

# COMP4107 - Assignment 2

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1. a) The graphs and tables below can be reproduced by running the relevant q1\*.py file.

The 10x10 grid described in the assignment was created and the order randomized. The actual values  $z = f(x,y)$  were computed and stored in a matrix representing  $[x, y, z]$  for all 100 training items. After training on the 10x10 grid for 50,000 epochs, error predicting  $z$  values from the test data (the 9x9 grid) was very low for both 8 neurons and 50 neurons. Note that using 2 neurons shows to be insufficient to approximate the function in both dimensions.

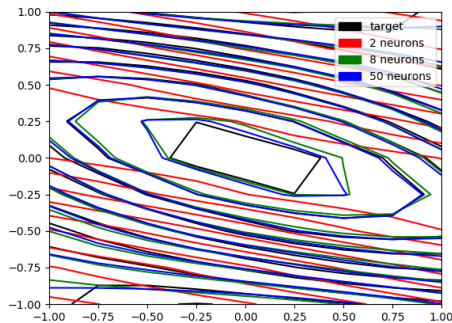


Figure 1: Function Contours

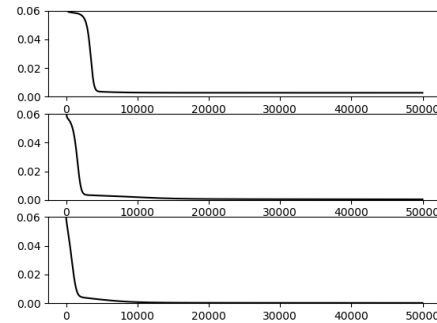


Figure 2: Cost (MSE) at epoch

Using 8 neurons for the hidden layer is appropriate for this function. The MSE for the test data with 8 neurons is better than that required, and the training converges after fewer epochs than the network using 50 neurons for the hidden layer.

The table below corresponds to the experiment shown in the graph above.

MSE with LR = 0.1 and 50000 epochs:
2 neurons: 0.0028752042643646267

8 neurons:	0.0004576152783257549
50 neurons:	0.0002225187166484513

b) With a tolerance of 0.02 for MSE of the training data, the appropriate number of epochs for convergence varies by training method. For traingrms (RMSPropOptimizer), having a maximum of 100 training epochs is appropriate. The other methods converge much more slowly, as seen in Figure 3.

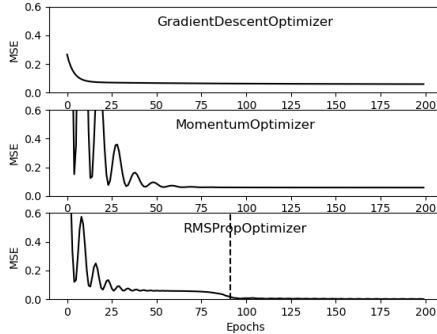


Figure 3: Optimizers

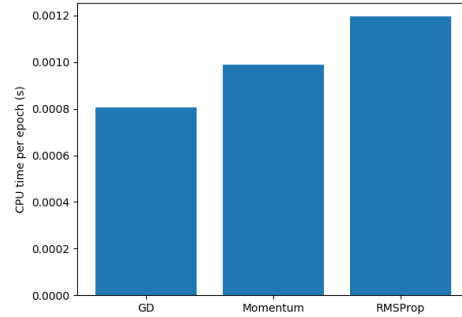


Figure 4: CPU time vs optimizer

The reduced number of required training epochs for RMSPropOptimizer (seen in the table below) more than compensates for the increased CPU time for each epoch, seen in Figure 4.

```
Test MSE with LR = 0.02 and 100 epochs:
0.061681683118449925 (GradientDescentOptimizer)
0.058683357733909404 (MomentumOptimizer)
0.005489751198996285 (RMSPropOptimizer) <- BEST

Test MSE with LR = 0.02 and 200 epochs (as shown in Figure 3):
0.060366321060214334 (GradientDescentOptimizer)
0.059178147674373405 (MomentumOptimizer)
0.000918757108116926 (RMSPropOptimizer) <- BEST

Test MSE with LR = 0.02 (Stopping when the training error < 0.02):
0.020440891382299493 (GradientDescentOptimizer - Goal reached after 9623 epochs)
0.020200175134976295 (MomentumOptimizer - Goal reached after 918 epochs)
0.011620827855204354 (RMSPropOptimizer - Goal reached after 109 epochs) <- BEST
```

c) We can further show that 8 neurons is a good choice by noting that early stopping has no effect. Our experiments have not been able to demonstrate an overtraining phenomenon with even 50 hidden neurons, but a premature early stop can be seen in Figure 6, and the table below.

