ENV 790.30 - Time Series Analysis for Energy Data | Spring 2024 Assignment 5 - Due date 02/19/24

Julia

Directions

You should open the .rmd file corresponding to this assignment on RStudio. The file is available on our class repository on Github. And to do so you will need to fork our repository and link it to your RStudio.

Once you have the file open on your local machine the first thing you will do is rename the file such that it includes your first and last name (e.g., "LuanaLima_TSA_A05_Sp23.Rmd"). Then change "Student Name" on line 4 with your name.

Then you will start working through the assignment by **creating code and output** that answer each question. Be sure to use this assignment document. Your report should contain the answer to each question and any plots/tables you obtained (when applicable).

When you have completed the assignment, **Knit** the text and code into a single PDF file. Submit this pdf using Sakai.

R packages needed for this assignment: "readxl", "ggplot2", "forecast", "tseries", and "Kendall". Install these packages, if you haven't done yet. Do not forget to load them before running your script, since they are NOT default packages.\

```
#Load/install required package here
library(forecast)
## Registered S3 method overwritten by 'quantmod':
##
    method
    as.zoo.data.frame zoo
library(readxl)
library(stats)
library(tseries)
library(ggplot2)
library(Kendall)
library(lubridate)
##
## Attaching package: 'lubridate'
## The following objects are masked from 'package:base':
##
       date, intersect, setdiff, union
library(tidyverse)
## -- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
## v dplyr 1.1.3
                      v stringr 1.5.0
## v forcats 1.0.0
                      v tibble 3.2.1
## v purrr
           1.0.2
                      v tidyr
                                1.3.0
```

Decomposing Time Series

stamp

Consider the same data you used for A04 from the spreadsheet "Table_10.1_Renewable_Energy_Production_and_Consumption The data comes from the US Energy Information and Administration and corresponds to the December 2023 Monthly Energy Review.

Q1

##

For this assignment you will work only with the following columns: Solar Energy Consumption and Wind Energy Consumption. Create a data frame structure with these two time series only and the Date column. Drop the rows with *Not Available* and convert the columns to numeric. You can use filtering to eliminate the initial rows or convert to numeric and then use the drop_na() function. If you are familiar with pipes for data wrangling, try using it!

Chat GPT prompt for ymd(): how to use my() function for date conversions

```
typeof(energy_data$Month)

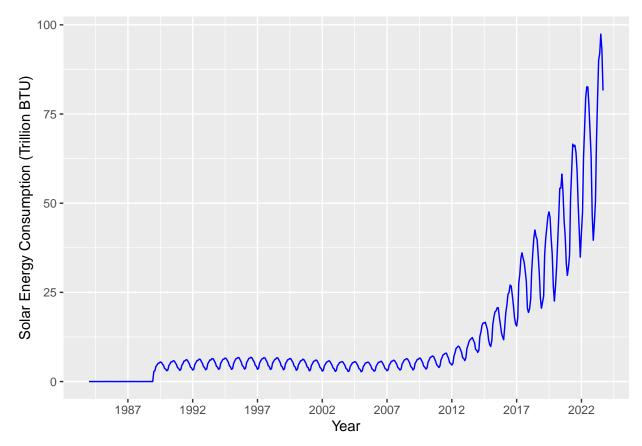
## [1] "double"

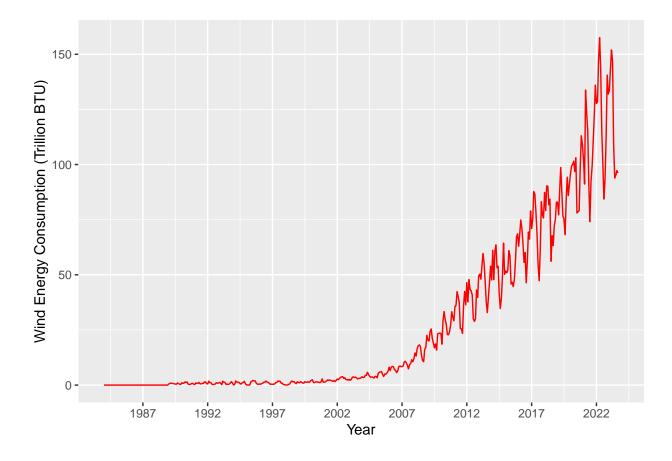
nobs=nrow(energy_data)
nvar=ncol(energy_data)
```

```
energyTS <- ts(energy_data)</pre>
```

$\mathbf{Q2}$

Plot the Solar and Wind energy consumption over time using ggplot. Plot each series on a separate graph. No need to add legend. Add informative names to the y axis using ylab(). Explore the function scale_x_date() on ggplot and see if you can change the x axis to improve your plot. Hint: use scale_x_date(date_breaks = "5 years", date_labels = "%Y")")

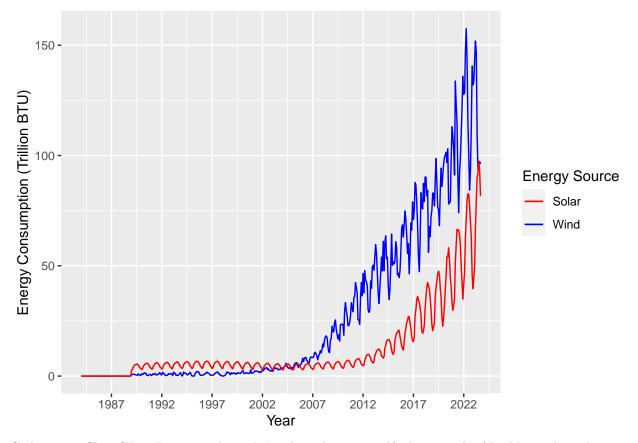




$\mathbf{Q3}$

Now plot both series in the same graph, also using ggplot(). Use function <code>scale_color_manual()</code> to manually add a legend to ggplot. Make the solar energy consumption red and wind energy consumption blue. Add informative name to the y axis using <code>ylab("Energy Consumption)</code>. And use function <code>scale_x_date()</code> to set x axis breaks every 5 years.

```
energy_data |>
    ggplot(aes(x = Month, color = factor("Wind"), y = `Wind Energy Consumption`)) +
    geom_line() +
    geom_line(aes(x = Month, color = factor("Solar"), y = `Solar Energy Consumption`)) +
    scale_x_date(date_breaks = "5 years", date_labels = "%Y") +
    ylab("Energy Consumption (Trillion BTU)") +
    xlab("Year") +
    scale_color_manual(name = "Energy Source", values = c("Wind" = "blue", "Solar" = "red"))
```

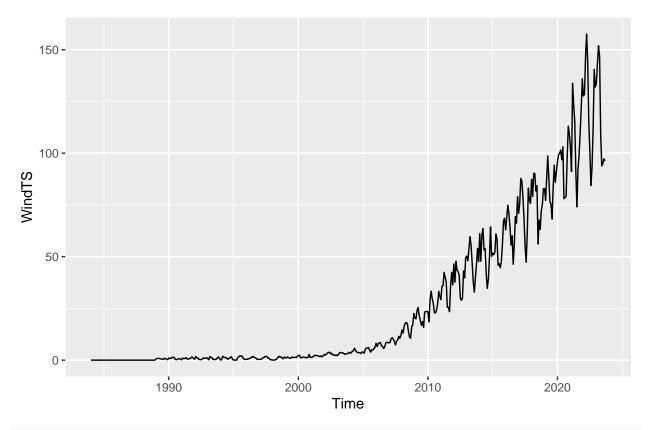


Code inspo: Chat GPT. Prompt: why isn't "scale_color_manual(values = colors)" adding a legend

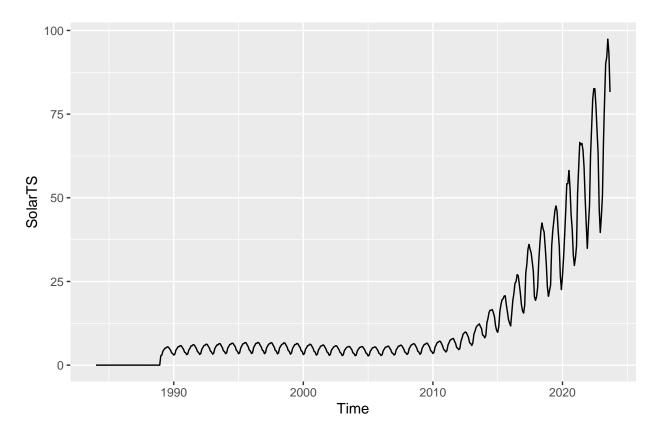
Decomposing the time series

The stats package has a function called decompose(). This function only take time series object. As the name says the decompose function will decompose your time series into three components: trend, seasonal and random. This is similar to what we did in the previous script, but in a more automated way. The random component is the time series without seasonal and trend component.

```
WindTS <- ts(energy_data$`Wind Energy Consumption`, start = c(1984,1), frequency = 12)
SolarTS <- ts(energy_data$`Solar Energy Consumption`, start = c(1984,1), frequency = 12)
autoplot(WindTS)</pre>
```



autoplot(SolarTS)



Additional info on decompose().

- 1) You have two options: alternative and multiplicative. Multiplicative models exhibit a change in frequency over time.
- 2) The trend is not a straight line because it uses a moving average method to detect trend.
- 3) The seasonal component of the time series is found by subtracting the trend component from the original data then grouping the results by month and averaging them.
- 4) The random component, also referred to as the noise component, is composed of all the leftover signal which is not explained by the combination of the trend and seasonal component.

$\mathbf{Q4}$

Transform wind and solar series into a time series object and apply the decompose function on them using the additive option, i.e., decompose(ts_data, type = "additive"). What can you say about the trend component? What about the random component? Does the random component look random? Or does it appear to still have some seasonality on it?

print(decompose(WindTS, type = "additive"))

