# (순한맛) Neural Network

임경태

## 실습 설정방법

본 강의에서 사용하는 Visdom을 실행하기 위해서는 Jupyter notebook을 개인 PC에 설치해서 실습 해야함

Colab에서 실행하고자 하는 경우 Visdom으로 시각화 하는 부분 주석 처리하면 됨

Jupyter, Visdom설치 관련 참조 https://github.com/jujbob/NLPApps

## **Linear Regression**

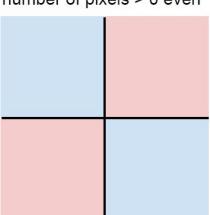
#### Hard cases for a linear classifier

#### Class 1:

number of pixels > 0 odd

#### Class 2

number of pixels > 0 even

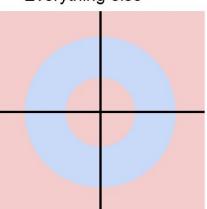


#### Class 1:

1 <= L2 norm <= 2

#### Class 2

Everything else

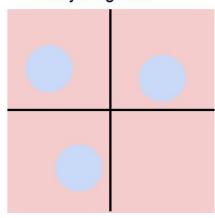


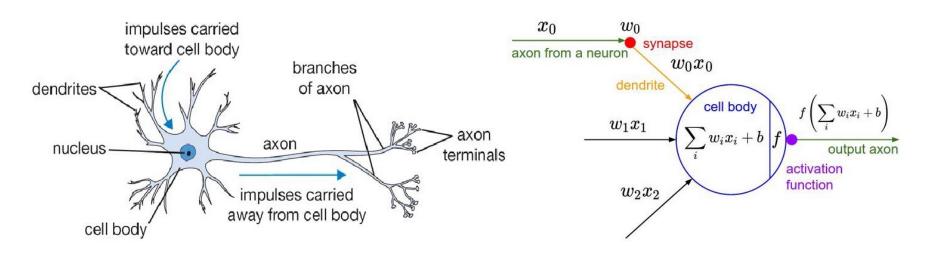
#### Class 1:

Three modes

#### Class 2

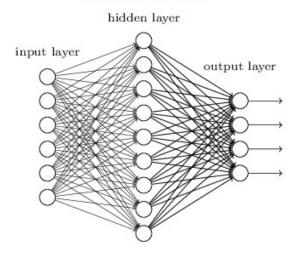
Everything else





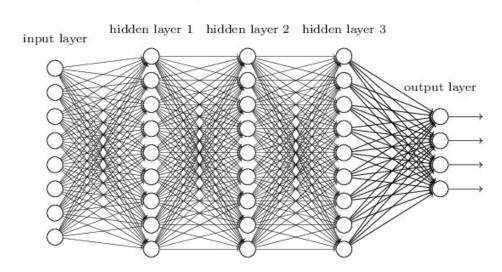
여러 자극이 들어오고 일정 기준을 넘으면 이를 다른 뉴런에 전달하는 구조

