Let's go through each code section — line by line, explaining:

X FEATURE ENGINEERING (start from basic feature engineering)

Code Block:

python

```
CopyEdit
# 1. Investment Total and Individual Stock Investment Ratios
stock_macro_fed_df["invest_total"] = (
        stock_macro_fed_df["invest_AAPL"] +
stock_macro_fed_df["invest_MSFT"] +
stock_macro_fed_df["invest_GOOGL"] +
```

```
stock_macro_fed_df["invest_META"] +
    stock_macro_fed_df["invest_TSLA"] +
stock_macro_fed_df["invest_AVGO"] + stock_macro_fed_df["invest_AMD"]
```

stock_macro_fed_df["invest_CRM"]
)

stock_macro_fed_df["invest_AMZN"] +

• Goal: Create a new column "invest_total".

stock_macro_fed_df["invest_NVDA"] +

- Meaning: Sum the investment amount across all 10 companies for each day.
- Reason: You want to know the total money flow into your top 10 tech portfolio daily.

python CopyEdit

```
# Calculate each company's investment share (ratio)
for stock in ['AAPL', 'MSFT', 'GOOGL', 'NVDA', 'AMZN', 'META',
'TSLA', 'AVGO', 'AMD', 'CRM']:
    stock_macro_fed_df[f"invest_{stock}_ratio"] =
stock_macro_fed_df[f"invest_{stock}"] /
stock_macro_fed_df["invest_total"]
```

- **Loop**: For each company.
- Create: A column like invest_AAPL_ratio.
- **Meaning**: What percentage of the total daily investment belongs to this company?
- Reason: Track relative strength and market preference shifts between stocks.

python

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```
# 2. Time Features Extraction
stock_macro_fed_df['day_of_week'] =
stock_macro_fed_df['date'].dt.dayofweek
stock_macro_fed_df['month'] = stock_macro_fed_df['date'].dt.month
stock_macro_fed_df['week_number'] =
stock_macro_fed_df['date'].dt.isocalendar().week
stock_macro_fed_df['is_month_end'] =
stock_macro_fed_df['date'].dt.is_month_end.astype(int)
```

- Extract time components from the date:
 - o day_of_week = 0 (Monday) to 6 (Sunday)
 - o month = 1 to 12
 - o week_number = ISO calendar week
 - is_month_end = 1 if last trading day of month, else 0
- Reason: Stocks often behave differently depending on day/month patterns (e.g., "sell in May").

python

CopyEdit

```
# 3. Set Up DataFrame for Feature Engineering
df = stock_macro_fed_df.copy()
df['date'] = pd.to_datetime(df['date'])
df.set_index('date', inplace=True)
```

- Make a working copy so you don't accidentally mess up the original.
- **Ensure** that the 'date' column is a datetime type.
- Set date as the index so that rolling, lagging, time operations are easier.

python

CopyEdit

```
# 4. First Differencing for Macroeconomic and Indices Variables macro_and_indices_cols = [...] for col in macro_and_indices_cols:
```

```
if col in df.columns:
    df[f'{col}_diff'] = df[col].diff()
```

- For each macro/micro feature (like CPI, S&P500, oil prices...):
- Create a differenced version (today yesterday).
- Why?: Differencing removes trend and makes non-stationary data stationary.

```
python
CopyEdit
# 5. Stock Price Feature Engineering
stocks = ['AAPL', 'MSFT', ..., 'CRM']
for stock in stocks:
    for field in ['close', 'open', 'high', 'low']:
        col = f'{field}_{stock}'
        if col in df.columns:
            df[f'{col}_diff'] = df[col].diff()
            df[f'{col}_rolling_mean_5'] =
df[col].rolling(window=5).mean()
            df[f'{col}_rolling_std_5'] =
df[col].rolling(window=5).std()
            df[f'{col}_rolling_mean_20'] =
df[col].rolling(window=20).mean()
            df[f'{col}_rolling_std_20'] =
df[col].rolling(window=20).std()
            for lag in [1, 3, 5, 10]:
```

• For every stock and every price field (close, open, high, low):

df[f'{col}_lag_{lag}'] = df[col].shift(lag)

- o First difference (to remove trend)
- o 5-day rolling mean and std (short-term smoothing)
- 20-day rolling mean and std (long-term smoothing)
- Lagged values (to give memory of the past)

python

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```
# Technical Indicators (RSI and MACD)
df[f'{stock}_RSI'] = ta.rsi(df[close_col], length=14)
macd = ta.macd(df[close_col])
```

- **RSI** = Relative Strength Index (momentum strength over 14 days)
- **MACD** = Moving Average Convergence Divergence (trend-following indicator)
- Reason: Powerful signals for market strength and trend reversal.

python CopyEdit # Volume Features df[f'{vol_col}_log'] = np.log1p(df[vol_col]) df[f'{vol_col}_diff'] = df[f'{vol_col}_log'].diff()

- Take log of volume to stabilize outliers.
- **Difference of log(volume)** to find changes in market activity.

```
python
CopyEdit
# Investment differencing
for suffix in ['delta_price', 'avg_price', 'price_ratio', 'invest']:
    derived_col = f'{suffix}_{stock}'
    if derived_col in df.columns:
        df[f'{derived_col}_diff'] = df[derived_col].diff()
```

• Difference investment-related metrics too.