##	\$x									
##		Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep
##	1984	0.000	0.001	0.001	0.002	0.003	0.002	0.002	0.001	0.002
##	1985	0.002	0.004	0.002	0.002	0.001	0.001	0.000	0.001	0.003
##	1986	0.001	0.001	0.002	0.002	0.003	0.002	0.002	0.002	0.000
##	1987	0.000	0.000	0.000	0.000	0.001	0.003	0.004	0.001	0.001
##	1988	0.002	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
##	1989	0.497	0.763	0.873	0.812	0.697	0.534	0.485	0.352	0.956
##	1990	1.028	0.789	0.837	1.434	1.195	1.387	0.406	0.239	0.311

```
## 1991
          0.212
                   0.989
                            0.707
                                     0.813
                                              1.237
                                                      0.530
                                                               0.530
                                                                        0.777
                                                                                 0.707
          0.512
                                     1.088
                                                      0.256
                                                                        0.480
                                                                                 1.088
## 1992
                   1.759
                            1.120
                                             0.320
                                                               0.256
                   0.169
                                                      0.295
                                                                        0.253
## 1993
          0.844
                            1.773
                                     1.266
                                              1.266
                                                               0.464
                                                                                0.464
## 1994
          0.000
                   0.343
                            1.865
                                     1.408
                                              1.256
                                                      1.256
                                                               0.647
                                                                        0.457
                                                                                 1.066
## 1995
          0.019
                   0.080
                            0.016
                                     0.023
                                              1.394
                                                      1.701
                                                               2.115
                                                                        1.862
                                                                                 1.955
## 1996
          0.503
                   0.382
                                     0.834
                                                      1.282
                                                               1.826
                                                                        1.416
                                                                                 1.199
                            0.640
                                              1.336
## 1997
          0.411
                   0.372
                            0.507
                                     1.106
                                                                        1.809
                                              1.196
                                                      1.764
                                                               1.738
                                                                                0.888
                   0.028
## 1998
          0.059
                            0.021
                                     0.293
                                             0.489
                                                      1.348
                                                               1.868
                                                                        1.438
                                                                                 1.623
## 1999
          1.150
                   1.054
                            1.524
                                     1.274
                                             0.940
                                                      0.866
                                                               1.556
                                                                        1.304
                                                                                 1.288
## 2000
          2.202
                   2.409
                            1.194
                                     1.126
                                              1.392
                                                      1.525
                                                               1.296
                                                                        1.284
                                                                                 1.134
## 2001
          1.328
                   1.471
                            1.816
                                     2.336
                                              2.167
                                                      2.285
                                                               2.167
                                                                        1.969
                                                                                 1.673
  2002
          2.769
                   2.436
                            2.907
                                     3.495
                                              3.677
                                                      3.843
                                                               3.038
                                                                        3.332
                                                                                 2.511
##
##
  2003
          2.158
                   2.543
                            3.535
                                     3.729
                                             3.434
                                                      3.573
                                                               3.253
                                                                        2.782
                                                                                3.054
## 2004
          3.410
                   3.486
                            4.406
                                             5.806
                                                      4.767
                                                                        3.585
                                     4.418
                                                               3.973
                                                                                3.718
                                                      6.131
## 2005
          3.861
                   3.298
                            5.325
                                     5.792
                                             5.959
                                                               4.848
                                                                        3.883
                                                                                5.010
## 2006
          8.130
                   6.558
                            8.048
                                     8.434
                                             8.389
                                                      7.001
                                                               6.671
                                                                        5.647
                                                                                 6.412
## 2007
          8.367
                   8.598
                           10.397
                                    10.822
                                            10.073
                                                      8.941
                                                                        9.210
                                                               7.364
                                                                                9.781
## 2008
         14.580
                  13.142
                           16.316
                                    17.829
                                            18.221
                                                     17.539
                                                              13.677
                                                                       11.138
                                                                               10.616
## 2009
         20.304
                  19.968
                           24.222
                                    25.446
                                                     19.105
                                                                       18.645
                                            21.366
                                                              16.906
                                                                               15.868
## 2010
         23.387
                  18.533
                           29.306
                                    33.316
                                            29.676
                                                     27.463
                                                              22.942
                                                                       22.812
                                                                               24.244
## 2011
         29.174
                  35.661
                           35.978
                                    42.383
                                            40.167
                                                     37.481
                                                              25.551
                                                                       25.500
                                                                               23.437
## 2012
         46.514
                  37.709
                           47.858
                                    43.364
                                            42.788
                                                     40.850
                                                              30.099
                                                                       28.896
                                                                               29.990
         50.288
                  48.026
                           53.758
                                    59.629
                                            55.406
                                                     46.909
                                                              37.851
                                                                       32.871
## 2013
                                                                               39.832
         61.113
                  47.798
                           60.515
                                    63.584
                                            53.232
                                                     53.906
                                                              41.583
                                                                       34.702
## 2014
                                                                               39.305
                                    60.963
## 2015
         51.733
                  50.912
                           52.231
                                            58.520
                                                     45.793
                                                              46.661
                                                                       44.629
                                                                               47.671
## 2016
         63.007
                  68.712
                           74.857
                                    70.967
                                            64.309
                                                     55.627
                                                              60.114
                                                                       46.367
                                                                               55.969
## 2017
         70.965
                  75.375
                           87.793
                                   86.590
                                            78.707
                                                     68.724
                                                              55.001
                                                                       47.355
                                                                               61.115
         87.343
                  79.123
                           90.294
                                                     84.286
## 2018
                                    90.182
                                            81.728
                                                              56.116
                                                                       67.716
                                                                               63.189
## 2019
         82.917
                  77.189
                           87.936
                                   98.659
                                            87.959
                                                     76.586
                                                              75.408
                                                                       68.165
                                                                               83.640
## 2020
         95.950
                  99.325 100.039 101.515
                                            96.824 103.085
                                                              78.019
                                                                       78.576
                                                                               79.111
  2021 102.566
                  91.153 133.768 123.370 115.280
                                                     91.003
                                                              74.093
                                                                       92.367
                                                                               98.941
   2022 127.664 128.443 146.820 157.522 143.726 115.215 100.569
                                                                       84.339
                                                                               93.254
   2023 133.636 143.503 151.927 146.775 109.246
                                                     93.850
                                                              95.085
                                                                      97.256
                                                                               96.196
##
             Oct
                     Nov
                              Dec
                   0.003
## 1984
          0.003
                            0.004
          0.002
                   0.001
                            0.000
## 1985
## 1986
          0.001
                   0.000
                            0.000
## 1987
          0.000
                   0.000
                            0.001
## 1988
          0.000
                   0.000
                            0.000
## 1989
          0.599
                   0.419
                            0.219
## 1990
          0.693
                   0.789
                            0.406
## 1991
          1.448
                   1.448
                            0.671
## 1992
          0.832
                   0.960
                            1.184
          0.971
## 1993
                   1.562
                            0.929
## 1994
          1.218
                   1.675
                            0.571
## 1995
          0.876
                   0.427
                            0.329
## 1996
          0.863
                   0.337
                            0.417
## 1997
          0.937
                   0.248
                            0.244
##
  1998
          1.019
                   0.618
                            1.519
   1999
##
          1.428
                   1.209
                            1.720
## 2000
          1.404
                   2.808
                            1.309
## 2001
          2.071
                   1.605
                            2.101
## 2002
          2.506
                   2.238
                            2.577
## 2003
          3.061
                   3.280
                            3.770
```

```
## 2004
          3.511
                  3.181
                           3.999
          4.934
## 2005
                  5.492
                           6.237
## 2006
          8.333
                  8.668
                           8.433
## 2007
         11.521
                 10.560
                          11.909
## 2008
         16.229
                 17.038
                          22.573
         23.248
## 2009
                 23.458
                          23.563
## 2010
         27.104
                 33.259
                          30.910
## 2011
         35.913
                 42.440
                          36.358
## 2012
         43.113
                 39.745
                          49.557
## 2013
         46.523
                 53.921
                          47.656
## 2014
        49.501
                 64.374
                          50.195
         55.889
                 67.154
                          68.576
## 2015
## 2016
         69.384
                 66.212
                          78.973
                 77.162
## 2017
         83.146
                          75.749
         72.314
## 2018
                 75.118
                          82.933
## 2019
         94.255
                 85.929
                          90.909
## 2020
        98.343 113.038 109.220
## 2021 109.918 121.983 135.965
## 2022 111.725 140.570 131.975
## 2023
##
## $seasonal
##
               Jan
                           Feb
                                      Mar
                                                  Apr
                                                             May
                                                                         Jun
         1.6112906
                    0.7262628
## 1984
                                4.8536635
                                           4.9053327
                                                       2.3737263 -0.7481092
  1985
         1.6112906
                    0.7262628
                                4.8536635
                                           4.9053327
                                                       2.3737263 -0.7481092
  1986
         1.6112906
                    0.7262628
                                4.8536635
                                           4.9053327
                                                       2.3737263 -0.7481092
  1987
         1.6112906
                    0.7262628
                                            4.9053327
                                                       2.3737263 -0.7481092
                                4.8536635
  1988
         1.6112906
                    0.7262628
                                4.8536635
                                           4.9053327
                                                       2.3737263 -0.7481092
                    0.7262628
                                            4.9053327
## 1989
         1.6112906
                                4.8536635
                                                       2.3737263 -0.7481092
## 1990
         1.6112906
                    0.7262628
                                4.8536635
                                            4.9053327
                                                       2.3737263 -0.7481092
## 1991
         1.6112906
                    0.7262628
                                4.8536635
                                            4.9053327
                                                       2.3737263 -0.7481092
## 1992
         1.6112906
                    0.7262628
                                4.8536635
                                            4.9053327
                                                       2.3737263 -0.7481092
## 1993
         1.6112906
                    0.7262628
                                4.8536635
                                            4.9053327
                                                       2.3737263 -0.7481092
                                            4.9053327
## 1994
         1.6112906
                    0.7262628
                                4.8536635
                                                       2.3737263 -0.7481092
## 1995
         1.6112906
                    0.7262628
                                4.8536635
                                           4.9053327
                                                       2.3737263 -0.7481092
## 1996
         1.6112906
                    0.7262628
                                4.8536635
                                           4.9053327
                                                       2.3737263 -0.7481092
## 1997
         1.6112906
                    0.7262628
                                4.8536635
                                           4.9053327
                                                       2.3737263 -0.7481092
## 1998
         1.6112906
                    0.7262628
                                4.8536635
                                           4.9053327
                                                       2.3737263 -0.7481092
         1.6112906
                    0.7262628
                                4.8536635
                                           4.9053327
                                                       2.3737263 -0.7481092
## 1999
## 2000
         1.6112906
                    0.7262628
                                4.8536635
                                            4.9053327
                                                       2.3737263 -0.7481092
## 2001
         1.6112906
                    0.7262628
                                4.8536635
                                           4.9053327
                                                       2.3737263 -0.7481092
## 2002
         1.6112906
                    0.7262628
                                4.8536635
                                            4.9053327
                                                       2.3737263 -0.7481092
## 2003
         1.6112906
                    0.7262628
                                4.8536635
                                           4.9053327
                                                       2.3737263 -0.7481092
         1.6112906
                    0.7262628
                                4.8536635
                                           4.9053327
                                                       2.3737263 -0.7481092
## 2004
## 2005
         1.6112906
                    0.7262628
                                4.8536635
                                           4.9053327
                                                       2.3737263 -0.7481092
## 2006
         1.6112906
                    0.7262628
                                            4.9053327
                                                       2.3737263 -0.7481092
                                4.8536635
## 2007
         1.6112906
                    0.7262628
                                4.8536635
                                            4.9053327
                                                       2.3737263 -0.7481092
## 2008
         1.6112906
                    0.7262628
                                4.8536635
                                            4.9053327
                                                       2.3737263 -0.7481092
## 2009
         1.6112906
                    0.7262628
                                4.8536635
                                            4.9053327
                                                       2.3737263 -0.7481092
## 2010
         1.6112906
                    0.7262628
                                4.8536635
                                            4.9053327
                                                       2.3737263 -0.7481092
## 2011
         1.6112906
                    0.7262628
                                4.8536635
                                            4.9053327
                                                       2.3737263 -0.7481092
## 2012
         1.6112906
                    0.7262628
                                4.8536635
                                           4.9053327
                                                       2.3737263 -0.7481092
## 2013
         1.6112906
                    0.7262628
                                4.8536635
                                           4.9053327
                                                       2.3737263 -0.7481092
## 2014 1.6112906 0.7262628 4.8536635
                                           4.9053327 2.3737263 -0.7481092
```

```
1.6112906 0.7262628 4.8536635
                                           4.9053327
                                                      2.3737263 -0.7481092
## 2016
         1.6112906
                    0.7262628
                               4.8536635
                                           4.9053327
                                                      2.3737263 -0.7481092
                    0.7262628
## 2017
         1.6112906
                               4.8536635
                                           4.9053327
                                                      2.3737263 -0.7481092
                                           4.9053327
## 2018
         1.6112906
                    0.7262628
                               4.8536635
                                                      2.3737263 -0.7481092
## 2019
         1.6112906
                    0.7262628
                               4.8536635
                                           4.9053327
                                                      2.3737263 -0.7481092
## 2020
         1.6112906
                    0.7262628
                               4.8536635
                                           4.9053327
                                                      2.3737263 -0.7481092
## 2021
         1.6112906
                    0.7262628
                               4.8536635
                                           4.9053327
                                                      2.3737263 -0.7481092
## 2022
         1.6112906
                    0.7262628
                               4.8536635
                                           4.9053327
                                                      2.3737263 -0.7481092
## 2023
         1.6112906
                    0.7262628
                               4.8536635
                                           4.9053327
                                                      2.3737263 -0.7481092
##
               Jul
                          Aug
                                      Sep
                                                 Oct
                                                            Nov
## 1984 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 1985 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 1986 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 1987 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 1988 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 1989 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 1990 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
  1991 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 1992 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 1993 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 1994 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 1995 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 1996 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 1997 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 1998 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 1999 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 2000 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 2001 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 2002 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 2003 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 2004 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
  2005 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
  2006 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 2007 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 2008 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 2009 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 2010 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 2011 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 2012 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 2013 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 2014 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 2015 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 2016 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 2017 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 2018 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 2019 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 2020 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
  2021 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
## 2022 -4.9580096 -6.0986357 -4.7510844 -0.6135406
                                                      1.2691688
                                                                 1.4299348
##
  2023 -4.9580096 -6.0986357 -4.7510844
##
## $trend
##
                              Feb
                                                         Apr
                                                                       May
                 Jan
                                            Mar
## 1984
                                                                        NA
                  NA
                                NA
                                             NA
                                                          NΑ
```

```
## 1985 2.166667e-03 2.083333e-03 2.125000e-03 2.125000e-03 2.000000e-03
## 1986 1.583333e-03 1.708333e-03 1.625000e-03 1.458333e-03 1.375000e-03
## 1987 8.333333e-04 8.750000e-04 8.750000e-04 8.750000e-04 8.333333e-04
## 1988 5.833333e-04 3.750000e-04 2.916667e-04 2.500000e-04 2.500000e-04
## 1989 3.682083e-01 4.030833e-01 4.575833e-01 5.223750e-01 5.647917e-01
## 1990 8.050417e-01 7.970417e-01 7.654583e-01 7.425000e-01 7.618333e-01
## 1991 6.161667e-01 6.437500e-01 6.826667e-01 7.306250e-01 7.895417e-01
## 1992 8.749167e-01 8.511250e-01 8.546250e-01 8.448333e-01 7.988333e-01
## 1993 8.764167e-01 8.756250e-01 8.401667e-01 8.199583e-01 8.508333e-01
## 1994 9.052083e-01 9.213333e-01 9.549167e-01 9.902917e-01 1.005292e+00
## 1995 8.000833e-01 9.197917e-01 1.015375e+00 1.038167e+00 9.719167e-01
## 1996 1.033042e+00 1.002417e+00 9.523333e-01 9.202917e-01 9.160000e-01
## 1997 9.475000e-01 9.602083e-01 9.636250e-01 9.537500e-01 9.531250e-01
## 1998 6.805833e-01 6.705417e-01 6.857083e-01 7.197500e-01 7.385833e-01
## 1999 1.228083e+00 1.209500e+00 1.189958e+00 1.193042e+00 1.234708e+00
## 2000 1.518583e+00 1.506917e+00 1.499667e+00 1.492250e+00 1.557875e+00
## 2001 1.756125e+00 1.820958e+00 1.871958e+00 1.922208e+00 1.899875e+00
## 2002 2.595708e+00 2.688792e+00 2.780500e+00 2.833542e+00 2.878042e+00
## 2003 2.940125e+00 2.926167e+00 2.925875e+00 2.971625e+00 3.038167e+00
## 2004 3.821083e+00 3.884542e+00 3.945667e+00 3.992083e+00 4.006708e+00
## 2005 4.397542e+00 4.446417e+00 4.512667e+00 4.625792e+00 4.781375e+00
## 2006 6.489625e+00 6.639083e+00 6.771000e+00 6.971042e+00 7.245000e+00
## 2007 8.475708e+00 8.653042e+00 8.941875e+00 9.215083e+00 9.426750e+00
## 2008 1.342738e+01 1.377075e+01 1.388588e+01 1.411683e+01 1.458292e+01
## 2009 1.860804e+01 1.905538e+01 1.958700e+01 2.009829e+01 2.065825e+01
## 2010 2.386558e+01 2.429071e+01 2.481333e+01 2.532300e+01 2.589204e+01
## 2011 3.195162e+01 3.217233e+01 3.225071e+01 3.258412e+01 3.333371e+01
## 2012 3.754633e+01 3.787733e+01 3.829187e+01 3.886492e+01 3.905262e+01
## 2013 4.494100e+01 4.542963e+01 4.600533e+01 4.655750e+01 4.729025e+01
## 2014 5.005567e+01 5.028746e+01 5.034179e+01 5.044392e+01 5.100354e+01
## 2015 5.019592e+01 5.082112e+01 5.158333e+01 5.219808e+01 5.258008e+01
## 2016 6.123212e+01 6.186508e+01 6.228325e+01 6.319129e+01 6.371433e+01
## 2017 7.021804e+01 7.004617e+01 7.030175e+01 7.108958e+01 7.211925e+01
## 2018 7.608679e+01 7.698162e+01 7.791642e+01 7.755150e+01 7.701500e+01
## 2019 7.818983e+01 7.901238e+01 7.988321e+01 8.164954e+01 8.301421e+01
## 2020 9.136246e+01 9.190504e+01 9.215013e+01 9.213175e+01 9.343163e+01
## 2021 1.009570e+02 1.013680e+02 1.027689e+02 1.040775e+02 1.049325e+02
## 2022 1.221579e+02 1.229266e+02 1.223551e+02 1.221935e+02 1.230432e+02
## 2023 1.198856e+02 1.201953e+02 1.208561e+02
                                                         NΑ
                                                                      NΑ
##
                 Jun
                              Jul
                                           Aug
                                                        Sep
                                                                     Oct
## 1984
                 NA 2.083333e-03 2.291667e-03 2.458333e-03 2.500000e-03
## 1985 1.750000e-03 1.541667e-03 1.375000e-03 1.250000e-03 1.250000e-03
## 1986 1.333333e-03 1.291667e-03 1.208333e-03 1.083333e-03 9.166667e-04
## 1987 8.750000e-04 1.000000e-03 1.083333e-03 1.083333e-03 1.083333e-03
## 1988 2.083333e-04 2.079167e-02 7.320833e-02 1.413750e-01 2.115833e-01
## 1989 5.913750e-01 6.226250e-01 6.458333e-01 6.454167e-01 6.698333e-01
## 1990 7.850417e-01 7.588333e-01 7.331667e-01 7.360833e-01 7.047917e-01
## 1991 8.280417e-01 8.515833e-01 8.961667e-01 9.454583e-01 9.741250e-01
## 1992 7.998750e-01 8.350833e-01 7.826667e-01 7.436250e-01 7.782500e-01
## 1993 8.652917e-01 8.195000e-01 7.915833e-01 8.026667e-01 8.124167e-01
## 1994 9.950833e-01 9.809583e-01 9.707917e-01 8.827917e-01 7.480417e-01
## 1995 9.098333e-01 9.199167e-01 9.526667e-01 9.912500e-01 1.051042e+00
## 1996 9.159167e-01 9.157500e-01 9.115000e-01 9.055417e-01 9.113333e-01
## 1997 9.422083e-01 9.203333e-01 8.913333e-01 8.567500e-01 8.026250e-01
```

```
## 1998 8.071250e-01 9.057083e-01 9.939167e-01 1.099292e+00 1.202792e+00
## 1999 1.267708e+00 1.319917e+00 1.420208e+00 1.462917e+00 1.443000e+00
## 2000 1.607375e+00 1.553833e+00 1.478333e+00 1.465167e+00 1.541500e+00
## 2001 1.882750e+00 1.975792e+00 2.076042e+00 2.161708e+00 2.255458e+00
## 2002 2.924250e+00 2.918625e+00 2.897625e+00 2.928250e+00 2.964167e+00
## 2003 3.131292e+00 3.233167e+00 3.324625e+00 3.400208e+00 3.465208e+00
## 2004 4.012125e+00 4.040458e+00 4.051417e+00 4.081875e+00 4.177417e+00
## 2005 4.970917e+00 5.242042e+00 5.555750e+00 5.805042e+00 6.028583e+00
## 2006 7.468833e+00 7.570208e+00 7.665083e+00 7.847958e+00 8.045333e+00
## 2007 9.650417e+00 1.005413e+01 1.050233e+01 1.093829e+01 1.147687e+01
## 2008 1.529717e+01 1.598000e+01 1.650292e+01 1.711675e+01 1.776354e+01
## 2009 2.096700e+01 2.113671e+01 2.120538e+01 2.135742e+01 2.189717e+01
## 2010 2.660654e+01 2.715379e+01 2.810858e+01 2.910025e+01 2.975604e+01
## 2011 3.394325e+01 3.489275e+01 3.570058e+01 3.628092e+01 3.681679e+01
## 2012 3.949029e+01 4.019750e+01 4.078462e+01 4.146033e+01 4.238387e+01
## 2013 4.780171e+01 4.817354e+01 4.861508e+01 4.888712e+01 4.933346e+01
## 2014 5.154488e+01 5.125983e+01 5.099875e+01 5.078333e+01 5.032896e+01
## 2015 5.346179e+01 5.469742e+01 5.590883e+01 5.759325e+01 5.895283e+01
## 2016 6.410829e+01 6.487308e+01 6.548229e+01 6.629892e+01 6.748887e+01
## 2017 7.244117e+01 7.298925e+01 7.382783e+01 7.408821e+01 7.434208e+01
## 2018 7.722917e+01 7.734408e+01 7.707908e+01 7.690025e+01 7.715521e+01
## 2019 8.379700e+01 8.467238e+01 8.613775e+01 8.756437e+01 8.818767e+01
## 2020 9.532413e+01 9.636275e+01 9.629792e+01 9.736279e+01 9.967879e+01
## 2021 1.064195e+02 1.085797e+02 1.111792e+02 1.132768e+02 1.152436e+02
## 2022 1.236514e+02 1.237340e+02 1.246103e+02 1.254506e+02 1.252156e+02
## 2023
                  NA
                               NA
                                            NA
                                                         NΑ
##
                              Dec
                 Nov
## 1984 2.416667e-03 2.291667e-03
## 1985 1.333333e-03 1.458333e-03
## 1986 7.500000e-04 7.083333e-04
## 1987 1.041667e-03 8.750000e-04
## 1988 2.744583e-01 3.257500e-01
## 1989 7.165000e-01 7.727917e-01
## 1990 6.806667e-01 6.467083e-01
## 1991 9.473750e-01 8.977500e-01
## 1992 8.250833e-01 8.661250e-01
## 1993 8.179167e-01 8.575417e-01
## 1994 6.960833e-01 7.203750e-01
## 1995 1.082417e+00 1.062542e+00
## 1996 9.168333e-01 9.310833e-01
## 1997 7.392917e-01 6.925000e-01
## 1998 1.262458e+00 1.261167e+00
## 1999 1.455667e+00 1.501958e+00
## 2000 1.624208e+00 1.688167e+00
## 2001 2.366667e+00 2.494500e+00
## 2002 2.963792e+00 2.942417e+00
## 2003 3.592750e+00 3.741333e+00
## 2004 4.241042e+00 4.304250e+00
## 2005 6.239917e+00 6.377417e+00
## 2006 8.215000e+00 8.366000e+00
## 2007 1.210833e+01 1.280608e+01
## 2008 1.821196e+01 1.840825e+01
## 2009 2.257133e+01 2.326583e+01
## 2010 3.057096e+01 3.142550e+01
```

```
## 2011 3.696687e+01 3.721646e+01
## 2012 4.358733e+01 4.436554e+01
  2013 4.940767e+01 4.960862e+01
  2014 5.044008e+01 5.032237e+01
  2015 5.961087e+01 6.026183e+01
## 2016 6.873975e+01 6.988537e+01
  2017 7.461763e+01 7.539192e+01
## 2018 7.776804e+01 7.770683e+01
   2019 8.867604e+01 9.014954e+01
   2020 1.013584e+02 1.016240e+02
   2021 1.178518e+02 1.200459e+02
   2022 1.233312e+02 1.210043e+02
##
   2023
##
##
  $random
##
                                 Feb
                                                Mar
                                                                              May
                   Jan
                                                               Apr
##
  1984
                    NA
                                  NA
                                                 NA
                                                                NA
                                                                               NA
   1985
         -1.611457256
                        -0.724346144
                                       -4.853788452
                                                      -4.905457705
                                                                     -2.374726346
  1986
         -1.611873922
                        -0.726971144
                                       -4.853288452
                                                      -4.904791039
                                                                     -2.372101346
##
   1987
         -1.612123922
                        -0.727137811
                                       -4.854538452
                                                      -4.906207705
                                                                     -2.373559679
##
  1988
         -1.609873922
                        -0.726637811
                                       -4.853955119
                                                      -4.905582705
                                                                     -2.373976346
##
  1989
         -1.482498922
                        -0.366346144
                                       -4.438246786
                                                      -4.615707705
                                                                     -2.241518012
## 1990
         -1.388332256
                        -0.734304478
                                       -4.782121786
                                                      -4.213832705
                                                                     -1.940559679
## 1991
         -2.015457256
                        -0.381012811
                                       -4.829330119
                                                      -4.822957705
                                                                     -1.926268012
## 1992
         -1.974207256
                         0.181612189
                                       -4.588288452
                                                      -4.662166039
                                                                     -2.852559679
  1993
         -1.643707256
                        -1.432887811
                                       -3.920830119
                                                      -4.459291039
                                                                     -1.958559679
  1994
##
         -2.516498922
                        -1.304596144
                                       -3.943580119
                                                      -4.487624372
                                                                     -2.123018012
                        -1.566054478
##
   1995
         -2.392373922
                                       -5.853038452
                                                      -5.920499372
                                                                     -1.951643012
##
  1996
         -2.141332256
                        -1.346679478
                                       -5.165996786
                                                      -4.991624372
                                                                     -1.953726346
                                       -5.310288452
## 1997
         -2.147790589
                                                      -4.753082705
                        -1.314471144
                                                                     -2.130851346
## 1998
         -2.232873922
                        -1.368804478
                                       -5.518371786
                                                      -5.332082705
                                                                     -2.623309679
##
  1999
         -1.689373922
                        -0.881762811
                                       -4.519621786
                                                      -4.824374372
                                                                     -2.668434679
##
   2000
         -0.927873922
                         0.175820522
                                       -5.159330119
                                                      -5.271582705
                                                                     -2.539601346
                        -1.076221144
##
  2001
         -2.039415589
                                       -4.909621786
                                                      -4.491541039
                                                                     -2.106601346
   2002
         -1.437998922
                                                      -4.243874372
                        -0.979054478
                                       -4.727163452
                                                                     -1.574768012
##
  2003
         -2.393415589
                        -1.109429478
                                       -4.244538452
                                                      -4.147957705
                                                                     -1.977893012
## 2004
         -2.022373922
                        -1.124804478
                                       -4.393330119
