

Data Import

Modifications in the Dataset

Width Feature

Thickness Feature

Time Windows Generation by Data Partitioning

Investigation of Constraints Impact in Time Windows

Simple Association Networks

Width Feature

Thickness Feature

Fixed Step Size Networks

Width Feature

Thickness Feature

Fixed Bucket Size Networks

Width Feature

Thickness Feature

Data Import

```
In[2]:= SetDirectory[
  "C:/Users/serha/OneDrive/Masaüstü/MyRepo/master_thesis_MMT003/210210_impacts_in_time_
    _windows"];

In[3]:= datafull = Import["../data/ccm1_data_modified.csv", HeaderLines -> 1];
datafullwithheading = Import["../data/ccm1_data_modified.csv"];

In[5]:= Get["../algorithm_packages/SingleNetworks-algorithm-package.wl"]
(* ?SingleNetworks` * *)

In[6]:= Print["Dataset Length: ", Dimensions@datafull[[All, 9]]]

Dataset Length: {459 203}

In[10]:= Magnify[TableView[datafullwithheading], 0.6]
```

Out[10]=

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	
1		SEQUENC E_ID	R_OS_ID	PRODUCTION _LINE_NAME	REFERENCE _DATE	PIECE_ID	MATERIAL _ID	MOLD_ WIDTH	WIDTH	THICKNESS	WEIGHT	LENGTH	HEAT_ID	STEEL_ GRADE	EXIT_ TEMP	SLAB_TR ANSITIO	
2	1	122	115 686	CCM1	14.12 .16	16 000 181	148 956	NAME?	1.24×10^6	87.	2.74×10^9	3.35×10^9	16 000 181	26	0	0	
3	2	122	115 686	CCM1	14.12 .16	16 000 181	148 958	NAME?	1.24×10^6	87.	2.74×10^9	3.35×10^9	16 000 181	26	0	0	
4	3	122	115 686	CCM1	14.12 .16	16 000 181	148 959	NAME?	1.24×10^6	87.	2.74×10^9	3.35×10^9	16 000 181	26	0	0	
5	4	122	115 686	CCM1	14.12 .16	16 000 181	148 957	NAME?	1.24×10^6	87.	2.74×10^9	3.35×10^9	16 000 181	26	0	0	
6	5	122	115 686	CCM1	14.12 .16	16 000 181	000 000-1	NAME?	1.24×10^6	87.	2.74×10^9	3.35×10^9	16 000 181	26	0	0	
7	6	122	115 686	CCM1	14.12 .16	16 000 181	148 954	NAME?	1.24×10^6	87.	2.74×10^9	3.35×10^9	16 000 181	26	0	0	
8	7	122	115 686	CCM1	14.12 .16	16 000 181	148 955	NAME?	1.24×10^6	87.	2.74×10^9	3.35×10^9	16 000 181	26	0	0	
9	8	173	117 744	CCM1	03.01 .17	17 000 341	150 353	NAME?	1.23×10^6	65.	1.97×10^9	3.23×10^9	17 000 341	30	0	0	
10	9	173	117 744	CCM1	03.01 .17	17 000 341	150 351	NAME?	1.23×10^6	65.	1.97×10^9	3.23×10^9	17 000 341	30	0	0	
11	10	173	117 744	CCM1	03.01 .17	17 000 341	150 352	NAME?	1.23×10^6	65.	1.97×10^9	3.23×10^9	17 000 341	30	0	0	
12	11	173	117 744	CCM1	03.01 .17	17 000 341	150 354	NAME?	1.23×10^6	65.	1.97×10^9	3.23×10^9	17 000 341	30	0	0	
13	12	173	117 744	CCM1	03.01 .17	17 000 341	150 355	NAME?	1.23×10^6	65.	1.97×10^9	3.23×10^9	17 000 341	30	0	0	
14	13	173	117 744	CCM1	03.01 .17	17 000 341	150 356	NAME?	1.23×10^6	65.	1.97×10^9	3.23×10^9	17 000 341	30	0	0	
15	14	173	117 744	CCM1	03.01 .17	17 000 341	150 357	NAME?	1.23×10^6	65.	1.97×10^9	3.23×10^9	17 000 341	30	0	0	
16	15	169	117 701	CCM1	03.01 .17	17 000 281	150 467	NAME?	1.22×10^6	65.	2.07×10^9	3.42×10^9	17 000 281	30	0	4	
17	16	169	117 701	CCM1	03.01 .17	17 000 281	150 469	NAME?	1.22×10^6	65.	2.07×10^9	3.42×10^9	17 000 281	30	0	4	
18	17	169	117 701	CCM1	03.01 .17	17 000 281	150 470	NAME?	1.22×10^6	65.	2.07×10^9	3.42×10^9	17 000 281	30	0	4	

```
In[ ]:= Print["Width Feature Data Summary: ", Counts@ (Head /@ datafull[[All, 9]])]
Print["Thickness Feature Data Summary: ", Counts@ (Head /@ datafull[[All, 10]])]

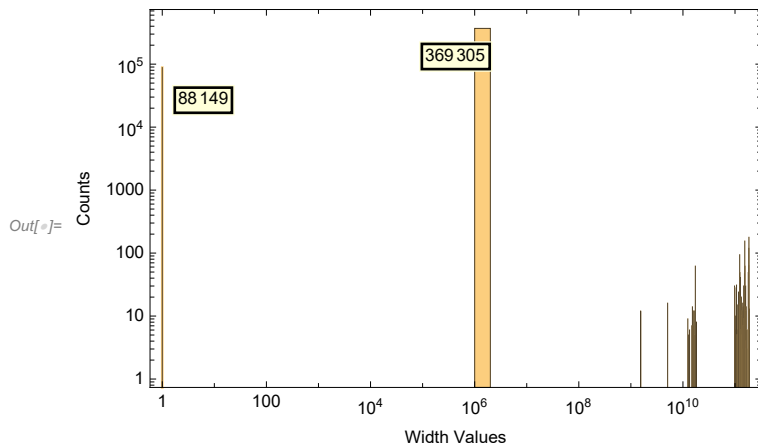
Width Feature Data Summary: <|Real -> 397 873, Integer -> 61 183, String -> 147|>

Thickness Feature Data Summary: <|Real -> 397 860, Integer -> 61 199, String -> 144|>
```

Modifications in the Dataset

Width Feature

```
In[ ]:= Histogram[datafull[[All, 9]], {10^6}, ScalingFunctions -> {"Log", "Log"},
  PlotRange -> Full, Frame -> True, ChartLabels -> Placed[{88 149, 369 305},
    {{0.07, 0.8}, Top}, Framed[#, FrameMargins -> 1, Background -> LightYellow] &],
  FrameLabel -> {"Width Values", "Counts"}]
```



```
In[ ]:= widthmodified = Table[
  If[StringQ@i, i, If[(RealDigits@i)[[2]] > 4, i / 10^((RealDigits@i)[[2]] - 4), i, i]],
  {i, datafull[[All, 9]]}]
Counts@Head /@ widthmodified
```

Out[]:=

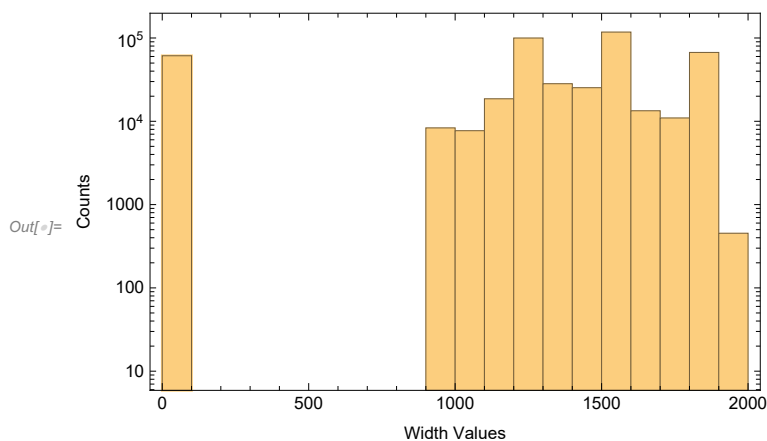
```
{1240., 1240., 1240., 1240., 1240., 1240., 1240., 1230., 1230., 1230., 1230., 1230.,
1230., 1230., 1220., 1220., 1220., 1220., 1220., 1220., 1220., 1220., 1230., 1230.,
1230., 1230., 1230., 1230., 1530., 1530., 1530., 1530., 1530., 1530., 1530., 1520.,
1520., 1520., 1520., 1520., 1520., 1520., 1520., 1520., 0, 0, 0, 0, 1240., 1240.,
... 459103 ..., 0, 0, 0, 0, 0, 0, 1350., 1350., 1350., 1350., 1350., 1350., 1350.,
1350., 1350., 1350., 1350., 1350., 1360., 1360., 1360., 1360., 0, 0, 0, 0, 1360.,
1360., 1360., 1360., 1360., 1360., 1360., 1360., 1360., 1360., 1360., 1360.,
1360., 1360., 1360., 1360., 1360., 1360., 1350., 1350., 1350., 1350., NA, NA}
```

large output

[show less](#)[show more](#)[show all](#)[set size limit...](#)

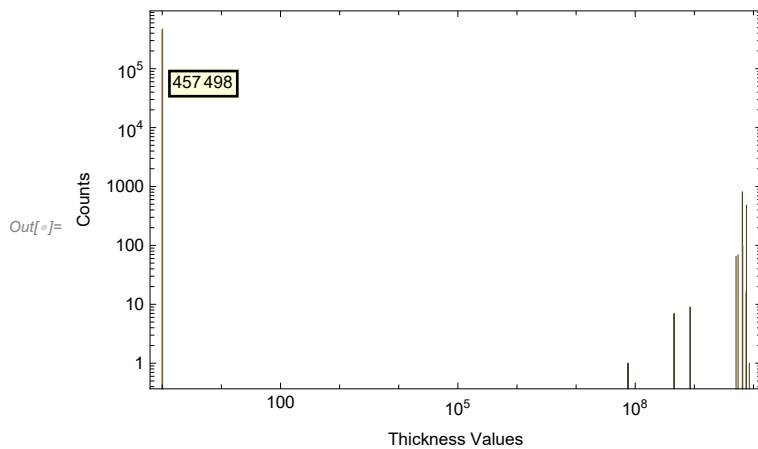
Out[]:= < | Real → 397873, Integer → 61183, String → 147 | >

```
In[ ]:= Histogram[widthmodified, ScalingFunctions → "Log",
  PlotRange → {{0, 2000}, All}, Frame → True, FrameLabel → {"Width Values", "Counts"}]
```



Thickness Feature

```
In[ ]:= Histogram[datafull[[All, 10]], {10^6},
  ScalingFunctions -> {"Log", "Log"}, PlotRange -> Full, Frame -> True, ChartLabels ->
  Placed[457498, {0.07, 0.85}], Framed[#, FrameMargins -> 1, Background -> LightYellow] &],
  FrameLabel -> {"Thickness Values", "Counts"}]
```



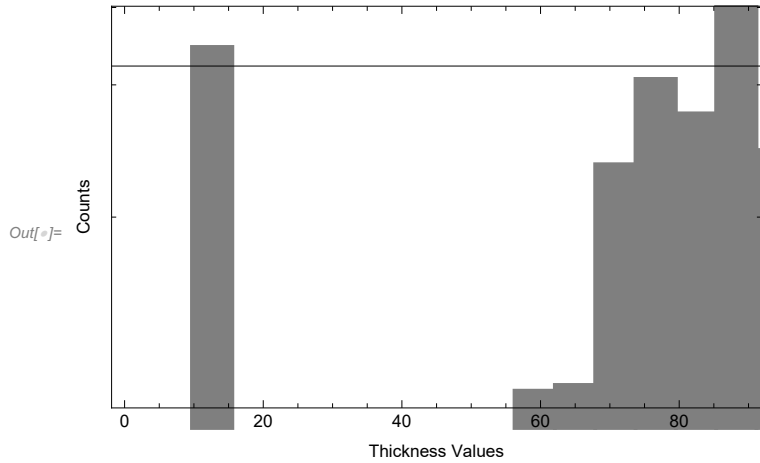
```
ln[*]:= thicknessmodified = Table[
  If[StringQ@i, i, If[(RealDigits@i)[[2]] > 2, i / 10^((RealDigits@i)[[2]] - 2), i, i]],
  {i, datafull[[All, 10]]}]
Counts@ (Head /@ thicknessmodified)
```

```
Out[6]= {87., 87., 87., 87., 87., 87., 87., 87., 65., 65., 65., 65., 65., 65., 65., 65.,  
65., 65., 65., 65., 65., 65., 65., 65., 65., 65., 65., 65., 66., 66., 66., 66., 66.,  
66., 66., 66., 66., 66., 66., 66., 66., 66., 66., 0, 0, 0, 0, 67., 67., 67., 67.,  
67., 67., 65., 65., 65., 65., 65., 65., 65., 65., 65., 0, 0, 0, 0, 0, 0, 0, ... 459 065 ...,  
67., 67., 67., 67., 67., 67., 67., 67., 67., 67., 67., 67., 67., 67., 67., 67., 67.,  
67., 67., 67., 0, 0, 0, 0, 0, 0, 67., 67., 67., 67., 67., 67., 66., 66., 66., 66.,  
66., 66., 67., 67., 67., 67., 0, 0, 0, 0, 67., 67., 67., 67., 67., 67., 67., 67.,  
67., 67., 67., 67., 67., 67., 67., 67., 67., 67., 67., NA, NA}
```

large output [show less](#) [show more](#) [show all](#) [set size limit...](#)

$$Out[*]= \langle \text{Real} \rightarrow 397\,860, \text{Integer} \rightarrow 61\,199, \text{String} \rightarrow 144 \rangle$$

```
ln[ ]:= Histogram[thicknessmodified, ScalingFunctions -> "Log",  
    PlotRange -> Full, Frame -> True, FrameLabel -> {"Thickness Values", "Counts"}]
```



Time Windows Generation by Data Partitioning

```
In[ ]:= datafull[[All, 9]] = widthmodified;
datafull[[All, 10]] = thicknessmodified;
data = Table[Take[datafull, UpTo@i],
  {i, {46 497, 91 690, 138 440, 183 584, 230 005, 275 844, 320 350, 367 179, 413 106, 459 203}}];

(* Export["data_with_time_windows.mx",data] *)
```

Investigation of Constraints Impact in Time Windows

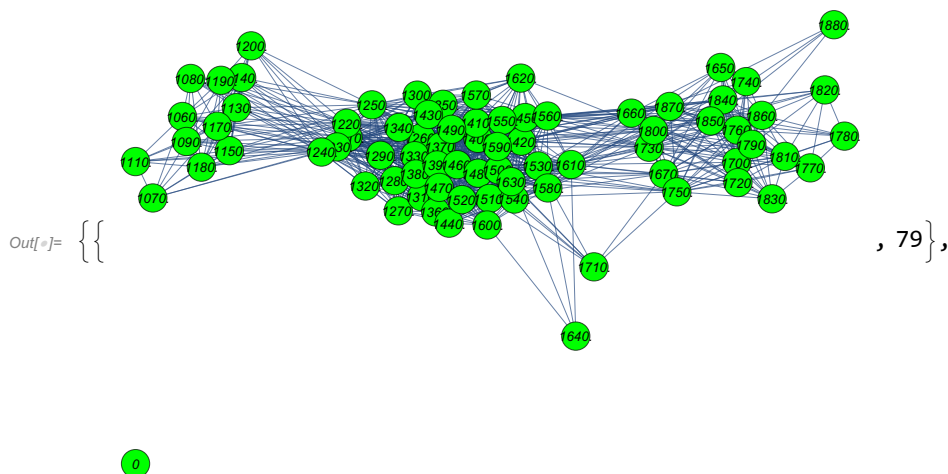
Simple Association Networks

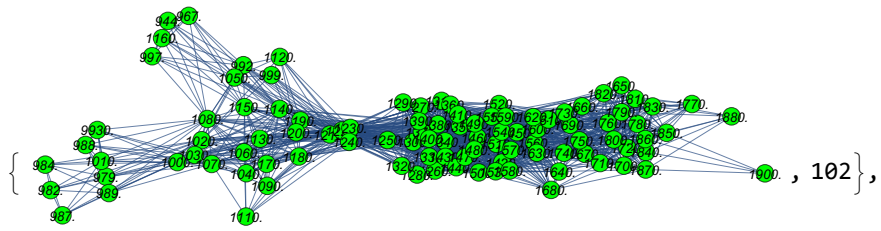
Width Feature

```
In[ ]:= AbsoluteTiming[widthdataintimewindows = snetworkdatasingleintimewindows[9, 10];]
Out[ ]:= {3.9276, Null}

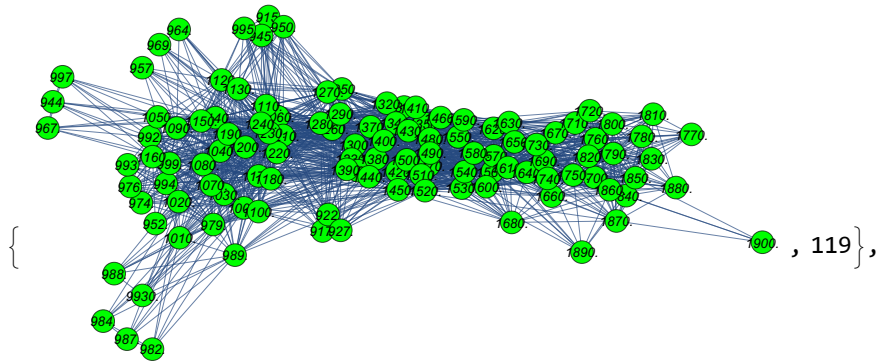
In[ ]:= graphsandnodenumbers = Table[snetworkgraphsinglenodes[widthdataintimewindows[[1]][[i]],
  widthdataintimewindows[[2]][[i]], 2, 7, 400, Green], {i, Range@10}];

In[ ]:= graphsandnodenumbers
```