### "Non-deep" feedforward neural network

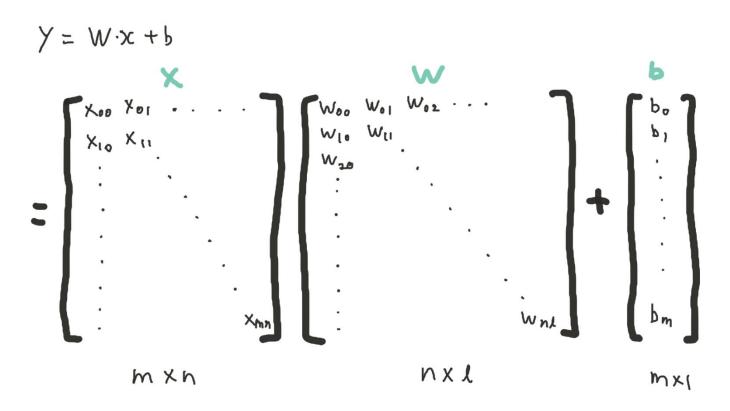


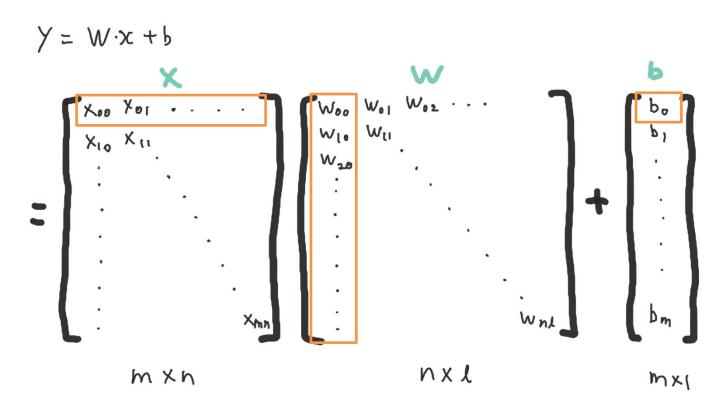
$$y = w2(act(w1 * input + b1)) + b2$$

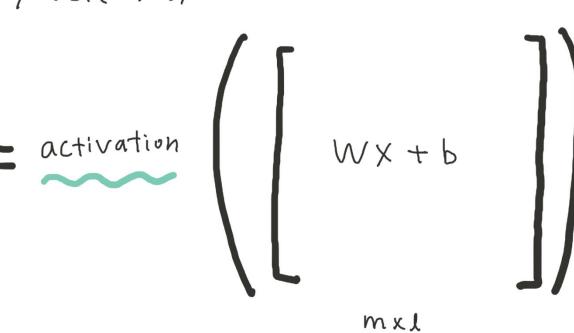
#### Deep neural network



$$y = w4(act(w3(act(w2(act(w1*input + b1)) + b2)) + b3)) + b4$$







만약 activation function이 없다면 아래의 식은 결국 linear function.

$$y = w4(act(w3(act(w1*input + b1)) + b2)) + b3)) + b4$$

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activation function으로 non-linearity를 추가해야 함

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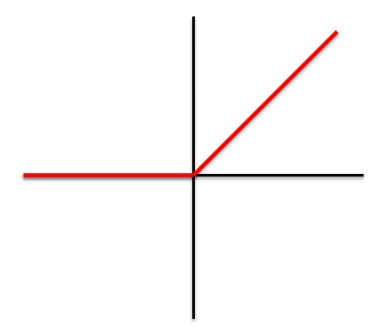
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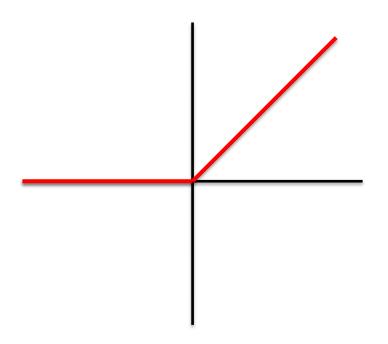
activation function으로 non-linearity를 추가해야 함

그렇다면 어떤 activation function을 써야 할까?

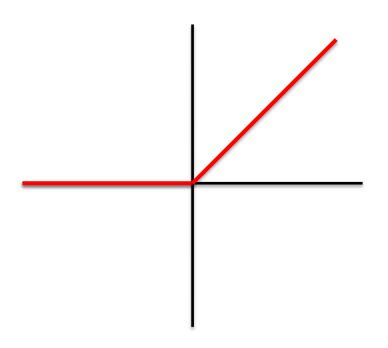
Activation function	Equation	Example	1D Graph		
Unit step (Heaviside)	$\phi(z) = \begin{cases} 0, & z < 0, \\ 0.5, & z = 0, \\ 1, & z > 0, \end{cases}$	Perceptron variant	+		
Sign (Signum)	$\phi(z) = \begin{cases} -1, & z < 0, \\ 0, & z = 0, \\ 1, & z > 0, \end{cases}$	Perceptron variant	-		
Linear	$\phi(z)=z$	Adaline, linear regression			
Piece-wise linear	$\phi(z) = \begin{cases} 1, & z \ge \frac{1}{2}, \\ z + \frac{1}{2}, & -\frac{1}{2} < z < \frac{1}{2}, \\ 0, & z \le -\frac{1}{2}, \end{cases}$	Support vector machine			
Logistic (sigmoid)	$\phi(z) = \frac{1}{1 + e^{-z}}$	Logistic regression, Multi-layer NN			
Hyperbolic tangent	$\phi(z) = \frac{e^z - e^{-z}}{e^z + e^{-z}}$	Multi-layer NN	-		

(출처: http://www.kdnuggets.com/2016/08/role-activation-function-neural-network.html)



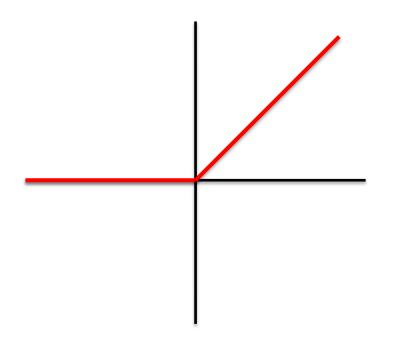


Rectified Linear Unit (ReLU)



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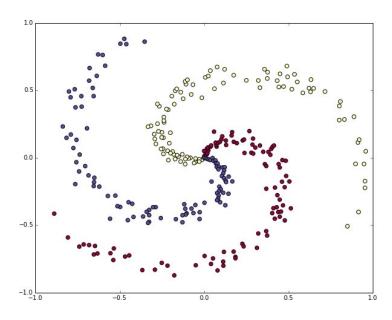
$$f(x) = max(0,x)$$

