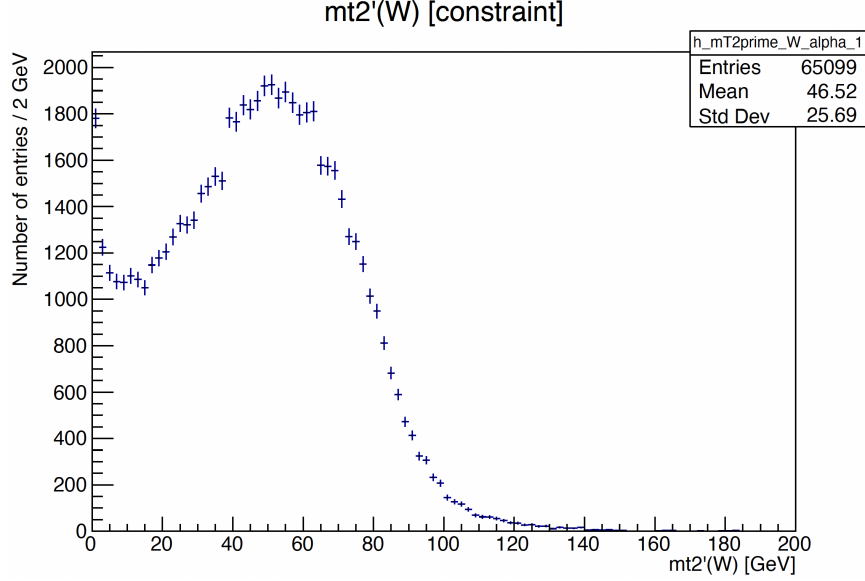


# DOCUMENTING THE MEANING OF THE PARAMETERS



## 1. SIMPLE FIT: $f_4(x) = a \arctan(k(x - h)) + C$

### 1. $h$ :

- $h$  governs the horizontal translation of the graph.
- Here, wishing the drop of arctan to be *anti-symmetric* at 80 GeV,  $h \sim 80$  GeV.

### 2. $C$ :

- When  $x \sim 80$ ,  $f_4(80) \sim C$ . Accordingly,  $C$  determines the vertical translation of the graph and, in particular, the value which  $f_4$  assumes at 80 GeV.
- Here,  $C \sim 800$ .

### 3. $a$ :

- $a$  governs the vertical stretch or compression of the graph as well as its reflection across the  $x$ -axis. Its value is dependent upon  $k$  and the number of entries of the histogram.
- Here, the basic shape is not arctan, but rather  $-\arctan$ , rendering  $a < 0$ .

### 4. $k$ :

- $k$  governs the horizontal stretch or compression of the graph. Its value is dependent upon  $a$  and the number of entries in the histogram.
- Here, as arctan is stretched, so that its great drop extends from 60 to 120 GeV, one should expect  $k < 1$ . In particular, as  $f_4$  diminishes from  $\sim 1700$  to  $\sim 50$  in the interval  $[60, 120]$ , then one good initial guess might be  $(a, k) \simeq (-800, 0.1)$ .
- We can further quantify the interdependency of  $a, k$  by observing that, for  $x$  close to  $h$ ,  $f_4(x) \sim a * k(x - 80) + 800$ . This forms a straight line, whose slope is equal to  $a * k$ . In approximating the slope of this line as  $\frac{1700-50}{120-60} \sim -30$ , which the pair  $(-800, 0.1)$  satisfies to the order of magnitude.

## 2. MORE COMPLEX FIT: $f_0(x) = (P_3 + P_4x) \arctan((x - P_1)/P_2) + C$

### 1. $P_1$ :

- $P_1$  governs the horizontal translation of the graph.