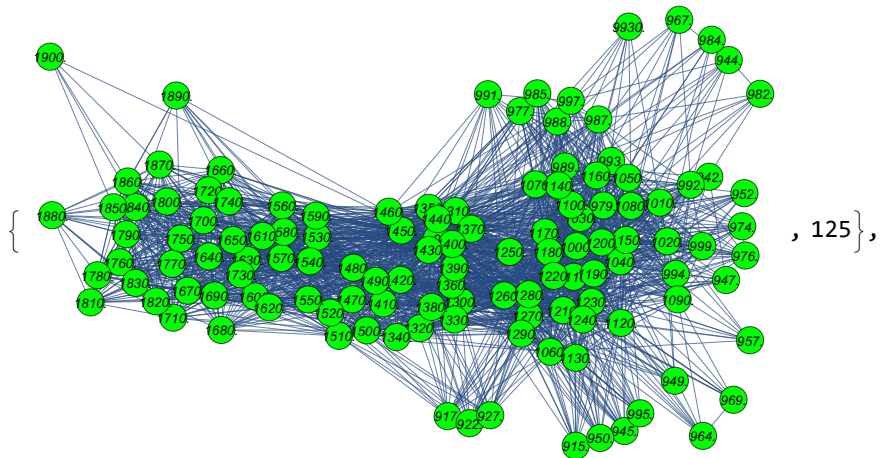


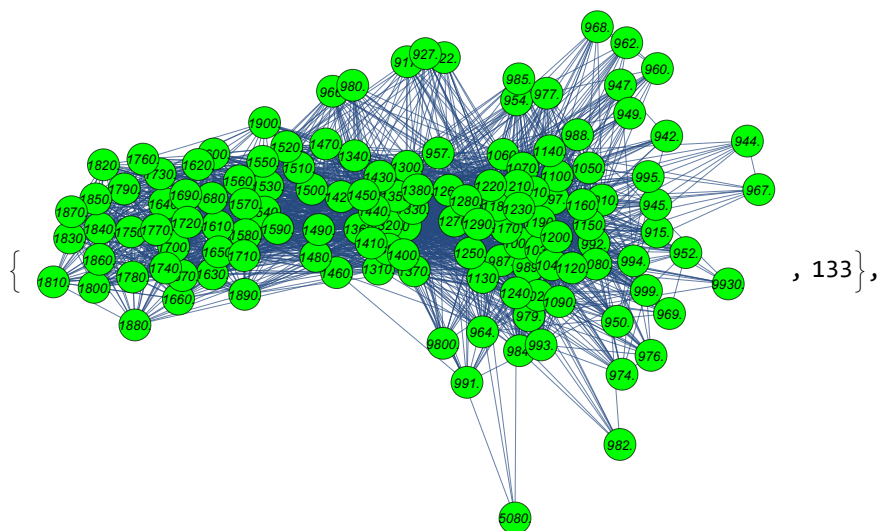
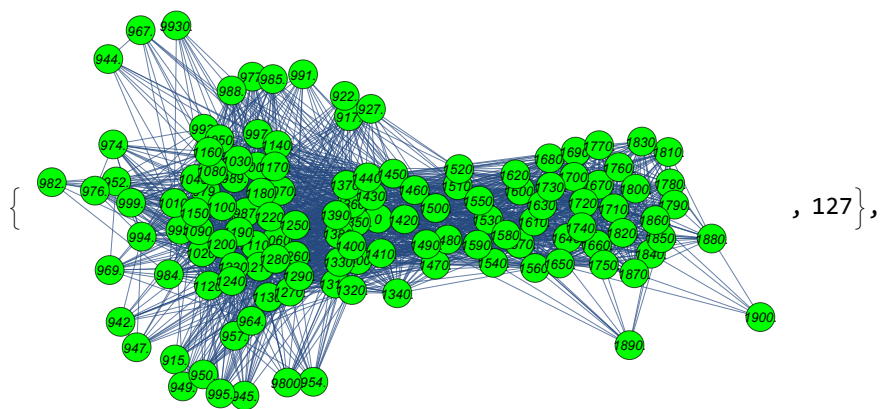


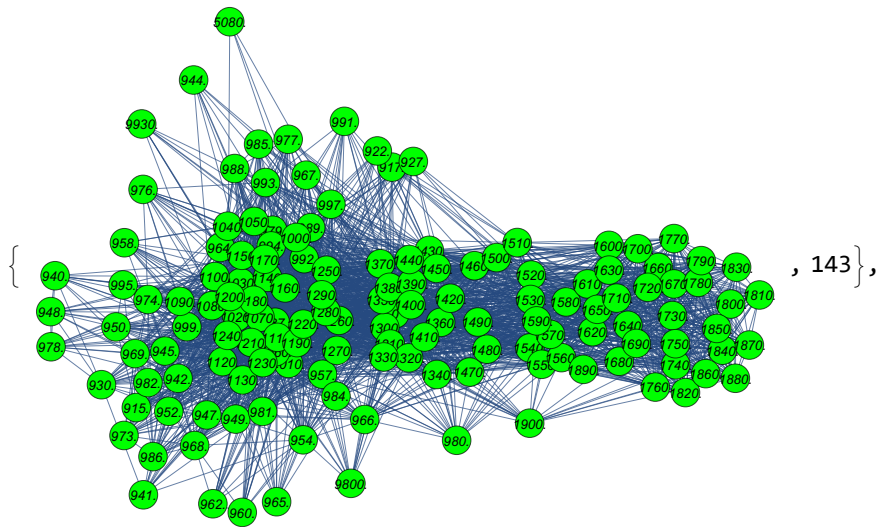
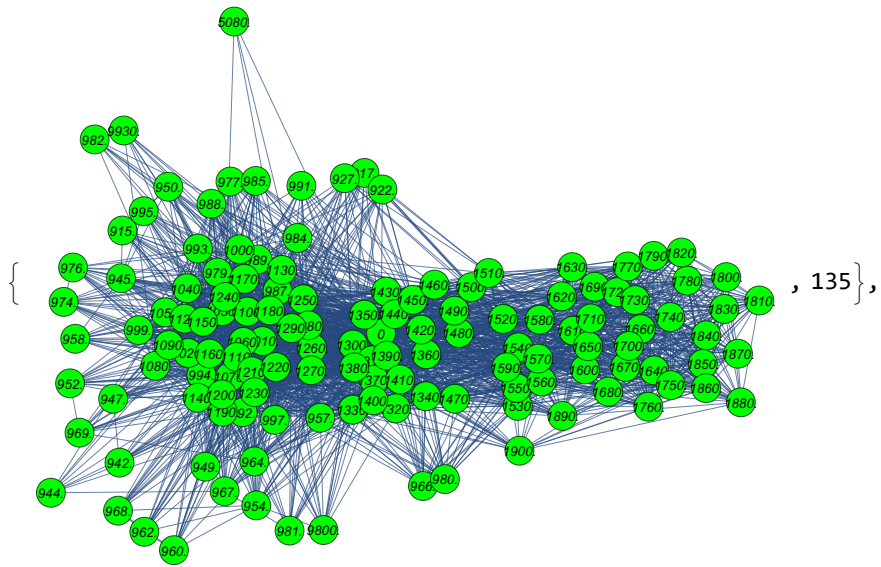
0

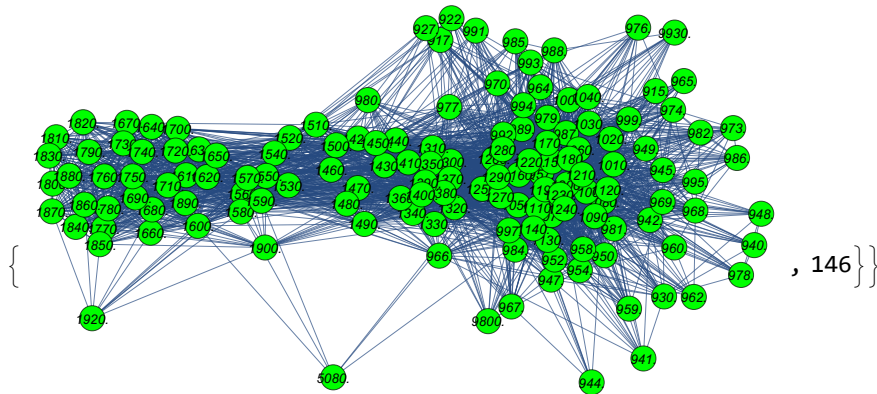
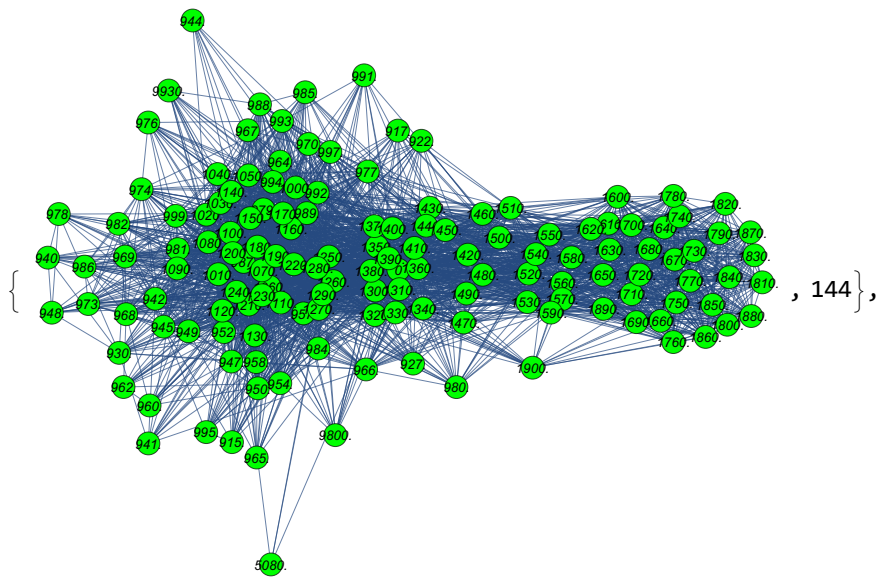


0









0

```

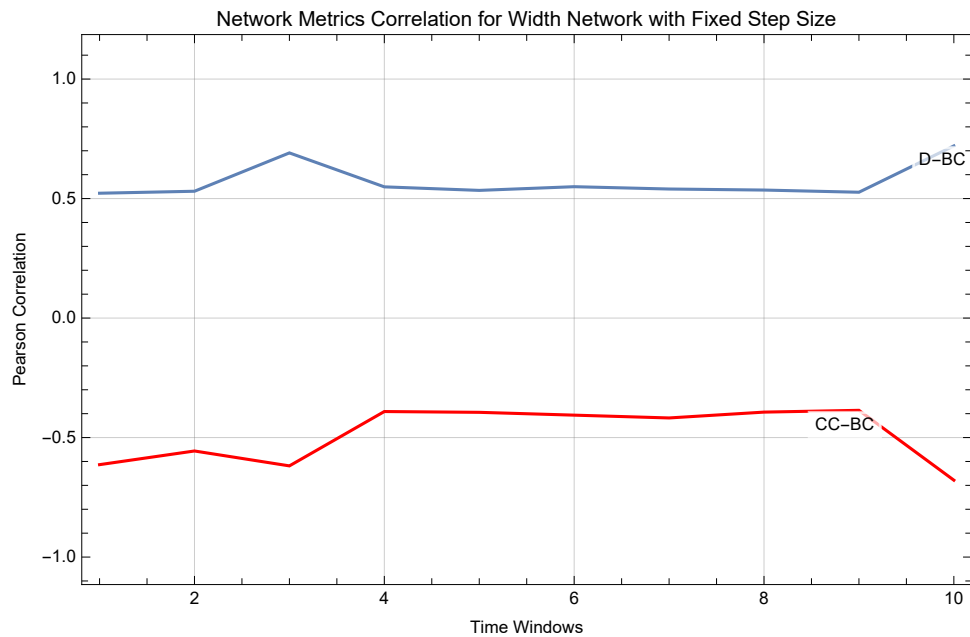
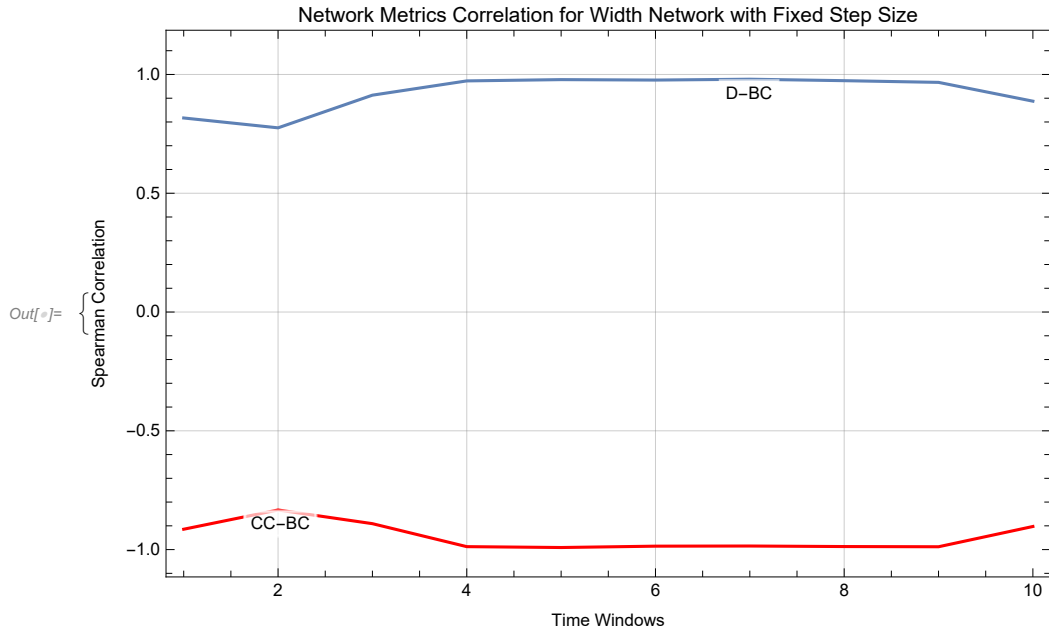
In[ ]:= correlationvaluesthroughwindowsspearman =
  Table[correlationfunction[i, 1], {i, graphsandnodenumbers[[All, 1]]}];
correlationvaluesthroughwindowsspearson =
  Table[correlationfunction[i, 2], {i, graphsandnodenumbers[[All, 1]]}];

In[ ]:= correlationvaluesthroughwindowsspearman
correlationvaluesthroughwindowsspearson

Out[ ]:= {{0.816837, -0.914287}, {0.775318, -0.833272}, {0.912826, -0.890899}, {0.9729, -0.987608},
  {0.978297, -0.991312}, {0.976393, -0.985596}, {0.979992, -0.984999},
  {0.973833, -0.987195}, {0.966704, -0.988102}, {0.887562, -0.902762}}
```

```
Out[ ]:= {{0.522385, -0.613315}, {0.530661, -0.556155}, {0.691093, -0.618492}, {0.549054, -0.3911},
{0.534222, -0.394403}, {0.549708, -0.406185}, {0.539973, -0.417934},
{0.535635, -0.393469}, {0.526522, -0.386032}, {0.720341, -0.678254}}
```

```
In[ ]:= {Show[ListPlot[Transpose[
  {Range@10, Table[correlationvaluesthroughwindowsspearman[[j, 1]], {j, 1, 10}]]],
  Joined → True, PlotLabels → Placed[{"D-BC"}, Top], Frame → True,
  FrameLabel → {"Time Windows", "Spearman Correlation"}], ListPlot[Transpose[
  {Range@10, Table[correlationvaluesthroughwindowsspearman[[j, 2]], {j, 1, 10}]]],
  Joined → True, PlotLabels → Placed[{"CC-BC"}, Top], PlotStyle → Red,
  Frame → True, FrameLabel → {"Time Windows", "Spearman Correlation"}],
  PlotRange → {All, {-1, 1}}, Axes → False, ImageSize → 500, GridLines → Automatic,
  PlotLabel → "Network Metrics Correlation for Width Network with Fixed Step Size"],
  Show[ListPlot[Transpose[
  {Range@10, Table[correlationvaluesthroughwindowsspearson[[j, 1]], {j, 1, 10}]]],
  Joined → True, PlotLabels → Placed[{"D-BC"}, Top], Frame → True,
  FrameLabel → {"Time Windows", "Pearson Correlation"}], ListPlot[Transpose[
  {Range@10, Table[correlationvaluesthroughwindowsspearson[[j, 2]], {j, 1, 10}]]],
  Joined → True, PlotLabels → Placed[{"CC-BC"}, Top], PlotStyle → Red,
  Frame → True, FrameLabel → {"Time Windows", "Pearson Correlation"}],
  PlotRange → {All, {-1, 1}}, Axes → False, ImageSize → 500, GridLines → Automatic,
  PlotLabel → "Network Metrics Correlation for Width Network with Fixed Step Size"]}
```



```
In[#]:= ZscoreDeBCspearman = Transpose[{Range[1, 10],
  Table[randomnessfunction[i, 1], {i, graphsandnodenumbers[[All, 1]]}][[All, 1]]}]
```

```
Out[#]:= {{1, -15.3086}, {2, -27.6464}, {3, -10.1391}, {4, -0.619594}, {5, 0.370311},
  {6, -0.281378}, {7, 0.426047}, {8, -1.50236}, {9, -3.50008}, {10, -24.4219}}
```

```
In[#]:= ZscoreCCBCspearman = Transpose[{Range[1, 10],
  Table[randomnessfunction[i, 1], {i, graphsandnodenumbers[[All, 1]]}][[All, 2]]}]
```

```
Out[#]:= {{1, -5.60894}, {2, -5.8892}, {3, -6.9099}, {4, -7.9931}, {5, -7.9275},
  {6, -7.91104}, {7, -8.34481}, {8, -8.37427}, {9, -7.98517}, {10, -7.71136}}
```