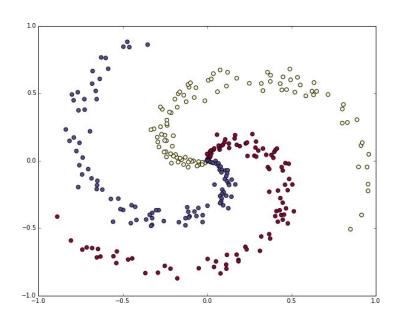


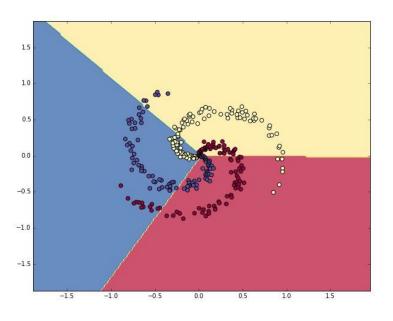
Rectified Linear Unit (ReLU)

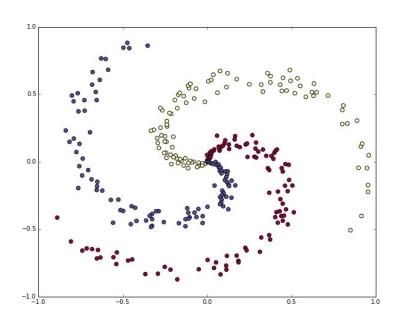
$$f(x) = \max(0,x)$$

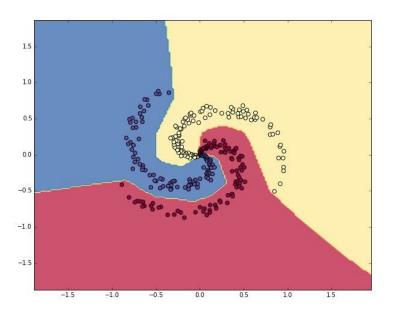
기존의 sigmoid와 tanh로는 학습이 잘 안됐었는데 relu는 gradient의 전달이 좋아서 default로 사용되고 있음