- Here, wishing the drop of arctan to be *anti-symmetric* at 80 GeV,  $P_1 \sim 80$  GeV.
2.  $P_2$ :
- $P_2 \sim 1/k$  governs the horizontal stretch or compression of the graph.
  - Here,  $P_2 \sim 1/0.1 = 10$ .
3.  $P_4$ :
- For large  $|x|$ ,  $\arctan \rightarrow \pm\pi/2$ , so  $f_1(x) \rightsquigarrow \{(P_3 + C) + P_4x\}$ . Accordingly,  $P_4$  governs the slope of the line which  $f_4$  approaches for large  $x$ .
  - Here, wishing for the slopes to be flat upon either end,  $P_4 \sim 0$ .
4.  $P_3$ :
- If  $P_4 \sim 0$ , then the equation reduces to  $f_4$ , where  $P_3 \sim a$  governs the vertical stretch of the graph.
  - Here,  $P_3 \sim -800$ .
5.  $C$ :
- When  $x \sim 80$ ,  $f_4(80) \sim C$ , as discussed above.
  - Here,  $C \sim 800$ .
3. EVEN MORE COMPLEX FIT:  $f_0(x) = (P_3 + P_4x) \arctan((x - P_1)/P_2) + P_5x + 1$
1.  $P_5$ :
- For large  $x$ ,  $f_0 \rightsquigarrow (P_3 + 1) + (P_4 + P_5)x$ .
  - Ideally, for flat tails,  $P_5 \sim 0$ . But, if that is so, then  $f_0$  should not attain its desired value when  $x = 80$ . Instead,  $P_5(80) + 1 \sim 800 \rightarrow P_5 \sim 10$ .
  - Accordingly, this might imply that  $P_4 \sim -10$ , in order that the slopes might ‘cancel out’ for large  $x$ .
2. All other relevant parameters may retain their values, given in 2.
4. ALTERNATIVE SIMPLER FIT #1:  $f_2(x) = (P_3 + P_4x) \frac{x - P_1}{\sqrt{P_2 + (x - P_1)^2}} + C$ .
1.  $P_1$ :
- $P_1$  governs the horizontal translation of the graph.
  - Here,  $P_1 \sim 80$ .
2.  $C$ :
- Again,  $C \sim 800$ , as discussed above.
3.  $P_4$ :
- For large  $x$ ,  $f_1(x) \rightsquigarrow \{(P_3 + C) + P_4x\}$ .
  - Wishing for flat tails,  $P_4 \sim 0$ .
4.  $P_3$ :
- $P_3$  governs the vertical stretch of the graph.
  - Here,  $P_3 < 0$ . Further, when  $|x|$  becomes ‘far away’ from 80, say,  $x = 80$  (where the graph begins to level off), we know  $f_1(80) \sim 50$ . If  $f_1(80) \sim \{(P_3 + C) + 0(80)\}$  and  $C = 800$ , then  $P_3 \sim -800$ .
5.  $P_2$ :

- For no discontinuity at  $x = 80$ ,  $P_2 > 0$ .
- For  $x \sim 80$ ,  $P_3 \frac{x-P_1}{\sqrt{P_2+(x-P_1)^2}} \sim \frac{P_3}{\sqrt{P_2}}(x-P_1)$ . This forms a straight line approximation to the graph, whose slope is  $P_3/\sqrt{P_2}$ . In approximating the slope of this line as  $\sim -45$ , then  $-800/\sqrt{P_2} \sim -45$ , whence  $P_2 \sim 300$ .

5. ALTERNATIVE FIT #1:  $f_3(x) = (P_3 + P_4x) \frac{x-P_1}{\sqrt{P_2+(x-P_1)^2}} + P_5x + 1$ .

1.  $P_5$ :

- For large  $x$ ,  $f_3 \rightsquigarrow (P_3 + 1) + (P_4 + P_5)x$ .
- Ideally, for flat tails,  $P_5 \sim 0$ . But, if that is so, then  $f_3$  should not attain its desired value when  $x = 80$ . Instead,  $P_5(80) + 1 \sim 800 \rightarrow P_5 \sim 10$ .
- Accordingly, this might imply that  $P_4 \sim -10$ , in order that the slopes might ‘cancel out’ for large  $x$ .

2. All other relevant parameters may retain their values, given in 4.