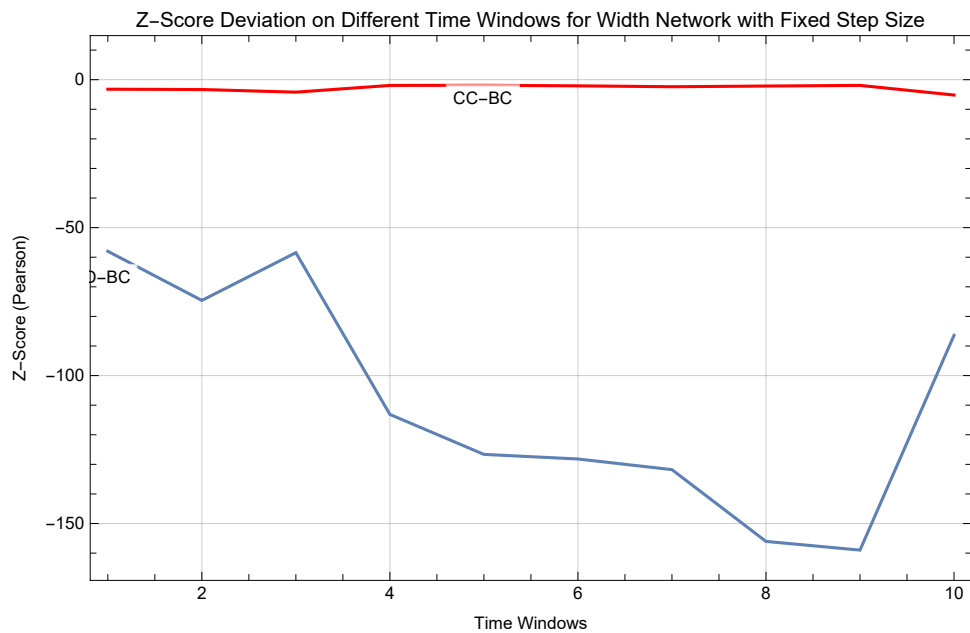
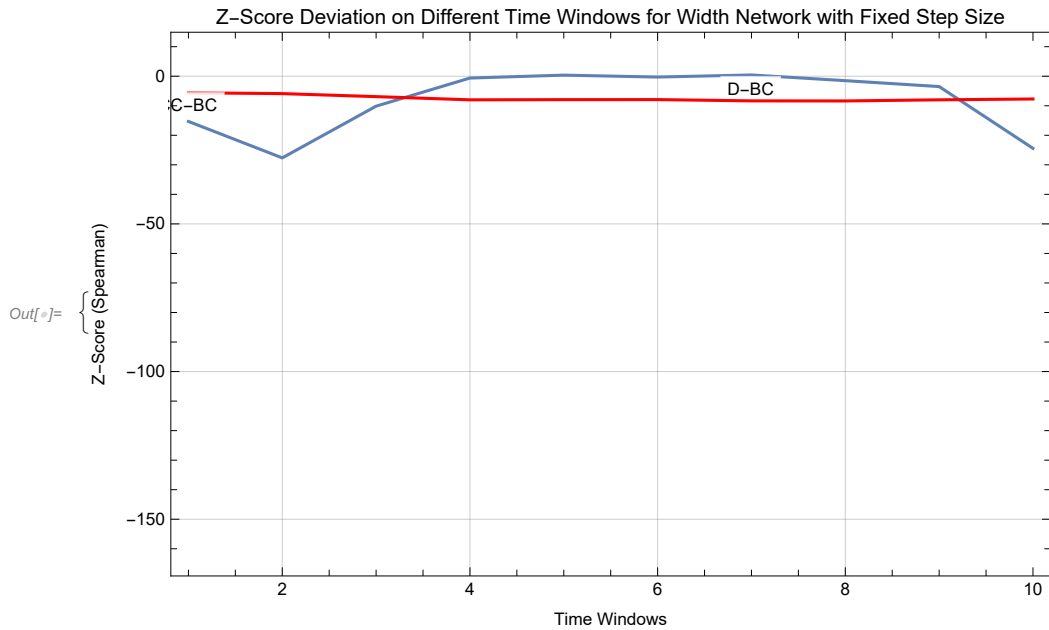
```

In[ ]:= ZscoreDeBCpearson = Transpose[{Range[1, 10],
    Table[randomnessfunction[i, 2], {i, graphsandnodenumbers[[All, 1]]}][[All, 1]]}]
Out[ ]:= {{1, -57.9931}, {2, -74.5995}, {3, -58.4635}, {4, -113.126}, {5, -126.63},
    {6, -128.182}, {7, -131.784}, {8, -156.037}, {9, -158.978}, {10, -86.3946}}

In[ ]:= ZscoreCCBCpearson = Transpose[{Range[1, 10],
    Table[randomnessfunction[i, 2], {i, graphsandnodenumbers[[All, 1]]}][[All, 2]]}]
Out[ ]:= {{1, -3.22148}, {2, -3.32278}, {3, -4.21425}, {4, -1.94097}, {5, -1.89757},
    {6, -2.08029}, {7, -2.38328}, {8, -2.14969}, {9, -1.93196}, {10, -5.18526}}

In[ ]:= {Show[ListPlot[ZscoreDeBCspearman, Joined → True, PlotLabels → Placed[{"D-BC"}, Top],
    Frame → True, FrameLabel → {"Time Windows", "Z-Score (Spearman)"}],
    ListPlot[ZscoreCCBCspearman, Joined → True, PlotLabels → Placed[{"CC-BC"}, Top],
    PlotStyle → Red, Frame → True, FrameLabel → {"Time Windows", "Z-Score (Spearman)"}],
    PlotRange → {All, {-160, 0}}, Axes → False, ImageSize → 500,
    GridLines → Automatic, PlotLabel →
    "Z-Score Deviation on Different Time Windows for Width Network with Fixed Step Size"],
    Show[ListPlot[ZscoreDeBCpearson, Joined → True, PlotLabels → Placed[{"D-BC"}, Top],
    Frame → True, FrameLabel → {"Time Windows", "Z-Score (Pearson)"}],
    ListPlot[ZscoreCCBCpearson, Joined → True, PlotLabels → Placed[{"CC-BC"}, Top],
    PlotStyle → Red, Frame → True, FrameLabel → {"Time Windows", "Z-Score (Pearson)"}],
    PlotRange → {All, {-160, 0}}, Axes → False, ImageSize → 500,
    GridLines → Automatic, PlotLabel →
    "Z-Score Deviation on Different Time Windows for Width Network with Fixed Step Size"]}

```



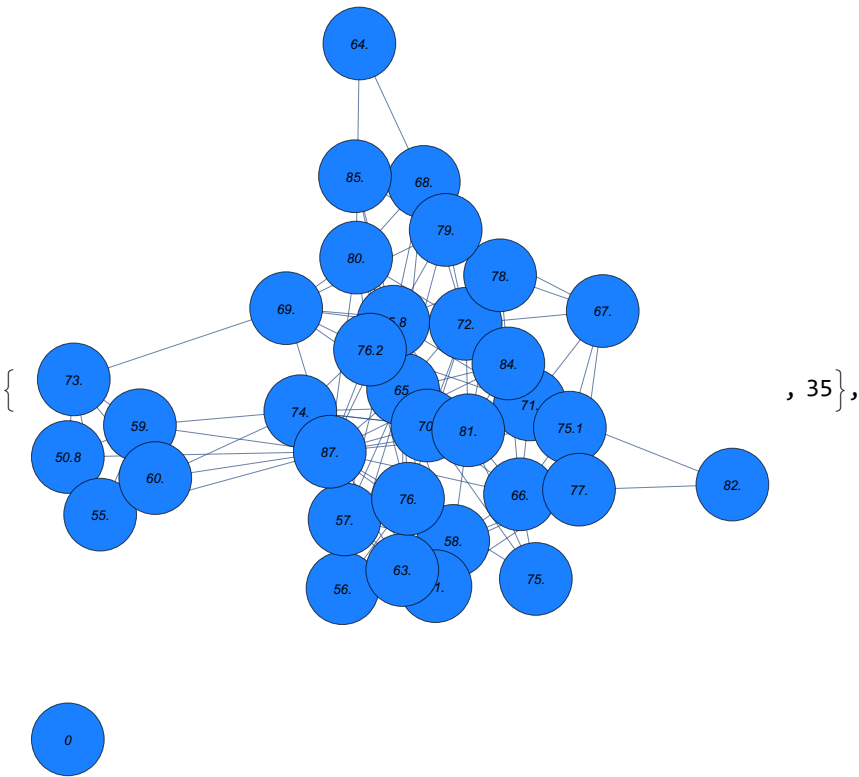
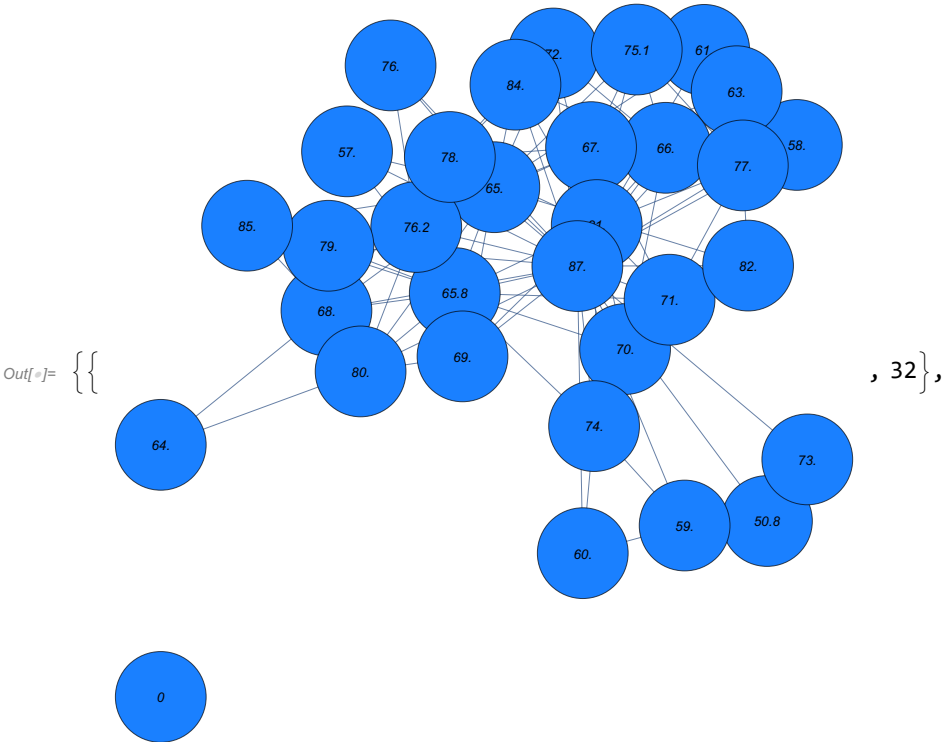
Thickness Feature

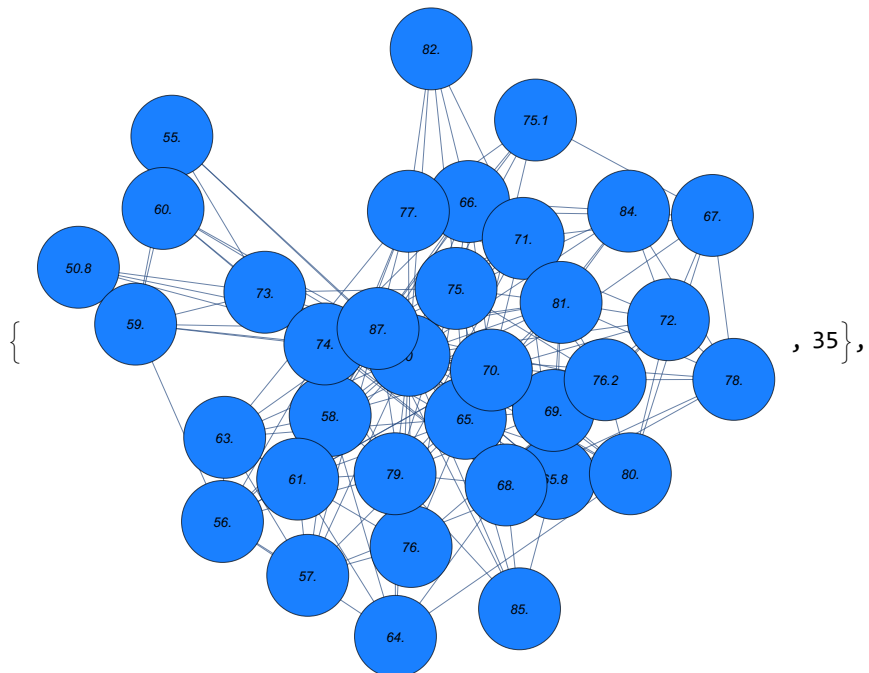
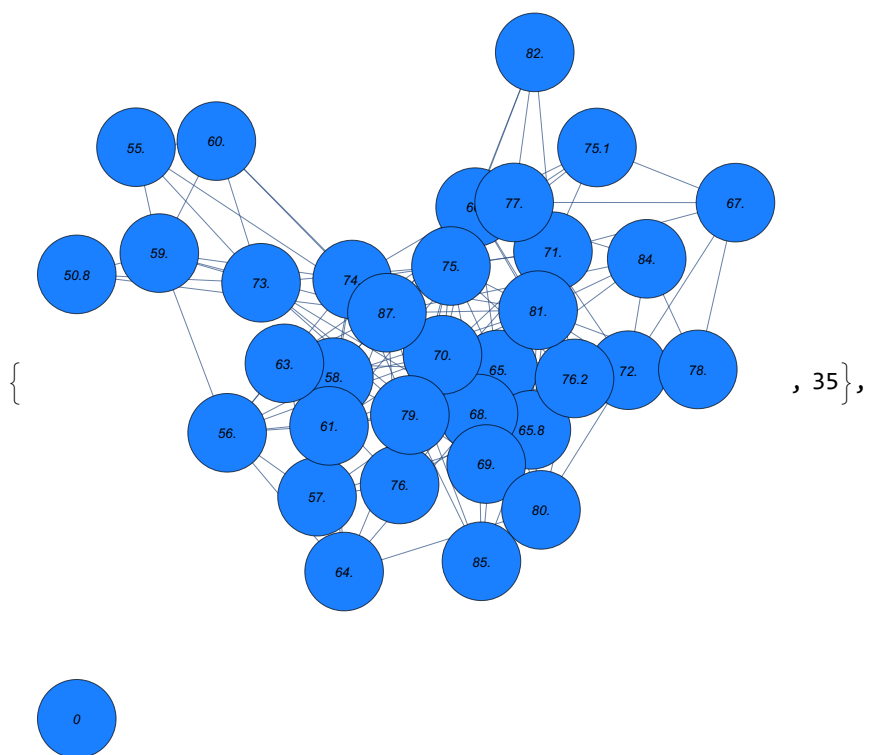
```
In[ ]:= AbsoluteTiming[thicknessdataintimewindows = snetworkdatasingleintimewindows[10, 10];]
```