Test MSE with LR = 0.02, 50 neurons:	
0.001858	at 10000 epochs
0.019969	at goal reached (2031 epochs)

0.075565 at early stop (399 epochs)

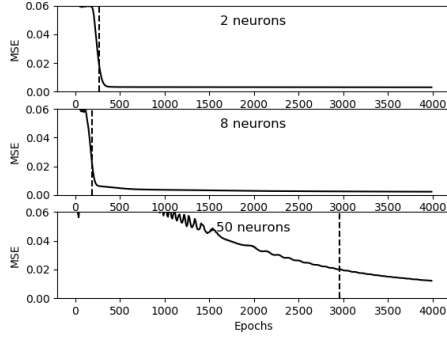


Figure 5: Slow convergence

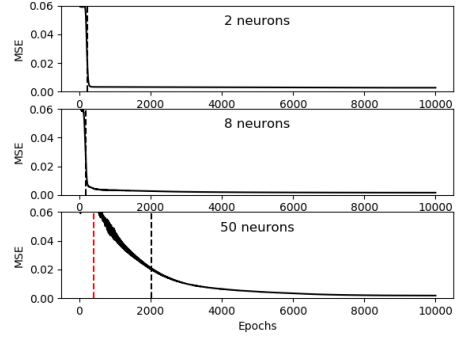


Figure 6: Premature early stop

The network with 50 hidden neurons also is very slow to converge to the target MSE - even using the RMSPropOptimizer - compared to when using 8 hidden neurons (Figure 5).

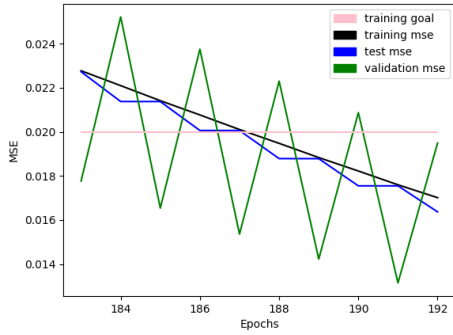


Figure 7: Optimizers

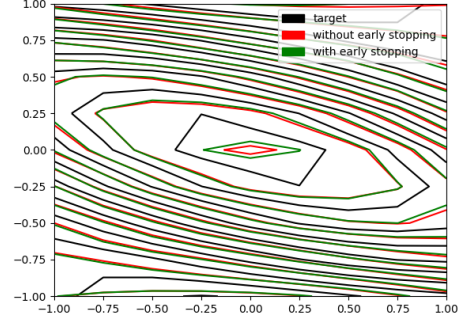


Figure 8: Early stopping not triggered

Figure 7 shows the MSE at each epoch near where the training goal is reached. This captures the expected trend - that the training error will decrease consistently, while the test error (9x9 grid) has more variation. The validation data is most different from the training data (as it is randomly sampled from the function), so it is expected that its error would also have the highest variance.

Figure 8 shows that having an early stopping mechanism for this function makes no difference, as the early stopping mechanism is never triggered (8 hidden neurons, 4000 epochs, 0.02 LR). Thus, the two contours are virtually identical, differing only by the stochastic elements of the experiments (initial weights, order of training data).

## 2. Question 2

Instructions on how to run this file:

To run this file, if you simply run by 'python3 q2.py' without changing anything, then it will run all these three parts, which may take a while as in our code, we modified so that it runs 10 experiments for each number of hidden neurons, and after one is finished, then a new NN is created to run the second one, etc. Therefore, it will take about 1 min for it to finish and plot the graphs. If you want to run parts only, then comment out the corresponding line in the experiment function.

- (a) We did the experiment with 5, 10, 15, 20, 25 hidden neurons and we are able to produce the following result by running each experiment 10 times and take the average of all the accuracies. In the following graph, the lines are coloured using red, blue, green, black, purple, each corresponds to a number of hidden neurons. The line in red is the line for using 5 as number of hidden neurons, etc.

