearmanRho[CC, BC], choice == 2, Correlation[CC, BC], choice == 3,
    Kendall1Tau[[CC, BC]]];
  out = {DeBC, CCBC}]

```

```

Clear[randomnessfunction]
randomnessfunction[network_,choice_] :=
Module[{randomgraphs,MuDeBC,MuCCBC,XDeBC,XCCBC,SigmaDeBC,SigmaCCBC,ZDeBC,ZCCBC,final},
SeedRandom[17];
randomgraphs=RandomGraph[{VertexCount[network],EdgeCount[network]},1000];
MuDeBC=Mean[Table[correlationfunction[randomgraphs[[i]],choice][[1]],{i,1000}]];
MuCCBC=Mean[Table[correlationfunction[randomgraphs[[i]],choice][[2]],{i,1000}]];
XDeBC=correlationfunction[network,choice][[1]];
XCCBC=correlationfunction[network,choice][[2]];
SigmaDeBC=StandardDeviation[Table[correlationfunction[randomgraphs[[i]],choice][[1]],{i,1000}]];
SigmaCCBC=StandardDeviation[Table[correlationfunction[randomgraphs[[i]],choice][[2]],{i,1000}]];
ZDeBC=(XDeBC-MuDeBC)/SigmaDeBC;
ZCCBC=(XCCBC-MuCCBC)/SigmaCCBC;
final={ZDeBC,ZCCBC}]

```

```

Clear[GirvanNewmanmodularity]
GirvanNewmanmodularity[xx_] := Module[{network, m, Aij, B, u,  $\beta$ , s, Q, div1, div2, moditer, r1, r11, r12, r21, r22, subfinal1Q, subfinal2Q, finalQ},
network = xx;
m = EdgeCount@network;
Aij = AdjacencyMatrix@network;
B = N@ (Aij - Outer[Times, VertexDegree@network, VertexDegree@network] / (2 * m));
u = Eigenvectors@B;
 $\beta$  = Eigenvalues@B;
s = (u /. x_ /; x < 0 -> -1) /. x_ /; x >= 0 -> 1;
Q = (Total@ (Table[{u[[i]] . Flatten@s[[Flatten@Position[ $\beta$ , Max@ $\beta$ ][[1]]]]]^2,
{i, VertexList@network} *  $\beta$ )) / (4 * m);
div1 = Flatten@Position[Flatten@s[[Flatten@Position[ $\beta$ , Max@ $\beta$ ][[1]]]], _?Negative];
div2 = Flatten@Position[Flatten@s[[Flatten@Position[ $\beta$ , Max@ $\beta$ ][[1]]]], _?Positive];
moditer[pos_, B1_] := Module[{Bg, ug,  $\beta$ g, sg, deltaQ, divv1, divv2, Bg1, Bg2},
Bg = (Table[B1[[i, j]] - KroneckerDelta[i, j] * Total@B1[[i, pos]], {i, Length@B1}, {j, Length@B1}][[pos, pos]]);
ug = Eigenvectors@Bg;
 $\beta$ g = Eigenvalues@Bg;
sg = (ug /. x_ /; x < 0 -> -1) /. x_ /; x >= 0 -> 1;
deltaQ = (Total@ (Table[{ug[[i]] . Flatten@sg[[Flatten@Position[ $\beta$ g, Max@ $\beta$ g][[1]]]]]^2,
{i, Range@Length@pos} *  $\beta$ g)) / (4 * m);
divv1 = Flatten@Position[Flatten@sg[[Flatten@Position[ $\beta$ g, Max@ $\beta$ g][[1]]]], _?Negative];
divv2 = Flatten@Position[Flatten@sg[[Flatten@Position[ $\beta$ g, Max@ $\beta$ g][[1]]]], _?Positive];
{deltaQ, divv1, divv2, Bg}};
r1 = moditer[div1, B];
r11 = If[r1[[1]] > 0.001, moditer[r1[[2]], r1[[4]]], {0, 0, 0, 0}];
r12 = If[r1[[1]] > 0.001, moditer[r1[[3]], r1[[4]]], {0, 0, 0, 0}];
r2 = moditer[div2, B];
r21 = If[r2[[1]] > 0.001, moditer[r2[[2]], r2[[4]]], {0, 0, 0, 0}];
r22 = If[r2[[1]] > 0.001, moditer[r2[[3]], r2[[4]]], {0, 0, 0, 0}];
subfinal1Q = If[r1[[1]] > 0.001, If[r11[[1]] > 0.001, If[r12[[1]] > 0.001, r12[[1]] + r11[[1]] + r1[[1]] + r11[[1]] + r1[[1]], If[r12[[1]] > 0.001, r12[[1]] + r1[[1]], r1[[1]]], 0];
subfinal2Q = If[r2[[1]] > 0.001, If[r21[[1]] > 0.001, If[r22[[1]] > 0.001, r22[[1]] + r21[[1]] + r2[[1]] + r21[[1]] + r2[[1]], If[r22[[1]] > 0.001, r22[[1]] + r2[[1]], r2[[1]]], 0];
finalQ = Q + subfinal1Q + subfinal2Q]

```