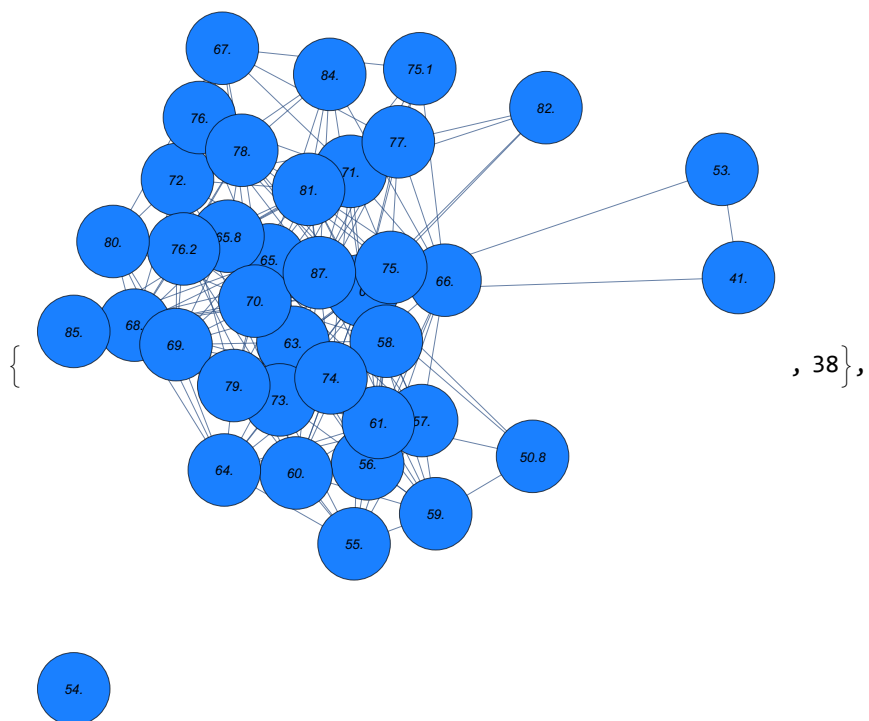
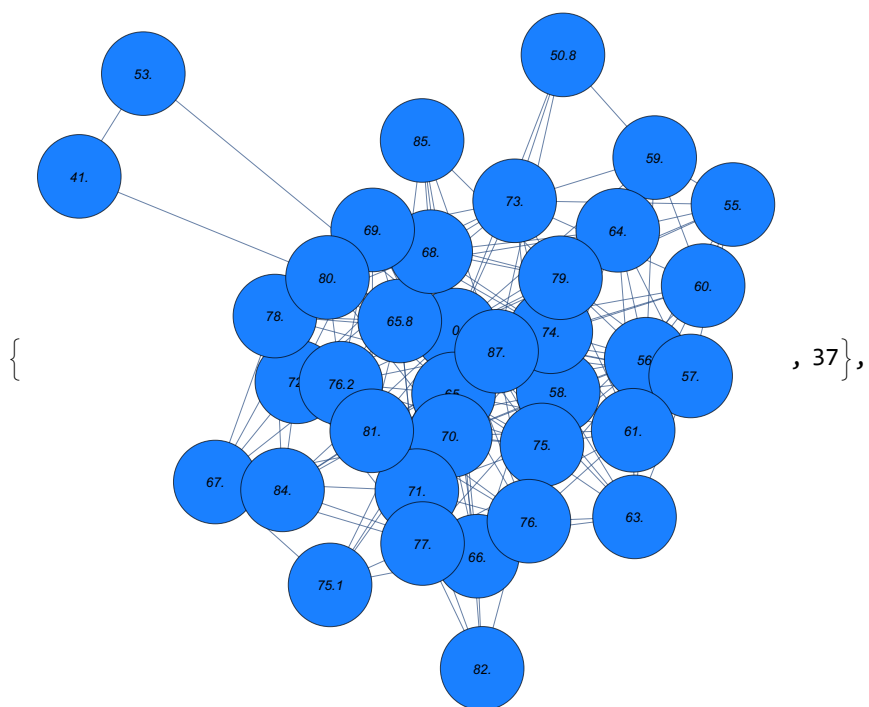
```
Out[ ]:= {4.35942, Null}
```

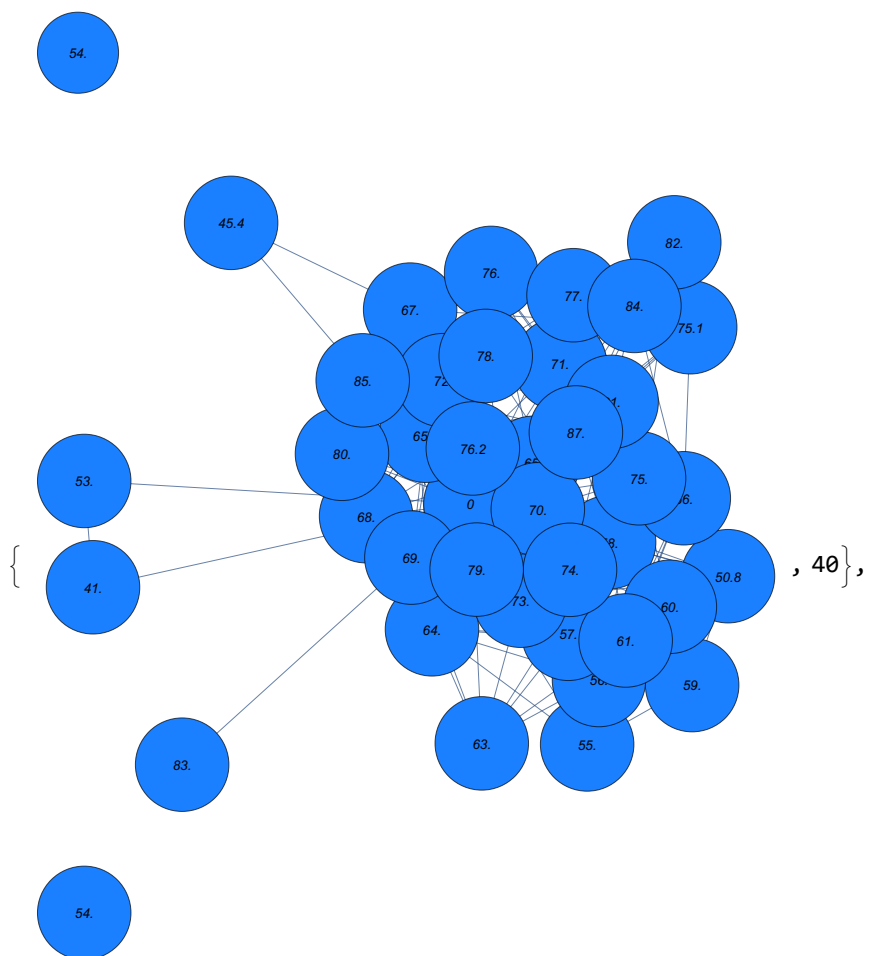
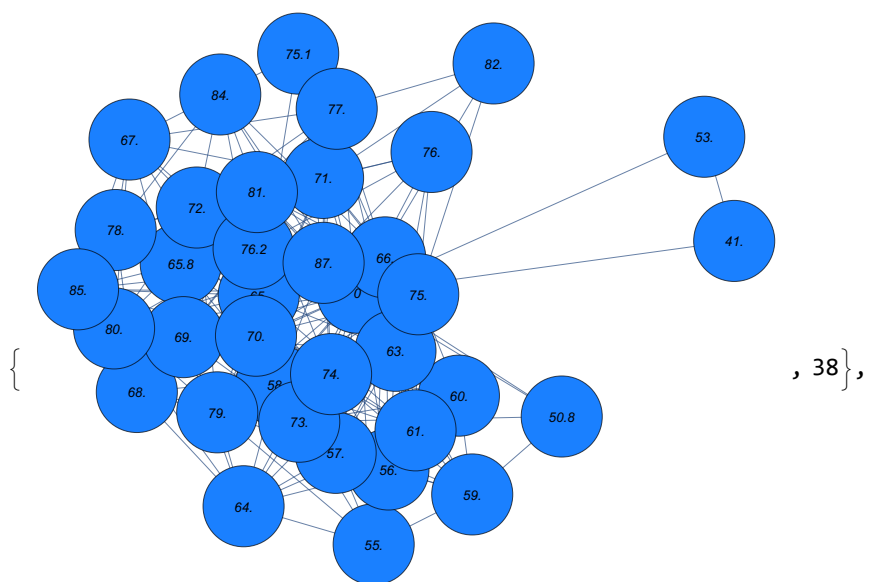
```
In[ ]:= graphsandnodenumbers = Table[snetworkgraphsinglenodes[
    thicknessdataintimewindows[[1]][[i]], thicknessdataintimewindows[[2]][[i]],
    2, 7, 400, RGBColor[0.1, 0.5, 1.]], {i, Range@10}];
```

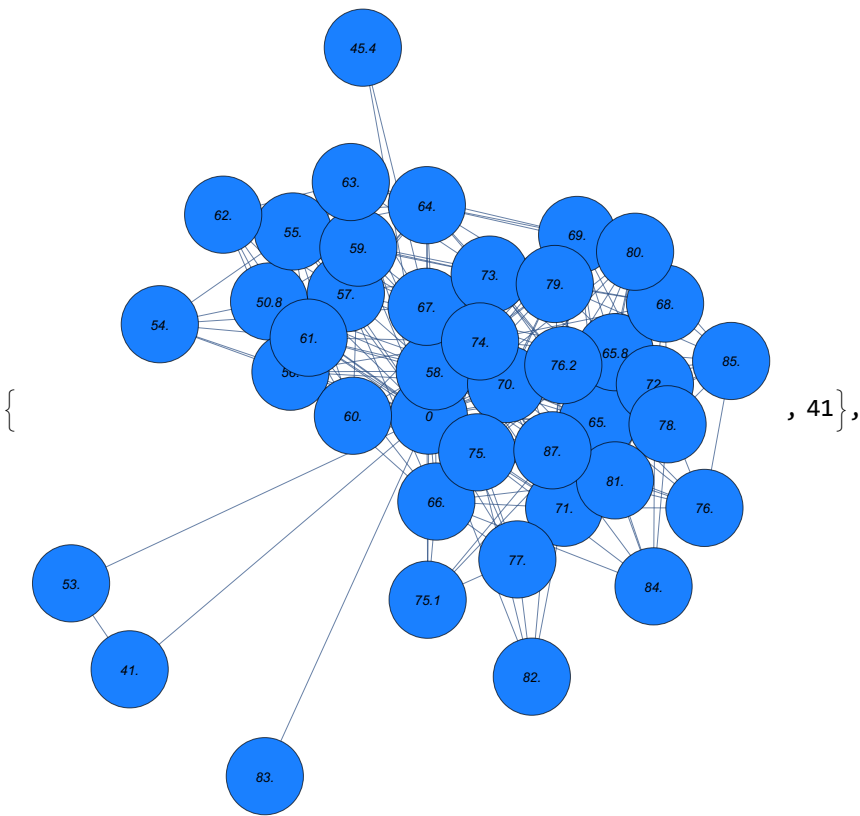
```
In[ ]:= graphsandnodenumbers
```

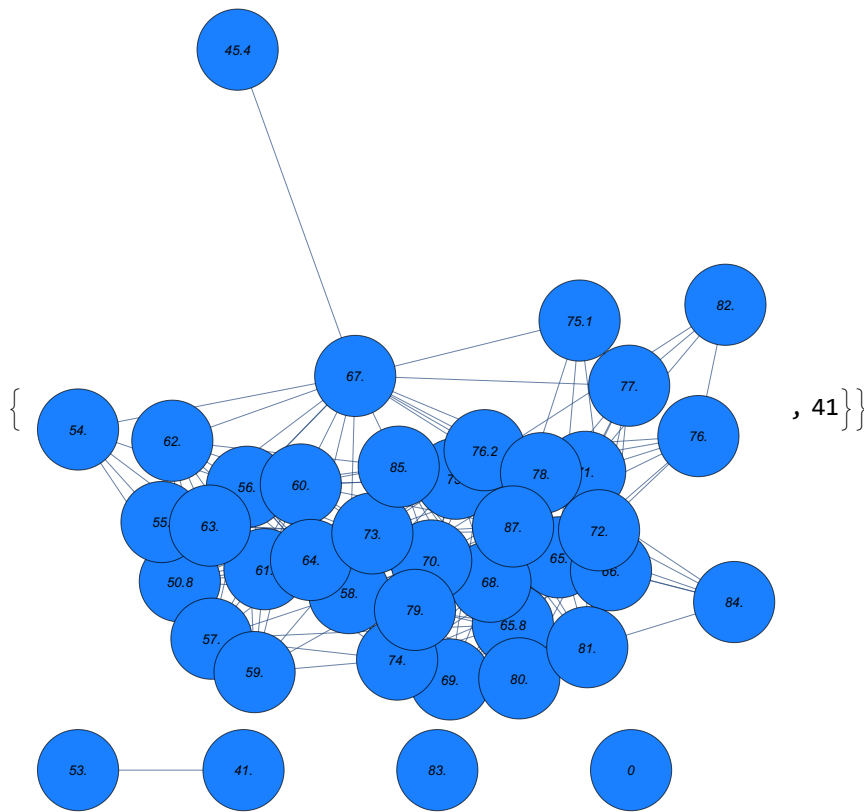












```
In[ ]:= correlationvaluesthroughwindowsspearman =
  Table[correlationfunction[i, 1], {i, graphsandnodenumbers[All, 1]}];
correlationvaluesthroughwindowsspearson =
  Table[correlationfunction[i, 2], {i, graphsandnodenumbers[All, 1]}];
```

```
In[ ]:= correlationvaluesthroughwindowsspearman
correlationvaluesthroughwindowsspearson
```

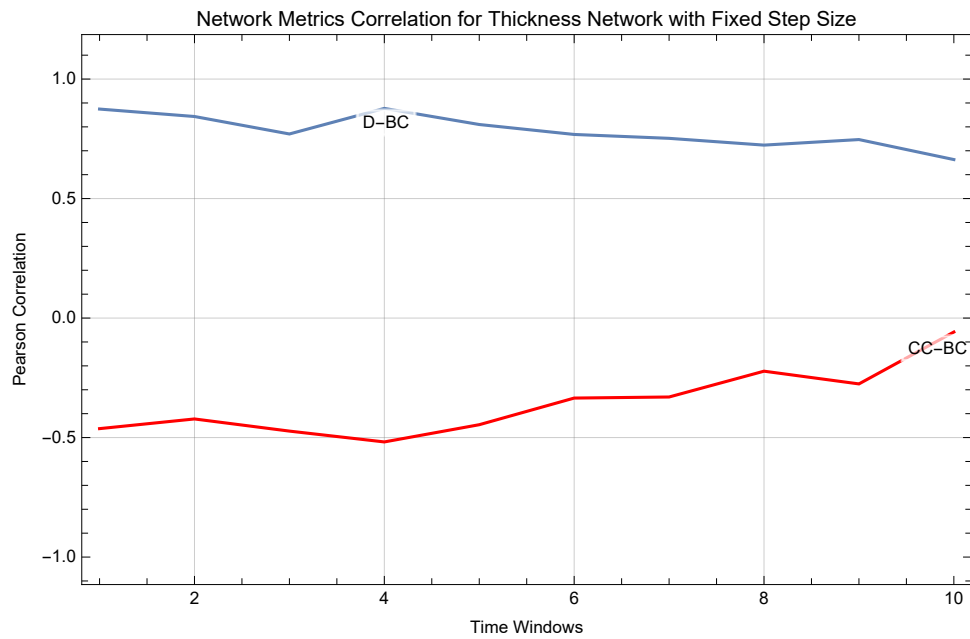
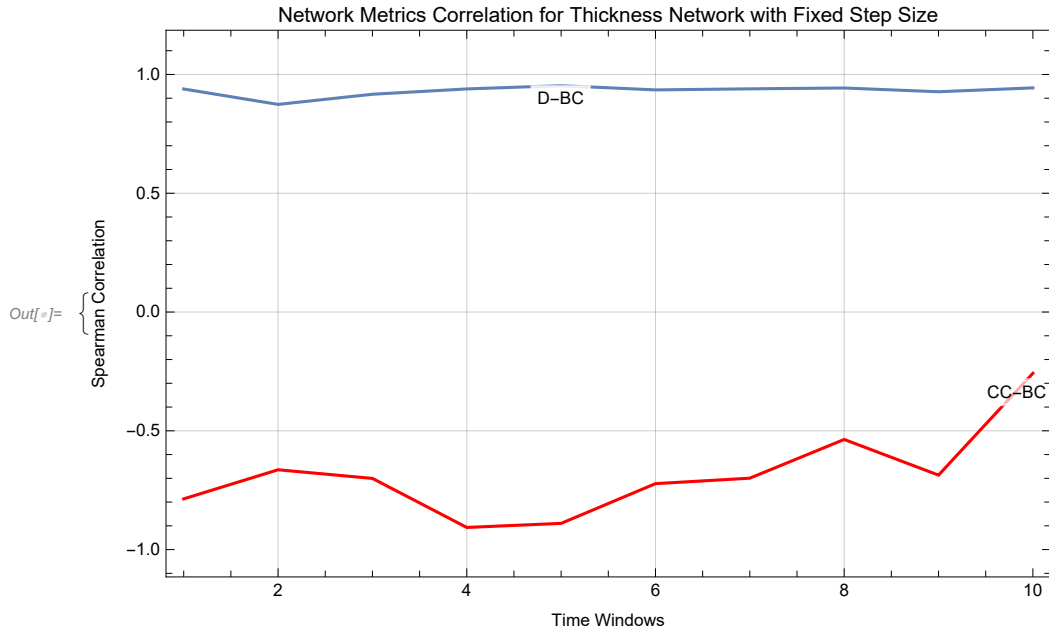
```
Out[ ]:= {{0.938808, -0.78658}, {0.873987, -0.663998}, {0.916719, -0.7004}, {0.93912, -0.906811},
{0.95285, -0.889666}, {0.935017, -0.722435}, {0.939483, -0.699436},
{0.943043, -0.53645}, {0.927237, -0.686511}, {0.94354, -0.25778}}
```

```
Out[ ]:= {{0.874484, -0.462631}, {0.843387, -0.422115},
{0.770286, -0.472945}, {0.877292, -0.518271}, {0.809918, -0.446188},
{0.768257, -0.334724}, {0.752032, -0.330238}, {0.723693, -0.22225},
{0.746908, -0.275495}, {0.663251, -0.0583977}}
```

```

In[ ]:= {Show[ListPlot[Transpose[
  {Range@10, Table[correlationvaluesthroughwindowsspearman[[j, 1]], {j, 1, 10}]}],
  Joined → True, PlotLabels → Placed[{"D-BC"}, Top], Frame → True,
  FrameLabel → {"Time Windows", "Spearman Correlation"}], ListPlot[Transpose[
  {Range@10, Table[correlationvaluesthroughwindowsspearman[[j, 2]], {j, 1, 10}]}],
  Joined → True, PlotLabels → Placed[{"CC-BC"}, Top], PlotStyle → Red,
  Frame → True, FrameLabel → {"Time Windows", "Spearman Correlation"}],
  PlotRange → {All, {-1, 1}}, Axes → False, ImageSize → 500, GridLines → Automatic,
  PlotLabel → "Network Metrics Correlation for Thickness Network with Fixed Step Size"],
Show[ListPlot[Transpose[
  {Range@10, Table[correlationvaluesthroughwindowsspearson[[j, 1]], {j, 1, 10}]}],
  Joined → True, PlotLabels → Placed[{"D-BC"}, Top], Frame → True,
  FrameLabel → {"Time Windows", "Pearson Correlation"}], ListPlot[Transpose[
  {Range@10, Table[correlationvaluesthroughwindowsspearson[[j, 2]], {j, 1, 10}]}],
  Joined → True, PlotLabels → Placed[{"CC-BC"}, Top], PlotStyle → Red,
  Frame → True, FrameLabel → {"Time Windows", "Pearson Correlation"}],
  PlotRange → {All, {-1, 1}}, Axes → False, ImageSize → 500, GridLines → Automatic,
  PlotLabel → "Network Metrics Correlation for Thickness Network with Fixed Step Size"]}