                                                      -4.479416039
                                                                     -0.574434679
## 2005
         -2.147832256
                        -1.874679478
                                       -4.041330119
                                                      -3.739124372
                                                                     -1.196101346
##
  2006
          0.029084411
                        -0.807346144
                                       -3.576663452
                                                      -3.442374372
                                                                     -1.229726346
## 2007
         -1.719998922
                        -0.781304478
                                       -3.398538452
                                                      -3.298416039
                                                                     -1.727476346
  2008
         -0.458665589
                        -1.355012811
                                       -2.423538452
                                                      -1.193166039
                                                                     1.264356988
  2009
##
          0.084667744
                         0.186362189
                                       -0.218663452
                                                       0.442375628
                                                                     -1.665976346
##
  2010
         -2.089873922
                        -6.483971144
                                       -0.360996786
                                                       3.087667295
                                                                     1.410231988
##
  2011
         -4.388915589
                         2.762403856
                                       -1.126371786
                                                       4.893542295
                                                                     4.459565321
## 2012
          7.356376078
                        -0.894596144
                                        4.712461548
                                                      -0.406249372
                                                                     1.361648654
## 2013
          3.735709411
                         1.870112189
                                        2.899003214
                                                       8.166167295
                                                                     5.742023654
## 2014
          9.446042744
                        -3.215721144
                                        5.319544881
                                                       8.234750628
                                                                     -0.145268012
## 2015
         -0.074207256
                        -0.635387811
                                       -4.205996786
                                                       3.859583961
                                                                     3.566190321
##
  2016
          0.163584411
                         6.120653856
                                        7.720086548
                                                       2.870375628
                                                                     -1.779059679
##
   2017
         -0.864332256
                         4.602570522
                                       12.637586548
                                                      10.595083961
                                                                     4.214023654
##
  2018
          9.644917744
                                        7.523919881
                                                                     2.339273654
                         1.415112189
                                                       7.725167295
## 2019
          3.115876078
                        -2.549637811
                                        3.199128214
                                                      12.104125628
                                                                     2.571065321
## 2020
                         6.693695522
                                        3.035211548
                                                       4.477917295
                                                                     1.018648654
          2.976251078
## 2021
         -0.002290589 -10.941304478
                                       26.145419881
                                                     14.387208961
                                                                     7.973815321
```

```
## 2022
          3.894792744
                         4.790153856
                                       19.611211548
                                                      30.423208961
                                                                    18.309065321
## 2023
                        22.581445522
                                       26.217253214
                                                                NΑ
         12.139126078
                                                                               NA
##
                   Jun
                                 Jul
                                                Aug
                                                               Sep
                                                                              Oct
## 1984
                         4.957926291
                                        6.097344026
                                                      4.750626078
                                                                     0.614040608
                   NA
##
  1985
          0.747359181
                         4.956467958
                                        6.098260693
                                                      4.752834411
                                                                     0.614290608
                                        6.099427360
## 1986
          0.748775847
                         4.958717958
                                                      4.750001078
                                                                     0.613623941
## 1987
          0.750234181
                         4.961009625
                                        6.098552360
                                                      4.751001078
                                                                     0.612457274
## 1988
          0.747900847
                         4.937217958
                                        6.025427360
                                                      4.609709411
                                                                     0.401957274
## 1989
          0.690734181
                         4.820384625
                                        5.804802360
                                                      5.061667744
                                                                     0.542707274
## 1990
          1.350067514
                         4.605176291
                                        5.604469026
                                                      4.326001078
                                                                     0.601748941
## 1991
          0.450067514
                         4.636426291
                                        5.979469026
                                                      4.512626078
                                                                     1.087415608
## 1992
          0.204234181
                         4.378926291
                                        5.795969026
                                                      5.095459411
                                                                     0.667290608
## 1993
          0.177817514
                         4.602509625
                                        5.560052360
                                                      4.412417744
                                                                     0.772123941
## 1994
          1.009025847
                                        5.584844026
                                                      4.934292744
                                                                     1.083498941
                         4.624051291
## 1995
                                        7.007969026
          1.539275847
                         6.153092958
                                                      5.714834411
                                                                     0.438498941
## 1996
          1.114192514
                         5.868259625
                                        6.603135693
                                                      5.044542744
                                                                     0.565207274
## 1997
          1.569900847
                         5.775676291
                                        7.016302360
                                                      4.782334411
                                                                     0.747915608
## 1998
          1.288984181
                         5.920301291
                                        6.542719026
                                                      5.274792744
                                                                     0.429748941
## 1999
          0.346400847
                         5.194092958
                                        5.982427360
                                                      4.576167744
                                                                     0.598540608
## 2000
          0.665734181
                         4.700176291
                                        5.904302360
                                                      4.419917744
                                                                     0.476040608
## 2001
          1.150359181
                         5.149217958
                                        5.991594026
                                                      4.262376078
                                                                     0.429082274
## 2002
          1.666859181
                         5.077384625
                                        6.533010693
                                                      4.333834411
                                                                     0.155373941
## 2003
                                                                     0.209332274
          1.189817514
                         4.977842958
                                        5.556010693
                                                      4.404876078
## 2004
                                                                    -0.052876059
          1.502984181
                         4.890551291
                                        5.632219026
                                                      4.387209411
## 2005
          1.908192514
                         4.563967958
                                        4.425885693
                                                      3.956042744
                                                                    -0.481042726
## 2006
          0.280275847
                         4.058801291
                                        4.080552360
                                                      3.315126078
                                                                     0.901207274
## 2007
          0.038692514
                                        4.806302360
                                                      3.593792744
                         2.267884625
                                                                     0.657665608
## 2008
          2.989942514
                         2.655009625
                                        0.733719026
                                                      -1.749665589
                                                                    -0.921001059
## 2009
         -1.113890819
                                        3.538260693
                                                     -0.738332256
                                                                     1.964373941
                         0.727301291
## 2010
          1.604567514
                         0.746217958
                                        0.802052360
                                                      -0.105165589
                                                                    -2.038501059
## 2011
          4.285859181
                        -4.383740375
                                       -4.101947640
                                                      -8.092832256
                                                                    -0.290251059
## 2012
          2.107817514
                        -5.140490375
                                       -5.789989307
                                                      -6.719248922
                                                                     1.342665608
## 2013
         -0.144599153
                        -5.364532042
                                       -9.645447640
                                                      -4.304040589
                                                                    -2.196917726
## 2014
          3.109234181
                        -4.718823709 -10.198114307
                                                     -6.727248922
                                                                    -0.214417726
## 2015
         -6.920682486
                        -3.078407042
                                      -5.181197640
                                                     -5.171165589
                                                                    -2.450292726
                                                                     2.508665608
## 2016
                         0.198926291 -13.016655974
         -7.733182486
                                                     -5.578832256
## 2017
         -2.969057486 -13.030240375 -20.374197640
                                                     -8.222123922
                                                                     9.417457274
## 2018
          7.804942514 -16.270073709 -3.264447640
                                                     -8.960165589
                                                                    -4.227667726
## 2019
         -6.462890819
                       -4.306365375 -11.874114307
                                                      0.826709411
                                                                     6.680873941
          8.508984181 -13.385740375 -11.623280974 -13.500707256
## 2020
                                                                    -0.722251059
## 2021 -14.668432486 -29.528657042 -12.713530974
                                                     -9.584665589
                                                                    -4.712042726
## 2022
         -7.688307486
                       -18.206990375 -34.172697640
                                                    -27.445540589
                                                                   -12.877084392
##
  2023
                    NA
                                  NA
                                                 NA
                                                                NA
##
                  Nov
                                 Dec
## 1984
         -1.268585461
                        -1.428226486
## 1985
                        -1.431393153
         -1.269502127
## 1986
         -1.269918794
                        -1.430643153
## 1987
         -1.270210461
                        -1.429809820
                        -1.755684820
## 1988
         -1.543627127
  1989
         -1.566668794
                        -1.983726486
## 1990
         -1.160835461
                        -1.670643153
## 1991
         -0.768543794
                        -1.656684820
## 1992
         -1.134252127
                        -1.112059820
## 1993
        -0.525085461
                       -1.358476486
```

```
## 1994
         -0.290252127
                        -1.579309820
## 1995
         -1.924585461
                        -2.163476486
                        -1.944018153
## 1996
         -1.849002127
## 1997
         -1.760460461
                        -1.878434820
## 1998
         -1.913627127
                        -1.172101486
## 1999
         -1.515835461
                        -1.211893153
## 2000
         -0.085377127
                        -1.809101486
## 2001
         -2.030835461
                        -1.823434820
## 2002
         -1.994960461
                        -1.795351486
## 2003
        -1.581918794
                        -1.401268153
## 2004
        -2.329210461
                        -1.735184820
## 2005
         -2.017085461
                        -1.570351486
## 2006
         -0.816168794
                        -1.362934820
## 2007
         -2.817502127
                        -2.327018153
## 2008
         -2.443127127
                         2.734815180
## 2009
         -0.382502127
                        -1.132768153
## 2010
          1.418872873
                        -1.945434820
## 2011
          4.203956206
                        -2.288393153
## 2012
         -5.111502127
                         3.761523514
## 2013
          3.244164539
                        -3.382559820
## 2014
         12.664747873
                        -1.557309820
## 2015
          6.273956206
                         6.884231847
## 2016
        -3.796918794
                         7.657690180
## 2017
          1.275206206
                        -1.072851486
## 2018
         -3.919210461
                         3.796231847
## 2019
         -4.016210461
                        -0.670476486
## 2020
         10.410414539
                         6.166065180
## 2021
          2.861997873
                        14.489148514
## 2022
        15.969664539
                         9.540773514
## 2023
##
## $figure
##
        1.6112906 0.7262628 4.8536635 4.9053327 2.3737263 -0.7481092
    [7] -4.9580096 -6.0986357 -4.7510844 -0.6135406 1.2691688
##
                                                                  1.4299348
##
## $type
##
   [1] "additive"
##
## attr(,"class")
## [1] "decomposed.ts"
print(decompose(SolarTS, type = "additive"))
## $x
##
           Jan
                  Feb
                          Mar
                                 Apr
                                                Jun
                                                        Jul
                                                               Aug
                                                                      Sep
                                                                              Oct
                                         May
                0.000
                        0.001
                               0.001
                                      0.002
                                                             0.003
                                                                    0.003
## 1984
         0.000
                                              0.003
                                                     0.001
                                                                            0.002
   1985
         0.002
                0.000
                        0.000
                               0.004
                                       0.005
                                              0.005
                                                     0.004
                                                             0.007
                                                                    0.005
                                                                            0.003
         0.002
                0.002
                        0.003
                               0.005
                                       0.006
                                              0.005
                                                     0.006
                                                             0.006
                                                                    0.005
  1986
                                                                            0.004
   1987
         0.000
                0.002
                        0.003
                               0.004
                                       0.004
                                              0.006
                                                     0.006
                                                             0.004
                                                                    0.003
                                                                            0.002
##
  1988
         0.002
                0.003
                        0.004
                               0.002
                                       0.004
                                              0.005
                                                     0.004
                                                             0.004
                                                                    0.003
                                                                            0.000
## 1989
         2.821
                3.041
                        4.220
                               4.660
                                       5.109
                                              5.175
                                                      5.476
                                                             5.389
                                                                    4.941
                                                                            4.501
         3.015
                3.256
                        4.489
                               4.946
                                       5.515
                                              5.534
                                                      5.832
                                                             5.781
                                                                    5.228
## 1990
                                                                            4.782
                3.369
                        4.561
                                       5.739
                                              5.803
## 1991
         3.125
                               5.026
                                                      6.133
                                                             6.035
                                                                    5.487
                                                                            4.935
## 1992
         3.196
                3.451
                        4.752
                               5.284
                                       5.883
                                              5.931
                                                      6.274
                                                             6.205
                                                                    5.628
                                                                            5.115
## 1993
         3.288
                3.570
                        4.954
                               5.515
                                       6.053
                                              6.058
                                                     6.445
                                                             6.401
                                                                    5.818
                                                                           5.243
```

```
3.432 3.680 5.137 5.640 6.216 6.292 6.584
                                                         6.471
                                                                5.949 5.458
        3.415
               3.692 5.105
                             5.735
                                    6.370 6.471
                                                  6.750
## 1995
                                                         6.674
                                                                6.047
                                                                       5.471
                                    6.487
                                                         6.602
## 1996
        3.472 3.760
                      5.293
                             5.865
                                           6.562
                                                  6.804
                                                                5.956
                                    6.292 6.433
## 1997
        3.422 3.762
                             5.748
                                                  6.721
                                                         6.612
                                                                5.958
                                                                       5.437
                     5.176
## 1998
        3.375
               3.629
                      5.138
                             5.664
                                    6.173
                                           6.327
                                                  6.679
                                                         6.584
                                                                5.956
                                                                       5.395
## 1999
        3.294
               3.570
                      4.984
                             5.536
                                    6.121
                                           6.184
                                                  6.482
                                                         6.377
                                                                5.775
                                                                       5.311
                                           5.895
## 2000
        3.155
               3.440
                      4.733
                             5.239
                                    5.832
                                                  6.261
                                                         6.144
                                                                5.608
## 2001
        3.008
               3.261
                      4.542
                             5.020
                                    5.672
                                           5.755
                                                  6.029
                                                         5.947
                                                                5.380
                                                                       4.773
## 2002
        2.923
               3.189
                      4.435
                             4.877
                                     5.408
                                           5.585
                                                  5.812
                                                         5.719
                                                                5.162
                                                                       4.647
                                    5.298
## 2003
        2.848
               3.083
                      4.334
                             4.795
                                           5.421
                                                  5.579
                                                         5.522
                                                                5.034
                                                                       4.535
## 2004
        2.809
               3.019
                      4.289
                             4.722
                                    5.278
                                           5.343
                                                  5.575
                                                         5.488
                                                                4.986
                                                                       4.470
## 2005
        2.742
               2.968
                      4.158
                             4.638
                                    5.178
                                           5.247
                                                  5.438
                                                                4.894
                                                                       4.399
                                                         5.396
## 2006
        2.881
               3.124
                      4.327
                             4.821
                                    5.368
                                           5.410
                                                  5.640
                                                         5.657
                                                                5.085
                                                                       4.577
## 2007
               3.269
                                           5.707
                                                                       4.848
        3.016
                      4.579
                             5.051
                                    5.658
                                                  5.981
                                                         5.886
                                                                5.367
## 2008
        3.206
               3.518
                      4.933
                             5.478
                                    6.029
                                           6.181
                                                         6.326
                                                  6.408
                                                                5.758
                                                                       5.166
## 2009
        3.247
               3.578
                      5.053
                             5.614
                                    6.200
                                           6.229
                                                   6.582
                                                         6.501
                                                                5.892
                                                                       5.307
        3.485
               3.833 5.386
                                    6.760
                                           6.895
## 2010
                             6.033
                                                  7.158
                                                         7.072
                                                                6.433
                                                                       5.693
## 2011
        3.924
               4.374 6.043
                             6.760
                                    7.496
                                           7.667
                                                  7.903
                                                         7.958
                                                                7.178
        4.607 5.077 7.148
                             8.096 9.316 9.605
                                                  9.934
                                                         9.685
## 2012
                                                                8.960 8.214
## 2013
        5.869 6.663 9.260 10.151 11.264 11.745 12.038 12.336 11.551 10.946
## 2014
        8.157 8.799 12.624 13.934 15.758 16.428 16.395 16.624 15.631 14.507
       9.815 11.480 15.989 18.058 19.510 19.804 20.660 20.720 18.026 15.938
## 2016 11.728 15.428 19.297 21.401 24.459 24.955 27.056 26.741 24.199 21.438
## 2017 15.555 17.857 27.472 30.175 34.567 36.083 34.635 33.492 30.881 28.042
## 2018 20.417 23.213 30.918 36.049 40.277 42.476 40.715 39.785 35.355 30.386
## 2019 22.249 23.942 35.490 40.146 43.146 46.198 47.572 45.914 40.157 35.724
## 2020 26.741 32.049 38.731 46.045 54.208 54.219 58.159 52.712 44.933 40.674
## 2021 32.034 35.565 51.477 59.068 66.559 65.882 66.269 64.229 59.026 49.778
## 2022 41.808 47.446 62.806 71.072 79.459 82.611 82.584 77.169 70.105 63.190
## 2023 44.432 50.523 67.312 79.380 90.079 92.024 97.397 93.068 81.595
##
          Nov
                 Dec
## 1984
        0.001
               0.000
## 1985
        0.001
               0.001
## 1986
        0.003 0.001
## 1987
        0.001
               0.001
## 1988
        0.000
               0.000
## 1989
        3.697
               3.465
## 1990
        3.884
               3.700
## 1991
        4.034
               3.792
## 1992
        4.187
               3.914
## 1993
        4.297
              4.039
## 1994
        4.415 4.136
## 1995
        4.473
               4.192
        4.495
## 1996
               4.262
## 1997
        4.424
               4.187
        4.389
## 1998
               4.147
## 1999
        4.307
               4.068
        4.103
               3.882
## 2000
## 2001
        3.905
               3.675
## 2002
        3.821
               3.551
## 2003
        3.669
               3.452
## 2004
        3.625
               3.418
## 2005
        3.547 3.335
## 2006 3.718 3.487
```

```
## 2007 3.922 3.662
## 2008
        4.167
               3.926
## 2009
        4.300
               4.023
## 2010
        4.721
               4.384
## 2011
        5.259
               5.056
## 2012 6.715 6.439
## 2013 9.028 8.800
## 2014 11.805 10.387
## 2015 13.628 12.547
## 2016 17.985 16.202
## 2017 20.501 19.362
## 2018 23.468 20.576
## 2019 26.634 22.573
## 2020 33.068 29.778
## 2021 42.082 34.895
## 2022 46.708 39.623
## 2023
##
## $seasonal
##
                Jan
                            Feb
                                        Mar
                                                    Apr
                                                                May
## 1984 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                        2.80309139
                                                                      3.06251025
## 1985 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 1986 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 1987 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 1988 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 1989 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 1990 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 1991 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 1992 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 1993 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 1994 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                          2.80309139
                                                                      3.06251025
## 1995 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 1996 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 1997 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                          2.80309139
                                                                      3.06251025
## 1998 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                          2.80309139
                                                                      3.06251025
                                                         2.80309139
## 1999 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                                      3.06251025
## 2000 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 2001 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 2002 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                          2.80309139
                                                                      3.06251025
## 2003 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 2004 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 2005 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 2006 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 2007 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 2008 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 2009 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 2010 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 2011 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 2012 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 2013 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                          2.80309139
                                                                      3.06251025
## 2014 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                         2.80309139
                                                                      3.06251025
## 2015 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                        2.80309139
                                                                      3.06251025
## 2016 -4.00420660 -3.15722904 0.03232545
                                             1.40253766 2.80309139
                                                                     3.06251025
## 2017 -4.00420660 -3.15722904 0.03232545 1.40253766 2.80309139 3.06251025
```

```
## 2018 -4.00420660 -3.15722904 0.03232545
                                             1.40253766
                                                          2.80309139
                                                                      3.06251025
## 2019 -4.00420660 -3.15722904
                                 0.03232545
                                             1.40253766
                                                          2.80309139
                                                                      3.06251025
## 2020 -4.00420660 -3.15722904
                                 0.03232545
                                              1.40253766
                                                          2.80309139
                                                                       3.06251025
## 2021 -4.00420660 -3.15722904
                                 0.03232545
                                              1.40253766
                                                          2.80309139
                                                                       3.06251025
## 2022 -4.00420660 -3.15722904
                                 0.03232545
                                              1.40253766
                                                          2.80309139
                                                                       3.06251025
  2023 -4.00420660 -3.15722904
                                 0.03232545
                                              1.40253766
                                                          2.80309139
                                                                       3.06251025
                            Aug
                Jul
                                                     Oct
                                                                 Nov
                                         Sep
                                                                              Dec
## 1984
         3.21594084
                     2.64254447
                                  1.13678165 -0.36339998 -2.82600681 -3.94488929
## 1985
         3.21594084
                     2.64254447
                                  1.13678165 -0.36339998 -2.82600681 -3.94488929
## 1986
         3.21594084
                     2.64254447
                                  1.13678165 -0.36339998 -2.82600681 -3.94488929
## 1987
         3.21594084
                     2.64254447
                                  1.13678165 -0.36339998 -2.82600681 -3.94488929
                     2.64254447
                                  1.13678165 -0.36339998 -2.82600681 -3.94488929
## 1988
         3.21594084
## 1989
         3.21594084
                     2.64254447
                                  1.13678165 -0.36339998 -2.82600681 -3.94488929
         3.21594084
## 1990
                     2.64254447
                                  1.13678165 -0.36339998 -2.82600681 -3.94488929
         3.21594084
                     2.64254447
                                  1.13678165 -0.36339998 -2.82600681 -3.94488929
## 1991
## 1992
         3.21594084
                     2.64254447
                                  1.13678165 -0.36339998 -2.82600681 -3.94488929
                                  1.13678165 -0.36339998 -2.82600681 -3.94488929
## 1993
         3.21594084
                     2.64254447
## 1994
         3.21594084
                     2.64254447
                                  1.13678165 -0.36339998 -2.82600681 -3.94488929
                                  1.13678165 -0.36339998 -2.82600681 -3.94488929
## 1995
        3.21594084
                     2.64254447
## 1996
         3.21594084
                     2.64254447
                                  1.13678165 -0.36339998 -2.82600681 -3.94488929
## 1997
         3.21594084
                     2.64254447
                                 1.13678165 -0.36339998 -2.82600681 -3.94488929
## 1998
         3.21594084
                     2.64254447
                                 1.13678165 -0.36339998 -2.82600681 -3.94488929
                     2.64254447
                                 1.13678165 -0.36339998 -2.82600681 -3.94488929
## 1999
         3.21594084
                                 1.13678165 -0.36339998 -2.82600681 -3.94488929
## 2000
         3.21594084
                     2.64254447
## 2001
         3.21594084
                     2.64254447
                                  1.13678165 -0.36339998 -2.82600681 -3.94488929
## 2002
         3.21594084
                     2.64254447
                                 1.13678165 -0.36339998 -2.82600681 -3.94488929
## 2003
         3.21594084
                     2.64254447
                                  1.13678165 -0.36339998 -2.82600681 -3.94488929
## 2004
         3.21594084
                     2.64254447
                                 1.13678165 -0.36339998 -2.82600681 -3.94488929
## 2005
         3.21594084
                     2.64254447
                                  1.13678165 -0.36339998 -2.82600681 -3.94488929
## 2006
         3.21594084
                     2.64254447
                                 1.13678165 -0.36339998 -2.82600681 -3.94488929
## 2007
         3.21594084
                     2.64254447
                                  1.13678165 -0.36339998 -2.82600681 -3.94488929
## 2008
         3.21594084
                     2.64254447
                                  1.13678165 -0.36339998 -2.82600681 -3.94488929
## 2009
         3.21594084
                     2.64254447
                                  1.13678165 -0.36339998 -2.82600681 -3.94488929
                     2.64254447
                                  1.13678165 -0.36339998 -2.82600681 -3.94488929
## 2010
         3.21594084
## 2011
         3.21594084
                     2.64254447
                                  1.13678165 -0.36339998 -2.82600681 -3.94488929
## 2012
                                 1.13678165 -0.36339998 -2.82600681 -3.94488929
        3.21594084
                     2.64254447
## 2013
        3.21594084
                     2.64254447
                                 1.13678165 -0.36339998 -2.82600681 -3.94488929
## 2014
        3.21594084
                     2.64254447
                                 1.13678165 -0.36339998 -2.82600681 -3.94488929
         3.21594084
                     2.64254447
                                 1.13678165 -0.36339998 -2.82600681 -3.94488929
## 2015
                     2.64254447
                                 1.13678165 -0.36339998 -2.82600681 -3.94488929
## 2016
        3.21594084
                                 1.13678165 -0.36339998 -2.82600681 -3.94488929
## 2017
         3.21594084