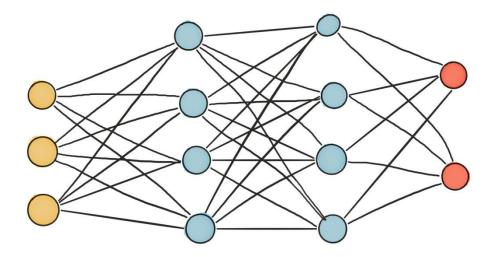


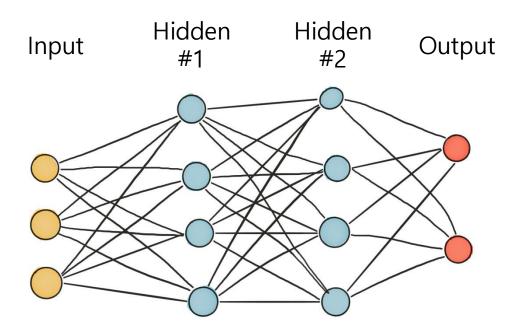


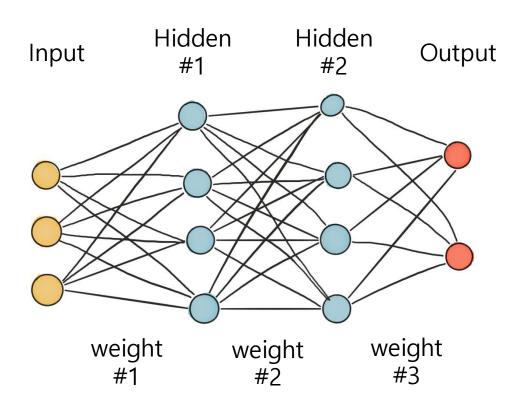


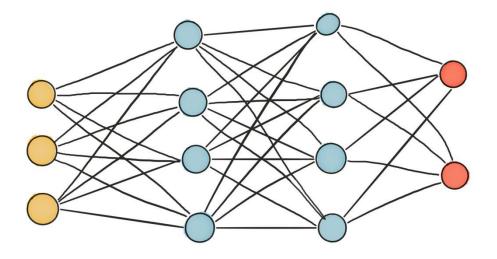


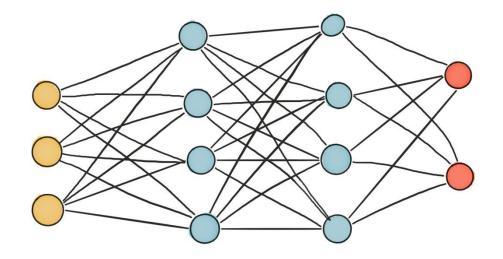




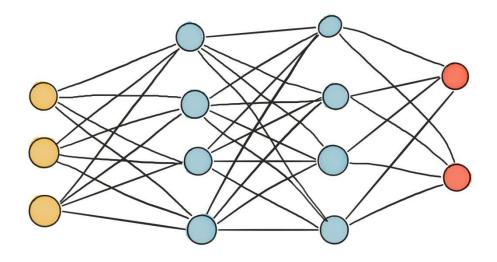






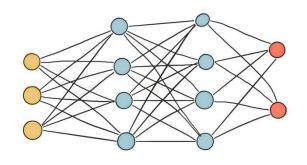


$w_{oo}$	$w_{01}$	$w_{02}$	$w_{03}$		$\lceil w_{oo} \rceil$	$w_{01}$	$w_{02}$	$w_{03}$		$W_{00}$	$w_{01}$	
$w_{10}$	$W_{11}$	$w_{12}$	$w_{13}$	X	$w_{10}$	$w_{11}$	$w_{12}$	$w_{13}$		$w_{10}$	$w_{11} \\ w_{21}$	l
$ w_{20} $	W21	$w_{22}$	$W_{23}$	, , , , , , , , , , , , , , , , , , ,	$w_{20}$	$w_{11}\\w_{21}$	$w_{22}$	$W_{23}$	Х	$w_{20}$	$w_{21}$	l
L	21		_		$w_{30}$	$w_{31}$	$w_{32}$	$W_{33}$		$w_{30}$	$w_{31}$	l



$\begin{bmatrix} w_{oo} \\ w_{10} \\ w_{20} \end{bmatrix}$	$w_{01} \\ w_{11} \\ w_{21}$	$w_{02} \\ w_{12} \\ w_{22}$	$w_{03} \ w_{13} \ w_{23} \ $	X	$\begin{bmatrix} w_{oo} \\ w_{10} \\ w_{20} \\ w_{30} \end{bmatrix}$	$w_{01} \\ w_{11} \\ w_{21} \\ w_{31}$	$w_{02} \\ w_{12} \\ w_{22} \\ w_{32}$	$w_{03} \ w_{13} \ w_{23} \ w_{33} \]$	X	$\begin{bmatrix} w_{00} \\ w_{10} \\ w_{20} \\ w_{30} \end{bmatrix}$	$w_{01} \ w_{11} \ w_{21} \ w_{31} ]$	
	3>	κ4				4)	x4			4>	κ2	

$$y^* = w3 * sig(w2 * sig(w1 * x + b1) + b2) + b3$$

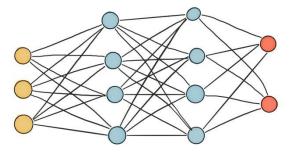


쉽게 이해되도록 loss = 예측값-실제로 설정

$$y^* = w3 * sig(w2 * sig(w1 * x + b1) + b2) + b3$$

$$loss = y^* - y$$

$$= w3 * sig(w2 * sig(w1 * x + b1) + b2) + b3 - y$$



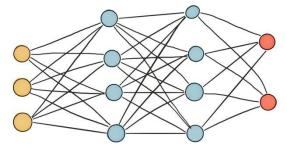
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$$\frac{\partial loss}{\partial w} = sig(w2 * sig(w1 * x + b1) + b2)$$
3



쉽게 이해되도록 loss = 예측값-실제로 설정

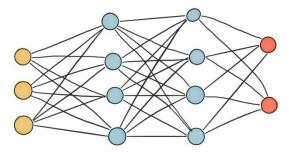
$$y^* = w3 * sig(w2 * sig(w1 * x + b1) + b2) + b3$$

$$loss = y^* - y$$

$$= w3 * sig(w2 * sig(w1 * x + b1) + b2) + b3 - y$$

$$\frac{\partial loss}{\partial w} = sig(w2 * sig(w1 * x + b1) + b2)$$

$$\frac{\partial loss}{\partial b3} = 1$$



쉽게 이해되도록 loss = 예측값-실제로 설정

$$y^* = w3 * sig(w2 * sig(w1 * x + b1) + b2) + b3$$

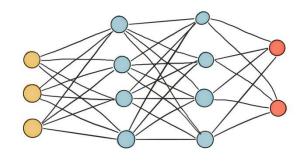
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$$\frac{\partial loss}{\partial w3} = sig(w2 * sig(w1 * x + b1) + b2)$$

$$\frac{\partial loss}{\partial b3} = 1$$

$$\frac{\partial loss}{\partial w2} = ??$$



쉽게 이해되도록 loss = 예측값-실제로 설정

$$y^* = w3 * sig(w2 * sig(w1 * x + b1) + b2) + b3$$

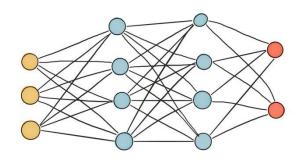
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$$= w3 * sig(w2 * sig(w1 * x + b1) + b2) + b3 - y$$

$$\frac{\partial loss}{\partial w3} = sig(w2 * sig(w1 * x + b1) + b2)$$

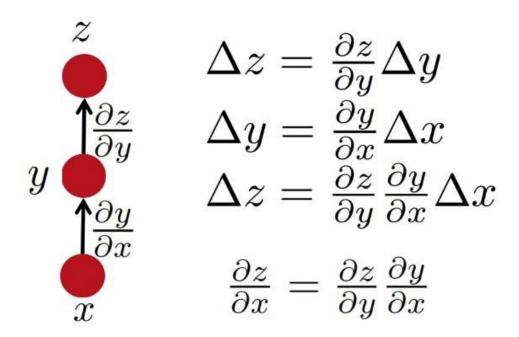
$$\frac{\partial loss}{\partial b3} = 1$$