```



```
In[n]:= ZscoreDeBCspearman = Transpose[{Range[1, 10],
Table[randomnessfunction[i, 1], {i, graphsandnodenumbers[[All, 1]]}][[All, 1]]}]
```

```
Out[n]= {{1, 0.616193}, {2, -1.28733}, {3, -0.104282}, {4, 0.565508}, {5, 1.07189},
{6, 0.367045}, {7, 0.478779}, {8, 0.559077}, {9, -0.0694945}, {10, 0.590463}}
```

```
In[n]:= ZscoreCCBCspearman = Transpose[{Range[1, 10],
Table[randomnessfunction[i, 1], {i, graphsandnodenumbers[[All, 1]]}][[All, 2]]}]
```

```
Out[n]= {{1, -2.93182}, {2, -2.53266}, {3, -2.40751}, {4, -3.46177}, {5, -3.3986},
{6, -2.49543}, {7, -2.42854}, {8, -1.50394}, {9, -2.47674}, {10, 0.109912}}
```

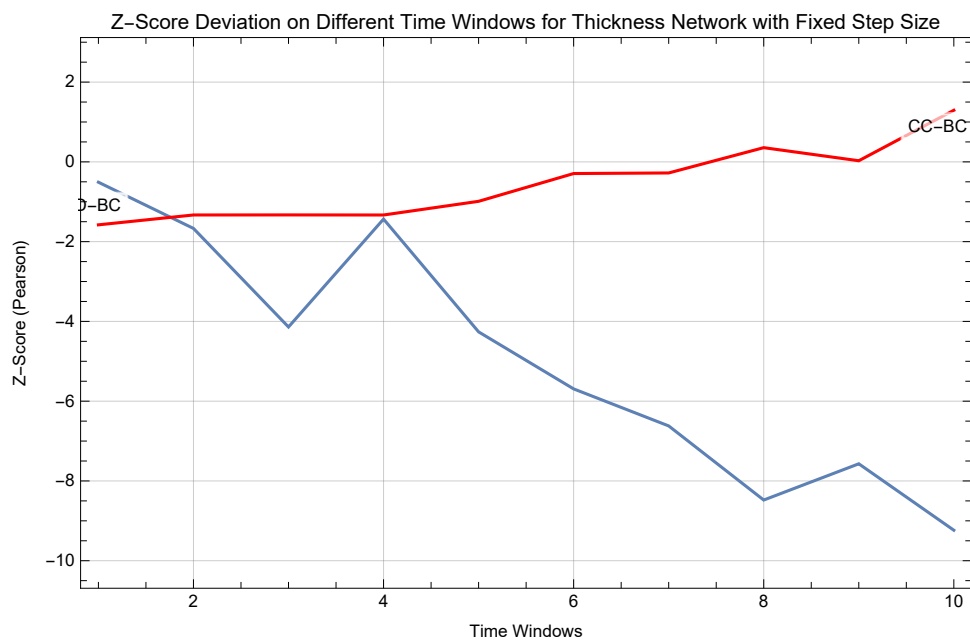
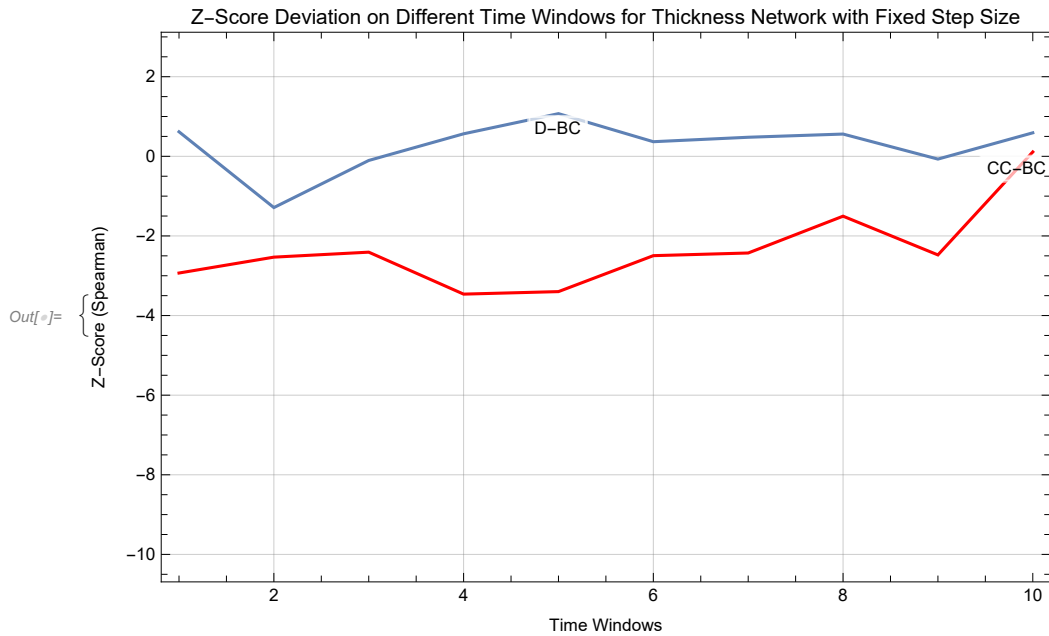
```

In[ ]:= ZscoreDeBCpearson = Transpose[{Range[1, 10],
    Table[randomnessfunction[i, 2], {i, graphsandnodenumbers[[All, 1]]}][[All, 1]]}]
Out[ ]:= {{1, -0.510046}, {2, -1.66848}, {3, -4.13987}, {4, -1.43423}, {5, -4.2623},
    {6, -5.6921}, {7, -6.62055}, {8, -8.47877}, {9, -7.56998}, {10, -9.23535}}

In[ ]:= ZscoreCCBCpearson = Transpose[{Range[1, 10],
    Table[randomnessfunction[i, 2], {i, graphsandnodenumbers[[All, 1]]}][[All, 2]]}]
Out[ ]:= {{1, -1.57851}, {2, -1.33152}, {3, -1.32984}, {4, -1.33201}, {5, -0.9891},
    {6, -0.2925}, {7, -0.278031}, {8, 0.356254}, {9, 0.0282377}, {10, 1.29413}}

In[ ]:= {Show[ListPlot[ZscoreDeBCspearman, Joined → True, PlotLabels → Placed[{"D-BC"}, Top],
    Frame → True, FrameLabel → {"Time Windows", "Z-Score (Spearman)"}],
    ListPlot[ZscoreCCBCspearman, Joined → True, PlotLabels → Placed[{"CC-BC"}, Top],
    PlotStyle → Red, Frame → True, FrameLabel → {"Time Windows", "Z-Score (Spearman)"}],
    PlotRange → {All, {-10, 2}}, Axes → False, ImageSize → 500,
    GridLines → Automatic, PlotLabel → "Z-Score Deviation on Different
        Time Windows for Thickness Network with Fixed Step Size"],
    Show[ListPlot[ZscoreDeBCpearson, Joined → True, PlotLabels → Placed[{"D-BC"}, Top],
    Frame → True, FrameLabel → {"Time Windows", "Z-Score (Pearson)"}],
    ListPlot[ZscoreCCBCpearson, Joined → True, PlotLabels → Placed[{"CC-BC"}, Top],
    PlotStyle → Red, Frame → True, FrameLabel → {"Time Windows", "Z-Score (Pearson)"}],
    PlotRange → {All, {-10, 2}}, Axes → False, ImageSize → 500,
    GridLines → Automatic, PlotLabel → "Z-Score Deviation on Different
        Time Windows for Thickness Network with Fixed Step Size"]}

```



Fixed Step Size Networks

Width Feature

```

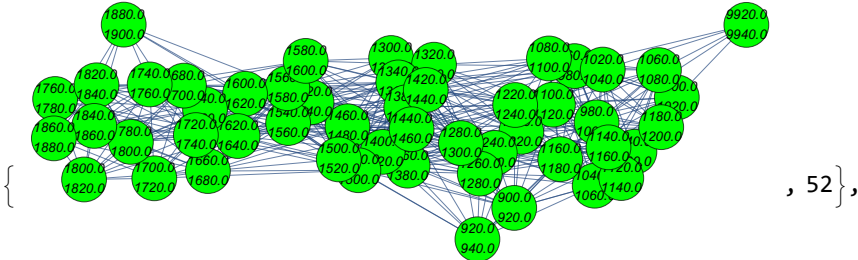
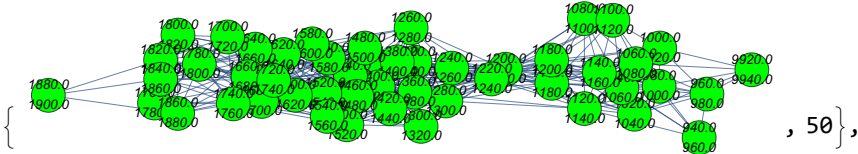
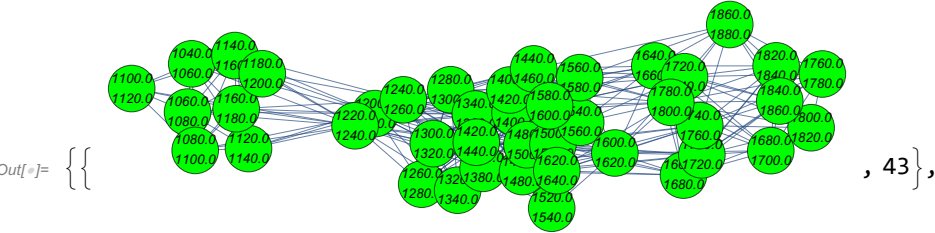
In[ ]:= AbsoluteTiming[
  widthdataintimewindowsFixedstep = snetworkdatabinnedintimewindows[9, 20, 10];]

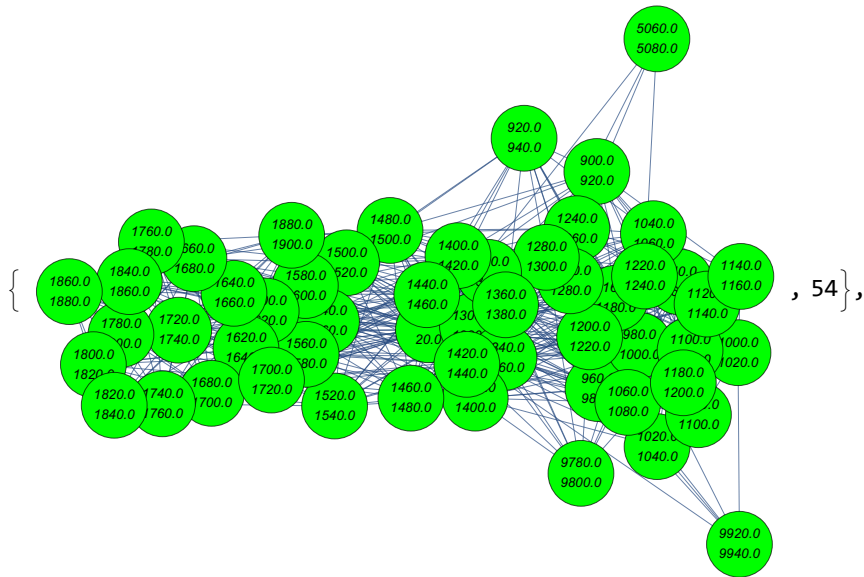
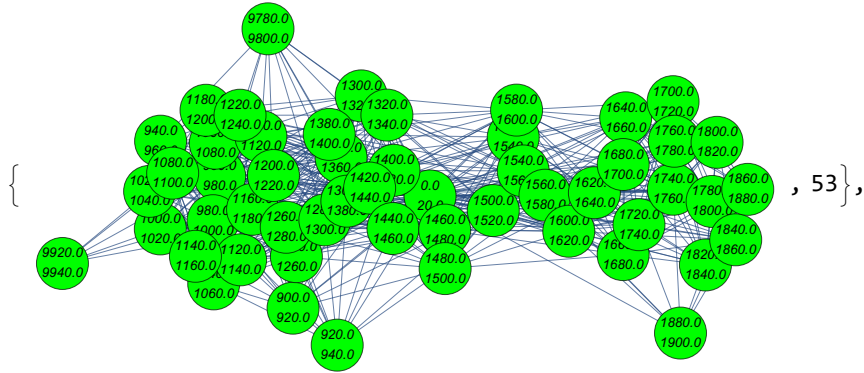
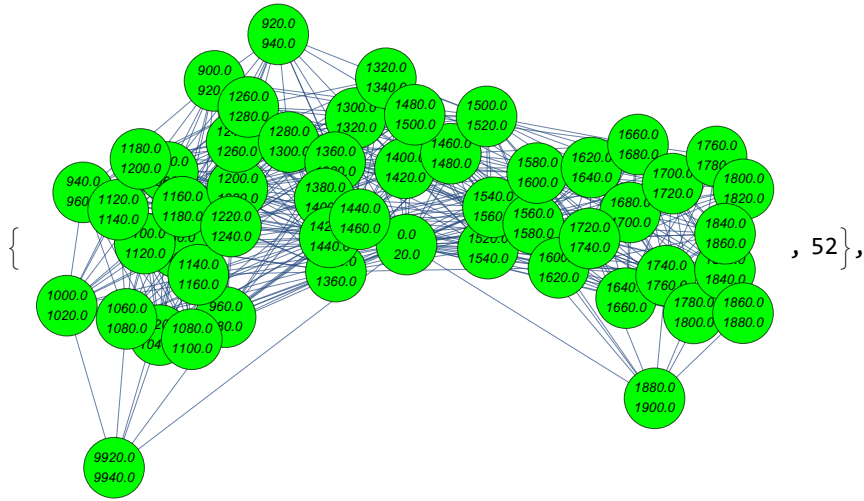
Out[ ]:= {939.348, Null}

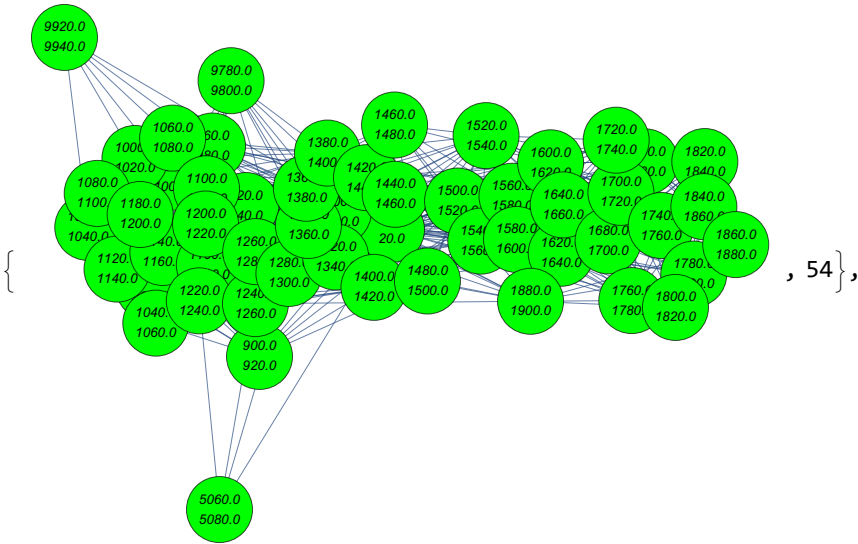
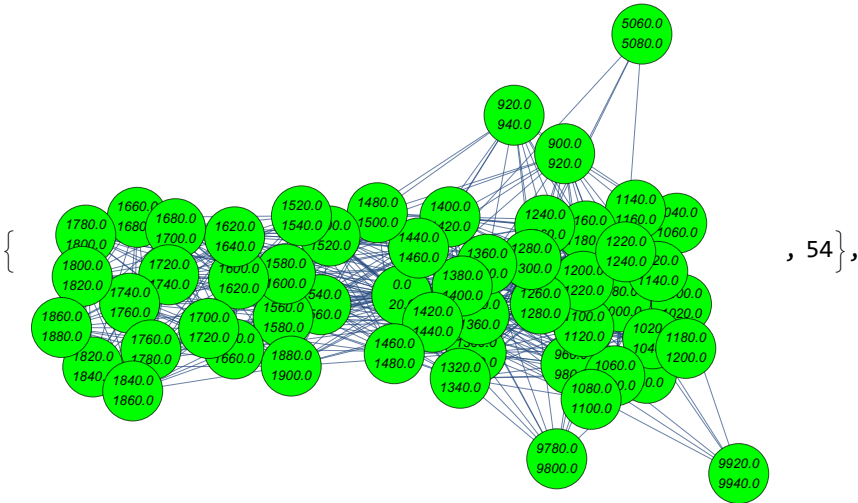
In[ ]:= graphsandnodenumbers = Table[snetworkgraph[widthdataintimewindowsFixedstep[[1]][[i]],
  widthdataintimewindowsFixedstep[[2]][[i]], 2, 7, 400, Green], {i, Range@10}];

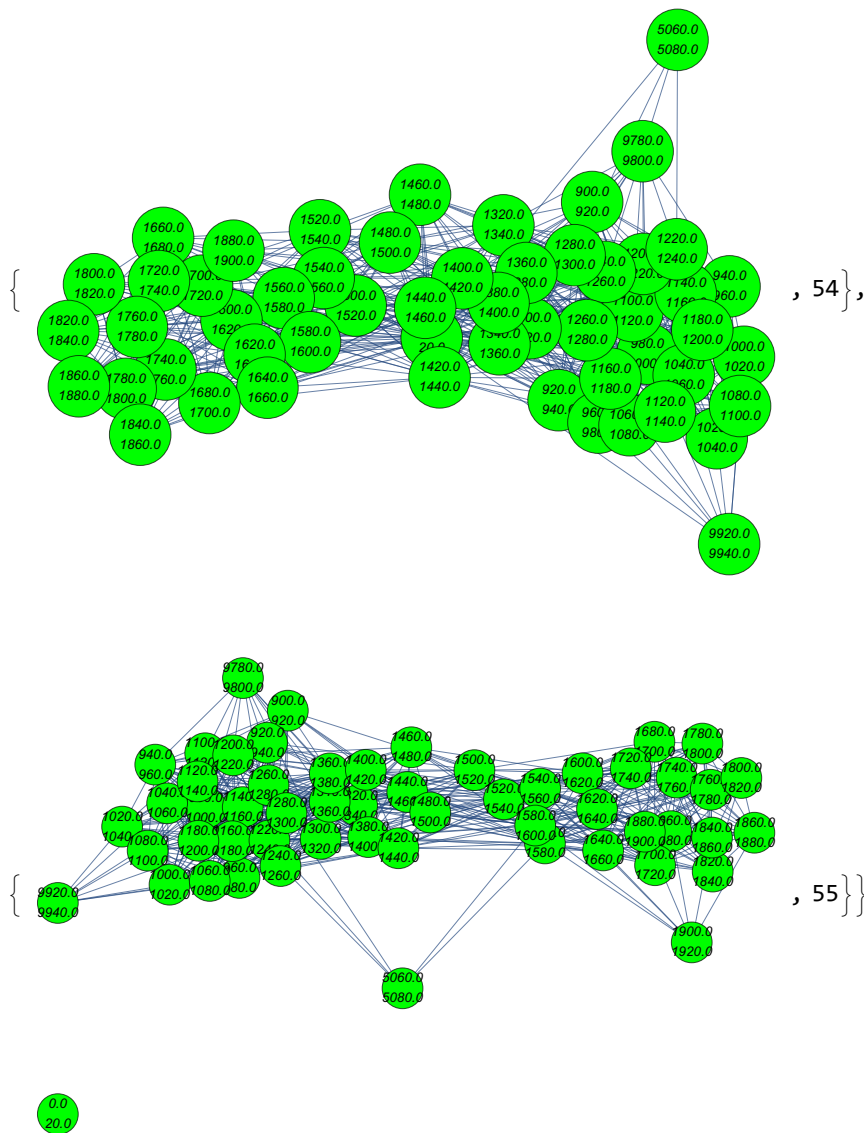
```

