Math 210 Midterm 1

Name: Answer Key

This is the midterm for unit 1.

Carefully read each question and understand what is being asked before you start to solve the problem. Please show your work in an orderly fashion, and circle or mark in some way your final answers.

No calculators nor other electronic devices are allowed.

1. (5 points) What is the derivative of $q(x) = e^{x/7}$ What is q'(-1)?

2. (5 points) Differentiate $y(t) = t^9 - 6t^7 - t^3 + t^2 + 17t - 400$.

3. (10 points) Consider the function

$$f(x) = \frac{4\sqrt{x+2}-8}{x-2}$$

Compute the following limits:

$$\lim_{x\to 2} f(x) = \frac{O}{O}$$

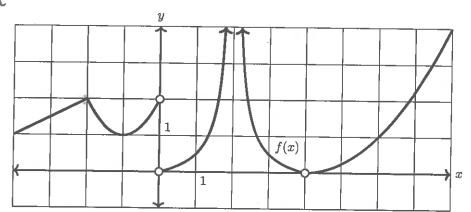
$$\lim_{x \to \infty} f(x)$$

$$= \lim_{x \to \infty} 4 \sqrt{x}$$



3pts Conjugate
2pts algebra

4. (20 points) The function f(x) with domain a subset of [-4, 8] is given by the below graph.



Determine each of these limits, writing "DNE" if the limit doesn't exist:

$$\lim_{x\to 0^-}f(x)=$$

$$\lim_{x\to 0^+}f(x)=$$

$$\lim_{x\to 0}f(x)=\bigcirc\bigcirc\bigcirc\bigcirc\bigcirc$$

$$\lim_{x\to 2} f(x) = \bigcirc$$

$$\lim_{x \to 4} f(x) =$$

$$\lim_{x\to 6}f(x)=\underbrace{1}$$

Identify each discontinuity and f(x) and classify it.

X-0 Jump

x=Z Infinite

×=4 Removable

Identify everywhere that f(x) is continuous but not differentiable.

at x==2 is a corner

HS Note: Natural language 15 always somewhat ambigues. It you had a different supportation by your reasoning was correct for that interprelation. I went with it.

5. (10 points) You bike along a hilly route, going both uphill and downhill. Must there be a moment when your instancous change in elevation is 0 feet per minute? Explain why or why not.

Yes. Your change in elevation is continued, you so by the memoriale value theorem you must lit the manufale value of.

While you are biking a bird is flying. At the start of your bike ride the ground directly beneath the bird has a height of 2800 feet. When you finish I hour later the ground beneath the bird has a height of 2600 feet. Can you conclude that at some point during your trip the ground beneath the bird had a height of 2700 feet? Explain why or why not.

Lifthak Ivi latasem mil No, because that need not be continuous.

There is a jump

2500 disront multy at the cliff.

6. (10 points) Consider $a(x) = \ln(x^2 + 9)$. Find a'(x) and a''(x).

$$\alpha''(x) = \frac{2(x^2+9)-2x^2x}{(x^2+9)^2} = \frac{18-4x}{(9+x^2)^2}$$

7. (10 points) Consider the piecewise-defined function

$$p(x) = \begin{cases} 4x - 3 & \text{if } x \leq 1 \\ 2x^2 & \text{if } x > 1 \end{cases}$$

Find all discontinuities of p(x) and classify them. Write a sentence or two to explain the classification, or if there are none to explain why.

Non at x=1:

(m pa)= 4.1-3=1

lim p60=7.1=2

Jump Discont musty at X=1
because the one-sided limits

are different.

8. (5 points) Differentiate $x^e \sin x - e^{-x} \tan x$.

E () = e. x - 1. smx * 1 + x cosx - (-e* tanx + e* sec x) = ex sonx + x cosx + e + fanx m e x sec x

9. (5 points) Differentiate $\arctan(\sqrt{x})$.

12. Extra Credit (Up to +10) Consider the function

$$C(x) = \begin{cases} x & \text{if } x \text{ is rational} \\ 0 & \text{if } x \text{ is irrational} \end{cases}$$

Determine the taputs where C(x) is continuous, and write a short explanation for why it's continuous

only at x=0: ((a) =0 I'm (CX) = 0 became the artests for both vationals x00 f renternals both >0 = ((0)

At x +0, the Imstr for rationals tivrationals and disserved: rational, >x so limst does

Consider next the function

 $D(x) = \begin{cases} 1/q & \text{if } x = p/q \text{ is rational, where } p \text{ and } q \text{ are integers with no common factors} \\ 0 & \text{if } x \text{ is irrational} \end{cases}$

Determine the inputs where D(x) is continuous, and write a short explanation for why it's continuous

only if x is irrational For irratoonals the land is always O.

For raturnals: if x is national, the limbt is &

But C# = so the multing mps DNE.

if x 15 irrational, the limit - Frationals -> 150

becase the denominators - 700 to approach a referred value and =>0.

5. the limit Frall mosts is 0= ((x).

D (x)