$$\frac{\partial loss}{\partial w} = chain rule!!$$



쉽게 이해되도록 loss = 예측값-실제로 설정

#### **Simple Chain Rule**



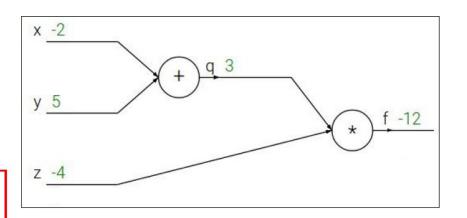
Backpropagation: a simple example

$$f(x,y,z) = (x+y)z$$
  
e.g. x = -2, y = 5, z = -4

$$q=x+y \qquad rac{\partial q}{\partial x}=1, rac{\partial q}{\partial y}=1$$

$$f=qz$$
  $rac{\partial f}{\partial q}=z, rac{\partial f}{\partial z}=q$ 

Want:  $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$ 



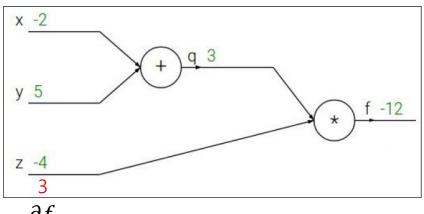
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Want:  $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$ 



$$\frac{\partial f}{\partial z} = q = x + y = -2 + 5 = 3$$

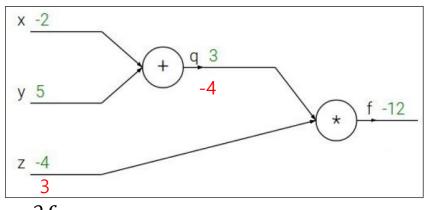
Backpropagation: a simple example

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e.g. x = -2, y = 5, z = -4

$$q=x+y \qquad rac{\partial q}{\partial x}=1, rac{\partial q}{\partial y}=1$$

$$f=qz$$
  $rac{\partial f}{\partial q}=z, rac{\partial f}{\partial z}=q$ 

Want:  $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$ 



$$\frac{\partial f}{\partial z} = q = x + y = -2 + 5 = 3$$

$$\frac{\partial f}{\partial q} = z = -4$$

Backpropagation: a simple example

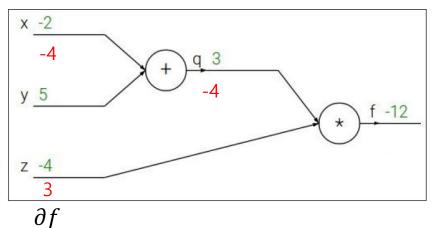
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  $rac{\partial f}{\partial q}=z, rac{\partial f}{\partial z}=q$ 

Want:

$$\frac{\partial f}{\partial x}$$
,  $\frac{\partial f}{\partial y}$ ,  $\frac{\partial f}{\partial z}$ 



$$\frac{\partial f}{\partial z} = q = x + y = -2 + 5 = 3$$

$$\frac{\partial f}{\partial q} = z = -4 \qquad \frac{\partial f}{\partial x} = \frac{\partial f}{\partial q} \frac{\partial q}{\partial x} = -4 * 1 = -4$$

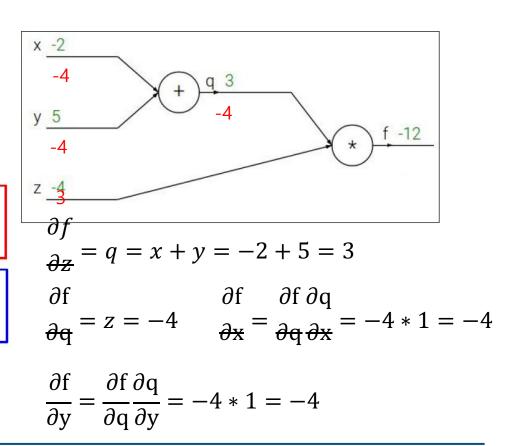
Backpropagation: a simple example

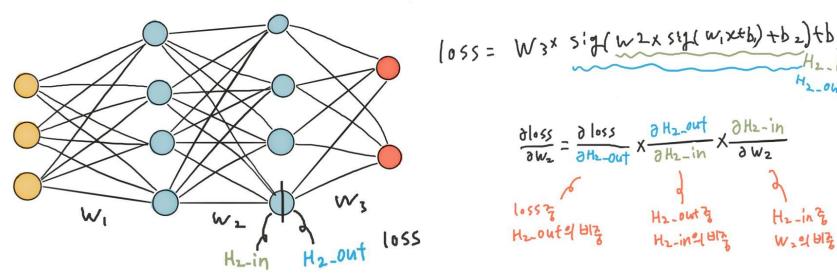
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Want:  $\frac{\partial f}{\partial x}$ ,  $\frac{\partial f}{\partial y}$ ,  $\frac{\partial f}{\partial z}$ 