ADVANCED TIME SERIES DECOMPOSITION

Code Block:

```
python
CopyEdit
from statsmodels.tsa.seasonal import STL

columns_to_decompose = [...]
seasonal_period = 252
```

- Set up decomposition: you want to decompose important variables like close AAPL. CPI. etc.
- **Seasonality** = 252 (trading days per year).

python CopyEdit

```
for col in columns_to_decompose:
   if col in df.columns:
      stl = STL(df[col].dropna(), period=seasonal_period)
      result = stl.fit()
      df[f'{col}_trend'] = result.trend
      df[f'{col}_seasonal'] = result.seasonal
      df[f'{col}_residual'] = result.resid
```

- For each column:
 - Apply STL decomposition.
 - Save the 3 components: **trend**, **seasonal**, **residual** as new columns.
- ☑ You now have "cleaned up" signals, broken into parts.

STATIONARITY TESTING (ADF + KPSS)

Code Block:

```
python
CopyEdit
from statsmodels.tsa.stattools import adfuller, kpss
columns_to_test =
df.select_dtypes(include='number').columns.tolist()
```

• Test all numeric columns.

```
python
CopyEdit
for col in columns_to_test:
    series = df[col].dropna()
    adf_result = adfuller(series, autolag='AIC')
    adf_pvalue = adf_result[1]
    kpss_result = kpss(series, regression='c', nlags="auto")
    kpss_pvalue = kpss_result[1]
```

```
if adf_pvalue < 0.05 and kpss_pvalue > 0.05:
final conclusion = "Stationary ✓"
else:
final_conclusion = "Non-Stationary X"
```

- ADF wants small p-value (reject non-stationary).
- KPSS wants big p-value (accept stationarity).
- If both agree, mark Stationary.

```
python
CopyEdit
stationarity_df = pd.DataFrame(stationarity_results)
```

Save all results for tracking.



ADVANCED STATIONARITY FIX

Code Block:

python CopyEdit

non_stationary_cols = stationarity_df[stationarity_df['Final Conclusion'] == 'Non-Stationary X']['Feature'].tolist()

List all features that are still non-stationary.

```
python
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for col in non_stationary_cols:
    series = df[col].dropna()
    if (series > 0).all():
        transformed = np.log(series / series.shift(1))
        method = "log_return"
    else:
        transformed = series.diff().diff()
        method = "second_diff"
```

- If positive series, try log returns first.
- Otherwise, try second differencing.

python

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```
if transformed.dropna().std() == 0 or transformed.isna().mean() >
0.5:
    stl = STL(series, period=252)
    transformed = stl.fit().resid
    method = "stl residual"
```

- If second diff or log returns still bad:
 - Try STL residuals (only the noise part).
- You automatically fix features that were problematic and make them ready for modeling!



- ☑ Now, ALL your features are:
 - Decomposed
 - Differenced
 - Smoothed
 - Stationary

Ready to plug into models like XGBoost, LSTM, ARIMA, Prophet, etc!

Final Takeaways:

Section	Purpose	Result
Feature Engineering	Create rich, predictive features	Rolling, lags, diff, ratios
Decomposition	Separate trend/seasonality/noise	Residuals useful for stationary data
Stationarity Testing	Confirm series is stable	Avoids model drift

X FEATURE ENGINEERING — BIG PICTURE

Feature Engineering = You create new columns based on the original data. The goal is:

- Expose hidden patterns
 Make the data easier for models to understand
- Fix statistical problems (like trend, non-stationarity)
- Make future prediction possible

Detailed Breakdown of What You Engineered

1. First Differencing (diff())

Technical background:

Differencing means **subtracting today's value - yesterday's value**: python CopyEdit

```
df['close_AAPL_diff'] = df['close_AAPL'].diff()
```

• It's **the most classic tool** to transform a non-stationary series (with trend) into a stationary series.

Why?

- Removes trend.
- Flattens the data around a constant mean.

Use Case:

- Time series models like **ARIMA**, **VAR**, and even **LSTM networks** prefer stationary data.
- Without differencing, forecasts would drift over time.

☑ Differencing solves stationarity problems caused by trends.

2. Log Differencing (Log Returns)

Technical background:

- Especially for financial data (stocks), you want to model returns, not prices.
- Log return = log(Price todayPrice yesterday)log(Price yesterdayPrice today)

Code hint (notebook does it conditionally):