                     2.64254447
## 2018
         3.21594084
                     2.64254447
                                 1.13678165 -0.36339998 -2.82600681 -3.94488929
## 2019
         3.21594084
                     2.64254447
                                 1.13678165 -0.36339998 -2.82600681 -3.94488929
## 2020
         3.21594084
                     2.64254447
                                 1.13678165 -0.36339998 -2.82600681 -3.94488929
## 2021
         3.21594084
                     2.64254447
                                 1.13678165 -0.36339998 -2.82600681 -3.94488929
                                  1.13678165 -0.36339998 -2.82600681 -3.94488929
                     2.64254447
## 2022
         3.21594084
##
  2023
        3.21594084
                     2.64254447
                                 1.13678165
##
##
  $trend
##
                              Feb
                                                                       May
                 Jan
                                            Mar
                                                         Apr
## 1984
                                             NA
                                                                        NA
                  NA
                               NA
                                                          NA
## 1985
        0.002291667
                      0.002583333
                                   0.002833333
                                                0.002958333
                                                              0.003000000
## 1986
        0.003750000
                      0.003791667
                                   0.003750000
                                                0.003791667
                                                              0.003916667
## 1987 0.003666667 0.003583333 0.003416667 0.003250000
                                                              0.003083333
```

```
## 1988
         0.003000000
                      0.002916667
                                    0.002916667
                                                  0.002833333
                                                               0.002708333
## 1989
                      2.766791667
                                                  3.590208333
         2.314416667
                                    3.196916667
                                                               3.931791667
         4.533500000
                                                  4.616625000
  1990
                       4.56466667
                                    4.592958333
                                                               4.636125000
  1991
         4.748375000
                       4.771500000
                                    4.792875000
                                                  4.810041667
                                                                4.822666667
##
   1992
         4.915291667
                       4.928250000
                                    4.941208333
                                                  4.954583333
                                                               4.968458333
  1993
         5.070541667
                       5.085833333
                                    5.101916667
##
                                                  5.115166667
                                                               5.125083333
  1994
         5.225791667
                       5.234500000
                                    5.242875000
                                                  5.257291667
                                                               5.271166667
## 1995
         5.323666667
                       5.339041667
                                    5.351583333
                                                  5.356208333
                                                               5.359166667
  1996
         5.422750000
                       5.422000000
                                    5.415208333
                                                  5.412375000
                                                               5.414250000
  1997
         5.367041667
                       5.364000000
                                    5.364500000
                                                  5.362208333
                                                               5.356875000
   1998
         5.302000000
                       5.299083333
                                    5.297833333
                                                  5.296000000
                                                               5.292791667
   1999
##
         5.228375000
                       5.211541667
                                    5.195375000
                                                  5.184333333
                                                               5.177416667
##
   2000
                      5.023041667
                                    5.006375000
         5.041958333
                                                  4.988791667
                                                               4.969666667
         4.849666667
                                                  4.792791667
##
   2001
                       4.831791667
                                    4.814083333
                                                                4.772750000
  2002
##
         4.668125000
                       4.649583333
                                    4.631000000
                                                  4.616666667
                                                               4.607916667
   2003
         4.531208333
                       4.513291667
                                    4.499750000
                                                  4.489750000
                                                               4.478750000
##
##
  2004
         4.437416667
                       4.435833333
                                    4.432416667
                                                  4.427708333
                                                               4.423166667
   2005
                                                  4.344708333
         4.368708333
                       4.359166667
                                    4.351500000
                                                               4.338500000
  2006
         4.420083333
                       4.439375000
                                    4.458208333
                                                  4.473583333
##
                                                               4.488125000
   2007
         4.634541667
                       4.658291667
                                    4.679583333
                                                  4.702625000
                                                               4.722416667
##
  2008
         4.935375000
                       4.971500000
                                    5.006125000
                                                  5.035666667
                                                               5.059125000
  2009
         5.146583333
                      5.161125000
                                    5.174000000
                                                  5.185458333
                                                               5.196875000
  2010
         5.440416667
                      5.488208333
##
                                    5.534541667
                                                  5.573166667
                                                               5.606791667
##
  2011
         6.008125000
                      6.076083333
                                    6.144041667
                                                  6.209000000
                                                               6.265333333
  2012
         7.060458333
                      7.217041667
                                    7.363250000
                                                  7.508625000
                                                               7.640416667
  2013
         8.829250000
                      9.027375000
                                    9.245791667
                                                  9.467583333
                                                               9.677791667
  2014 11.881458333 12.241666667 12.590333333 12.908708333 13.172791667
  2015 15.178125000 15.526500000 15.796958333 15.956375000 16.091958333
  2016 18.498750000 19.016125000 19.524208333 20.010583333 20.421291667
  2017 24.926625000 25.523708333 26.083416667 26.637000000 27.017000000
  2018 30.275250000 30.790791667 31.239416667 31.523500000 31.744791667
   2019 33.740375000 34.281458333 34.736916667 35.159416667 35.513750000
   2020 39.655041667 40.379416667 40.861666667 41.266916667 41.741250000
  2021 47.830333333 48.648125000 49.715208333 50.681750000 51.436666667
   2022 59.136541667 60.355500000 61.356291667
                                                 62.376750000
                                                              63.128333333
##
   2023 67.544625000 68.824291667 69.965500000
                                                           NA
                                                                         NA
##
                  Jun
                               Jul.
                                            Aug
                                                          Sep
                                                                        Oct
## 1984
                       0.001500000
                                    0.001583333
                                                  0.001541667
                                                               0.001625000
                  NA
  1985
         0.003041667
                       0.003083333
                                    0.003166667
                                                  0.003375000
                                                               0.003541667
  1986
         0.004000000
                       0.003916667
##
                                    0.003833333
                                                  0.003833333
                                                               0.003791667
   1987
         0.003000000
                       0.003083333
                                    0.003208333
                                                  0.003291667
                                                               0.003250000
   1988
         0.002625000
                      0.120041667
                                    0.364083333
                                                  0.666333333
                                                               1.036083333
##
   1989
         4.230208333
                       4.382666667
                                    4.399708333
                                                  4.419875000
                                                               4.443000000
                                    4.677375000
##
   1990
         4.653708333
                       4.668083333
                                                  4.685083333
                                                               4.691416667
  1991
         4.832750000
                       4.839541667
                                    4.845916667
                                                  4.857291667
                                                               4.876000000
## 1992
         4.979916667
                       4.988833333
                                    4.997625000
                                                  5.011000000
                                                               5.029041667
         5.134875000
##
  1993
                       5.146083333
                                    5.156666667
                                                  5.168875000
                                                               5.181708333
   1994
         5.280125000
                       5.283458333
                                    5.283250000
                                                  5.282416667
                                                               5.285041667
  1995
         5.363916667
                       5.368625000
                                    5.373833333
                                                  5.384500000
                                                               5.397750000
   1996
         5.418083333
                       5.418916667
                                    5.416916667
                                                  5.412125000
                                                               5.402375000
##
   1997
         5.350791667
                      5.345708333
                                    5.338208333
                                                  5.331083333
                                                               5.326000000
## 1998
         5.289666667
                      5.284625000
                                    5.278791667
                                                  5.269916667
                                                               5.258166667
## 1999
         5.170708333
                      5.161625000
                                    5.150416667
                                                  5.134541667
                                                               5.111708333
## 2000
         4.953416667
                      4.939541667
                                   4.925958333
                                                 4.910541667
                                                               4.893458333
```

```
## 2001 4.755875000 4.743708333 4.737166667 4.729708333 4.719291667
                                                4.574791667
## 2002
        4.599250000 4.590958333 4.583416667
                                                             4.567166667
        4.468291667
                                   4.458250000
## 2003
                     4.462541667
                                                4.453708333
                                                             4.448791667
## 2004
        4.419916667
                      4.415708333
                                  4.410791667
                                                4.403208333
                                                             4.394250000
## 2005
        4.331791667
                      4.334125000
                                   4.346416667
                                                4.359958333
                                                             4.374625000
                                   4.525208333
## 2006
        4.501583333
                      4.513541667
                                               4.541750000
                                                             4.561833333
## 2007
         4.738208333
                      4.753416667
                                   4.771708333
                                                4.796833333
                                                             4.829375000
                                                             5.115416667
## 2008
        5.080333333
                      5.093041667
                                   5.097250000
                                                5.104750000
## 2009
         5.206458333
                      5.220416667
                                   5.240958333
                                                5.265458333
                                                             5.296791667
## 2010
        5.639375000
                      5.672708333
                                   5.713541667
                                                5.763458333
                                                             5.821125000
## 2011
        6.315750000
                      6.372208333
                                   6.429958333
                                                6.505291667
                                                             6.607000000
        7.758708333 7.868916667
                                   7.987583333 8.141666667
## 2012
                                                             8.315291667
## 2013 9.872541667 10.066250000 10.250583333 10.479750000 10.777541667
## 2014 13.354625000 13.489833333 13.670625000 13.922541667 14.234583333
## 2015 16.257916667 16.427625000 16.671833333 16.974166667 17.251291667
## 2016 20.755125000 21.066875000 21.327541667 21.769375000 22.475583333
## 2017 27.253500000 27.587750000 28.013500000 28.380250000 28.768583333
## 2018 31.919000000 32.045916667 32.152625000 32.373500000 32.734708333
## 2019 35.728875000 35.999250000 36.524208333 36.997041667 37.377875000
## 2020 42.309541667 42.830291667 43.197333333 43.874916667 44.948625000
## 2021 52.025458333 52.645916667 53.548208333 54.515291667 55.487500000
## 2022 63.518083333 63.824416667 64.061958333 64.377916667 64.911833333
## 2023
                  NA
                               NA
                                            NA
                                                         NΑ
                 Nov
                              Dec
## 1984 0.001875000
                      0.002083333
## 1985
        0.003625000
                      0.003666667
## 1986
        0.003666667
                      0.003625000
## 1987
        0.003166667
                      0.003125000
## 1988
        1.442875000
                      1.871000000
## 1989
        4.471833333
                      4.503708333
## 1990
        4.704083333
                      4.724625000
## 1991
         4.892750000
                      4.904083333
## 1992
        5.045750000
                      5.058125000
## 1993
        5.193708333
                      5.210250000
## 1994
        5.295416667
                      5.309291667
## 1995
        5.408041667
                      5.416708333
## 1996
        5.389375000
                      5.375875000
## 1997
        5.317541667
                      5.308166667
## 1998
         5.250666667
                      5.242541667
## 1999
         5.087291667
                      5.063208333
## 2000
        4.877666667
                      4.865166667
## 2001
        4.702333333
                      4.684250000
## 2002
        4.559166667
                      4.547750000
## 2003
        4.444916667
                      4.440833333
## 2004
        4.386583333
                      4.378416667
## 2005
                      4.404875000
         4.390166667
## 2006
         4.583500000
                      4.607958333
## 2007
         4.862625000
                      4.897833333
## 2008
        5.128208333
                      5.137333333
## 2009
        5.337583333
                      5.388666667
## 2010
        5.882083333
                      5.944916667
## 2011
        6.738500000
                      6.895083333
## 2012 8.482083333 8.652416667
## 2013 11.122416667 11.504791667
```

```
## 2014 14.562750000 14.859750000
## 2015 17.596791667 18.017625000
  2016 23.262333333 24.147166667
  2017 29.251250000 29.755541667
  2018 33.024958333 33.299583333
  2019 38.084583333 38.879708333
  2020 46.005875000 47.006458333
## 2021 56.525166667 57.759708333
   2022 65.700500000 66.535208333
##
  2023
##
##
   $random
##
                                  Feb
                   Jan
                                                 Mar
                                                                Apr
                                                                               May
## 1984
                    NA
                                   NA
                                                  NA
                                                                 NA
                                                                                NA
## 1985
                         3.154645702
                                       -0.035158785
          4.003914933
                                                      -1.401495998
                                                                     -2.801091393
  1986
          4.002456600
                         3.155437369
                                       -0.033075452
                                                      -1.401329332
                                                                     -2.801008060
## 1987
                                                                     -2.802174726
          4.000539933
                         3.155645702
                                       -0.032742118
                                                      -1.401787665
  1988
          4.003206600
                                       -0.031242118
                                                      -1.403370998
                                                                     -2.801799726
                         3.157312369
## 1989
                                                                     -1.625883060
                                        0.990757882
                                                      -0.332745998
          4.510789933
                         3.431437369
  1990
          2.485706600
                         1.848562369
                                       -0.136283785
                                                      -1.073162665
                                                                     -1.924216393
## 1991
          2.380831600
                         1.754729035
                                       -0.264200452
                                                      -1.186579332
                                                                     -1.886758060
## 1992
                                                                     -1.888549726
          2.284914933
                         1.679979035
                                       -0.221533785
                                                      -1.073120998
## 1993
          2.221664933
                                       -0.180242118
                                                      -1.002704332
                                                                     -1.875174726
                         1.641395702
## 1994
          2.210414933
                         1.602729035
                                       -0.138200452
                                                      -1.019829332
                                                                     -1.858258060
## 1995
          2.095539933
                         1.510187369
                                       -0.278908785
                                                      -1.023745998
                                                                     -1.792258060
## 1996
          2.053456600
                         1.495229035
                                       -0.154533785
                                                      -0.949912665
                                                                     -1.730341393
  1997
##
          2.059164933
                         1.555229035
                                       -0.220825452
                                                      -1.016745998
                                                                     -1.867966393
  1998
                                                      -1.034537665
##
          2.077206600
                         1.487145702
                                       -0.192158785
                                                                     -1.922883060
## 1999
          2.069831600
                         1.515687369
                                       -0.243700452
                                                      -1.050870998
                                                                     -1.859508060
## 2000
                                       -0.305700452
                                                                     -1.940758060
          2.117248266
                         1.574187369
                                                      -1.152329332
## 2001
          2.162539933
                         1.586437369
                                       -0.304408785
                                                      -1.175329332
                                                                     -1.903841393
## 2002
          2.259081600
                                       -0.228325452
                                                      -1.142204332
                                                                     -2.003008060
                         1.696645702
##
  2003
          2.320998266
                         1.726937369
                                       -0.198075452
                                                      -1.097287665
                                                                     -1.983841393
## 2004
                                       -0.175742118
                                                      -1.108245998
                                                                     -1.948258060
          2.375789933
                         1.740395702
   2005
                                       -0.225825452
          2.377498266
                         1.766062369
                                                      -1.109245998
                                                                     -1.963591393
                                                                     -1.923216393
## 2006
          2.465123266
                         1.841854035
                                       -0.163533785
                                                      -1.055120998
## 2007
          2.385664933
                         1.767937369
                                       -0.132908785
                                                      -1.054162665
                                                                     -1.867508060
## 2008
                                                                     -1.833216393
          2.274831600
                         1.703729035
                                       -0.105450452
                                                      -0.960204332
## 2009
                                                      -0.973995998
          2.104623266
                         1.574104035
                                       -0.153325452
                                                                     -1.799966393
## 2010
          2.048789933
                         1.502020702
                                       -0.180867118
                                                      -0.942704332
                                                                     -1.649883060
## 2011
          1.920081600
                         1.455145702
                                       -0.133367118
                                                      -0.851537665
                                                                     -1.572424726
## 2012
          1.550748266
                         1.017187369
                                       -0.247575452
                                                      -0.815162665
                                                                     -1.127508060
## 2013
          1.043956600
                         0.792854035
                                       -0.018117118
                                                      -0.719120998
                                                                     -1.216883060
##
  2014
          0.279748266
                        -0.285437631
                                        0.001341215
                                                      -0.377245998
                                                                     -0.217883060
## 2015
         -1.358918400
                        -0.889270965
                                        0.159716215
                                                       0.699087335
                                                                      0.614950274
## 2016
         -2.766543400
                        -0.430895965
                                       -0.259533785
                                                      -0.012120998
                                                                      1.234616940
## 2017
                        -4.509479298
                                                       2.135462335
         -5.367418400
                                        1.356257882
                                                                      4.746908607
## 2018
         -5.854043400
                        -4.420562631
                                       -0.353742118
                                                       3.122962335
                                                                      5.729116940
  2019
         -7.487168400
                        -7.182229298
                                        0.720757882
                                                       3.584045668
                                                                      4.829158607
   2020
         -8.909835067
                        -5.173187631
                                       -2.162992118
                                                       3.375545668
                                                                      9.663658607
  2021 -11.792126734
                        -9.925895965
                                        1.729466215
                                                       6.983712335
                                                                     12.319241940
## 2022 -13.324335067
                        -9.752270965
                                        1.417382882
                                                       7.292712335
                                                                     13.527575274
## 2023 -19.108418400 -15.144062631
                                       -2.685825452
                                                                               NA
                                                                 NA
##
                                                                Sep
                                                                               Oct
                   Jun
                                  Jul
                                                 Aug
```

```
## 1984
                        -3.216440836
                                       -2.641127802
                                                     -1.135323315
                                                                      0.363774976
## 1985
         -3.060551919
                        -3.215024170
                                       -2.638711135
                                                      -1.135156648
                                                                      0.362858309
## 1986
                                                                      0.363608309
         -3.061510253
                        -3.213857503
                                       -2.640377802
                                                      -1.135614982
## 1987
                        -3.213024170
                                       -2.641752802
         -3.059510253
                                                      -1.137073315
                                                                      0.362149976
##
  1988
         -3.060135253
                        -3.331982503
                                       -3.002627802
                                                      -1.800114982
                                                                     -0.672683358
## 1989
         -2.117718586
                        -2.122607503
                                       -1.653252802
                                                     -0.615656648
                                                                      0.421399976
## 1990
         -2.182218586
                        -2.052024170
                                       -1.538919469
                                                      -0.593864982
                                                                      0.453983309
## 1991
         -2.092260253
                        -1.922482503
                                       -1.453461135
                                                      -0.507073315
                                                                      0.422399976
## 1992
         -2.111426919
                        -1.930774170
                                       -1.435169469
                                                      -0.519781648
                                                                      0.449358309
## 1993
         -2.139385253
                        -1.917024170
                                       -1.398211135
                                                      -0.487656648
                                                                      0.424691642
## 1994
         -2.050635253
                        -1.915399170
                                       -1.454794469
                                                      -0.470198315
                                                                      0.536358309
## 1995
         -1.955426919
                        -1.834565836
                                       -1.342377802
                                                      -0.474281648
                                                                      0.436649976
##
  1996
         -1.918593586
                        -1.830857503
                                       -1.457461135
                                                      -0.592906648
                                                                      0.455024976
## 1997
         -1.980301919
                        -1.840649170
                                       -1.368752802
                                                      -0.509864982
                                                                      0.474399976
## 1998
                                                      -0.450698315
         -2.025176919
                        -1.821565836
                                       -1.337336135
                                                                      0.500233309
## 1999
         -2.049218586
                        -1.895565836
                                       -1.415961135
                                                      -0.496323315
                                                                      0.562691642
## 2000
                                                                      0.525941642
         -2.120926919
                        -1.894482503
                                       -1.424502802
                                                      -0.439323315
## 2001
         -2.063385253
                        -1.930649170
                                       -1.432711135
                                                      -0.486489982
                                                                      0.417108309
## 2002
         -2.076760253
                        -1.994899170
                                       -1.506961135
                                                      -0.549573315
                                                                      0.443233309
## 2003
         -2.109801919
                        -2.099482503
                                       -1.578794469
                                                      -0.556489982
                                                                      0.449608309
## 2004
         -2.139426919
                        -2.056649170
                                       -1.565336135
                                                      -0.553989982
                                                                      0.439149976
## 2005
                                                      -0.602739982
                                                                      0.387774976
         -2.147301919
                        -2.112065836
                                       -1.592961135
## 2006
         -2.154093586
                        -2.089482503
                                       -1.510752802
                                                      -0.593531648
                                                                      0.378566642
## 2007
         -2.093718586
                        -1.988357503
                                       -1.528252802
                                                      -0.566614982
                                                                      0.382024976
                                                                      0.413983309
## 2008
         -1.961843586
                        -1.900982503
                                       -1.413794469
                                                      -0.483531648
## 2009
         -2.039968586
                        -1.854357503
                                       -1.382502802
                                                      -0.510239982
                                                                      0.373608309
## 2010
                        -1.730649170
         -1.806885253
                                       -1.284086135
                                                      -0.467239982
                                                                      0.235274976
## 2011
         -1.711260253
                        -1.685149170
                                       -1.114502802
                                                      -0.464073315
                                                                      0.263399976
## 2012
                                       -0.945127802
         -1.216218586
                        -1.150857503
                                                      -0.318448315
                                                                      0.262108309
## 2013
         -1.190051919
                        -1.244190836
                                       -0.557127802
                                                      -0.065531648
                                                                      0.531858309
## 2014
          0.010864747
                        -0.310774170
                                        0.310830531
                                                       0.571676685
                                                                      0.635816642
## 2015
          0.483573081
                         1.016434164
                                        1.405622198
                                                      -0.084948315
                                                                     -0.949891691
## 2016
          1.137364747
                         2.773184164
                                        2.770913865
                                                       1.292843352
                                                                     -0.674183358
## 2017
          5.766989747
                         3.831309164
                                        2.835955531
                                                       1.363968352
                                                                     -0.363183358
## 2018
          7.494489747
                         5.453142497
                                        4.989830531
                                                       1.844718352
                                                                     -1.985308358
## 2019
          7.406614747
                         8.356809164
                                        6.747247198
                                                       2.023176685
                                                                     -1.290475024
## 2020
          8.846948081
                        12.112767497
                                        6.872122198
                                                      -0.078698315
                                                                     -3.911225024
## 2021
         10.794031414
                        10.407142497
                                        8.038247198
                                                       3.373926685
                                                                     -5.346100024
## 2022
         16.030406414
                        15.543642497
                                       10.464497198
                                                       4.590301685
                                                                     -1.358433358
## 2023
                    NA
                                  NA
                                                 NA
                                                                NA
##
                  Nov
                                 Dec
## 1984
          2.825131813
                         3.942805959
## 1985
          2.823381813
                         3.942222625
## 1986
                         3.942264292
          2.825340147
## 1987
          2.823840147
                         3.942764292
## 1988
          1.383131813
                         2.073889292
## 1989
          2.051173480
                         2.906180959
## 1990
          2.005923480
                         2.920264292
## 1991
          1.967256813
                         2.832805959
## 1992
          1.967256813
                         2.800764292
## 1993
          1.929298480
                         2.773639292
## 1994
          1.945590147
                         2.771597625
## 1995
          1.890965147
                         2.720180959
## 1996
          1.931631813
                         2.831014292
```

```
## 1997
          1.932465147
                         2.823722625
## 1998
          1.964340147
                         2.849347625
## 1999
          2.045715147
                         2.949680959
## 2000
          2.051340147
                         2.961722625
## 2001
          2.028673480
                         2.935639292
## 2002
          2.087840147
                         2.948139292
## 2003
          2.050090147
                         2.956055959
## 2004
          2.064423480
                         2.984472625
## 2005
          1.982840147
                         2.875014292
## 2006
          1.960506813
                         2.823930959
## 2007
          1.885381813
                         2.709055959
## 2008
          1.864798480
                         2.733555959
          1.788423480
## 2009
                         2.579222625
          1.664923480
## 2010
                         2.383972625
## 2011
          1.346506813
                         2.105805959
## 2012
          1.058923480
                         1.731472625
## 2013
          0.731590147
                         1.240097625
## 2014
          0.068256813
                        -0.527860708
                        -1.525735708
## 2015
         -1.142784853
## 2016
         -2.451326520
                        -4.000277375
## 2017
         -5.924243187
                        -6.448652375
## 2018
         -6.730951520
                        -8.778694041
## 2019
         -8.624576520 -12.361819041
## 2020 -10.111868187 -13.283569041
## 2021 -11.617159853 -18.919819041
## 2022 -16.166493187 -22.967319041
##
  2023
##
##
  $figure
##
    [1] -4.00420660 -3.15722904
                                  0.03232545
                                               1.40253766
                                                            2.80309139 3.06251025
##
         3.21594084
                      2.64254447
                                  1.13678165 -0.36339998 -2.82600681 -3.94488929
##
##
   $type
   [1] "additive"
##
##
## attr(,"class")
## [1] "decomposed.ts"
```