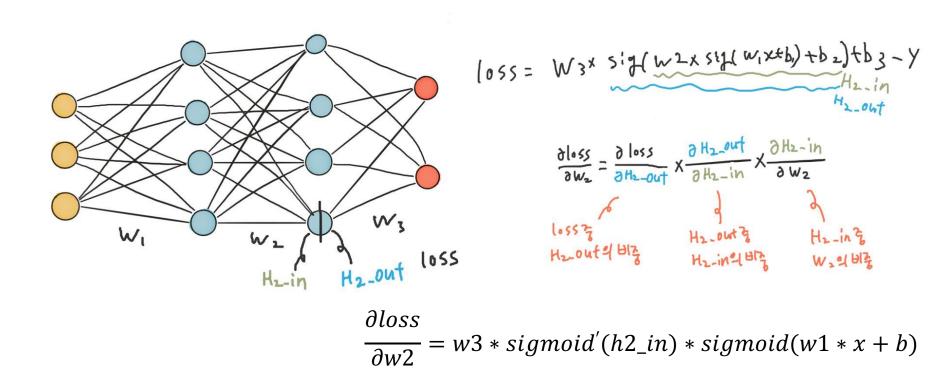




$$| 055 = W_3 \times \frac{5!9(w_1 \times 4b) + b_2}{h_2 - in} \times \frac{\partial H_2 - in}{\partial W_2} = \frac{\partial \log 5}{\partial H_2 - out} \times \frac{\partial H_2 - in}{\partial H_2 - in} \times \frac{\partial H_2 - in}{\partial W_2}$$

$$| 055 = W_3 \times \frac{5!9(w_1 \times 4b) + b_2}{h_2 - out} \times \frac{\partial H_2 - in}{\partial W_2} \times \frac{\partial H_2 - in}{\partial W_2}$$

$$| 055 = W_3 \times \frac{5!9(w_1 \times 4b) + b_2}{\partial W_2 - out} \times \frac{\partial H_2 - in}{\partial W_2} \times \frac$$

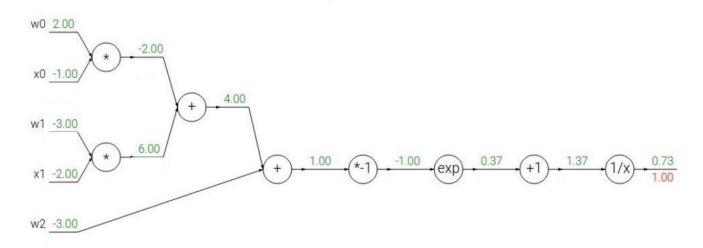


(참고) sigmoid 함수의 미분

$$\sigma(x)' = \frac{\delta\{1 + e^{-x}\}^{-1}}{\delta x} = -(1 + e^{-x})^{-2} - e^{-x} = \frac{e^{-x}}{(1 + e^{-x})^2}$$

$$\sigma(x)(1 - \sigma(x)) = \frac{1}{1 + e^{-x}}(1 - \frac{1}{1 + e^{-x}}) = \frac{1}{1 + e^{-x}}(\frac{e^{-x}}{1 + e^{-x}}) = \frac{e^{-x}}{(1 + e^{-x})^2}$$

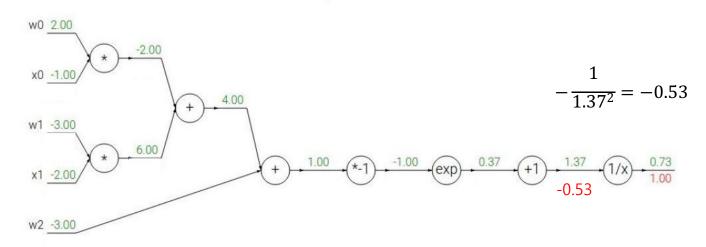
$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$



$$f(x) = e^x \hspace{1cm} o \hspace{1cm} rac{df}{dx} = e^x \ f_a(x) = ax \hspace{1cm} o \hspace{1cm} rac{df}{dx} = e^x \$$

$$f(x)=rac{1}{x} \qquad \qquad 
ightarrow \qquad rac{df}{dx}=-1/x \ f_c(x)=c+x \qquad \qquad 
ightarrow \qquad rac{df}{dx}=1$$

