Advanced Topics in Computer Graphics I - Sheet R03

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Assignment 2

Reflection Equation

Radiance of Sun: $L_s = 20.045 \frac{MW}{m^2 \cdot sr}$

Irradiance of table:

Solid Angle Sun:

$$\Omega = \pi \cdot \frac{r_s^2}{d_s^2}$$
$$= 6.81 \cdot 10^{-5} sr$$

Where r_s is the radius of the sun and d_s is the distance to the sun.

$$E_T = \int_{\Omega} L_{\theta} \cdot \cos(\theta) \cdot d\omega$$

$$= L_s \cdot \cos(45^{\circ}) \cdot \int_{\Omega} d\omega$$

$$= 20.045 \cdot 10^6 \frac{W}{m^2 \cdot sr} \cdot \cos(45^{\circ}) \cdot 6.81 \cdot 10^{-5} sr$$

$$= 965.246 \frac{W}{m^2}$$

Radiance of table:

$$\begin{split} L_T &= L_e + f_{BRDF} \cdot E_T \\ &= 0 + \frac{0.5}{\pi} \cdot E_T \\ &= \frac{0.5}{\pi} \cdot 965.246 \frac{W}{m^2} \\ &= 153.624 \frac{W}{m^2 \cdot sr} \end{split}$$

Irradiance of Lens:

Solid Angle Table:

$$\begin{split} \Omega &= 4 \cdot \arctan\left(\frac{l^2}{2d \cdot \sqrt{4d^2 + 2l^2}}\right) \\ &= 4 \cdot \arctan\left(\frac{(0.8m)^2}{2 \cdot 1.2m \cdot \sqrt{4 \cdot (1.2m)^2 + 2 \cdot (0.8m)^2}}\right)) \\ &= 0.401 sr \end{split}$$

$$\begin{split} E_L &= \int_{\Omega} L_{\theta} \cdot \cos(\theta) \cdot d\omega \\ &= L_T \cdot \cos(45^{\circ}) \cdot \int_{\Omega} d\omega \\ &= 153.624 \frac{W}{m^2 \cdot sr} \cdot \cos(0\circ) \cdot 0.401 sr \\ &= 61.552 \frac{W}{m^2} \end{split}$$

Radiant Power of Lens:

$$A = \pi \cdot r^2$$
$$= \pi \cdot (0.025m)^2$$
$$= 0.0019635m^2$$

$$\begin{split} P_L &= E_L \cdot A \\ &= 61.552 \frac{W}{m^2} \cdot 0.0019635 m^2 \\ &= 0.121 W \end{split}$$