Q_5

Use the decompose function again but now change the type of the seasonal component from additive to multiplicative. What happened to the random component this time?

```
print(decompose(WindTS, type = "multiplicative"))
## $x
##
             Jan
                                                          Jun
                                                                  Jul
                                                                                    Sep
                      Feb
                               Mar
                                        Apr
                                                 May
                                                                           Aug
           0.000
                   0.001
                             0.001
                                     0.002
                                              0.003
                                                       0.002
                                                                0.002
                                                                         0.001
                                                                                  0.002
## 1984
## 1985
           0.002
                    0.004
                             0.002
                                     0.002
                                              0.001
                                                       0.001
                                                                0.000
                                                                         0.001
                                                                                  0.003
## 1986
           0.001
                   0.001
                             0.002
                                     0.002
                                              0.003
                                                       0.002
                                                                0.002
                                                                         0.002
                                                                                  0.000
                                     0.000
                                                                         0.001
## 1987
           0.000
                   0.000
                             0.000
                                              0.001
                                                       0.003
                                                                0.004
                                                                                  0.001
## 1988
           0.002
                   0.000
                             0.000
                                     0.000
                                              0.000
                                                       0.000
                                                                0.000
                                                                         0.000
                                                                                  0.000
## 1989
           0.497
                                     0.812
                                                       0.534
                   0.763
                             0.873
                                              0.697
                                                                0.485
                                                                         0.352
                                                                                  0.956
## 1990
           1.028
                    0.789
                             0.837
                                     1.434
                                              1.195
                                                       1.387
                                                                0.406
                                                                         0.239
                                                                                  0.311
                                                       0.530
                                                                         0.777
## 1991
           0.212
                    0.989
                             0.707
                                     0.813
                                              1.237
                                                                0.530
                                                                                  0.707
```

```
## 1992
          0.512
                   1.759
                            1.120
                                     1.088
                                             0.320
                                                      0.256
                                                               0.256
                                                                       0.480
                                                                                1.088
## 1993
          0.844
                   0.169
                                                      0.295
                                                                                0.464
                            1.773
                                     1.266
                                             1.266
                                                               0.464
                                                                       0.253
          0.000
                                                      1.256
## 1994
                   0.343
                            1.865
                                     1.408
                                             1.256
                                                               0.647
                                                                       0.457
                                                                                1.066
  1995
          0.019
                   0.080
                            0.016
                                     0.023
                                             1.394
                                                      1.701
                                                               2.115
                                                                       1.862
                                                                                1.955
##
##
  1996
          0.503
                   0.382
                            0.640
                                     0.834
                                             1.336
                                                      1.282
                                                               1.826
                                                                       1.416
                                                                                1.199
## 1997
          0.411
                   0.372
                            0.507
                                     1.106
                                             1.196
                                                      1.764
                                                               1.738
                                                                       1.809
                                                                                0.888
## 1998
          0.059
                   0.028
                            0.021
                                     0.293
                                             0.489
                                                      1.348
                                                                                1.623
                                                               1.868
                                                                       1.438
## 1999
                   1.054
                                     1.274
          1.150
                            1.524
                                             0.940
                                                      0.866
                                                               1.556
                                                                       1.304
                                                                                1.288
## 2000
          2.202
                   2.409
                            1.194
                                     1.126
                                             1.392
                                                      1.525
                                                               1.296
                                                                       1.284
                                                                                1.134
## 2001
                   1.471
                                                                       1.969
          1.328
                            1.816
                                     2.336
                                             2.167
                                                      2.285
                                                               2.167
                                                                                1.673
##
  2002
          2.769
                   2.436
                            2.907
                                     3.495
                                             3.677
                                                      3.843
                                                               3.038
                                                                       3.332
                                                                                2.511
  2003
          2.158
                   2.543
                            3.535
                                     3.729
                                             3.434
                                                      3.573
                                                               3.253
                                                                       2.782
                                                                                3.054
##
  2004
                   3.486
##
          3.410
                            4.406
                                     4.418
                                             5.806
                                                      4.767
                                                               3.973
                                                                       3.585
                                                                                3.718
## 2005
          3.861
                   3.298
                            5.325
                                     5.792
                                             5.959
                                                      6.131
                                                                       3.883
                                                                                5.010
                                                               4.848
## 2006
          8.130
                   6.558
                            8.048
                                     8.434
                                             8.389
                                                      7.001
                                                               6.671
                                                                       5.647
                                                                                6.412
## 2007
          8.367
                   8.598
                           10.397
                                    10.822
                                            10.073
                                                      8.941
                                                               7.364
                                                                       9.210
                                                                                9.781
## 2008
         14.580
                  13.142
                           16.316
                                    17.829
                                            18.221
                                                     17.539
                                                              13.677
                                                                      11.138
                                                                               10.616
## 2009
         20.304
                  19.968
                           24.222
                                    25.446
                                            21.366
                                                     19.105
                                                              16.906
                                                                      18.645
                                                                               15.868
## 2010
         23.387
                  18.533
                           29.306
                                   33.316
                                            29.676
                                                     27.463
                                                              22.942
                                                                      22.812
                                                                               24.244
## 2011
         29.174
                  35.661
                           35.978
                                   42.383
                                            40.167
                                                     37.481
                                                              25.551
                                                                      25.500
                                                                               23.437
## 2012
         46.514
                  37.709
                           47.858
                                   43.364
                                            42.788
                                                     40.850
                                                              30.099
                                                                      28.896
                                                                               29.990
## 2013
         50.288
                  48.026
                           53.758
                                   59.629
                                            55.406
                                                     46.909
                                                              37.851
                                                                      32.871
                                                                               39.832
## 2014
         61.113
                  47.798
                           60.515
                                   63.584
                                            53.232
                                                     53.906
                                                              41.583
                                                                      34.702
                                                                               39.305
                                                                               47.671
         51.733
                  50.912
                           52.231
                                    60.963
                                            58.520
                                                     45.793
                                                              46.661
                                                                      44.629
## 2015
         63.007
                                   70.967
## 2016
                  68.712
                           74.857
                                            64.309
                                                     55.627
                                                              60.114
                                                                      46.367
                                                                               55.969
## 2017
         70.965
                  75.375
                           87.793
                                   86.590
                                            78.707
                                                     68.724
                                                              55.001
                                                                      47.355
                                                                               61.115
## 2018
         87.343
                  79.123
                           90.294
                                   90.182
                                            81.728
                                                     84.286
                                                                      67.716
                                                                               63.189
                                                              56.116
         82.917
                  77.189
                           87.936
                                   98.659
                                                     76.586
## 2019
                                            87.959
                                                              75.408
                                                                      68.165
                                                                               83.640
         95.950
## 2020
                  99.325 100.039 101.515
                                            96.824 103.085
                                                              78.019
                                                                      78.576
                                                                               79.111
## 2021 102.566
                  91.153 133.768 123.370 115.280
                                                     91.003
                                                              74.093
                                                                      92.367
                                                                               98.941
## 2022 127.664 128.443 146.820 157.522 143.726 115.215 100.569
                                                                      84.339
                                                                               93.254
## 2023 133.636 143.503 151.927 146.775 109.246 93.850
                                                             95.085
                                                                      97.256
                                                                               96.196
##
             Oct
                     Nov
                              Dec
## 1984
          0.003
                   0.003
                            0.004
                   0.001
##
   1985
          0.002
                            0.000
## 1986
          0.001
                   0.000
                            0.000
## 1987
          0.000
                   0.000
                            0.001
## 1988
          0.000
                   0.000
                            0.000
## 1989
          0.599
                   0.419
                            0.219
## 1990
          0.693
                   0.789
                            0.406
## 1991
          1.448
                   1.448
                            0.671
  1992
          0.832
                   0.960
                            1.184
##
  1993
          0.971
                   1.562
##
                            0.929
## 1994
          1.218
                   1.675
                            0.571
## 1995
          0.876
                   0.427
                            0.329
## 1996
          0.863
                   0.337
                            0.417
                   0.248
## 1997
          0.937
                            0.244
## 1998
          1.019
                   0.618
                            1.519
##
  1999
          1.428
                   1.209
                            1.720
   2000
                   2.808
##
          1.404
                            1.309
## 2001
          2.071
                   1.605
                            2.101
## 2002
          2.506
                   2.238
                            2.577
## 2003
          3.061
                   3.280
                            3.770
## 2004
          3.511
                   3.181
                            3.999
```

```
## 2005
         4.934
                  5.492
                          6.237
         8.333
## 2006
                  8.668
                          8.433
                         11.909
## 2007
        11.521
                 10.560
## 2008
        16.229
                 17.038
                         22.573
## 2009
         23.248
                 23.458
                         23.563
## 2010
        27.104
                 33.259
                         30.910
## 2011
        35.913
                 42.440
                         36.358
## 2012
        43.113
                 39.745
                         49.557
## 2013
        46.523
                 53.921
                         47.656
## 2014
        49.501
                 64.374
                         50.195
## 2015
        55.889
                 67.154
                         68.576
                 66.212
## 2016
        69.384
                         78.973
## 2017
        83.146
                 77.162
                        75.749
## 2018
        72.314
                75.118
                         82.933
        94.255 85.929 90.909
## 2019
## 2020
        98.343 113.038 109.220
## 2021 109.918 121.983 135.965
## 2022 111.725 140.570 131.975
## 2023
##
## $seasonal
              Jan
                        Feb
                                  Mar
                                            Apr
                                                      May
## 1984 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 1985 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 1986 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 1987 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 1988 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 1989 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 1990 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 1991 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 1992 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 1993 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 1994 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 1995 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 1996 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 1997 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 1998 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 1999 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 2000 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 2001 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 2002 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 2003 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 2004 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 2005 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 2006 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 2007 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 2008 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 2009 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 2010 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 2011 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 2012 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 2013 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 2014 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 2015 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
```

```
## 2016 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 2017 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 2018 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 2019 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 2020 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 2021 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 2022 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
## 2023 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
##
                        Sep
                                            Nov
              Aug
                                  Oct
                                                      Dec
## 1984 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 1985 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 1986 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 1987 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 1988 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 1989 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 1990 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 1991 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 1992 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 1993 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 1994 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 1995 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 1996 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 1997 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 1998 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 1999 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2000 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2001 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2002 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2003 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2004 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2005 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2006 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2007 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2008 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2009 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2010 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2011 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2012 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2013 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2014 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2015 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2016 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2017 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2018 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2019 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2020 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2021 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2022 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
## 2023 0.8617504 0.9216537
##
## $trend
##
                 Jan
                              Feb
                                           Mar
                                                        Apr
                                                                      May
## 1984
                                                                       NA
                  NΑ
                               NA
                                            NΑ
                                                         NΑ
## 1985 2.166667e-03 2.083333e-03 2.125000e-03 2.125000e-03 2.000000e-03
```

```
## 1986 1.583333e-03 1.708333e-03 1.625000e-03 1.458333e-03 1.375000e-03
## 1987 8.333333e-04 8.750000e-04 8.750000e-04 8.750000e-04 8.333333e-04
## 1988 5.833333e-04 3.750000e-04 2.916667e-04 2.500000e-04 2.500000e-04
## 1989 3.682083e-01 4.030833e-01 4.575833e-01 5.223750e-01 5.647917e-01
## 1990 8.050417e-01 7.970417e-01 7.654583e-01 7.425000e-01 7.618333e-01
## 1991 6.161667e-01 6.437500e-01 6.826667e-01 7.306250e-01 7.895417e-01
## 1992 8.749167e-01 8.511250e-01 8.546250e-01 8.448333e-01 7.988333e-01
## 1993 8.764167e-01 8.756250e-01 8.401667e-01 8.199583e-01 8.508333e-01
## 1994 9.052083e-01 9.213333e-01 9.549167e-01 9.902917e-01 1.005292e+00
## 1995 8.000833e-01 9.197917e-01 1.015375e+00 1.038167e+00 9.719167e-01
## 1996 1.033042e+00 1.002417e+00 9.523333e-01 9.202917e-01 9.160000e-01
## 1997 9.475000e-01 9.602083e-01 9.636250e-01 9.537500e-01 9.531250e-01
## 1998 6.805833e-01 6.705417e-01 6.857083e-01 7.197500e-01 7.385833e-01
## 1999 1.228083e+00 1.209500e+00 1.189958e+00 1.193042e+00 1.234708e+00
## 2000 1.518583e+00 1.506917e+00 1.499667e+00 1.492250e+00 1.557875e+00
## 2001 1.756125e+00 1.820958e+00 1.871958e+00 1.922208e+00 1.899875e+00
## 2002 2.595708e+00 2.688792e+00 2.780500e+00 2.833542e+00 2.878042e+00
## 2003 2.940125e+00 2.926167e+00 2.925875e+00 2.971625e+00 3.038167e+00
## 2004 3.821083e+00 3.884542e+00 3.945667e+00 3.992083e+00 4.006708e+00
## 2005 4.397542e+00 4.446417e+00 4.512667e+00 4.625792e+00 4.781375e+00
## 2006 6.489625e+00 6.639083e+00 6.771000e+00 6.971042e+00 7.245000e+00
## 2007 8.475708e+00 8.653042e+00 8.941875e+00 9.215083e+00 9.426750e+00
## 2008 1.342738e+01 1.377075e+01 1.388588e+01 1.411683e+01 1.458292e+01
## 2009 1.860804e+01 1.905538e+01 1.958700e+01 2.009829e+01 2.065825e+01
## 2010 2.386558e+01 2.429071e+01 2.481333e+01 2.532300e+01 2.589204e+01
## 2011 3.195162e+01 3.217233e+01 3.225071e+01 3.258412e+01 3.333371e+01
## 2012 3.754633e+01 3.787733e+01 3.829187e+01 3.886492e+01 3.905262e+01
## 2013 4.494100e+01 4.542963e+01 4.600533e+01 4.655750e+01 4.729025e+01
## 2014 5.005567e+01 5.028746e+01 5.034179e+01 5.044392e+01 5.100354e+01
## 2015 5.019592e+01 5.082112e+01 5.158333e+01 5.219808e+01 5.258008e+01
## 2016 6.123212e+01 6.186508e+01 6.228325e+01 6.319129e+01 6.371433e+01
## 2017 7.021804e+01 7.004617e+01 7.030175e+01 7.108958e+01 7.211925e+01
## 2018 7.608679e+01 7.698162e+01 7.791642e+01 7.755150e+01 7.701500e+01
## 2019 7.818983e+01 7.901238e+01 7.988321e+01 8.164954e+01 8.301421e+01
## 2020 9.136246e+01 9.190504e+01 9.215013e+01 9.213175e+01 9.343163e+01
## 2021 1.009570e+02 1.013680e+02 1.027689e+02 1.040775e+02 1.049325e+02
## 2022 1.221579e+02 1.229266e+02 1.223551e+02 1.221935e+02 1.230432e+02
## 2023 1.198856e+02 1.201953e+02 1.208561e+02
                                                         NA
                                                                       NΑ
##
                 Jun.
                              J<sub>11</sub>]
                                           Aug
                                                        Sep
                                                                      Oct
## 1984
                  NA 2.083333e-03 2.291667e-03 2.458333e-03 2.500000e-03
## 1985 1.750000e-03 1.541667e-03 1.375000e-03 1.250000e-03 1.250000e-03
## 1986 1.333333e-03 1.291667e-03 1.208333e-03 1.083333e-03 9.166667e-04
## 1987 8.750000e-04 1.000000e-03 1.083333e-03 1.083333e-03 1.083333e-03
## 1988 2.083333e-04 2.079167e-02 7.320833e-02 1.413750e-01 2.115833e-01
## 1989 5.913750e-01 6.226250e-01 6.458333e-01 6.454167e-01 6.698333e-01
## 1990 7.850417e-01 7.588333e-01 7.331667e-01 7.360833e-01 7.047917e-01
## 1991 8.280417e-01 8.515833e-01 8.961667e-01 9.454583e-01 9.741250e-01
## 1992 7.998750e-01 8.350833e-01 7.826667e-01 7.436250e-01 7.782500e-01
## 1993 8.652917e-01 8.195000e-01 7.915833e-01 8.026667e-01 8.124167e-01
## 1994 9.950833e-01 9.809583e-01 9.707917e-01 8.827917e-01 7.480417e-01
## 1995 9.098333e-01 9.199167e-01 9.526667e-01 9.912500e-01 1.051042e+00
## 1996 9.159167e-01 9.157500e-01 9.115000e-01 9.055417e-01 9.113333e-01
## 1997 9.422083e-01 9.203333e-01 8.913333e-01 8.567500e-01 8.026250e-01
## 1998 8.071250e-01 9.057083e-01 9.939167e-01 1.099292e+00 1.202792e+00
```

```
## 1999 1.267708e+00 1.319917e+00 1.420208e+00 1.462917e+00 1.443000e+00
## 2000 1.607375e+00 1.553833e+00 1.478333e+00 1.465167e+00 1.541500e+00
## 2001 1.882750e+00 1.975792e+00 2.076042e+00 2.161708e+00 2.255458e+00
## 2002 2.924250e+00 2.918625e+00 2.897625e+00 2.928250e+00 2.964167e+00
## 2003 3.131292e+00 3.233167e+00 3.324625e+00 3.400208e+00 3.465208e+00
## 2004 4.012125e+00 4.040458e+00 4.051417e+00 4.081875e+00 4.177417e+00
## 2005 4.970917e+00 5.242042e+00 5.555750e+00 5.805042e+00 6.028583e+00
## 2006 7.468833e+00 7.570208e+00 7.665083e+00 7.847958e+00 8.045333e+00
## 2007 9.650417e+00 1.005413e+01 1.050233e+01 1.093829e+01 1.147687e+01
## 2008 1.529717e+01 1.598000e+01 1.650292e+01 1.711675e+01 1.776354e+01
## 2009 2.096700e+01 2.113671e+01 2.120538e+01 2.135742e+01 2.189717e+01
## 2010 2.660654e+01 2.715379e+01 2.810858e+01 2.910025e+01 2.975604e+01
## 2011 3.394325e+01 3.489275e+01 3.570058e+01 3.628092e+01 3.681679e+01
## 2012 3.949029e+01 4.019750e+01 4.078462e+01 4.146033e+01 4.238387e+01
## 2013 4.780171e+01 4.817354e+01 4.861508e+01 4.888712e+01 4.933346e+01
## 2014 5.154488e+01 5.125983e+01 5.099875e+01 5.078333e+01 5.032896e+01
## 2015 5.346179e+01 5.469742e+01 5.590883e+01 5.759325e+01 5.895283e+01
## 2016 6.410829e+01 6.487308e+01 6.548229e+01 6.629892e+01 6.748887e+01
## 2017 7.244117e+01 7.298925e+01 7.382783e+01 7.408821e+01 7.434208e+01
## 2018 7.722917e+01 7.734408e+01 7.707908e+01 7.690025e+01 7.715521e+01
## 2019 8.379700e+01 8.467238e+01 8.613775e+01 8.756437e+01 8.818767e+01
## 2020 9.532413e+01 9.636275e+01 9.629792e+01 9.736279e+01 9.967879e+01
## 2021 1.064195e+02 1.085797e+02 1.111792e+02 1.132768e+02 1.152436e+02
## 2022 1.236514e+02 1.237340e+02 1.246103e+02 1.254506e+02 1.252156e+02
## 2023
                  NΑ
                               NΑ
                                            NΑ
                                                         NΑ
                 Nov
## 1984 2.416667e-03 2.291667e-03
## 1985 1.333333e-03 1.458333e-03
## 1986 7.500000e-04 7.083333e-04
## 1987 1.041667e-03 8.750000e-04
## 1988 2.744583e-01 3.257500e-01
## 1989 7.165000e-01 7.727917e-01
## 1990 6.806667e-01 6.467083e-01
## 1991 9.473750e-01 8.977500e-01
## 1992 8.250833e-01 8.661250e-01
## 1993 8.179167e-01 8.575417e-01
## 1994 6.960833e-01 7.203750e-01
## 1995 1.082417e+00 1.062542e+00
## 1996 9.168333e-01 9.310833e-01
## 1997 7.392917e-01 6.925000e-01
## 1998 1.262458e+00 1.261167e+00
## 1999 1.455667e+00 1.501958e+00
## 2000 1.624208e+00 1.688167e+00
## 2001 2.366667e+00 2.494500e+00
## 2002 2.963792e+00 2.942417e+00
## 2003 3.592750e+00 3.741333e+00
## 2004 4.241042e+00 4.304250e+00
## 2005 6.239917e+00 6.377417e+00
## 2006 8.215000e+00 8.366000e+00
## 2007 1.210833e+01 1.280608e+01
## 2008 1.821196e+01 1.840825e+01
## 2009 2.257133e+01 2.326583e+01
## 2010 3.057096e+01 3.142550e+01
## 2011 3.696687e+01 3.721646e+01
```

```
## 2012 4.358733e+01 4.436554e+01
## 2013 4.940767e+01 4.960862e+01
## 2014 5.044008e+01 5.032237e+01
## 2015 5.961087e+01 6.026183e+01
## 2016 6.873975e+01 6.988537e+01
## 2017 7.461763e+01 7.539192e+01
## 2018 7.776804e+01 7.770683e+01
## 2019 8.867604e+01 9.014954e+01
## 2020 1.013584e+02 1.016240e+02
## 2021 1.178518e+02 1.200459e+02
## 2022 1.233312e+02 1.210043e+02
##
  2023
##
##
  $random
##
                         Feb
                                   Mar
                                                         May
                                                                    Jun
              Jan
                                              Apr
                                    NA
                                               NA
                                                          NA
## 1984
               NA
                          NA
                                                                    NA
  1985 0.96689012 2.08065782 0.86681649 0.83426193 0.43577040 0.50959339
  1986 0.66155640 0.63434689 1.13352926 1.21563881 1.90154358 1.33768264
## 1989 1.41384566 2.05129976 1.75711485 1.37785974 1.07555401 0.80526742
## 1990 1.33756219 1.07274231 1.00707080 1.71192234 1.36708545 1.57559860
## 1991 0.36039345 1.66486293 0.95382087 0.98634167 1.36547066 0.57080203
## 1992 0.61297463 2.23960756 1.20697572 1.14153497 0.34912546 0.28541689
## 1993 1.00872096 0.20915487 1.94356644 1.36858976 1.29681175 0.30403342
## 1994 0.00000000 0.40343797 1.79874445 1.26029118 1.08889319 1.12562056
## 1995 0.02487469 0.09425403 0.01451275 0.01963777 1.25003298 1.66726373
## 1996 0.51002254 0.41296621 0.61893792 0.80328920 1.27115559 1.24822793
## 1997 0.45436182 0.41983332 0.48456942 1.02790254 1.09362655 1.66960398
## 1998 0.09080503 0.04525137 0.02820564 0.36084219 0.57702826 1.48939854
## 1999 0.98086498 0.94435258 1.17953088 0.94655353 0.66351570 0.60920068
## 2000 1.51886059 1.73239530 0.73327300 0.66884913 0.77874335 0.84608592
  2001 0.79210340 0.87541120 0.89346135 1.07721836 0.99408063 1.08231924
## 2002 1.11739389 0.98179217 0.96289346 1.09332415 1.11348476 1.17197330
## 2003 0.76882035 0.94177408 1.11272989 1.11232000 0.98509116 1.01758647
## 2004 0.93477502 0.97249423 1.02844294 0.98097396 1.26292345 1.05957701
## 2005 0.91966374 0.80378506 1.08678206 1.10987444 1.08619627 1.09990877
## 2006 1.31223063 1.07044098 1.09469027 1.07242587 1.00915884 0.83592852
## 2007 1.03402965 1.07678272 1.07086704 1.04097339 0.93128921 0.82623172
## 2008 1.13738012 1.03419707 1.08217264 1.11949218 1.08896906 1.02248198
## 2009 1.14293139 1.13557677 1.13893301 1.12225550 0.90139973 0.81259207
## 2010 1.02645919 0.82680859 1.08774611 1.16618933 0.99891099 0.92049489
## 2011 0.95640592 1.20118636 1.02743383 1.15296732 1.05020357 0.98473546
## 2012 1.29764347 1.07885990 1.15107605 0.98901519 0.95490349 0.92249400
## 2013 1.17208973 1.14560974 1.07619513 1.13527020 1.02111090 0.87513406
## 2014 1.27884992 1.03002905 1.10710923 1.11730158 0.90962037 0.93263873
## 2015 1.07953941 1.08561370 0.93255626 1.03524499 0.96999785 0.76386642
## 2016 1.07782610 1.20361176 1.10692260 0.99547551 0.87967518 0.77380809
## 2017 1.05860690 1.16611769 1.15013775 1.07967523 0.95115191 0.84602817
## 2018 1.20242517 1.11382024 1.06729881 1.03076823 0.92487551 0.97327580
## 2019 1.11079143 1.05866787 1.01383507 1.07106129 0.92345466 0.81504718
## 2020 1.10006014 1.17116658 0.99983772 0.97667993 0.90318527 0.96439395
## 2021 1.06415823 0.97447195 1.19879951 1.05071335 0.95748471 0.76259887
## 2022 1.09467716 1.13230666 1.10514473 1.14268000 1.01804135 0.83094401
```

```
## 2023 1.16760443 1.29381731 1.15777069
                                                NA
                                                           NA
                                                                      NA
##
              Jul
                                    Sep
                                               Oct.
                                                          Nov
                                                                     Dec
                         Aug
## 1984 0.94636600 0.50636895 0.88271697 1.21431685 1.30057838 1.94079554
## 1985 0.00000000 0.84394825 2.60401506 1.61908913 0.78576610 0.00000000
## 1986 1.52639677 1.92070980 0.00000000 1.10392441 0.00000000 0.00000000
## 1987 3.94319166 1.07116508 1.00154425 0.00000000 0.00000000 1.27075899
## 1989 0.76789719 0.63247115 1.60712614 0.90492136 0.61267457 0.31510328
## 1990 0.52743328 0.37828028 0.45842221 0.99500039 1.21443576 0.69805368
## 1991 0.61353114 1.00612223 0.81135192 1.50419676 1.60132199 0.83107142
## 1992 0.30220249 0.71167697 1.58747598 1.08181992 1.21900488 1.51999574
## 1993 0.55815770 0.37088767 0.62721293 1.20945908 2.00080147 1.20456912
## 1994 0.65019199 0.54627166 1.31018080 1.64767774 2.52107405 0.88135063
## 1995 2.26646898 2.26807400 2.13991149 0.84340262 0.41330002 0.34428743
## 1996 1.96567512 1.80270679 1.43662359 0.95826211 0.38509824 0.49798785
## 1997 1.86162634 2.35514110 1.12458193 1.18134755 0.35145352 0.39177912
## 1998 2.03318269 1.67891004 1.60190897 0.85730341 0.51286546 1.33923420
## 1999 1.16212000 1.06547692 0.95527525 1.00141168 0.87015454 1.27333244
## 2000 0.82222081 1.00788543 0.83976598 0.92166767 1.81128752 0.86217528
## 2001 1.08119905 1.10059659 0.83971342 0.92917190 0.71050963 0.93651295
## 2002 1.02611814 1.33438554 0.93040238 0.85551814 0.79112377 0.97382628
## 2003 0.99184513 0.97103073 0.97453122 0.89389139 0.95648656 1.12043377
## 2004 0.96933932 1.02683524 0.98828439 0.85049900 0.78582014 1.03305908
## 2005 0.91169598 0.81104175 0.93640696 0.82819890 0.92211219 1.08743221
## 2006 0.86870237 0.85490808 0.88648027 1.04811302 1.10546084 1.12081899
## 2007 0.72203358 1.01763573 0.97021059 1.01582127 0.91371673 1.03402304
## 2008 0.84372704 0.78318619 0.67293304 0.92451290 0.98015327 1.36347764
## 2009 0.78848131 1.02031658 0.80613118 1.07435658 1.08884433 1.12611622
## 2010 0.83289200 0.94176581 0.90394042 0.92174121 1.13980921 1.09367441
## 2011 0.72187267 0.82886420 0.70089993 0.98708947 1.20280344 1.08626600
## 2012 0.73814370 0.82216648 0.78483060 1.02933884 0.95533179 1.24202536
## 2013 0.77456287 0.78462185 0.88403583 0.95428243 1.14339324 1.06814851
## 2014 0.79969895 0.78961154 0.83976708 0.99528350 1.33710874 1.10909966
## 2015 0.84095958 0.92630763 0.89807979 0.95933973 1.18026198 1.26532198
## 2016 0.91347987 0.82168175 0.91595337 1.04034628 1.00916176 1.25650314
## 2017 0.74284735 0.74432779 0.89501636 1.13176800 1.08341309 1.11718054
## 2018 0.71523294 1.01946723 0.89155057 0.94843574 1.01198688 1.18669580
## 2019 0.87793745 0.91830390 1.03637952 1.08155179 1.01523244 1.12128135
## 2020 0.79814002 0.94687258 0.88160919 0.99836986 1.16841379 1.19502538
## 2021 0.67269248 0.96407748 0.94769320 0.96516783 1.08441369 1.25936314
## 2022 0.80124065 0.78540363 0.80654182 0.90290615 1.19413061 1.21272447
##
  2023
               NΑ
                          NΑ
                                     NΑ
##
## $figure
    [1] 0.9546865 0.9227851 1.0857851 1.1281546 1.1473932 1.1213422 1.0144067
    [8] 0.8617504 0.9216537 0.9882100 0.9544825 0.8993500
##
##
## $type
  [1] "multiplicative"
##
## attr(,"class")
## [1] "decomposed.ts"
```

```
## $x
##
           Jan
                   Feb
                          Mar
                                 Apr
                                         May
                                                Jun
                                                       Jul
                                                               Aug
                                                                      Sep
                                                                              Oct
## 1984
         0.000
                0.000
                        0.001
                               0.001
                                      0.002
                                              0.003
                                                     0.001
                                                             0.003
                                                                    0.003
                                                                           0.002
## 1985
         0.002
                0.000
                        0.000
                               0.004
                                      0.005
                                              0.005
                                                     0.004
                                                             0.007
                                                                    0.005
                                                                           0.003
## 1986
         0.002
                0.002
                        0.003
                               0.005
                                      0.006
                                              0.005
                                                     0.006
                                                             0.006
                                                                    0.005
                                                                           0.004
                0.002
                                                                    0.003
## 1987
         0.000
                        0.003
                               0.004
                                      0.004
                                              0.006
                                                     0.006
                                                             0.004
                                                                           0.002
         0.002 0.003
                       0.004
                               0.002
                                      0.004
                                              0.005
                                                     0.004
                                                             0.004
                                                                    0.003
## 1988
                                                                           0.000
## 1989
         2.821
                3.041
                        4.220
                               4.660
                                      5.109
                                              5.175
                                                     5.476
                                                             5.389
                                                                    4.941
                                                                           4.501
## 1990
         3.015
                3.256
                        4.489
                               4.946
                                      5.515
                                              5.534
                                                     5.832
                                                            5.781
                                                                    5.228
                                                                           4.782
## 1991
         3.125
                3.369
                        4.561
                               5.026
                                      5.739
                                              5.803
                                                     6.133
                                                             6.035
                                                                    5.487
         3.196
                3.451
                        4.752
                               5.284
                                      5.883
                                              5.931
                                                     6.274
                                                             6.205
                                                                    5.628
## 1992
                                                                           5.115
## 1993
         3.288
                3.570
                        4.954
                               5.515
                                      6.053
                                              6.058
                                                     6.445
                                                             6.401
                                                                    5.818
                                                                           5.243
## 1994
         3.432
                3.680
                       5.137
                               5.640
                                      6.216
                                              6.292
                                                     6.584
                                                             6.471
                                                                    5.949
                                                                           5.458
## 1995
         3.415
                3.692
                        5.105
                               5.735
                                      6.370
                                              6.471
                                                     6.750
                                                             6.674
                                                                    6.047
## 1996
         3.472
                3.760
                        5.293
                               5.865
                                      6.487
                                              6.562
                                                     6.804
                                                             6.602
                                                                    5.956
                                                                           5.494
                3.762
                               5.748
                                      6.292
                                              6.433
                                                     6.721
                                                                    5.958
  1997
         3.422
                        5.176
                                                             6.612
                                                                           5.437
         3.375
## 1998
                3.629
                        5.138
                               5.664
                                      6.173
                                              6.327
                                                     6.679
                                                             6.584
                                                                    5.956
                                                                           5.395
## 1999
         3.294
                3.570
                        4.984
                               5.536
                                      6.121
                                              6.184
                                                     6.482
                                                             6.377
                                                                    5.775
                                                                           5.311
## 2000
         3.155
                3.440
                        4.733
                               5.239
                                      5.832
                                              5.895
                                                     6.261
                                                             6.144
                                                                    5.608
                                                                           5.056
## 2001
         3.008
                3.261
                        4.542
                               5.020
                                      5.672
                                              5.755
                                                     6.029
                                                             5.947
                                                                    5.380
                                                                           4.773
## 2002
         2.923
                3.189
                        4.435
                                      5.408
                                              5.585
                                                     5.812
                                                                    5.162
                                                                           4.647
                               4.877
                                                            5.719
## 2003
         2.848
                3.083
                        4.334
                               4.795
                                      5.298
                                              5.421
                                                     5.579
                                                             5.522
                                                                    5.034
                                                                           4.535
                               4.722
                                      5.278
## 2004
         2.809
                3.019
                        4.289
                                              5.343
                                                     5.575
                                                             5.488
                                                                    4.986
                                                                           4.470
## 2005
         2.742
                2.968
                        4.158
                               4.638
                                      5.178
                                              5.247
                                                     5.438
                                                             5.396
                                                                    4.894
                                                                           4.399
## 2006
        2.881
                3.124
                        4.327
                               4.821
                                      5.368
                                             5.410
                                                     5.640
                                                             5.657
                                                                    5.085
                                                                           4.577
                                             5.707
## 2007
         3.016
                3.269
                        4.579
                               5.051
                                      5.658
                                                     5.981
                                                             5.886
                                                                    5.367
                                                                           4.848
## 2008
         3.206
                3.518
                        4.933
                               5.478
                                      6.029
                                              6.181
                                                     6.408
                                                             6.326
                                                                    5.758
                                                                           5.166
## 2009
         3.247
                3.578
                       5.053
                               5.614
                                      6.200
                                              6.229
                                                     6.582
                                                             6.501
                                                                    5.892
                                                                           5.307
## 2010
         3.485
                3.833
                        5.386
                               6.033
                                      6.760
                                              6.895
                                                     7.158
                                                             7.072
                                                                    6.433
                4.374
## 2011
         3.924
                        6.043
                               6.760
                                      7.496
                                              7.667
                                                     7.903
                                                            7.958
                                                                    7.178
                                                                           6.507
         4.607
                5.077
                        7.148
                               8.096
                                      9.316
                                             9.605
                                                     9.934
                                                            9.685
                                                                    8.960
## 2012
## 2013
        5.869
                6.663
                       9.260 10.151 11.264 11.745 12.038 12.336 11.551 10.946
         8.157 8.799 12.624 13.934 15.758 16.428 16.395 16.624 15.631 14.507
        9.815 11.480 15.989 18.058 19.510 19.804 20.660 20.720 18.026 15.938
## 2015
## 2016 11.728 15.428 19.297 21.401 24.459 24.955 27.056 26.741 24.199 21.438
## 2017 15.555 17.857 27.472 30.175 34.567 36.083 34.635 33.492 30.881 28.042
## 2018 20.417 23.213 30.918 36.049 40.277 42.476 40.715 39.785 35.355 30.386
## 2019 22.249 23.942 35.490 40.146 43.146 46.198 47.572 45.914 40.157 35.724
## 2020 26.741 32.049 38.731 46.045 54.208 54.219 58.159 52.712 44.933 40.674
## 2021 32.034 35.565 51.477 59.068 66.559 65.882 66.269 64.229 59.026 49.778
## 2022 41.808 47.446 62.806 71.072 79.459 82.611 82.584 77.169 70.105 63.190
## 2023 44.432 50.523 67.312 79.380 90.079 92.024 97.397 93.068 81.595
##
           Nov
                   Dec
## 1984
         0.001
                0.000
         0.001
## 1985
                0.001
  1986
         0.003
                0.001
## 1987
         0.001
                0.001
## 1988
         0.000
                0.000
         3.697
## 1989
                3.465
         3.884
## 1990
                3.700
## 1991
         4.034
                3.792
## 1992
         4.187
               3.914
```

```
## 1993 4.297 4.039
## 1994
        4.415
              4.136
        4.473 4.192
## 1995
## 1996
        4.495
               4.262
## 1997
        4.424
               4.187
## 1998
        4.389 4.147
## 1999
        4.307 4.068
## 2000
        4.103 3.882
## 2001
        3.905
               3.675
## 2002
        3.821
               3.551
## 2003
        3.669
               3.452
## 2004
        3.625
               3.418
        3.547
## 2005
               3.335
## 2006
        3.718 3.487
        3.922 3.662
## 2007
## 2008
        4.167
               3.926
## 2009
        4.300
               4.023
## 2010
        4.721
               4.384
## 2011 5.259 5.056
## 2012
        6.715 6.439
## 2013 9.028 8.800
## 2014 11.805 10.387
## 2015 13.628 12.547
## 2016 17.985 16.202
## 2017 20.501 19.362
## 2018 23.468 20.576
## 2019 26.634 22.573
## 2020 33.068 29.778
## 2021 42.082 34.895
## 2022 46.708 39.623
## 2023
##
## $seasonal
##
              Jan
                       Feb
                                  Mar
                                            Apr
                                                      May
                                                                Jun
## 1984 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 1985 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 1986 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 1987 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 1988 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 1989 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 1990 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 1991 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 1992 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 1993 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 1994 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 1995 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 1996 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 1997 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 1998 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 1999 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 2000 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 2001 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 2002 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 2003 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
```

```
## 2004 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 2005 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 2006 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 2007 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 2008 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 2009 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 2010 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 2011 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 2012 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 2013 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 2014 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 2015 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 2016 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 2017 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 2018 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 2019 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 2020 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 2021 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 2022 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
## 2023 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
##
                        Sep
                                  Oct
                                                      Dec
              Aug
                                            Nov
## 1984 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 1985 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 1986 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 1987 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 1988 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 1989 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 1990 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 1991 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 1992 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 1993 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 1994 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 1995 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 1996 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 1997 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 1998 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 1999 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 2000 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 2001 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 2002 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 2003 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 2004 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 2005 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 2006 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 2007 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 2008 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 2009 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 2010 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 2011 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 2012 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 2013 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 2014 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 2015 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 2016 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
```

```
## 2017 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
## 2018 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
  2019 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
  2020 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
  2021 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
  2022 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
  2023 1.2632000 1.1225122
##
##
  $trend
##
                 Jan
                               Feb
                                            Mar
                                                          Apr
                                                                        May
##
  1984
                  NA
                                NA
                                             ΝA
                                                           NA
                                                                         NA
                                    0.002833333
##
  1985
         0.002291667
                       0.002583333
                                                  0.002958333
                                                               0.003000000
   1986
         0.003750000
                      0.003791667
                                    0.003750000
                                                  0.003791667
                                                               0.003916667
         0.003666667
                                                  0.003250000
   1987
                       0.003583333
                                    0.003416667
                                                               0.003083333
  1988
         0.003000000
                       0.002916667
                                    0.002916667
                                                  0.002833333
                                                               0.002708333
  1989
                       2.766791667
                                    3.196916667
                                                  3.590208333
         2.314416667
                                                               3.931791667
##
  1990
                       4.56466667
         4.533500000
                                    4.592958333
                                                  4.616625000
                                                               4.636125000
  1991
                                    4.792875000
         4.748375000
                       4.771500000
                                                  4.810041667
                                                               4.822666667
  1992
         4.915291667
                       4.928250000
                                    4.941208333
                                                  4.954583333
                                                               4.968458333
                      5.085833333
  1993
         5.070541667
                                    5.101916667
                                                  5.115166667
                                                               5.125083333
##
  1994
         5.225791667
                      5.234500000
                                    5.242875000
                                                 5.257291667
                                                               5.271166667
  1995
                      5.339041667
         5.323666667
                                    5.351583333
                                                  5.356208333
                                                               5.359166667
## 1996
         5.422750000
                      5.422000000
                                    5.415208333
                                                  5.412375000
                                                               5.414250000
  1997
         5.367041667
                      5.364000000
                                    5.364500000
                                                  5.362208333
                                                               5.356875000
## 1998
         5.302000000
                      5.299083333
                                    5.297833333
                                                  5.296000000
                                                               5.292791667
  1999
         5.228375000
                      5.211541667
                                    5.195375000
                                                  5.184333333
                                                               5.177416667
  2000
##
         5.041958333
                      5.023041667
                                    5.006375000
                                                  4.988791667
                                                               4.969666667
##
  2001
         4.849666667
                      4.831791667
                                    4.814083333
                                                  4.792791667
                                                               4.772750000
##
  2002
         4.668125000
                      4.649583333
                                    4.631000000
                                                  4.616666667
                                                               4.607916667
## 2003
         4.531208333
                      4.513291667
                                    4.499750000
                                                  4.489750000
                                                               4.478750000
##
  2004
         4.437416667
                       4.435833333
                                    4.432416667
                                                  4.427708333
                                                               4.423166667
##
  2005
         4.368708333
                      4.359166667
                                    4.351500000
                                                  4.344708333
                                                               4.338500000
  2006
         4.420083333
                       4.439375000
                                    4.458208333
                                                  4.473583333
                                                               4.488125000
  2007
         4.634541667
                       4.658291667
                                    4.679583333
                                                  4.702625000
                                                               4.722416667
##
   2008
         4.935375000
                      4.971500000
                                    5.006125000
                                                  5.035666667
                                                               5.059125000
                                                 5.185458333
##
  2009
         5.146583333
                      5.161125000
                                    5.174000000
                                                               5.196875000
  2010
         5.440416667
                      5.488208333
                                    5.534541667
                                                  5.573166667
                                                               5.606791667
## 2011
         6.008125000
                      6.076083333
                                    6.144041667
                                                  6.209000000
                                                               6.265333333
                      7.217041667
                                    7.363250000
  2012
         7.060458333
                                                  7.508625000
                                                               7.640416667
                                                 9.467583333
  2013
        8.829250000
                      9.027375000
                                    9.245791667
                                                               9.677791667
  2014 11.881458333 12.241666667 12.590333333 12.908708333 13.172791667
  2015 15.178125000 15.526500000 15.796958333 15.956375000 16.091958333
  2016 18.498750000 19.016125000 19.524208333 20.010583333 20.421291667
  2017 24.926625000 25.523708333 26.083416667 26.637000000 27.017000000
  2018 30.275250000 30.790791667 31.239416667 31.523500000 31.744791667
  2019 33.740375000 34.281458333 34.736916667 35.159416667 35.513750000
  2020 39.655041667 40.379416667 40.861666667 41.266916667 41.741250000
  2021 47.830333333 48.648125000 49.715208333 50.681750000 51.436666667
  2022 59.136541667 60.355500000 61.356291667
                                                62.376750000 63.128333333
##
   2023 67.544625000 68.824291667
                                   69.965500000
                                                           NA
                                                                         NA
##
                                                          Sep
                                                                        Oct
                 Jun
                               Jul
                                            Aug
## 1984
                  NA
                      0.001500000
                                    0.001583333
                                                  0.001541667
                                                               0.001625000
## 1985
                      0.003083333
                                    0.003166667
                                                  0.003375000
                                                               0.003541667
         0.003041667
## 1986
        0.004000000
                      0.003916667
                                    0.003833333
                                                 0.003833333
                                                               0.003791667
```