In[]:= **graphsandnodenumbers**









```

In[ ]:= correlationvaluesthroughwindowsspearman =
  Table[correlationfunction[i, 1], {i, graphsandnodenumbers[[All, 1]]}];
correlationvaluesthroughwindowsspearson =
  Table[correlationfunction[i, 2], {i, graphsandnodenumbers[[All, 1]]}];

In[ ]:= correlationvaluesthroughwindowsspearman
correlationvaluesthroughwindowsspearson

Out[ ]:= {{0.82433, -0.804068}, {0.734855, -0.811107}, {0.908269, -0.845656},
  {0.959018, -0.990457}, {0.904981, -0.977276}, {0.948857, -0.922007},
  {0.912036, -0.92532}, {0.906995, -0.932347}, {0.914195, -0.981357}, {0.839404, -0.81029}}

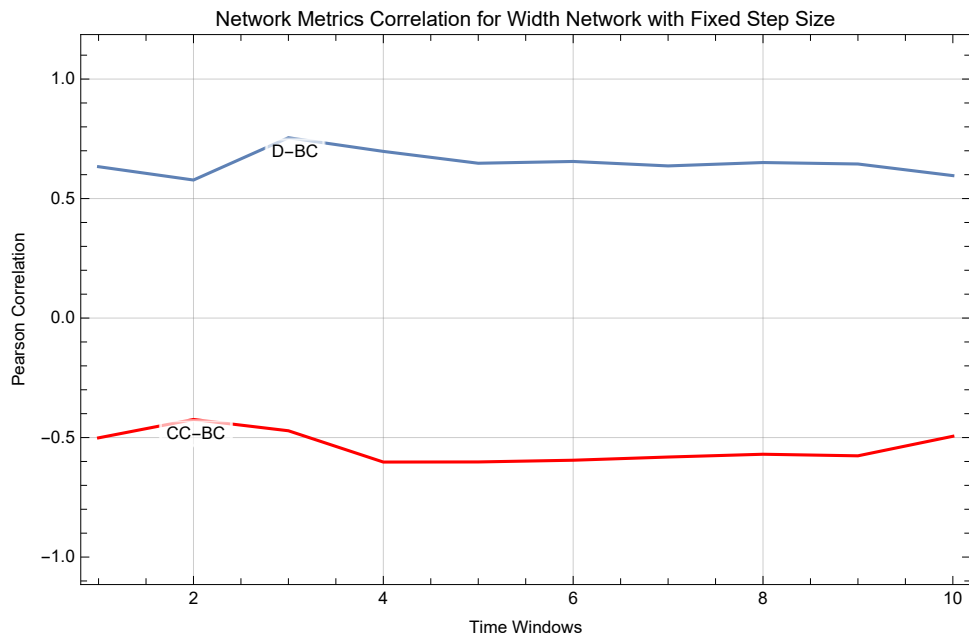
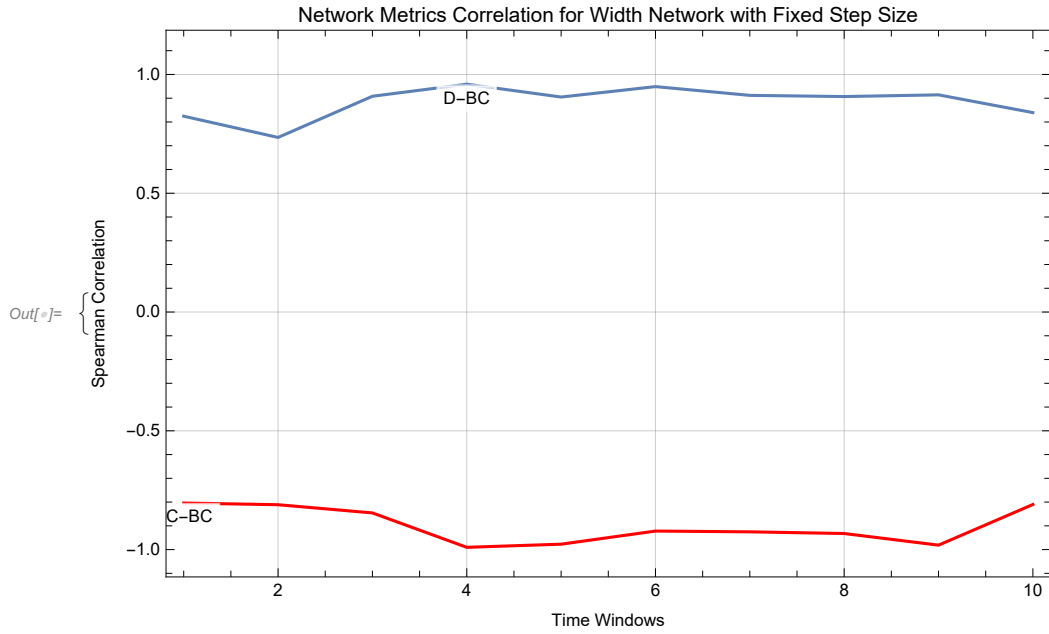
Out[ ]:= {{0.633363, -0.501172}, {0.577619, -0.424247},
  {0.754601, -0.471542}, {0.697417, -0.602426},
  {0.647809, -0.601992}, {0.655278, -0.594798}, {0.636646, -0.581435},
  {0.650767, -0.56981}, {0.644673, -0.576368}, {0.596069, -0.494557}}

```

```

In[ ]:= {Show[ListPlot[Transpose[
  {Range@10, Table[correlationvaluesthroughwindowsspearman[[j, 1]], {j, 1, 10}]}],
  Joined → True, PlotLabels → Placed[{"D-BC"}, Top], Frame → True,
  FrameLabel → {"Time Windows", "Spearman Correlation"}], ListPlot[Transpose[
  {Range@10, Table[correlationvaluesthroughwindowsspearman[[j, 2]], {j, 1, 10}]}],
  Joined → True, PlotLabels → Placed[{"CC-BC"}, Top], PlotStyle → Red,
  Frame → True, FrameLabel → {"Time Windows", "Spearman Correlation"}],
  PlotRange → {All, {-1, 1}}, Axes → False, ImageSize → 500, GridLines → Automatic,
  PlotLabel → "Network Metrics Correlation for Width Network with Fixed Step Size"],
Show[ListPlot[Transpose[
  {Range@10, Table[correlationvaluesthroughwindowsspearson[[j, 1]], {j, 1, 10}]}],
  Joined → True, PlotLabels → Placed[{"D-BC"}, Top], Frame → True,
  FrameLabel → {"Time Windows", "Pearson Correlation"}], ListPlot[Transpose[
  {Range@10, Table[correlationvaluesthroughwindowsspearson[[j, 2]], {j, 1, 10}]}],
  Joined → True, PlotLabels → Placed[{"CC-BC"}, Top], PlotStyle → Red,
  Frame → True, FrameLabel → {"Time Windows", "Pearson Correlation"}],
  PlotRange → {All, {-1, 1}}, Axes → False, ImageSize → 500, GridLines → Automatic,
  PlotLabel → "Network Metrics Correlation for Width Network with Fixed Step Size"]}

```



```
In[ ]:= ZscoreDeBCspearman = Transpose[{Range[1, 10],
Table[randomnessfunction[i, 1], {i, graphsandnodenumbers[[All, 1]]}][[All, 1]]}]
```

```
Out[ ]:= {{1, -5.1755}, {2, -11.6583}, {3, -2.47415}, {4, 0.543807}, {5, -3.0229},
{6, -0.266199}, {7, -2.79112}, {8, -3.14454}, {9, -2.76298}, {10, -7.74058}}
```

```
In[ ]:= ZscoreCCBCspearman = Transpose[{Range[1, 10],
Table[randomnessfunction[i, 1], {i, graphsandnodenumbers[[All, 1]]}][[All, 2]]}]
```

```
Out[ ]:= {{1, -3.10541}, {2, -3.49844}, {3, -3.74481}, {4, -4.40348}, {5, -4.34677},
{6, -4.13687}, {7, -4.03405}, {8, -4.18468}, {9, -4.52992}, {10, -3.36863}}
```

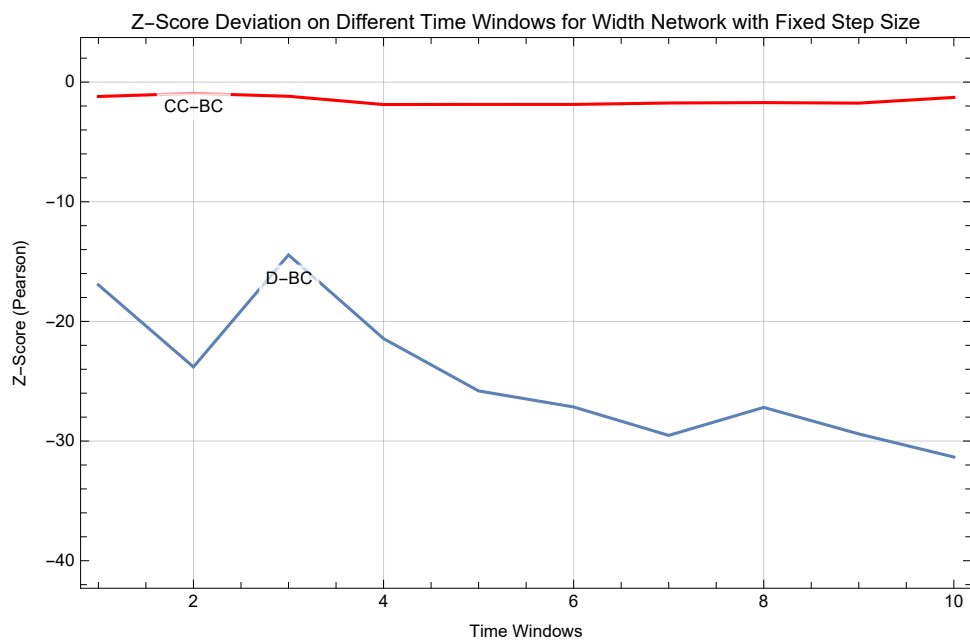
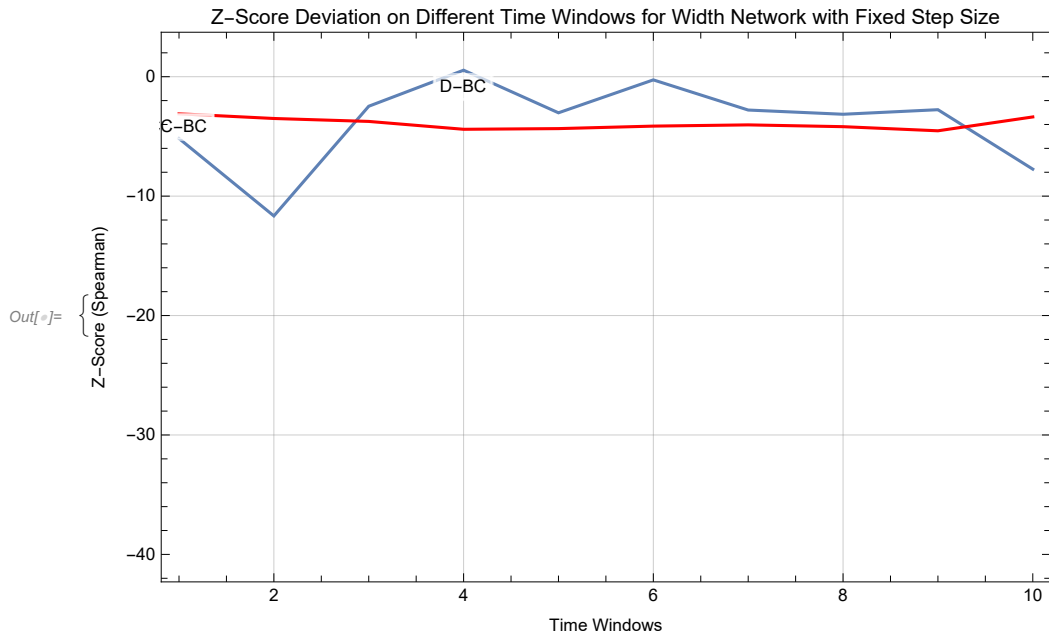
```

In[ ]:= ZscoreDeBCpearson = Transpose[{Range[1, 10],
    Table[randomnessfunction[i, 2], {i, graphsandnodenumbers[[All, 1]]}][[All, 1]]}]
Out[ ]:= {{1, -16.9464}, {2, -23.8082}, {3, -14.4413}, {4, -21.4366}, {5, -25.8088},
    {6, -27.1513}, {7, -29.5267}, {8, -27.1861}, {9, -29.4036}, {10, -31.3332}}

In[ ]:= ZscoreCCBCpearson = Transpose[{Range[1, 10],
    Table[randomnessfunction[i, 2], {i, graphsandnodenumbers[[All, 1]]}][[All, 2]]}]
Out[ ]:= {{1, -1.20444}, {2, -0.944433}, {3, -1.1856}, {4, -1.87577}, {5, -1.86207},
    {6, -1.86466}, {7, -1.74752}, {8, -1.71597}, {9, -1.75729}, {10, -1.28099}}

In[ ]:= {Show[ListPlot[ZscoreDeBCspearman, Joined → True, PlotLabels → Placed[{"D-BC"}, Top],
    Frame → True, FrameLabel → {"Time Windows", "Z-Score (Spearman)"}],
    ListPlot[ZscoreCCBCspearman, Joined → True, PlotLabels → Placed[{"CC-BC"}, Top],
    PlotStyle → Red, Frame → True, FrameLabel → {"Time Windows", "Z-Score (Spearman)"}],
    PlotRange → {All, {-40, 0}}, Axes → False, ImageSize → 500,
    GridLines → Automatic, PlotLabel →
    "Z-Score Deviation on Different Time Windows for Width Network with Fixed Step Size"],
    Show[ListPlot[ZscoreDeBCpearson, Joined → True, PlotLabels → Placed[{"D-BC"}, Top],
    Frame → True, FrameLabel → {"Time Windows", "Z-Score (Pearson)"}],
    ListPlot[ZscoreCCBCpearson, Joined → True, PlotLabels → Placed[{"CC-BC"}, Top],
    PlotStyle → Red, Frame → True, FrameLabel → {"Time Windows", "Z-Score (Pearson)"}],
    PlotRange → {All, {-40, 0}}, Axes → False, ImageSize → 500,
    GridLines → Automatic, PlotLabel →
    "Z-Score Deviation on Different Time Windows for Width Network with Fixed Step Size"]}