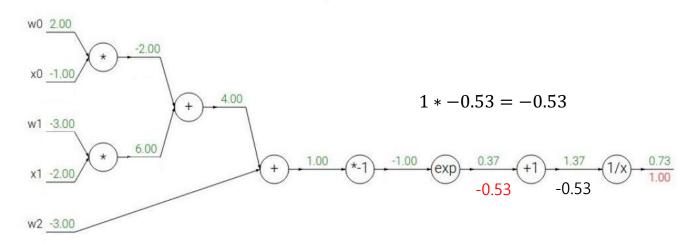
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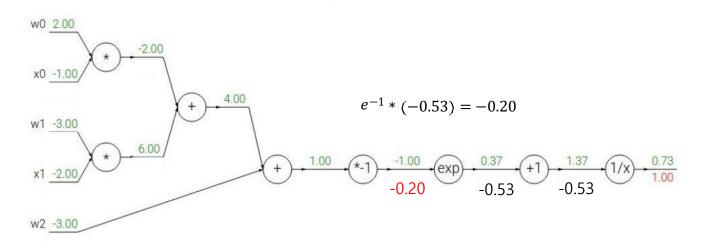
$$f(w,x) = rac{1}{1 + e^{-(w_0 x_0 + w_1 x_1 + w_2)}}$$



$$egin{aligned} f(x) = e^x & 
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$$f(x)=rac{1}{x} \qquad \qquad o \qquad rac{df}{dx}=-1/x \ f_c(x)=c+x \qquad \qquad o \qquad rac{df}{dx}=1$$

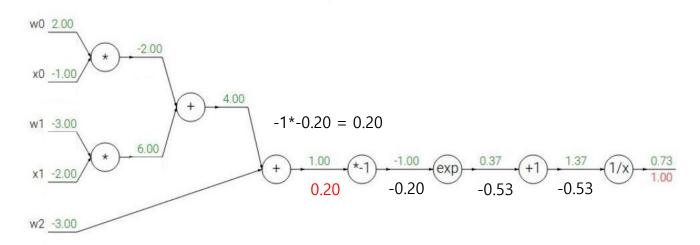
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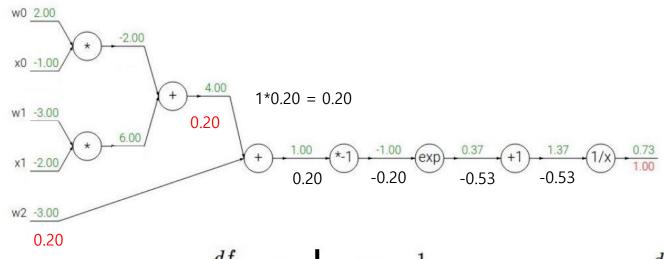
$$f(w,x) = rac{1}{1 + e^{-(w_0 x_0 + w_1 x_1 + w_2)}}$$



$$egin{aligned} f(x) = e^x & 
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$$f(w,x) = rac{1}{1 + e^{-(w_0 x_0 + w_1 x_1 + w_2)}}$$



$$f(x) = e^x$$
  $\rightarrow$ 

$$f_a(x)=ax$$
  $ightarrow$ 

$$\frac{df}{dx} = e^x$$

$$\frac{df}{dx} = a$$

$$f(x) = \frac{1}{2}$$

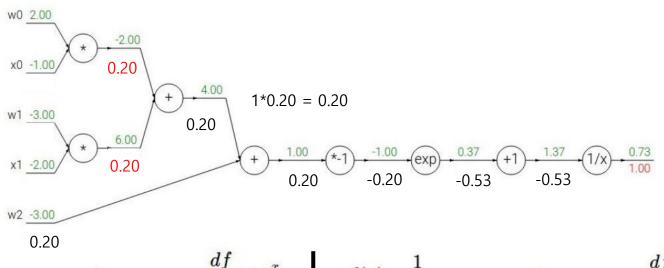
$$f_c(x) = c + 3$$

$$\rightarrow$$

$$\frac{df}{dx} = -1/x$$

$$rac{df}{dx} = 1$$

$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$



$$f(x) = e^x$$
  $\rightarrow$ 

$$f_a(x) = ax$$
  $o$ 

$$\frac{df}{dx} = e^x$$

$$\frac{df}{dx} = a$$

$$f(x) = rac{1}{x}$$

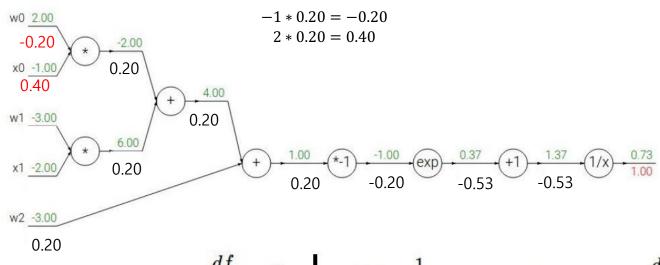
$$f_c(x) = c + s$$

$$\rightarrow$$

$$\frac{df}{dx} = -1/x$$

$$\frac{df}{dr} =$$

$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$



$$f(x) = e^x$$
  $\rightarrow$ 

$$f_a(x) = ax$$
  $ightarrow$ 

$$\frac{df}{dx} = e^x$$

$$\frac{df}{dx} = a$$

$$f(x) = \frac{1}{x}$$

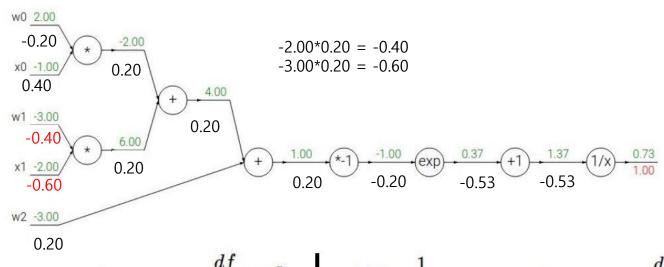
$$f_c(x) = c + a$$

$$\frac{\alpha}{\alpha}$$

$$\frac{df}{df} =$$

(출처: cs231n\_lecture4 p.31)