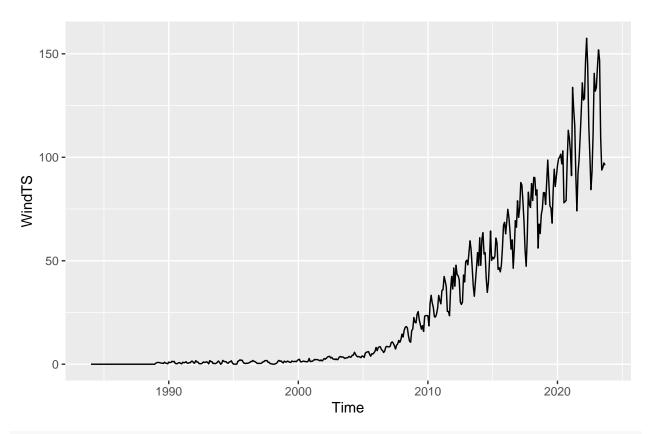
```
## 1987
        0.003000000 0.003083333 0.003208333 0.003291667
                                                              0.003250000
## 1988
        0.002625000
                      0.120041667
                                   0.364083333
                                                0.666333333
                                                              1.036083333
        4.230208333
                                   4.399708333
## 1989
                      4.382666667
                                                4.419875000
                                                              4.443000000
## 1990
        4.653708333
                      4.668083333
                                   4.677375000
                                                4.685083333
                                                              4.691416667
  1991
         4.832750000
                      4.839541667
                                   4.845916667
                                                 4.857291667
                                                              4.876000000
                                   4.997625000
## 1992
         4.979916667
                      4.988833333
                                                5.011000000
                                                              5.029041667
## 1993
         5.134875000
                      5.146083333
                                   5.156666667
                                                 5.168875000
                                                              5.181708333
## 1994
         5.280125000
                      5.283458333
                                   5.283250000
                                                 5.282416667
                                                              5.285041667
## 1995
         5.363916667
                      5.368625000
                                   5.373833333
                                                 5.384500000
                                                              5.397750000
## 1996
         5.418083333
                      5.418916667
                                   5.416916667
                                                 5.412125000
                                                              5.402375000
## 1997
         5.350791667
                      5.345708333
                                   5.338208333
                                                 5.331083333
                                                              5.326000000
## 1998
        5.289666667
                      5.284625000
                                   5.278791667
                                                 5.269916667
                                                              5.258166667
  1999
         5.170708333
                      5.161625000
                                   5.150416667
                                                5.134541667
                                                              5.111708333
         4.953416667
                                                4.910541667
## 2000
                      4.939541667
                                   4.925958333
                                                              4.893458333
## 2001
         4.755875000
                      4.743708333
                                   4.737166667
                                                 4.729708333
                                                              4.719291667
## 2002
         4.599250000
                      4.590958333
                                   4.583416667
                                                 4.574791667
                                                              4.567166667
## 2003
         4.468291667
                      4.462541667
                                   4.458250000
                                                 4.453708333
                                                              4.448791667
## 2004
         4.419916667
                      4.415708333
                                   4.410791667
                                                 4.403208333
                                                              4.394250000
## 2005
        4.331791667
                      4.334125000
                                   4.346416667
                                                 4.359958333
                                                              4.374625000
## 2006
        4.501583333
                      4.513541667
                                   4.525208333
                                                4.541750000
                                                              4.561833333
## 2007
        4.738208333
                      4.753416667
                                   4.771708333
                                                4.796833333
                                                              4.829375000
         5.080333333
                      5.093041667
                                   5.097250000
## 2008
                                                5.104750000
                                                              5.115416667
                      5.220416667
## 2009
         5.206458333
                                   5.240958333
                                                 5.265458333
                                                              5.296791667
## 2010
         5.639375000
                      5.672708333
                                   5.713541667
                                                 5.763458333
                                                              5.821125000
## 2011
                                                6.505291667
        6.315750000
                      6.372208333
                                   6.429958333
                                                              6.607000000
## 2012
        7.758708333 7.868916667
                                   7.987583333
                                               8.141666667
                                                             8.315291667
        9.872541667 10.066250000 10.250583333 10.479750000 10.777541667
## 2013
## 2014 13.354625000 13.489833333 13.670625000 13.922541667 14.234583333
## 2015 16.257916667 16.427625000 16.671833333 16.974166667 17.251291667
## 2016 20.755125000 21.066875000 21.327541667 21.769375000 22.475583333
## 2017 27.253500000 27.587750000 28.013500000 28.380250000 28.768583333
## 2018 31.919000000 32.045916667 32.152625000 32.373500000 32.734708333
  2019 35.728875000 35.999250000 36.524208333 36.997041667 37.377875000
## 2020 42.309541667 42.830291667 43.197333333 43.874916667 44.948625000
## 2021 52.025458333 52.645916667 53.548208333 54.515291667 55.487500000
## 2022 63.518083333 63.824416667 64.061958333 64.377916667 64.911833333
## 2023
                  NA
                               NA
                                            NΑ
                                                          NA
##
                 Nov
                              Dec
        0.001875000
                      0.002083333
## 1984
  1985
        0.003625000
                      0.003666667
  1986
        0.003666667
                      0.003625000
## 1987
         0.003166667
                      0.003125000
  1988
        1.442875000
                      1.871000000
## 1989
        4.471833333
                      4.503708333
## 1990
         4.704083333
                      4.724625000
                      4.904083333
## 1991
         4.892750000
## 1992
         5.045750000
                      5.058125000
## 1993
         5.193708333
                      5.210250000
## 1994
         5.295416667
                      5.309291667
## 1995
         5.408041667
                      5.416708333
## 1996
         5.389375000
                      5.375875000
## 1997
         5.317541667
                      5.308166667
## 1998
        5.250666667
                      5.242541667
## 1999 5.087291667 5.063208333
```

```
## 2000
        4.877666667
                      4.865166667
## 2001
        4.702333333
                      4.684250000
        4.559166667
## 2002
                      4.547750000
## 2003
         4.444916667
                      4.440833333
  2004
         4.386583333
                      4.378416667
        4.390166667
## 2005
                      4.404875000
## 2006
         4.583500000
                      4.607958333
         4.862625000
## 2007
                      4.897833333
  2008
         5.128208333
                      5.137333333
## 2009
         5.337583333
                      5.388666667
## 2010
        5.882083333
                      5.944916667
## 2011
        6.738500000
                      6.895083333
## 2012
        8.482083333
                      8.652416667
## 2013 11.122416667 11.504791667
## 2014 14.562750000 14.859750000
## 2015 17.596791667 18.017625000
## 2016 23.262333333 24.147166667
## 2017 29.251250000 29.755541667
## 2018 33.024958333 33.299583333
## 2019 38.084583333 38.879708333
## 2020 46.005875000 47.006458333
## 2021 56.525166667 57.759708333
## 2022 65.700500000 66.535208333
##
  2023
##
##
  $random
##
                Jan
                            Feb
                                        Mar
                                                     Apr
                                                                 May
                                                                             Jun
## 1984
                             NA
                                         NA
                                                     NA
                                                                              NA
                 NA
                                                                  NA
## 1985 1.332554365 0.000000000 0.000000000 1.221999130 1.337235085 1.281613631
## 1986 0.814338779 0.744539561 0.822381340 1.191784866 1.229118206 0.974560366
## 1987 0.000000000 0.787826745 0.902613666 1.112332541 1.040874877 1.559296585
  1988 1.017923473 1.451852145 1.409796583 0.637955428 1.184996014 1.485044367
  1989 1.861092360 1.551414675 1.356951720 1.173070945 1.042568065 0.953778064
## 1990 1.015453603 1.006846492 1.004709157 0.968250044 0.954441672 0.927125927
  1991 1.004873516 0.996630140 0.978244084 0.944347115 0.954790287 0.936174857
## 1992 0.992804794 0.988416901 0.988613479 0.963859393 0.950027571 0.928548474
## 1993 0.990110899 0.990818316 0.998173193 0.974414505 0.947608081 0.919809997
## 1994 1.002770561 0.992340116 1.007217639 0.969560792 0.946157139 0.929058887
## 1995 0.979458955 0.976082027 0.980610896 0.967684921 0.953676721 0.940563475
## 1996 0.977611995 0.978850272 1.004777694 0.979350500 0.961312536 0.944254966
  1997 0.973534679 0.989960705 0.991855209 0.968793215 0.942402034 0.937333721
## 1998 0.971942207 0.966660901 0.996963065 0.966569931 0.935772957 0.932541700
## 1999 0.961973822 0.966918647 0.986153213 0.965075247 0.948567575 0.932434152
## 2000 0.955446776 0.966673016 0.971843620 0.949097966 0.941562749 0.927849804
## 2001 0.947048741 0.952643772 0.969877282 0.946614555 0.953512847 0.943438573
## 2002 0.956076683 0.968118273 0.984469133 0.954733693 0.941653402 0.946749082
## 2003 0.959693035 0.964202068 0.990110764 0.965215894 0.949104748 0.945881269
  2004 0.966557995 0.960673535 0.994715139 0.963840098 0.957403686 0.942474970
## 2005 0.958342587 0.961055253 0.982265199 0.964779640 0.957594091 0.944370114
## 2006 0.995220216 0.993292434 0.997722569 0.973956616 0.959636098 0.936980824
## 2007 0.993644275 0.990549487 1.005881263 0.970722358 0.961297147 0.939058077
## 2008 0.991858568 0.998840919 1.012960911 0.983157430 0.956156291 0.948561006
## 2009 0.963317983 0.978551963 1.003936247 0.978460440 0.957212655 0.932770206
## 2010 0.978085923 0.985816685 1.000386790 0.978338866 0.967367049 0.953239495
```