```



Thickness Feature

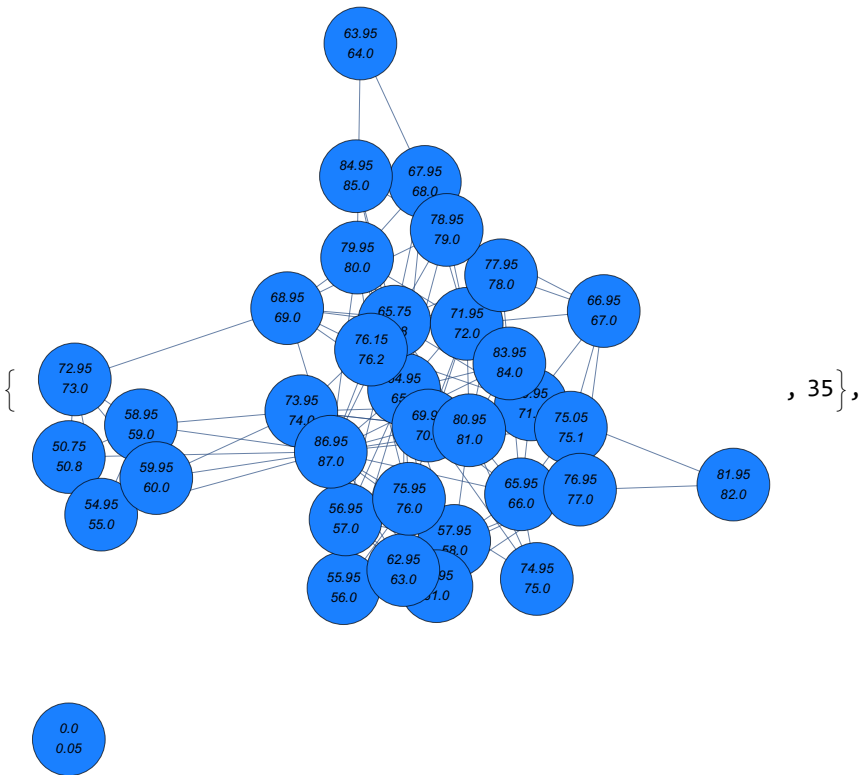
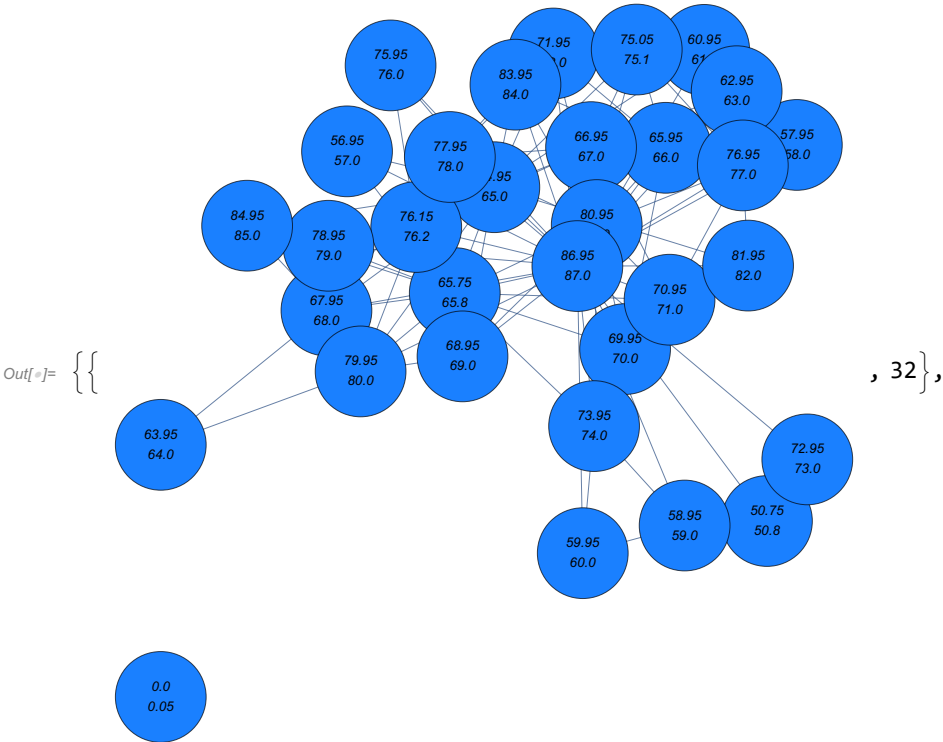
```

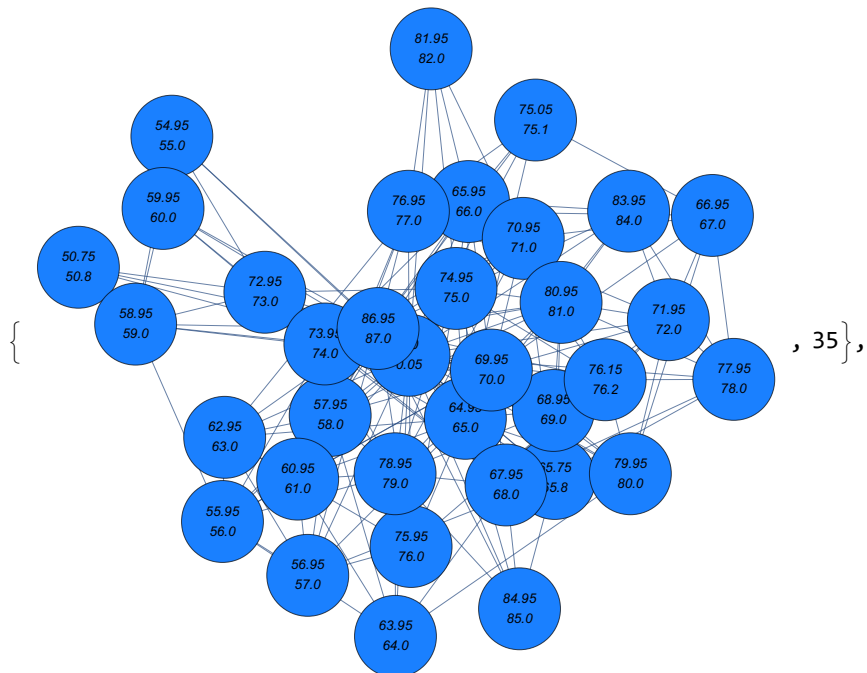
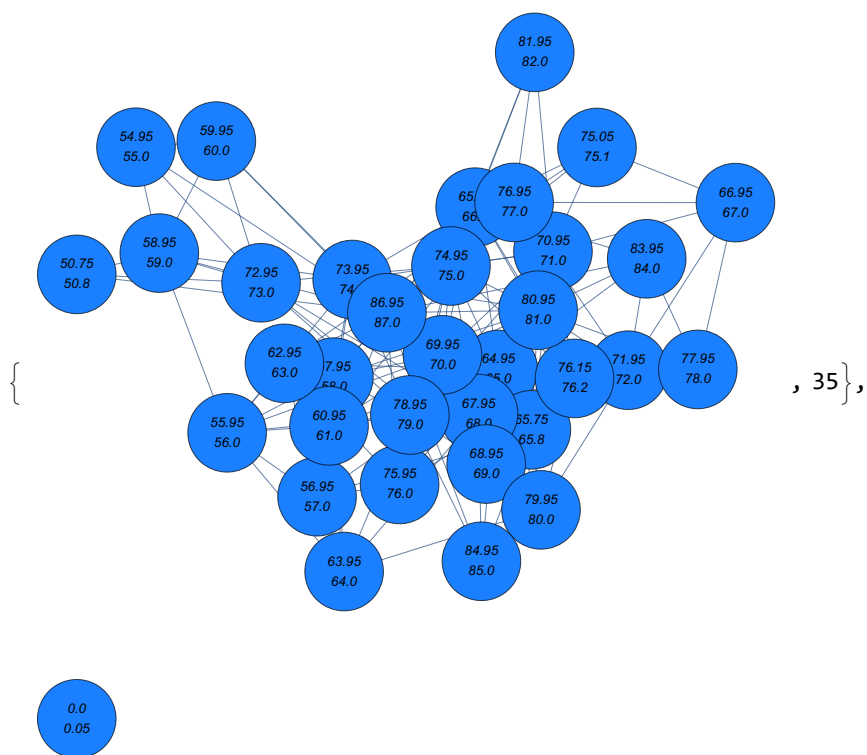
In[ ]:= AbsoluteTiming[
  thicknessdataintimewindowsFixedstep = snetworkdatabinintimewindows[10, 0.05, 10];
Out[ ]:= $Aborted

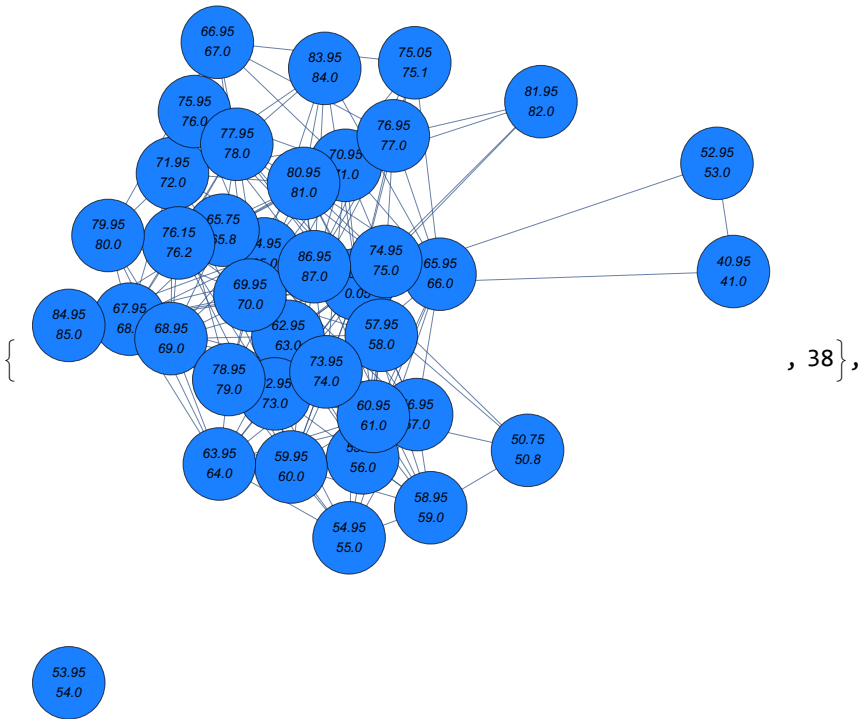
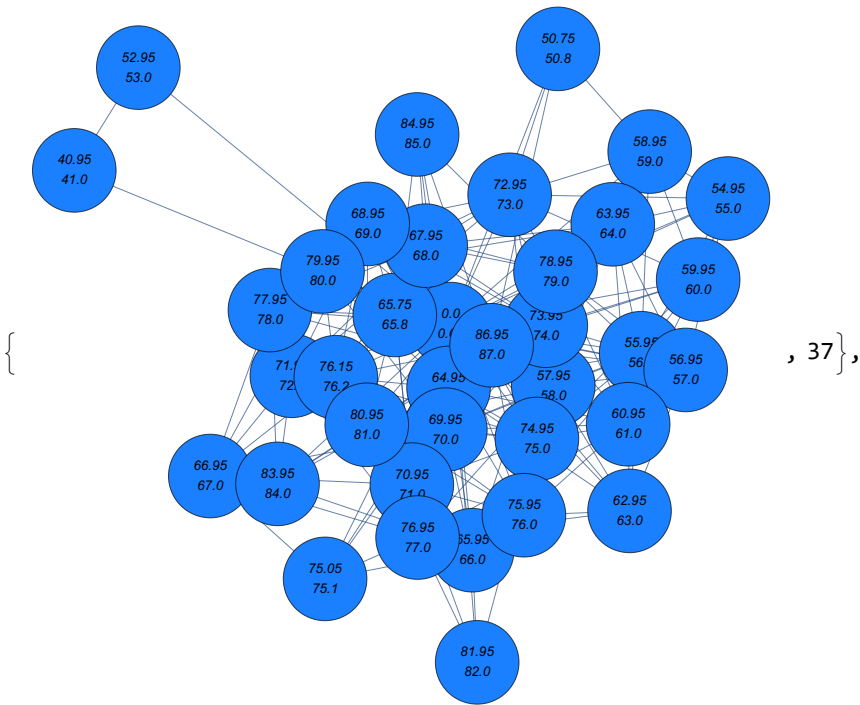
In[ ]:= graphsandnodenumbers = Table[snetworkgraph[thicknessdataintimewindowsFixedstep[[1]][[i]],
  thicknessdataintimewindowsFixedstep[[2]][[i]],
  2, 7, 400, RGBColor[0.1, 0.5, 1.]], {i, Range@10}];

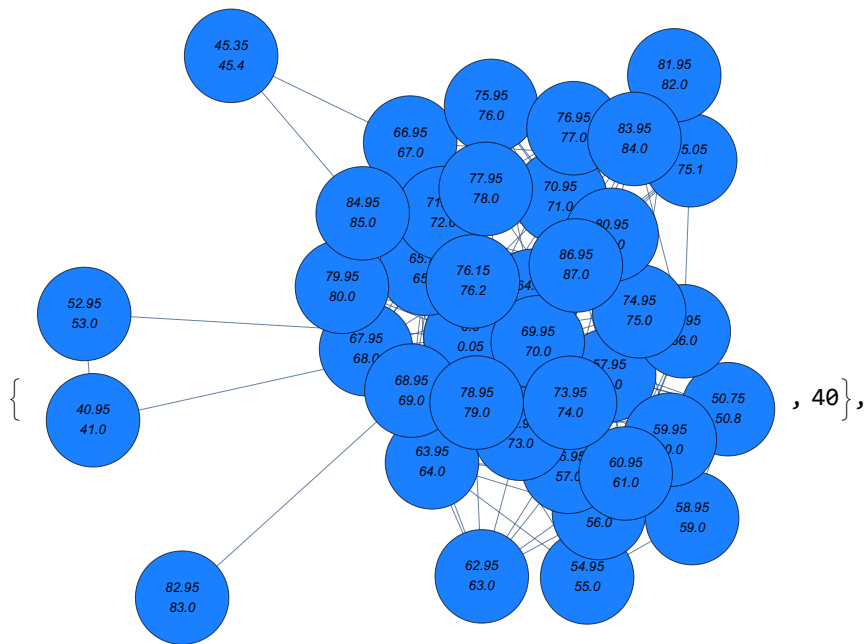
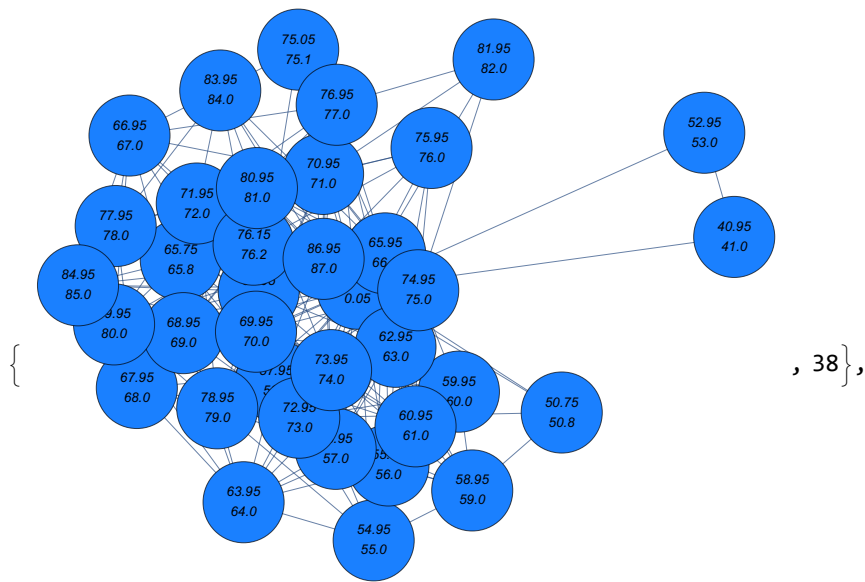
In[ ]:= graphsandnodenumbers

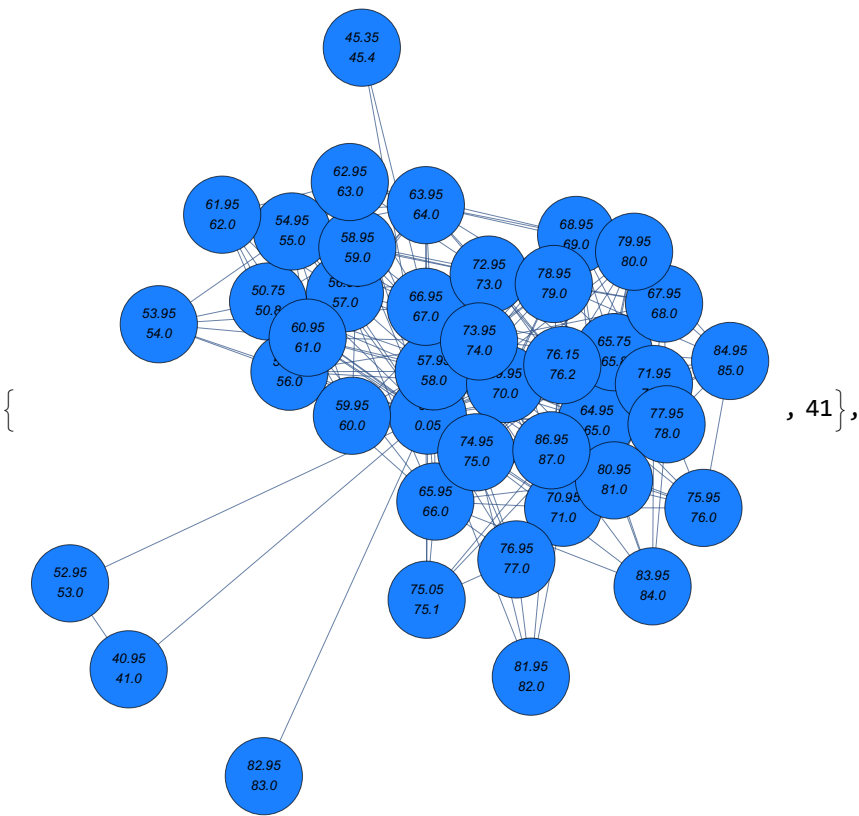
```