$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$



$$f(x) = e^x$$
  $\rightarrow$ 

$$f_a(x) = ax$$
  $ightarrow$ 

$$\frac{df}{dx} = e^x$$

$$\frac{df}{dx} = a$$

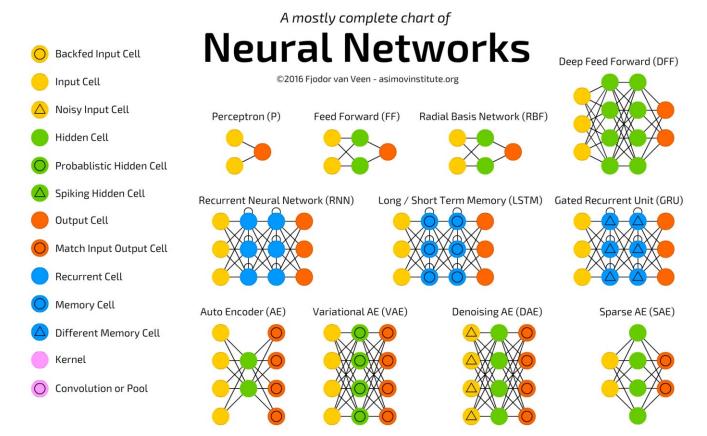
$$f(x) = \frac{1}{x}$$

$$f_c(x) = c + a$$

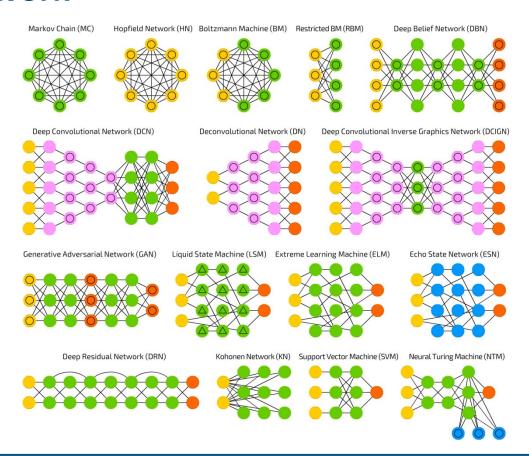
$$\frac{df}{dx} = -1/3$$

$$\frac{df}{dx} =$$

#### **Neural Network**



#### **Neural Network**



```
test.py
    import numpy as np
 2 import torch
 3 import torch.nn as nn
 4 import torch.optim as optim
 5 import torch.nn.init as init
 6 from torch.autograd import Variable
 7 from visdom import Visdom
   viz = Visdom()
    num data = 1000
11
    num epoch = 5000
12
    x = init.uniform(torch.Tensor(num_data,1),-15,15)
    y = 8*(x**2) + 7*x + 3
15
    noise = init.normal(torch.FloatTensor(num data,1),std=1)
    y noise = y + noise
```

```
필요한 라이브러리
```

```
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    import torch.optim as optim
    import torch.nn.init as init
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필요한 라이브러리
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                                 x = init.uniform(torch.Tensor(num_data,1),-15,15)
   데이터 생성
                             14
                                 y = 8*(x**2) + 7*x + 3
                             15
                                 noise = init.normal(torch.FloatTensor(num data,1),std=1)
                             16
                                 y noise = y + noise
```

```
model = nn.Sequential(
22
            nn.Linear(1,10),
            nn.ReLU(),
23
            nn.Linear(10,6),
            nn.ReLU(),
            nn.Linear(6,1),
26
        ).cuda()
    loss func = nn.L1Loss()
    optimizer = optim.SGD(model.parameters(), Lr=0.001)
31
    loss arr =[]
    label = Variable(y_noise.cuda())
    for i in range(num_epoch):
        output = model(Variable(x.cuda()))
        optimizer.zero_grad()
38
        loss = loss_func(output,label)
39
        loss.backward()
        optimizer.step()
        if i % 100 ==0:
            print(loss)
        loss_arr.append(loss.cpu().data.numpy()[0])
44
    param_list = list(model.parameters())
    print(param_list)
```

Neural Network 모델 생성

loss function 및 gradient descent optimizer 생성

```
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Neural Network 모델 생성

loss function 및 gradient descent optimizer 생성

<training 단계>

- 1. 모델로 결과값 추정
- 2. loss 및 gradient 계산
- 3. 모델 업데이트

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Neural Network 모델 생성

loss function 및 gradient descent optimizer 생성

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- 2. loss 및 gradient 계산
- 3. 모델 업데이트

training 이후 파라미터 값 확인

```
model = nn.Sequential(
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# Q&A