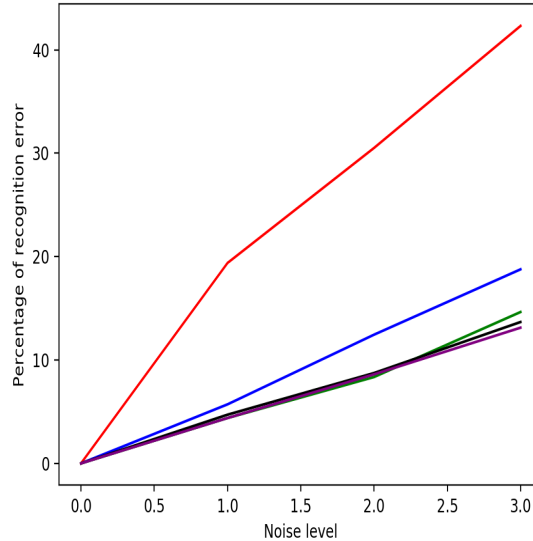


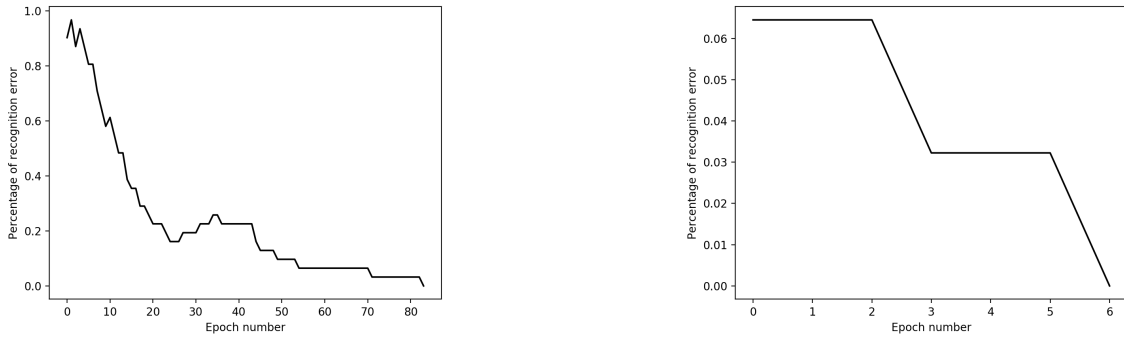
Figure 9: Percentage of Recognition Errors

```
Number of hidden neuron: 5 , error rate: [0.0, 20.967741935483865, 32.54838709677418, 42.32258064516129]
Number of hidden neuron: 10 , error rate: [0.0, 6.225806451612903, 11.419354838709705, 18.06451612903226]
Number of hidden neuron: 15 , error rate: [0.0, 4.129032258064513, 7.41935483870968, 13.774193548387114]
Number of hidden neuron: 20 , error rate: [0.0, 5.903225806451607, 10.41935483870967, 16.548387096774185]
Number of hidden neuron: 25 , error rate: [0.0, 4.935483870967749, 9.129032258064507, 14.225806451612899]
```

Figure 10: Error rate for different number of hidden neurons

- (b) 15 is chosen as the number of hidden neurons, since 15 is more accurate compared with 10, but using more neurons don't really make a big difference. When we used 15 neurons in the hidden layer, the number of epochs is less than the number of epochs in

the question, which we think is fine. So here is the graph,



- (c) With 15 hidden neurons, we are able to produce the following graph. The blue dashed line is trained without noisy data, and the red line is trained with noisy data.

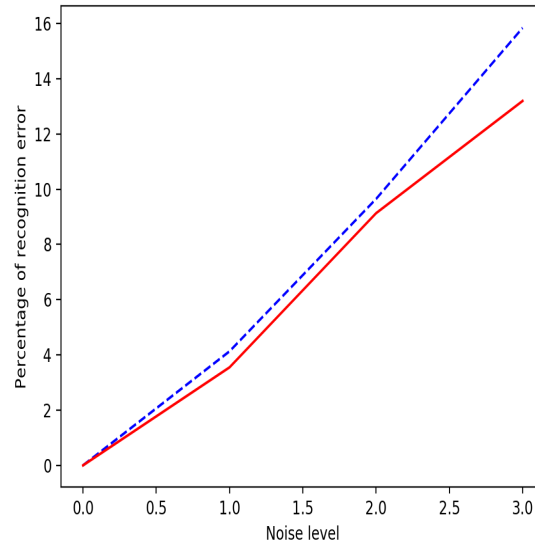


Figure 11: Percentage of Recognition Errors