```

Clear[randomizedgraphamongcommunities]
randomizedgraphamongcommunities[network_] :=
Module[{networknodes, communitylist, intralinks, interlinks, intralinkamount, rewiredintra,
interlinknodes, interlinkamount, rewiredinter, rewiredgraph},
networknodes=VertexList@network;
communitylist=FindGraphCommunities[network];
intralinks=EdgeList[Subgraph[network, #] ]&/@communitylist;
interlinks=Complement[EdgeList[network], Flatten@intralinks];
intraLinkAmount=Table[Length@intralinks[[i]], {i, Length@communitylist}];
rewiredintra=Table[#1->#2&@@@RandomSample[
Subsets[communitylist[[i]], {2}], intraLinkAmount[[i]], {i, Length@communitylist}];
interlinknodes=DeleteDuplicates@Join[interlinks[[All, 1]], interlinks[[All, 2]]];
interlinkamount=Length@interlinknodes;
rewiredinter=#1->#2&@@@RandomSample[Subsets[interlinknodes, {2}], interlinkamount];
rewiredgraph=Graph[networknodes, Flatten[{rewiredintra, rewiredinter}]]]

```

```

Clear[randomnessfunctionformodularity]
randomnessfunctionformodularity[network_,modularitytype_] :=
Module[{X,randomgraphserdösrenyi,modularityerdösrenyi, $\mu$ erdösrenyi, $\sigma$ erdösrenyi,
randomgraphsdegreesfxd,modularitydegreesfxd, $\mu$ degreesfxd, $\sigma$ degreesfxd,randomgraphscomm,
modularitycomm, $\mu$ comm, $\sigma$ comm,ZScores},

X=Which[modularitytype=="GN",GirvanNewmanmodularity[network],modularitytype=="Wolf",
N@GraphAssortativity[network,FindGraphCommunities[network],"Normalized"->False]];

randomgraphserdösrenyi=RandomGraph[{VertexCount[network],EdgeCount[network]},1000];
modularityerdösrenyi=Which[modularitytype=="GN",Table[GirvanNewmanmodularity[
randomgraphserdösrenyi[[i]],{i,1000}],modularitytype=="Wolf",Table[N@GraphAssortativity[
randomgraphserdösrenyi[[i]],FindGraphCommunities[randomgraphserdösrenyi[[i]]],
"Normalized"->False],{i,1000}]]];
 $\mu$ erdösrenyi=Mean[Table[modularityerdösrenyi[[i]],{i,1000}]]];
 $\sigma$ erdösrenyi=StandardDeviation[Table[modularityerdösrenyi[[i]],{i,1000}]]];

randomgraphsdegreesfxd=Table[Symbol["IGDegreeSequenceGame"][Total[AdjacencyMatrix@network
Method->"VigerLatapy"],{i,1000}]];
modularitydegreesfxd=Which[modularitytype=="GN",Table[GirvanNewmanmodularity[
randomgraphsdegreesfxd[[i]],{i,1000}],modularitytype=="Wolf",Table[N@GraphAssortativity[
randomgraphsdegreesfxd[[i]],FindGraphCommunities[randomgraphsdegreesfxd[[i]]],
"Normalized"->False],{i,1000}]]];
 $\mu$ degreesfxd=Mean[Table[modularitydegreesfxd[[i]],{i,1000}]]];
 $\sigma$ degreesfxd=StandardDeviation[Table[modularitydegreesfxd[[i]],{i,1000}]]];

randomgraphscomm=Table[randomizedgraphamongcommunities[network],1000];
modularitycomm=Which[modularitytype=="GN",Table[GirvanNewmanmodularity[
randomgraphscomm[[i]],{i,1000}],modularitytype=="Wolf",Table[N@GraphAssortativity[
randomgraphscomm[[i]],FindGraphCommunities[randomgraphscomm[[i]]],
"Normalized"->False],{i,1000}]]];
 $\mu$ comm=Mean[Table[modularitycomm[[i]],{i,1000}]]];
 $\sigma$ comm=StandardDeviation[Table[modularitycomm[[i]],{i,1000}]]];

