

**MATH454 HOMEWORK 2**  
**DUE THURSDAY, SEPTEMBER 12**

*Exercise 1.* Do Exercise 2.4 from the textbook.

*Exercise 2.* Do Exercise 2.6 from the textbook.

*Exercise 3.* Do Exercise 2.9 from the textbook.

*Exercise 4.* Do Exercise 2.10 from the textbook.

*Exercise 5 (Reach).* Do Exercise 2.13 from the textbook. (See pages 18–19 for the necessary definitions.)

*Exercise 6.* Do Exercise 3.1 from the textbook.

Let  $R$  be a binary relation on a set  $A$ . Say that  $R$  is *well-founded* if for any nonempty  $X \subseteq A$  there is  $x \in X$  so that there is no  $y \in X$  so that  $y R x$ .

*Exercise 7.* Prove that a (strict) total order  $(L, <)$  is a well-order if and only if  $<$  is well-founded.

*Exercise 8.* Give two different examples of well-founded relations which are not total orders. (Drawing a picture is a perfectly acceptable way to give an example.)

*Exercise 9.* Let  $A$  be a set and let  $E$  be the relation on  $A$  defined as: for  $x, y \in A$ ,  $(x, y) \in E$  if  $x \in y$ . Show that  $E$  is well-founded. (Hint: use the Foundation axiom.)