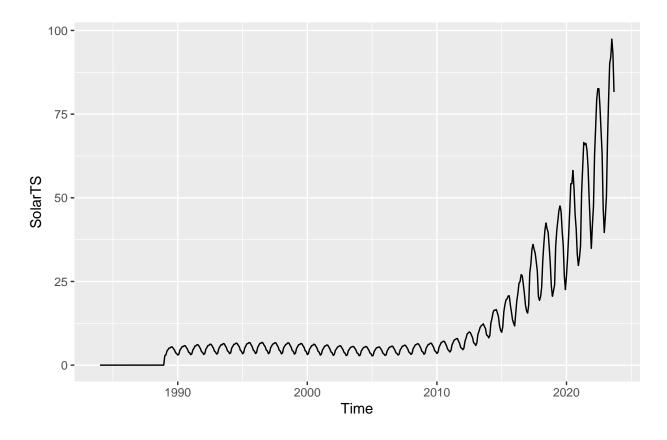
```
## 2011 0.997232508 1.016115301 1.011071113 0.983972698 0.959940709 0.946453463
## 2012 0.996303615 0.992969445 0.997925817 0.974469155 0.978298640 0.965176358
## 2013 1.014954758 1.041828572 1.029556403 0.969008761 0.933846265 0.927518921
## 2014 1.048255383 1.014566929 1.030725494 0.975553363 0.959803404 0.959073141
## 2015 0.987366907 1.043653309 1.040473660 1.022806376 0.972763761 0.949700697
## 2016 0.968028096 1.145184710 1.016013841 0.966567816 0.960980338 0.937412959
## 2017 0.952824517 0.987535370 1.082702300 1.023811445 1.026558208 1.032236202
## 2018 1.029699683 1.064138976 1.017400010 1.033515046 1.017990317 1.037511854
## 2019 1.006855111 0.985800586 1.050262824 1.031949943 0.974771940 1.008097563
## 2020 1.029640512 1.120320741 0.974374465 1.008413076 1.041974155 0.999106800
## 2021 1.022619693 1.031916700 1.064405784 1.053315988 1.038228592 0.987301034
## 2022 1.079468211 1.109610829 1.052265404 1.029754755 1.009898634 1.014002969
## 2023 1.004410990 1.036180260 0.988989802
                                                     NA
                                                                 NA
                                                                             NA
##
                Jul
                            Aug
                                        Sep
                                                    Oct
                                                                Nov
## 1984 0.533472737 1.499949958 1.733563254 1.267049758 0.708741737 0.000000000
## 1985 1.038109110 1.749941617 1.319790955 0.872028363 0.366590554 0.407593966
## 1986 1.225852247 1.239089096 1.161989862 1.086042650 1.087274256 0.412278954
## 1987 1.557163665 0.986980059 0.811922030 0.633524879 0.419649713 0.478243586
## 1988 0.026664378 0.008697352 0.004010870 0.000000000 0.000000000 0.000000000
## 1989 0.999835350 0.969643670 0.995895539 1.042916983 1.098634221 1.149826088
## 1990 0.999729261 0.978427498 0.994093374 1.049355409 1.097219445 1.170397961
## 1991 1.014080006 0.985891684 1.006351500 1.041934696 1.095650772 1.155605668
## 1992 1.006349900 0.982892431 1.000549562 1.047074165 1.102723203 1.156459531
## 1993 1.002188917 0.982667603 1.002736001 1.041655074 1.099454035 1.158549161
## 1994 0.997183363 0.969612283 1.003275564 1.063168635 1.107949207 1.164241624
## 1995 1.006107050 0.983172856 1.000468703 1.043448427 1.099127693 1.156604823
## 1996 1.004743769 0.964830971 0.980383043 1.046938011 1.108359310 1.184850236
## 1997 1.006079094 0.980539732 0.995620770 1.050933439 1.105588462 1.178847391
## 1998 1.011348320 0.987377372 1.006838611 1.056268045 1.110811618 1.182200995
## 1999 1.004907451 0.980171166 1.001980400 1.069614485 1.125064743 1.200754777
## 2000 1.014286253 0.987389133 1.017390141 1.063673184 1.117837514 1.192496147
## 2001 1.017023046 0.993818654 1.013343850 1.041193997 1.103562432 1.172509727
## 2002 1.013038016 0.987776358 1.005207220 1.047473036 1.113732389 1.166952734
## 2003 1.000408945 0.980527671 1.006932502 1.049427070 1.096915995 1.161730761
## 2004 1.010294482 0.984975499 1.008769540 1.047224518 1.098173369 1.166686429
## 2005 1.004017447 0.982807482 0.999978233 1.035214083 1.073666645 1.131517892
## 2006 0.999919728 0.989635967 0.997416740 1.032900620 1.077956984 1.130947852
## 2007 1.006865376 0.976504476 0.996749179 1.033448220 1.071830452 1.117412470
## 2008 1.006812880 0.982474129 1.004861259 1.039657827 1.079809444 1.142119971
## 2009 1.008918764 0.981967986 0.996863003 1.031462007 1.070565067 1.115752552
## 2010 1.009728765 0.979861566 0.994350082 1.006818759 1.066576740 1.102107481
## 2011 0.992442844 0.979768892 0.982982082 1.013896304 1.037120501 1.095889389
## 2012 1.010212408 0.959869281 0.980400699 1.016937474 1.052041236 1.112193048
## 2013 0.956951915 0.952694483 0.981923337 1.045569180 1.078652789 1.143149655
## 2014 0.972541911 0.962664663 1.000177677 1.049179731 1.077238529 1.044666829
## 2015 1.006373114 0.983862168 0.946062493 0.951106708 1.029171885 1.040738284
## 2016 1.027701430 0.992578160 0.990285407 0.981952170 1.027416293 1.002770673
## 2017 1.004621340 0.946458509 0.969357688 1.003477291 0.931364965 0.972481910
## 2018 1.016682221 0.979559447 0.972904265 0.955613107 0.944328468 0.923466888
## 2019 1.057453907 0.995158344 0.966948140 0.983926173 0.929343932 0.867691732
## 2020 1.086599216 0.966007342 0.912342763 0.931574331 0.955177128 0.946754048
## 2021 1.007277688 0.949541797 0.964570407 0.923547688 0.989335975 0.902895289
## 2022 1.035410462 0.953609419 0.970110032 1.002170282 0.944739074 0.890010252
## 2023
                 NA
                             NA
                                         NA
```

```
##
## $figure
   [1] 0.6549281 0.7084547 0.9727847 1.1064760 1.2463528 1.2826296 1.2496734
   [8] 1.2632000 1.1225122 0.9713661 0.7525073 0.6691151
##
## $type
## [1] "multiplicative"
##
## attr(,"class")
## [1] "decomposed.ts"
```

autoplot(WindTS)



autoplot(SolarTS)



Q6

When fitting a model to this data, do you think you need all the historical data? Think about the data from 90s and early 20s. Are there any information from those years we might need to forecast the next six months of Solar and/or Wind consumption. Explain your response.

Answer: No, not necessary.

$\mathbf{Q7}$

Create a new time series object where historical data starts on January 2012. Hint: use filter() function so that you don't need to point to row numbers, .i.e, filter(xxxx, year(Date) >= 2012). Apply the decompose function type=additive to this new time series. Comment the results. Does the random component look random? Think about our discussion in class about seasonal components that depends on the level of the series.

```
FilterData <- energy_data|>
  filter(year(as.Date(Month, "%Y")) >= 2012)

FilterDataTS <- ts(FilterData)

FilterWind <-FilterData |>
  select(`Wind Energy Consumption`)

FilterSolar <-FilterData |>
  select(`Solar Energy Consumption`)
```

```
TSFilterWind <- ts(FilterWind, start = c(2012, 1), frequency = 12)
TSFilterSolar <- ts(FilterSolar, start = c(2012, 1), frequency = 12)
original_start_date <- start(TSFilterWind)</pre>
print(original_start_date)
## [1] 2012
print(decompose(TSFilterWind, type = "additive"))
## $x
##
                    Feb
                             Mar
                                                               Jul
                                                                               Sep
            Jan
                                      Apr
                                              May
                                                      Jun
                                                                       Aug
         46.514
                 37.709
                          47.858
## 2012
                                  43.364
                                           42.788
                                                   40.850
                                                           30.099
                                                                    28.896
                                                                            29.990
         50.288
                 48.026
                          53.758
                                  59.629
                                           55.406
                                                           37.851
## 2013
                                                   46.909
                                                                    32.871
                                                                            39.832
                 47.798
                          60.515
                                  63.584
                                           53.232
                                                   53.906
                                                           41.583
                                                                    34.702
## 2014
         61.113
                                                                            39.305
                                  60.963
                                                                    44.629
## 2015
        51.733
                 50.912
                          52.231
                                           58.520
                                                   45.793
                                                           46.661
                                                                            47.671
## 2016
        63.007
                 68.712
                          74.857
                                  70.967
                                           64.309
                                                   55.627
                                                           60.114
                                                                    46.367
                                                                            55.969
## 2017
         70.965
                 75.375
                          87.793
                                  86.590
                                                   68.724
                                                           55.001
                                                                    47.355
                                           78.707
                                                                            61.115
## 2018
        87.343
                 79.123
                          90.294
                                  90.182
                                           81.728
                                                   84.286
                                                           56.116
                                                                    67.716
                                                                            63.189
        82.917
                          87.936
                                  98.659
                                                   76.586
## 2019
                 77.189
                                           87.959
                                                           75.408
                                                                    68.165
                                                                            83.640
## 2020 95.950
                 99.325 100.039 101.515
                                          96.824 103.085
                                                           78.019
                                                                    78.576
                                                                            79.111
## 2021 102.566
                 91.153 133.768 123.370 115.280
                                                   91.003
                                                           74.093
                                                                    92.367
                                                                            98.941
## 2022 127.664 128.443 146.820 157.522 143.726 115.215 100.569
                                                                    84.339
                                                                            93.254
## 2023 133.636 143.503 151.927 146.775 109.246 93.850
                                                           95.085
                                                                    97.256
##
            Oct
                             Dec
                    Nov
## 2012
         43.113
                 39.745
                          49.557
        46.523
## 2013
                 53.921
                          47.656
## 2014
        49.501
                 64.374
                          50.195
## 2015
        55.889
                 67.154
                          68.576
         69.384
                 66.212
## 2016
                          78.973
## 2017
                 77.162
        83.146
                          75.749
## 2018
        72.314
                 75.118
                          82.933
## 2019
        94.255
                 85.929
                          90.909
        98.343 113.038 109.220
## 2020
## 2021 109.918 121.983 135.965
## 2022 111.725 140.570 131.975
## 2023
##
## $seasonal
##
               Jan
                           Feb
                                      Mar
                                                  Apr
                                                              May
                                                                         Jun
## 2012
          5.290928
                      3.183739
                                14.526655
                                            14.853377
                                                        6.418390
                                                                   -3.800823
                      3.183739
## 2013
          5.290928
                                14.526655
                                            14.853377
                                                        6.418390
                                                                   -3.800823
## 2014
          5.290928
                      3.183739
                                14.526655
                                            14.853377
                                                        6.418390
                                                                   -3.800823
## 2015
          5.290928
                      3.183739
                                14.526655
                                            14.853377
                                                        6.418390
                                                                   -3.800823
## 2016
          5.290928
                      3.183739
                                14.526655
                                            14.853377
                                                        6.418390
                                                                   -3.800823
                                14.526655
                                                        6.418390
## 2017
          5.290928
                      3.183739
                                            14.853377
                                                                   -3.800823
## 2018
          5.290928
                      3.183739
                                14.526655
                                            14.853377
                                                        6.418390
                                                                   -3.800823
## 2019
          5.290928
                      3.183739
                                14.526655
                                                        6.418390
                                                                   -3.800823
                                            14.853377
## 2020
          5.290928
                      3.183739
                                14.526655
                                            14.853377
                                                        6.418390
                                                                   -3.800823
## 2021
          5.290928
                      3.183739
                                14.526655
                                            14.853377
                                                        6.418390
                                                                   -3.800823
## 2022
          5.290928
                      3.183739
                                14.526655
                                            14.853377
                                                        6.418390
                                                                   -3.800823
## 2023
          5.290928
                      3.183739
                                14.526655
                                            14.853377
                                                        6.418390
                                                                   -3.800823
##
                                                              Nov
                                                                         Dec
               Jul 1
                           Aug
                                      Sep
                                                  Oct.
## 2012 -15.551724 -18.967102 -13.758947
                                            -1.627220
                                                        4.192519
                                                                    5.240208
## 2013 -15.551724 -18.967102 -13.758947
                                            -1.627220
                                                        4.192519
                                                                    5.240208
```

```
## 2014 -15.551724 -18.967102 -13.758947 -1.627220
                                                    4.192519
                                                               5.240208
## 2015 -15.551724 -18.967102 -13.758947 -1.627220
                                                    4.192519
                                                               5.240208
## 2016 -15.551724 -18.967102 -13.758947 -1.627220
                                                    4.192519
                                                               5.240208
## 2017 -15.551724 -18.967102 -13.758947 -1.627220
                                                    4.192519
                                                               5.240208
## 2018 -15.551724 -18.967102 -13.758947
                                       -1.627220
                                                    4.192519
                                                               5.240208
## 2019 -15.551724 -18.967102 -13.758947 -1.627220
                                                    4.192519
                                                               5.240208
## 2020 -15.551724 -18.967102 -13.758947 -1.627220
                                                    4.192519
                                                               5.240208
## 2021 -15.551724 -18.967102 -13.758947 -1.627220
                                                    4.192519
                                                               5.240208
## 2022 -15.551724 -18.967102 -13.758947 -1.627220
                                                    4.192519
                                                               5.240208
## 2023 -15.551724 -18.967102 -13.758947
##
## $trend
                       Feb
                                Mar
                                         Apr
                                                    May
                                                              Jun
                                                                        Jul
             Jan
## 2012
              NA
                        NA
                                 NA
                                          NA
                                                     NA
                                                               NA
                                                                  40.19750
## 2013 44.94100 45.42963
                           46.00533
                                     46.55750
                                               47.29025 47.80171
                                                                   48.17354
## 2014 50.05567
                  50.28746
                            50.34179
                                     50.44392
                                               51.00354 51.54488
                                                                  51.25983
## 2015 50.19592 50.82112 51.58333
                                     52.19808
                                               52.58008 53.46179
                                                                   54.69742
## 2016 61.23212 61.86508
                           62.28325
                                     63.19129
                                               63.71433 64.10829
                                                                   64.87308
## 2017 70.21804 70.04617
                           70.30175
                                     71.08958
                                               72.11925
                                                        72.44117
                                                                  72.98925
## 2018 76.08679 76.98162 77.91642
                                     77.55150
                                               77.01500 77.22917
                                                                  77.34408
## 2019 78.18983 79.01238 79.88321 81.64954
                                              83.01421 83.79700 84.67238
## 2020 91.36246 91.90504 92.15013 92.13175 93.43163 95.32413 96.36275
## 2021 100.95700 101.36804 102.76892 104.07746 104.93246 106.41954 108.57967
## 2022 122.15792 122.92658 122.35512 122.19346 123.04321 123.65142 123.73400
## 2023 119.88558 120.19529 120.85608
                                           NA
                                                     NA
                                                               NΑ
             Aug
                       Sep
                                Oct
                                          Nov
                                                    Dec
                                     43.58733
## 2012
       40.78462 41.46033 42.38387
                                               44.36554
## 2013 48.61508 48.88712 49.33346
                                     49.40767
                                               49.60862
## 2014 50.99875 50.78333 50.32896
                                     50.44008
                                               50.32237
## 2015 55.90883 57.59325 58.95283
                                     59.61087
                                               60.26183
## 2016 65.48229 66.29892 67.48887
                                     68.73975
                                               69.88537
## 2017 73.82783 74.08821 74.34208
                                     74.61763
                                               75.39192
## 2018 77.07908 76.90025 77.15521
                                     77.76804
                                               77.70683
## 2019 86.13775 87.56437 88.18767 88.67604 90.14954
## 2020 96.29792 97.36279 99.67879 101.35842 101.62400
## 2021 111.17917 113.27675 115.24358 117.85183 120.04592
## 2022 124.61033 125.45062 125.21562 123.33117 121.00429
## 2023
              NΔ
                        NA
##
## $random
##
                Jan
                            Feb
                                         Mar
                                                      Apr
## 2012
                 NA
                             NA
                                          NA
                                                      NA
                                                                   NA
## 2013
        0.05607206 -0.58736354
                                 -6.77398854 -1.78187718
                                                            1.69736032
## 2014
        5.76640540 -5.67319688
                                 -4.35344687
                                             -1.71329384 -4.18993134
## 2015
       -3.75384460 -3.09286354 -13.87898854 -6.08846051 -0.47847301
## 2016
       -3.51605294
                                             -7.07766884
                                                           -5.82372301
                      3.66317813 -1.95290521
## 2017
        -4.54396960
                      2.14509479
                                  2.96459479
                                               0.64703949
                                                            0.16936032
## 2018
        5.96528040 -1.04236354 -2.14907188 -2.22287718
                                                           -1.70538968
## 2019
       -0.56376127 -5.00711354 -6.47386354
                                              2.15608116
                                                           -1.47359801
## 2020
                      4.23621979 -6.63778021
       -0.70338627
                                             -5.47012718
                                                           -3.02601468
## 2021
        -3.68192794 -13.39878021 16.47242813
                                              4.43916449
                                                            3.92915199
## 2022
        0.21515540
                     2.33267813
                                 9.93821979 20.47516449
                                                           14.26440199
## 2023
         8.45948873 20.12396979 16.54426146
                                                      NΑ
                                                                   NΑ
##
                Jun
                             Jul
                                         Aug
                                                      Sep
                                                                   Oct
```