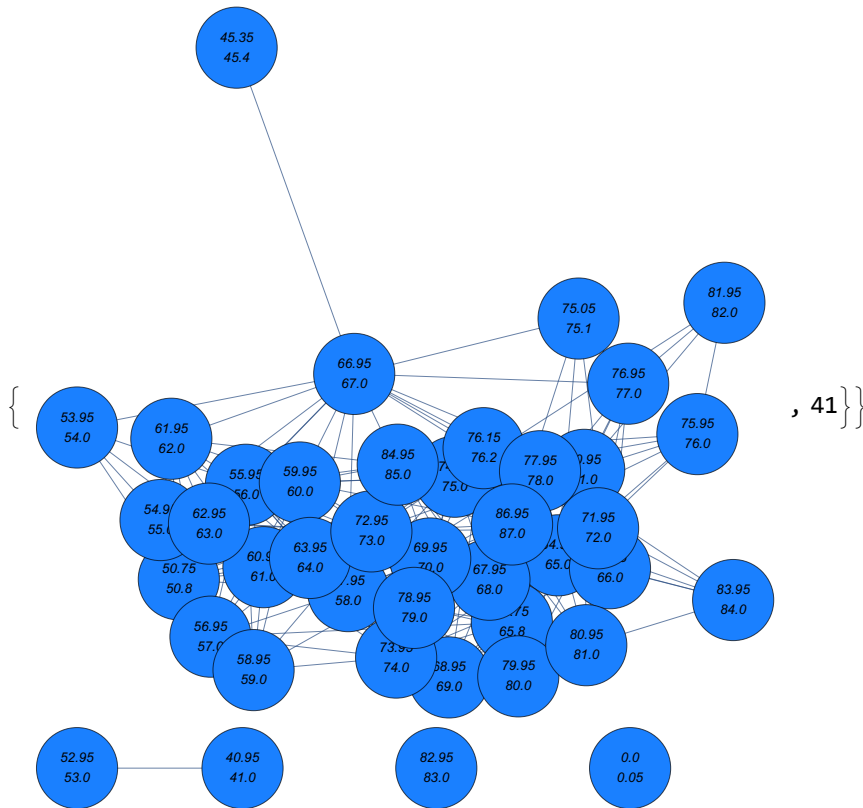












```

In[ ]:= correlationvaluesthroughwindowsspearman =
  Table[correlationfunction[i, 1], {i, graphsandnodenumbers[All, 1]}];
correlationvaluesthroughwindowsspearson =
  Table[correlationfunction[i, 2], {i, graphsandnodenumbers[All, 1]}];

In[ ]:= correlationvaluesthroughwindowsspearman
correlationvaluesthroughwindowsspearson

Out[ ]:= {{0.938808, -0.78658}, {0.873987, -0.663998}, {0.916719, -0.7004}, {0.93912, -0.906811},
  {0.95285, -0.889666}, {0.935017, -0.722435}, {0.939483, -0.699436},
  {0.943043, -0.53645}, {0.927237, -0.686511}, {0.94354, -0.25778}}

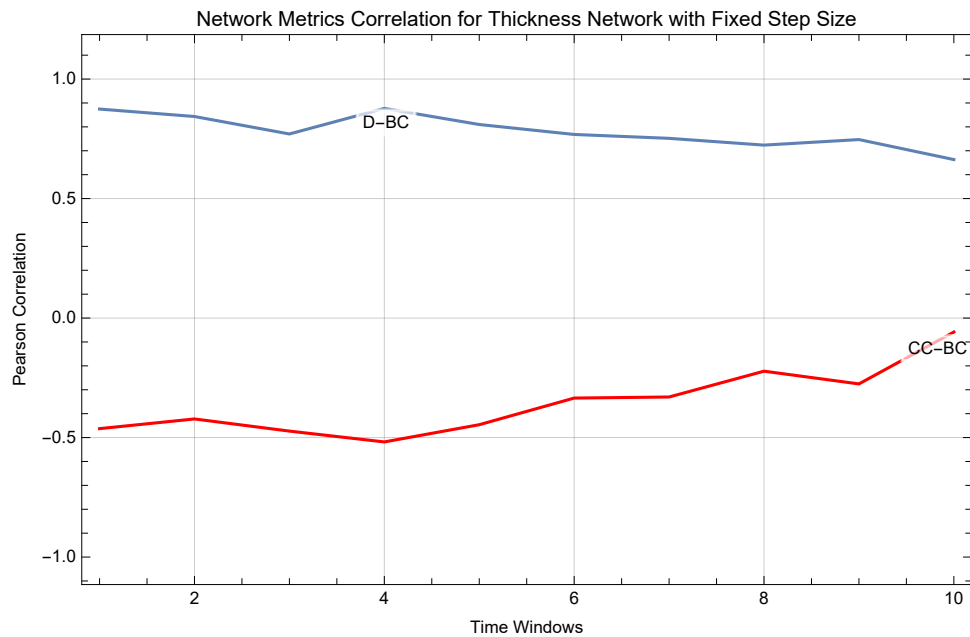
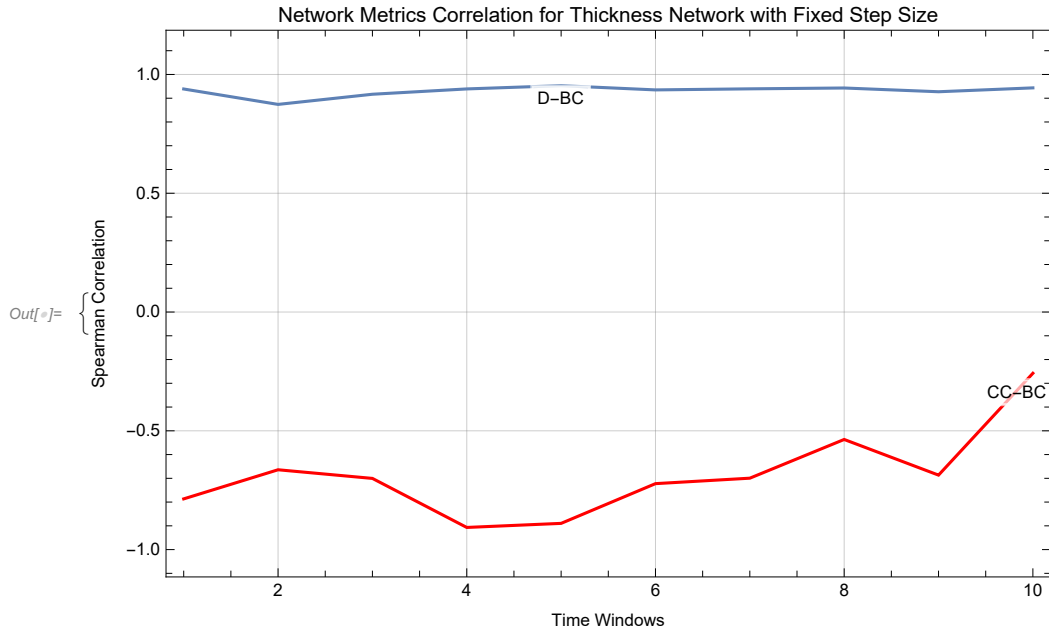
Out[ ]:= {{0.874484, -0.462631}, {0.843387, -0.422115},
  {0.770286, -0.472945}, {0.877292, -0.518271}, {0.809918, -0.446188},
  {0.768257, -0.334724}, {0.752032, -0.330238}, {0.723693, -0.22225},
  {0.746908, -0.275495}, {0.663251, -0.0583977}}

```

```

In[6]:= {Show[ListPlot[Transpose[
  {Range@10, Table[correlationvaluesthroughwindowsspearman[[j, 1]], {j, 1, 10}]}],
  Joined → True, PlotLabels → Placed[{"D-BC"}, Top], Frame → True,
  FrameLabel → {"Time Windows", "Spearman Correlation"}], ListPlot[Transpose[
  {Range@10, Table[correlationvaluesthroughwindowsspearman[[j, 2]], {j, 1, 10}]}],
  Joined → True, PlotLabels → Placed[{"CC-BC"}, Top], PlotStyle → Red,
  Frame → True, FrameLabel → {"Time Windows", "Spearman Correlation"}],
  PlotRange → {All, {-1, 1}}, Axes → False, ImageSize → 500, GridLines → Automatic,
  PlotLabel → "Network Metrics Correlation for Thickness Network with Fixed Step Size"],
Show[ListPlot[Transpose[
  {Range@10, Table[correlationvaluesthroughwindowsspearson[[j, 1]], {j, 1, 10}]}],
  Joined → True, PlotLabels → Placed[{"D-BC"}, Top], Frame → True,
  FrameLabel → {"Time Windows", "Pearson Correlation"}], ListPlot[Transpose[
  {Range@10, Table[correlationvaluesthroughwindowsspearson[[j, 2]], {j, 1, 10}]}],
  Joined → True, PlotLabels → Placed[{"CC-BC"}, Top], PlotStyle → Red,
  Frame → True, FrameLabel → {"Time Windows", "Pearson Correlation"}],
  PlotRange → {All, {-1, 1}}, Axes → False, ImageSize → 500, GridLines → Automatic,
  PlotLabel → "Network Metrics Correlation for Thickness Network with Fixed Step Size"]}

```



```
In[ ]:= ZscoreDeBCspearman = Transpose[{Range[1, 10],
Table[randomnessfunction[i, 1], {i, graphsandnodenumbers[[All, 1]]}][[All, 1]]}]
```

```
Out[ ]:= {{1, 0.616193}, {2, -1.28733}, {3, -0.104282}, {4, 0.565508}, {5, 1.07189},
{6, 0.367045}, {7, 0.478779}, {8, 0.559077}, {9, -0.0694945}, {10, 0.590463}}
```

```
In[ ]:= ZscoreCCBCspearman = Transpose[{Range[1, 10],
Table[randomnessfunction[i, 1], {i, graphsandnodenumbers[[All, 1]]}][[All, 2]]}]
```

```
Out[ ]:= {{1, -2.93182}, {2, -2.53266}, {3, -2.40751}, {4, -3.46177}, {5, -3.3986},
{6, -2.49543}, {7, -2.42854}, {8, -1.50394}, {9, -2.47674}, {10, 0.109912}}
```

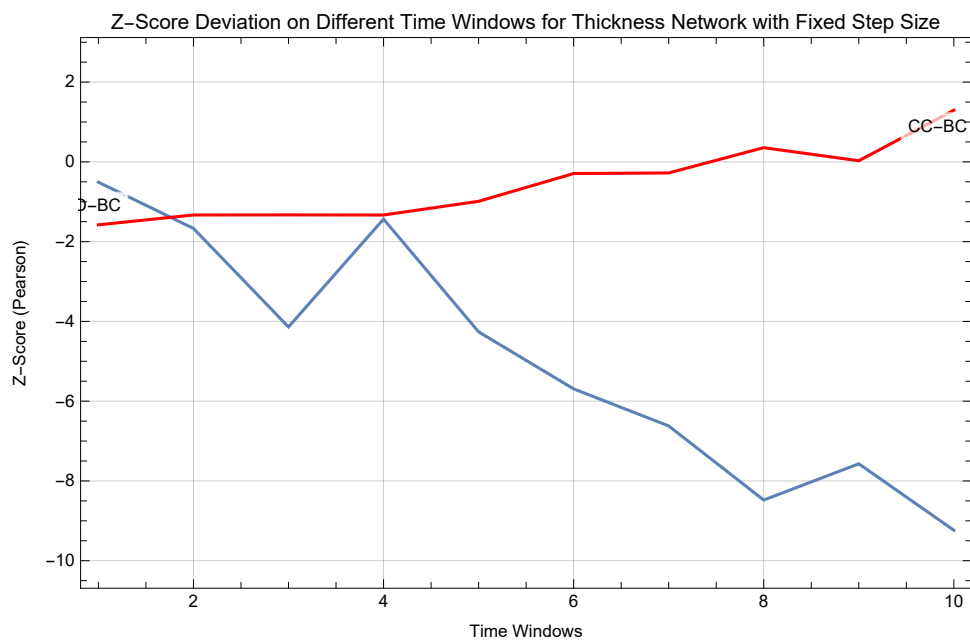
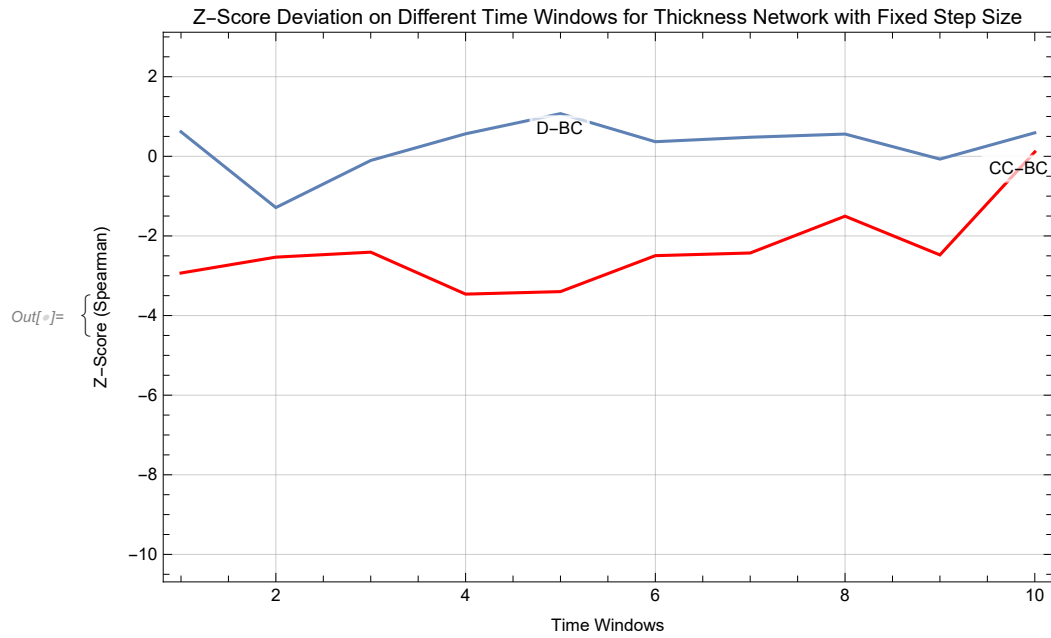
```

In[ ]:= ZscoreDeBCpearson = Transpose[{Range[1, 10],
    Table[randomnessfunction[i, 2], {i, graphsandnodenumbers[[All, 1]]}][[All, 1]]}]
Out[ ]:= {{1, -0.510046}, {2, -1.66848}, {3, -4.13987}, {4, -1.43423}, {5, -4.2623},
    {6, -5.6921}, {7, -6.62055}, {8, -8.47877}, {9, -7.56998}, {10, -9.23535}}

In[ ]:= ZscoreCCBCpearson = Transpose[{Range[1, 10],
    Table[randomnessfunction[i, 2], {i, graphsandnodenumbers[[All, 1]]}][[All, 2]]}]
Out[ ]:= {{1, -1.57851}, {2, -1.33152}, {3, -1.32984}, {4, -1.33201}, {5, -0.9891},
    {6, -0.2925}, {7, -0.278031}, {8, 0.356254}, {9, 0.0282377}, {10, 1.29413}}

In[ ]:= {Show[ListPlot[ZscoreDeBCspearman, Joined → True, PlotLabels → Placed[{"D-BC"}, Top],
    Frame → True, FrameLabel → {"Time Windows", "Z-Score (Spearman)"}],
    ListPlot[ZscoreCCBCspearman, Joined → True, PlotLabels → Placed[{"CC-BC"}, Top],
    PlotStyle → Red, Frame → True, FrameLabel → {"Time Windows", "Z-Score (Spearman)"}],
    PlotRange → {All, {-10, 2}}, Axes → False, ImageSize → 500,
    GridLines → Automatic, PlotLabel → "Z-Score Deviation on Different
        Time Windows for Thickness Network with Fixed Step Size"],
    Show[ListPlot[ZscoreDeBCpearson, Joined → True, PlotLabels → Placed[{"D-BC"}, Top],
    Frame → True, FrameLabel → {"Time Windows", "Z-Score (Pearson)"}],
    ListPlot[ZscoreCCBCpearson, Joined → True, PlotLabels → Placed[{"CC-BC"}, Top],
    PlotStyle → Red, Frame → True, FrameLabel → {"Time Windows", "Z-Score (Pearson)"}],
    PlotRange → {All, {-10, 2}}, Axes → False, ImageSize → 500,
    GridLines → Automatic, PlotLabel → "Z-Score Deviation on Different
        Time Windows for Thickness Network with Fixed Step Size"]}

```

Fixed Bucket Size Networks

Width Feature

Thickness Feature