ZScores={ (X- $\mu$ erdösrenyi) /  $\sigma$ erdösrenyi, (X- $\mu$ degreesfxd) /  $\sigma$ degreesfxd, (X- $\mu$ comm) /  $\sigma$ comm}

```

```

Clear[randomnessfunctionformodularityonenullmodel]
randomnessfunctionformodularityonenullmodel[network_] :=
Module[{X, randomgraphscomm, modularitycomm,  $\mu$ comm,  $\sigma$ comm, ZScore},

X=N@GraphAssortativity[network, FindGraphCommunities[network], "Normalized" -> False];

randomgraphscomm=Table[randomizedgraphamongcommunities[network], 1000];
modularitycomm=Table[N@GraphAssortativity[randomgraphscomm[[i]],
FindGraphCommunities[randomgraphscomm[[i]], "Normalized" -> False], {i, 1000}];
 $\mu$ comm=Mean[Table[modularitycomm[[i]], {i, 1000}]];
 $\sigma$ comm=StandardDeviation[Table[modularitycomm[[i]], {i, 1000}]];

ZScore=(X- $\mu$ comm)/ $\sigma$ comm]

```

```

Clear[randomnessfunctionformodularitytwonullmodel]
randomnessfunctionformodularitytwonullmodel[network_] :=
Module[{X, randomgraphserdösrenyi, modularityerdösrenyi,  $\mu$ erdösrenyi,  $\sigma$ erdösrenyi,
randomgraphscomm, modularitycomm,  $\mu$ comm,  $\sigma$ comm, ZScores},

X=N@GraphAssortativity[network, FindGraphCommunities[network], "Normalized" -> False];

randomgraphserdösrenyi=RandomGraph[{VertexCount[network], EdgeCount[network]}, 1000];
modularityerdösrenyi=Table[N@GraphAssortativity[
randomgraphserdösrenyi[[i]], FindGraphCommunities[randomgraphserdösrenyi[[i]],
"Normalized" -> False], {i, 1000}];
 $\mu$ erdösrenyi=Mean[Table[modularityerdösrenyi[[i]], {i, 1000}]];
 $\sigma$ erdösrenyi=StandardDeviation[Table[modularityerdösrenyi[[i]], {i, 1000}]];

randomgraphscomm=Table[randomizedgraphamongcommunities[network], 1000];
modularitycomm=Table[N@GraphAssortativity[randomgraphscomm[[i]],
FindGraphCommunities[randomgraphscomm[[i]], "Normalized" -> False], {i, 1000}];
 $\mu$ comm=Mean[Table[modularitycomm[[i]], {i, 1000}]];
 $\sigma$ comm=StandardDeviation[Table[modularitycomm[[i]], {i, 1000}]];

ZScores={ (X- $\mu$ erdösrenyi)/ $\sigma$ erdösrenyi, (X- $\mu$ comm)/ $\sigma$ comm} ]

```

```

Clear[randomnessvaluesformodularitytwonullmodel]
randomnessvaluesformodularitytwonullmodel[network_] :=
Module[{X, randomgraphserdösrenyi, modularityerdösrenyi, randomgraphscomm, modularitycomm},

X=N@GraphAssortativity[network, FindGraphCommunities[network], "Normalized" -> False];

randomgraphserdösrenyi=RandomGraph[{VertexCount[network], EdgeCount[network]}, 1000];
modularityerdösrenyi=Table[N@GraphAssortativity[
randomgraphserdösrenyi[[i]], FindGraphCommunities[randomgraphserdösrenyi[[i]]],
"Normalized" -> False], {i, 1000}];

randomgraphscomm=Table[randomizedgraphamongcommunities[network], 1000];
modularitycomm=Table[N@GraphAssortativity[randomgraphscomm[[i]],
FindGraphCommunities[randomgraphscomm[[i]]], "Normalized" -> False], {i, 1000}];

{X, modularityerdösrenyi, modularitycomm}]

End[];
EndPackage[];

```