```
python
CopyEdit
np.log(series / series.shift(1))
```

Why?

- Stabilizes variance (big prices don't cause artificially bigger differences).
- Helps when the stock value grows exponentially over time.

Use Case:

- In finance, returns are usually modeled instead of prices because they are closer to stationary.
- Log returns solve non-stationarity caused by exponential growth patterns.

3. Rolling Mean and Rolling Standard Deviation

Technical background:

Rolling mean = moving average:

```
python
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df['close_AAPL_rolling_mean_5'] =
df['close_AAPL'].rolling(window=5).mean()

•
Rolling std = moving standard deviation:
python
CopyEdit
df['close_AAPL_rolling_std_5'] =
df['close_AAPL'].rolling(window=5).std()
```

Why?

- Helps smooth the time series (moving average reduces noise).
- Captures **local patterns** (5-day, 20-day trends) instead of long-term trends.

Use Case:

- Useful in trend detection.
- In forecasting models, rolling features tell you whether things are locally rising or falling.
- Rolling features reduce volatility and help the model understand short-term momentum.

4. Lag Features (Past Values)

Technical background:

• Lag 1 = yesterday's value.

```
Lag 3 = value 3 days ago, and so on:
python
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df['close_AAPL_lag_1'] = df['close_AAPL'].shift(1)
```

•

Why?

- Most time series models predict the future using the past.
- Lag features inject memory into machine learning models (XGBoost, Random Forest, LSTM, etc.)

Use Case:

- You predict tomorrow's price based on today's and past days' prices.
- Lagged features give temporal context to a machine learning model.

5. Volume Features (Log Transformations and Diffs)

Technical background:

 Volumes can be very skewed: small volumes for some stocks, huge volumes for others.

```
Log transform:
python
CopyEdit
np.log1p(volume)
```

•

Difference to find changes: python
CopyEdit
volume.diff()

•

Why?

- Stabilizes scale differences.
- Captures volume shocks (important for market reactions).

Use Case:

• Volume jumps often signal important information about **future price changes**.

▼ Volume features capture market strength/weakness signals.

6. Investment Features (Total Investment and Ratios)

Technical background:

- You define investment = volume × avg price.
- Then you calculate:
 - Total daily investment
 - o Each company's share of total

Why?

- It shows where money is flowing.
- Changes in investment proportions are important for **portfolio behavior**.

Use Case:

- Useful in **building investment strategies** or **market regime detection**.
- ☑ Investment ratios capture macro shifts in market attention.

7. Time Features (Day, Month, Quarter, Year-End flags)

Technical background:

```
python
CopyEdit
df['day_of_week'] = df.index.dayofweek
df['month'] = df.index.month
df['quarter'] = df.index.quarter
df['is_month_end'] = df.index.is_month_end.astype(int)
```

Why?

- Stock behavior often depends on time:
 - Mondays vs Fridays are different.
 - o End of month trading patterns (portfolio rebalancing).

Use Case:

- Seasonality models or regression models love time flags.
- ☑ Time features allow the model to learn calendar-based behaviors.

QUICK SUMMARY TABLE

Feature Type	Solves What Problem?	Practical Use
First Difference	Non-stationary trends	Time series models
Log Return	Exponential growth	Financial forecasting
Rolling Mean/Std	High volatility	Trend smoothing
Lag Features	Memory (past values)	Forecasting
Volume Features	Scale instability	Event detection
Investment Ratios	Shifting attention	Portfolio modeling
Time Features	Seasonality	Calendar effects

How They All Help Together:

Differencing + log returns + decomposition = Make data stationary

Rolling + lags = Give local trend and momentum info

Time features + investment features = Give external explanatory signals

✓

When you feed all these into models (machine learning or statistical models), you create:

- A much richer, deeper, more predictable feature space.
- Better forecast accuracy ∠.
- Lower risk of overfitting \$\mathscr{g}\$.

Professional note:

In advanced ML competitions (like Kaggle), smart feature engineering like this wins more than just picking complex models!

The model is only as good as the data you feed it.



Your notebook's Feature Engineering was very professional because it:

- Fixed non-stationarity problems
- Created memory from past data
- Smoothed noise
- Built economic meaning into features

Step 9: Decompose Time Series

1. Theory: Why Decompose?

Real-world time series data is messy. It mixes three things:

- **Trend**: The general long-term movement (up or down)
- Seasonality: Short-term repeating patterns (weekly, monthly, yearly cycles)
- Residuals (Noise): Random fluctuations you can't predict
- Decomposition helps separate these parts so you can:
 - Analyze underlying patterns separately
 - Model or forecast each part differently if needed
 - Improve **stationarity** (important for Step 10)

2. Technical Approach: STL Decomposition

You used **statsmodels.tsa.seasonal.STL**, which is a **modern**, **robust** decomposition technique:

- Seasonal
- Trend
- Loess (local regression smoothing)

It's more flexible than classical decomposition because it doesn't assume constant seasonality.

3. Code Walkthrough

(directly from your notebook)

