

MATH 321: 9-1 GROUPWORK

- (1) Consider the following two English sentences. Translate each into a formula of propositional logic, then construct truth tables for them.
- If you don't eat your meat, you can't have any pudding.
 - A necessary and sufficient for me to not be cranky and to do well in math class is for me to get my coffee in the morning.
- (2) Consider the following two formulae.

$$b \rightarrow (a \vee \neg a) \quad \text{and} \quad c \rightarrow (b \rightarrow (a \vee \neg a))$$

Construct truth tables for these formulae to verify that they are tautologies. Further consider the formula

$$d \rightarrow (c \rightarrow (b \rightarrow (a \vee \neg a))).$$

Can you explain why this is a tautology without filling out the 16 line truth table? What about

$$e \rightarrow (d \rightarrow (c \rightarrow (b \rightarrow (a \vee \neg a))))?$$

And you can keep going in the obvious manner. Can you give a general explanation for why they are all tautologies?

- (3) Suppose you have two propositional formulae φ and ψ , using the same variables. Explain why φ and ψ are equivalent if and only if $(\varphi) \leftrightarrow (\psi)$ is a tautology.