

(A)

$$P(U) = P(U|R) * P(R) + P(U|\bar{R}) * P(\bar{R})$$

$$P(R) = P(R|S, A) + P(S \cap A) + P(R|\bar{S}A) * P(\bar{S} \cap A)$$

$$P(R|\bar{S}\bar{A}) * P(S \cap \bar{A}) + P(R|\bar{S}\bar{A}) * P(\bar{S} \cap \bar{A})$$

$$= 0.95 * 0.001 * 0.002 + 0.29 * 0.999 * 0.02 + 0.94 * 0.001 * 0.998 + 0.001 * 0.999 * 0.998$$

$$= 0.0000019 + 0.000579 + 0.0001$$

$$0.002159 = 0.9974$$

(B)

$$P(R=1|A=0) = P(R=1|S=0, A=0) * P(S=0)$$

$$+ P(R=1|S=1, A=0) * P(S=1)$$

$$0.001 * 0.999 + 0.94 * 0.001$$

$$= 0.001939$$

(C)

$$P(S=1|R=1) = P(R=1|S=1) * P(S=1)$$

$$P(R=1|S=1, A=0) * P(A=0) + P(R=1|S=1, A=1) * P(A=1)$$

$$0.94 * 0.998 + 0.95 * 0.002$$

$$= 0.93812 + 0.0019$$

$$= \frac{0.94002 * 0.001}{0.0025}$$

$$= 0.376$$