```
python
CopyEdit
from statsmodels.tsa.seasonal import STL
```

Parameters you used:

- period=252 → Why?
 - Because there are ~252 trading days in a year (stocks don't trade on weekends or holidays).
 - So **one year cycle =** 252 observations (for yearly seasonality).

Then for each feature you wanted to decompose:

```
python
CopyEdit
stl = STL(df[col].dropna(), period=seasonal_period)
result = stl.fit()
```

• .fit() performs the decomposition internally.

You extract:

```
python
CopyEdit
df[f'{col}_trend'] = result.trend
df[f'{col}_seasonal'] = result.seasonal
df[f'{col}_residual'] = result.resid

    result.trend — smooth long-term direction
    result.seasonal — repeating cycles
    result.resid — "random noise" leftover
```

4. Why Save These as New Columns?

Later, you can:

- Use only trends if you want to model growth.
- Study seasonality for repeated behaviors.
- Work on residuals to build better machine learning models (if you want stationary behavior).
- ☑ Decomposition makes your data much more "structured" and easier to model.

5. Important Notes:

- Before decomposition, your data needs to be properly timestamped (date as
- **NaNs** will appear at the beginning/end because smoothing needs a window.



Step 10: Stationarity Tests

1. Theory: What is Stationarity, Again?

A time series is stationary if:

- Mean is constant over time
- Variance is constant over time
- Covariance depends only on distance between observations (not actual time)
- Stationary data is predictable in structure.
- Non-stationary data might explode or drift unpredictably, making models unstable.

2. Technical Approach: ADF and KPSS Tests

You used both tests to double-check stationarity.

Test	What it checks	Null Hypothesis
ADF (Augmented Dickey-Fuller)	Checks for unit root	Series is non- stationary
KPSS (Kwiatkowski-Phillips-Schmidt-Shin)	Checks for trend stationarity	Series is stationary

☑ Good series = **ADF** p < 0.05 **AND KPSS** p > 0.05 (meaning, ADF rejects non-stationarity; KPSS fails to reject stationarity)

3. Code Walkthrough

adf_pvalue = adf_result[1] kpss_pvalue = kpss_result[1]

```
python
CopyEdit
from statsmodels.tsa.stattools import adfuller, kpss
adf_result = adfuller(series.dropna())
kpss_result = kpss(series.dropna(), regression='c', nlags="auto")
   • adfuller() returns ADF statistic and p-value.
   • kpss() returns KPSS statistic and p-value.
Then you interpret:
python
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```

You decide:

```
python
CopyEdit
if adf_pvalue < 0.05 and kpss_pvalue > 0.05:
  final_conclusion = "Stationary "
else:
  final_conclusion = "Non-Stationary X"
```

This double test is very strong because sometimes one test alone can be wrong.

4. If Non-Stationary: How to Fix?

In your notebook:

```
If series is all positive values → you try Log Return:
python
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np.log(series / series.shift(1))
```

```
If that doesn't work → you try Second Differencing:

python

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series.diff().diff()

•

If still bad → Take STL residual:

python

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STL decomposition □ use only resid part
```

☑ These transformations aim to remove trend, seasonality, and variance changes.

5. Final Output:

You create a table showing:

- Feature Name
- ADF p-value
- KPSS p-value
- Stationarity status

and only keep features that are stationary for modeling.

Why is this SO IMPORTANT?

- f your data is non-stationary:
 - Forecasting will fail X
 - Model coefficients will be biased X
 - Model evaluation will be misleading X

Stationarity = Stability = Learnable Patterns = Good Models ✓



Concept

Practical Goal

Decomposition (Step 9) Split signal into Trend + Seasonality + Noise

Stationarity Tests (Step Confirm that the data won't randomly drift or explode 10)



Timeline of your Process

```
plaintext
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Raw Data

Decomposition → Extract Trend / Seasonal / Residual

Stationarity Tests (ADF, KPSS)

If Non-Stationary → Transform (Diff / Log / Residuals)

Final Dataset → Ready for Modeling
```



Decomposition organizes the time series. **Stationarity tests** guarantee that you can safely model and forecast them.

This was **absolutely professional-level work** you did by using both STL and double stationarity tests.