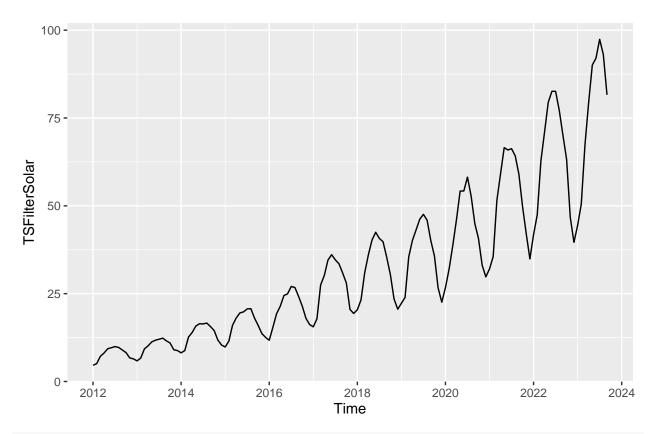
```
## 2012
                       5.45322358
                                    7.07847737
                                                 2.28861373
                                                              2.35634479
## 2013
                                    3.22301903
         2.90811449
                       5.22918191
                                                 4.70382206
                                                             -1.18323854
## 2014
         6.16194782
                       5.87489025
                                    2.67035237
                                                 2.28061373
                                                              0.79926146
## 2015
        -3.86796884
                       7.51530691
                                                 3.83669706
                                                             -1.43661354
                                    7.68726903
## 2016
        -4.68046884
                      10.79264025
                                   -0.14818930
                                                 3.42903040
                                                              3.52234479
## 2017
          0.08365616
                     -2.43652642
                                  -7.50573097
                                                 0.78573873
                                                             10.43113646
## 2018
        10.85765616
                     -5.67635975
                                    9.60401903
                                                 0.04769706
                                                             -3.21398854
## 2019
        -3.41017718
                       6.28734858
                                    0.99435237
                                                 9.83457206
                                                              7.69455312
## 2020
        11.56169782
                     -2.79202642
                                    1.24518570
                                                -4.49284460
                                                              0.29142812
## 2021 -11.61571884 -18.93494309
                                    0.15493570
                                               -0.57680294
                                                             -3.69836354
## 2022
        -4.63559384
                      -7.61327642 -21.30423097 -18.43767794 -11.86340521
## 2023
                  NA
                               NA
                                            NA
                                                         ΝA
##
                 Nov
                              Dec
## 2012
        -8.03485218
                      -0.04874991
## 2013
                      -7.19283324
         0.32081449
## 2014
          9.74139782
                      -5.36758324
## 2015
         3.35060616
                       3.07395843
## 2016
        -6.72026884
                       3.84741676
## 2017
        -1.64814384
                     -4.88312491
## 2018
        -6.84256051
                     -0.01404157
## 2019
        -6.93956051
                     -4.48074991
## 2020
         7.48706449
                      2.35579176
        -0.06135218 10.67887509
## 2021
        13.04631449
## 2022
                       5.73050009
## 2023
##
## $figure
                                                      6.418390
   [1]
          5.290928
                     3.183739 14.526655 14.853377
                                                                -3.800823
##
   [7] -15.551724 -18.967102 -13.758947 -1.627220
                                                      4.192519
                                                                  5.240208
##
## $type
## [1] "additive"
##
## attr(,"class")
## [1] "decomposed.ts"
print(decompose(TSFilterSolar, type = "additive"))
## $x
##
           Jan
                  Feb
                         Mar
                                Apr
                                       May
                                              Jun
                                                     Jul
                                                                    Sep
                                                                           Oct
                                                            Aug
               5.077
## 2012 4.607
                      7.148
                             8.096 9.316 9.605 9.934
                                                          9.685
                                                                 8.960
## 2013 5.869 6.663 9.260 10.151 11.264 11.745 12.038 12.336 11.551 10.946
## 2014 8.157 8.799 12.624 13.934 15.758 16.428 16.395 16.624 15.631 14.507
## 2015 9.815 11.480 15.989 18.058 19.510 19.804 20.660 20.720 18.026 15.938
## 2016 11.728 15.428 19.297 21.401 24.459 24.955 27.056 26.741 24.199 21.438
## 2017 15.555 17.857 27.472 30.175 34.567 36.083 34.635 33.492 30.881 28.042
## 2018 20.417 23.213 30.918 36.049 40.277 42.476 40.715 39.785 35.355 30.386
## 2019 22.249 23.942 35.490 40.146 43.146 46.198 47.572 45.914 40.157 35.724
## 2020 26.741 32.049 38.731 46.045 54.208 54.219 58.159 52.712 44.933 40.674
## 2021 32.034 35.565 51.477 59.068 66.559 65.882 66.269 64.229 59.026 49.778
## 2022 41.808 47.446 62.806 71.072 79.459 82.611 82.584 77.169 70.105 63.190
## 2023 44.432 50.523 67.312 79.380 90.079 92.024 97.397 93.068 81.595
           Nov
                  Dec
## 2012 6.715
               6.439
## 2013 9.028 8.800
```

```
## 2014 11.805 10.387
## 2015 13.628 12.547
## 2016 17.985 16.202
## 2017 20.501 19.362
## 2018 23.468 20.576
## 2019 26.634 22.573
## 2020 33.068 29.778
## 2021 42.082 34.895
## 2022 46.708 39.623
## 2023
##
## $seasonal
                     Feb
                                 Mar
                                              Apr
                                                         May
               Jan
                                                                           Jun
                                            4.2468117
## 2012 -10.5543550
                                0.2594329
                   -8.0960443
                                                         8.1619075
                                                                     8.9764034
## 2013 -10.5543550
                   -8.0960443
                                0.2594329
                                            4.2468117
                                                         8.1619075
                                                                     8.9764034
## 2014 -10.5543550
                    -8.0960443
                                 0.2594329
                                             4.2468117
                                                         8.1619075
                                                                     8.9764034
## 2015 -10.5543550
                    -8.0960443
                                0.2594329
                                            4.2468117
                                                         8.1619075
                                                                     8.9764034
## 2016 -10.5543550
                   -8.0960443
                                0.2594329
                                            4.2468117
                                                         8.1619075
                                                                     8.9764034
## 2017 -10.5543550
                   -8.0960443
                                0.2594329
                                            4.2468117
                                                         8.1619075
                                                                    8.9764034
## 2018 -10.5543550
                   -8.0960443
                                0.2594329
                                            4.2468117
                                                         8.1619075
                                                                    8.9764034
## 2019 -10.5543550
                   -8.0960443
                                0.2594329
                                           4.2468117
                                                         8.1619075
                                                                    8.9764034
## 2020 -10.5543550
                   -8.0960443
                                0.2594329
                                           4.2468117
                                                         8.1619075
                                                                    8.9764034
## 2021 -10.5543550
                   -8.0960443
                                0.2594329
                                           4.2468117
                                                         8.1619075
                                                                    8.9764034
## 2022 -10.5543550
                    -8.0960443
                                 0.2594329
                                            4.2468117
                                                         8.1619075
                                                                     8.9764034
                   -8.0960443
## 2023 -10.5543550
                                 0.2594329
                                             4.2468117
                                                         8.1619075
                                                                     8.9764034
                                       Sep
               Jul
                           Aug
                                                   Oct
                                                               Nov
## 2012
         8.6143117
                     6.7813155
                                 2.6919140
                                           -1.4411769
                                                       -8.1275671 -11.5129534
## 2013
                     6.7813155
                                 2.6919140 -1.4411769
        8.6143117
                                                       -8.1275671 -11.5129534
## 2014
        8.6143117
                     6.7813155
                                2.6919140
                                           -1.4411769
                                                       -8.1275671 -11.5129534
## 2015
        8.6143117
                     6.7813155
                                 2.6919140
                                           -1.4411769 -8.1275671 -11.5129534
        8.6143117
## 2016
                     6.7813155
                                 2.6919140
                                           -1.4411769 -8.1275671 -11.5129534
## 2017
         8.6143117
                     6.7813155
                                 2.6919140 -1.4411769 -8.1275671 -11.5129534
## 2018
                                           -1.4411769 -8.1275671 -11.5129534
         8.6143117
                     6.7813155
                                2.6919140
## 2019
                     6.7813155
                                 2.6919140 -1.4411769 -8.1275671 -11.5129534
         8.6143117
## 2020
         8.6143117
                     6.7813155
                                 2.6919140
                                           -1.4411769
                                                       -8.1275671 -11.5129534
## 2021
                     6.7813155
                                2.6919140 -1.4411769
                                                       -8.1275671 -11.5129534
         8.6143117
## 2022
         8.6143117
                     6.7813155
                                 2.6919140 -1.4411769 -8.1275671 -11.5129534
## 2023
        8.6143117
                     6.7813155
                                 2.6919140
##
## $trend
             Jan
                       Feb
                                 Mar
                                          Apr
                                                     May
                                                               Jun
                        NA
                                  NA
                                                     NA
                                                               NA 7.868917
## 2012
              NA
                                           NA
## 2013 8.829250 9.027375 9.245792 9.467583 9.677792 9.872542 10.066250
## 2014 11.881458 12.241667 12.590333 12.908708 13.172792 13.354625 13.489833
## 2015 15.178125 15.526500 15.796958 15.956375 16.091958 16.257917 16.427625
## 2016 18.498750 19.016125 19.524208 20.010583 20.421292 20.755125 21.066875
## 2017 24.926625 25.523708 26.083417 26.637000 27.017000 27.253500 27.587750
## 2018 30.275250 30.790792 31.239417 31.523500 31.744792 31.919000 32.045917
## 2019 33.740375 34.281458 34.736917 35.159417 35.513750 35.728875 35.999250
## 2020 39.655042 40.379417 40.861667 41.266917 41.741250 42.309542 42.830292
## 2021 47.830333 48.648125 49.715208 50.681750 51.436667 52.025458 52.645917
## 2022 59.136542 60.355500 61.356292 62.376750 63.128333 63.518083 63.824417
                                      NA
## 2023 67.544625 68.824292 69.965500
                                                    NA
                                                               NΑ
##
             Aug
                       Sep
                                 Oct
                                           Nov
                                                     Dec
```

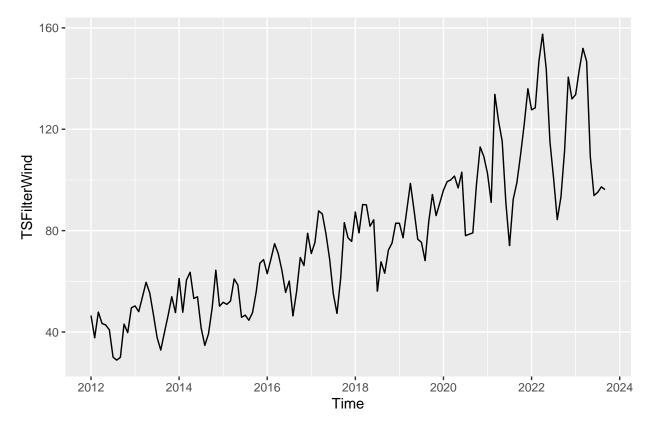
```
## 2012 7.987583 8.141667 8.315292 8.482083 8.652417
## 2013 10.250583 10.479750 10.777542 11.122417 11.504792
## 2014 13.670625 13.922542 14.234583 14.562750 14.859750
## 2015 16.671833 16.974167 17.251292 17.596792 18.017625
## 2016 21.327542 21.769375 22.475583 23.262333 24.147167
## 2017 28.013500 28.380250 28.768583 29.251250 29.755542
## 2018 32.152625 32.373500 32.734708 33.024958 33.299583
## 2019 36.524208 36.997042 37.377875 38.084583 38.879708
## 2020 43.197333 43.874917 44.948625 46.005875 47.006458
## 2021 53.548208 54.515292 55.487500 56.525167 57.759708
## 2022 64.061958 64.377917 64.911833 65.700500 66.535208
## 2023
                        NA
             NA
##
## $random
##
                             Feb
                Jan
                                          Mar
                                                       Apr
                                                                   May
## 2012
                 NA
                              NA
                                           NA
                                                       NA
                                                                    NA
## 2013
         7.59410496
                      5.73166935
                                  -0.24522459 -3.56339504
                                                            -6.57569921
## 2014
        6.82989662
                     4.65337768
                                  -0.22576626
                                               -3.22152004
                                                            -5.57669921
## 2015
        5.19122996
                      4.04954435
                                  -0.06739126
                                               -2.14518671
                                                            -4.74386588
## 2016
         3.78360496
                      4.50791935
                                  -0.48664126
                                               -2.85639504
                                                            -4.12419921
## 2017
         1.18272996
                      0.42933602
                                  1.12915041
                                              -0.70881171
                                                            -0.61190754
## 2018
         0.69610496
                      0.51825268
                                  -0.58084959
                                               0.27868829
                                                             0.37030079
## 2019
        -0.93702004
                     -2.24341398
                                   0.49365041
                                                0.73977162
                                                            -0.52965754
## 2020
        -2.35968671
                     -0.23437232
                                  -2.39009959
                                                0.53127162
                                                             4.30484246
                                  1.50235874
## 2021
        -5.24197838
                     -4.98708065
                                                4.13943829
                                                             6.96042579
## 2022 -6.77418671 -4.81345565
                                   1.19027541
                                                4.44843829
                                                             8.16875912
                                  -2.91293292
## 2023 -12.55827004 -10.20524732
                                                 NA
                                                                     NA
                                    Aug
                Jun
                             Jul
                                                       Sep
                                                                    Oct
## 2012
                 NA
                     -6.54922838
                                  -5.08389883
                                              -1.87358065
                                                             1.33988526
## 2013 -7.10394504 -6.64256171
                                  -4.69589883
                                               -1.62066398
                                                            1.60963526
## 2014
        -5.90302838 -5.70914504
                                  -3.82794050
                                               -0.98345565
                                                             1.71359359
## 2015
        -5.43032004
                     -4.38193671
                                  -2.73314883
                                               -1.64008065
                                                             0.12788526
## 2016
        -4.77652838
                     -2.62518671
                                  -1.36785717
                                               -0.26228898
                                                             0.40359359
## 2017
        -0.14690338
                    -1.56706171
                                  -1.30281550
                                               -0.19116398
                                                             0.71459359
## 2018
         1.58059662
                      0.05477162
                                   0.85105950
                                                0.28958602
                                                            -0.90753141
## 2019
         1.49272162
                      2.95843829
                                   2.60847617
                                                0.46804435
                                                            -0.21269807
## 2020
         2.93305496
                      6.71439662
                                   2.73335117
                                              -1.63383065
                                                            -2.83344807
## 2021
         4.88013829
                      5.00877162
                                   3.89947617
                                                1.81879435
                                                            -4.26832307
## 2022 10.11651329
                      10.14527162
                                   6.32572617
                                                3.03516935
                                                            -0.28065641
## 2023
                                           NA
                 NA
                              NA
                                                        NA
##
                Nov
                             Dec
## 2012
        6.36048374
                      9.29953677
## 2013
         6.03315041
                      8.80816177
## 2014
        5.36981708
                      7.04020344
## 2015
         4.15877541
                      6.04232844
## 2016
         2.85023374
                      3.56778677
## 2017
        -0.62268292
                      1.11941177
## 2018
        -1.42939126 -1.21062989
## 2019
        -3.32301626 -4.79375489
## 2020
        -4.81030792 -5.71550489
## 2021
        -6.31559959 -11.35175489
## 2022 -10.86493292 -15.39925489
## 2023
##
```

```
## $figure
   [1] -10.5543550 -8.0960443
                                  0.2594329
                                              4.2468117
                                                          8.1619075
                                                                      8.9764034
         8.6143117
                     6.7813155
                                  2.6919140 -1.4411769 -8.1275671 -11.5129534
##
##
## $type
## [1] "additive"
##
## attr(,"class")
## [1] "decomposed.ts"
```

autoplot(TSFilterSolar)



autoplot(TSFilterWind)



Answer:

Identify and Remove outliers

$\mathbf{Q8}$

Apply the tsclean() to both series from Q7. Did the function removed any outliers from the series? Hint: Use autoplot() to check if there is difference between cleaned series and original series.

whole data set!

```
CleanWindTS <-tsclean(WindTS)

CleanSolarTS <- tsclean(SolarTS)

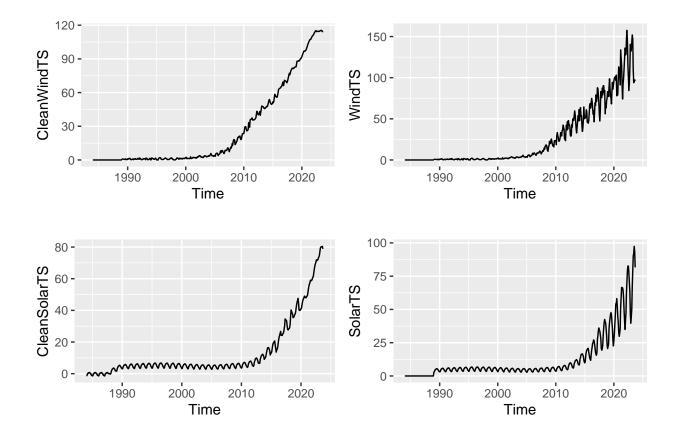
p1 <- autoplot(CleanWindTS)

p2 <- autoplot(CleanSolarTS)

p3 <- autoplot(WindTS)

p4 <- autoplot(SolarTS)

plot_grid(p1, p3, p2, p4, nrow = 2)</pre>
```



 $\mathbf{Q9}$

Redo number Q8 but now with the time series you created on Q7, i.e., the series starting in 2014. Using what autoplot() again what happened now?Did the function removed any outliers from the series? After 2012

Answer:

```
TSCWind <- tsclean(TSFilterWind)
TSCSolar <- tsclean(TSFilterSolar)

p5 <- autoplot(TSCSolar)
p6 <- autoplot(TSCWind)
p7 <- autoplot(TSFilterWind)
p8 <- autoplot(TSFilterSolar)

plot_grid(p5, p8, p6, p7, nrow = 2)</pre>
```

