# First Steps with COIN-OR

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# 5. Cbc Basics

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## 1 Overview

The goal is to study some simple elements of the COIN-OR branch-and-cut code Cbc. A reader interested in using Cbc as a black box, can just read the first four sections of this document. The remaining sections deal with the use of the Cbc library through a C++ code.

Section 2 covers the download and installation of the Cbc package and Section 3 deals with the generation of the html documentation and customization. Section 4 shows how to to use the code as a black box through the command line interface.

Section 5 gives instruction to compile the code of the project PROJ5. Section 6 describes the most important class of Cbc, the CbcModel class. Section 7 shows how to use the Cgl cut generators, while Section 8 presents some of the predefined heuristics and gives a simple example of a user-defined heuristic. Section 9 deals with some of the predefined node selection rules and shows how the user can easily define his own rule. Finally, Section 10 and Section 11 discuss the selection of branching variables for strong branching and the selection of the best of those after optimization for the candidates is done. Section 10 presents some candidate selection rules used during the strong branching phase of the code. A simple example of a user-defined selection rule is also given. Section 11 surveys an example using pseudocosts and priorities associated with the variables.

These sections can be used to customize most of the behavior of Cbc. However, unless the problem to be solved requires heavy customization, in general one wish to experiment with a slight variation of the default Cbc code. Section 12 show how to use callback and CbcEvent to do that, starting from the default settings and altering the behavior of Cbc by adding customization through code and command line parameters.

A more detailed presentation of Cbc is available on the web [8].

## 2 Download and Installation

This section covers the installation of the software Cbc on a machine running Linux Fedora 12 with the tc shell. If you run another shell or use another Linux distribution, some of the Linux commands might be slightly different. Note that this project can also be compiled under Cygwin on Windows machines.

There are more than one way to get code from COIN-OR. Besides the use of tar balls described below, it is also possible to use the Subversion

versioning software (svn) [11]. While using svn is more flexible, it is also more complex. For more information about using svn go to the COIN-OR help pages [6].

- 1. Go in your main directory.
- 2. Download the Cbc package tar ball: Using a web browser, go to the COIN-OR download site http://www.coin-or.org/download, click on Cbc and download the most recent tar ball of Cbc. At the time of this writing, this is Cbc-2.6.1.tgz.
- 3. Decompress the tar ball

```
% tar -xvf Cbc-2.6.1.tgz
```

4. Go in the newly created directory Cbc-2.6.1:

5. Create a build directory build and go there:

% mkdir build

% cd build

6. Configure the package according to your system:

```
% ../configure -C >& last_configure.txt
```

If the last lines of the file last\_configure.txt do not contain:

configure: Main configuration of Cbc successful

then the configuration failed and you might need to provide information to the configuration script. The Trac pages [6, 7] might help you figure out what is wrong.

It is advisable to use Cbc with Lapack and Blas for better numerical stability. The configure script installing a COIN-OR package does its best to find Lapack and Blas libraries on your system. These are usually, but not always, located in /usr/lib or /usr/lib64. To check if the configure script was successful in finding these libraries, use from build:

% grep lapack last\_configure.txt

If you get a line like:

#### checking whether -llapack has LAPACK... no

then configure was not able to find the Lapack library and you are advised to add it manually, although the code will work even if you do not do it. Please refer to Section 4 (and more specifically Section 4.1) of the first project (projl.pdf) for more detailled instructions.

7. Compile the code:

% make

8. Test the code:

% make test

If the last lines of the output do not contain (timing may vary, of course):

cbc\_clp solved 2 out of 2 and took 3.74443 seconds. then something is wrong. See the Trac pages [3, 4, 6, 7] for help.

9. To install the include files in the directory Cbc-2.6.1/build/include/coin, the libraries in the directory Cbc-2.6.1/build/lib, and the executables in the directory Cbc-2.6.1/build/bin use:

% make install

Note that the use of the directory Cbc-2.6.1/build is not absolutely necessary and it is possible to build the code from Cbc-2.6.1 or from any other directory of your choosing. See the first project (proj1.pdf) for more information.

The Cbc-2.6.1/build/bin directory now contains two executables: clp, and cbc. The code clp is a linear programming solver and the code cbc is a branch-and-cut code studied in Section 4 and beyond and works with clp.

The Cbc-2.6.1/build/lib directory contains, among others, the libraries libCbc and libOsiCbc and Cbc-2.6.1/build/include/coin contains all the header files. The directory Cbc-2.6.1/Cbc/examples contains several example codes that might be helpful for understanding a specific feature of Cbc. These can be compiled by typing in Cbc-2.6.1/build/Cbc/examples:

% make DRIVER=example\_name

where example\_name is one of: allCuts, barrier, CbcBranchFollow2, CbcBranchLink, cbc\_driverC\_sos, CbcBranchUser, CbcCompareUser, CbcSolver2, CbcSolver3, CbcSolverLongThin, ClpQuadInterface, crew, driver2, driver3, driver4, driver, fast0507b, fast0507, gear, hotstart, link, longthin, lotsize, minimum, modify, nway, qmip, qmip2, quad, quad2, repeat, sample1, sample2, sample3, sample4, sample5, simpleBAB, sos, sudoku.

Note that when linking your own code with libraries located in directory Cbc-2.6.1/build/lib, you should always use the header files in Cbc-2.6.1/build/include/coin, not the header files that you can find in other subdirectories of Cbc-2.6.1.

In the rest of this document, we will use SrcCbc as a shorthand for the directory Cbc-2.6.1/Cbc/src and we will look at header files there, but this is just for convenience, as this directory contains all the files we are interested in.

## 3 Documentation and Custom Configuration

The Trac pages for Cbc are located at [3, 4]. Additional information, access to mailing lists, and instructions for reporting bugs can be found there.

Please refer to the first project (see proj1.pdf) for the generation of the html documentation and useful flags for the configure scripts.

After generating the html documentation, open in a browser the file Cbc-2.6.1/build/doxydoc/html/index.html, click on the link Classes on top of the page and make a bookmark reference to that page. It will be referred to as DocCbc.

## 4 Command Line Interface

1. Go to the directory PROJ5.

The stand-alone code cbc can be run using:

2.  $\% \sim / \text{Cbc-2.6.1/build/bin/cbc dcmulti.mps}$ 

It reads the file dcmulti.mps (an integer linear program in MPS format) and solves the corresponding ILP using Cbc and Clp, using all defaults of cbc. (Cbc can also read input files in LP format.) Some of the parameters of cbc can be controlled using the command line interface. To enter the command line mode, use:

### 3. $\% \sim /\text{Cbc-2.6.1/build/bin/cbc}$ -

You should get the prompt "Coin:". Entering

#### 4. Coin: ?

gives a list of commands that cbc understands. Some of them, for example, are:

- option?: short help for command option;
- import name: read MPS or LP file name;
- export name: write MPS file name;
- gomory option where option is one of:
  - on: use Gomory cuts;
  - off: do not use Gomory cuts;
  - root: use Gomory cuts only at the root;
  - ifmove: use while Gomory cuts improve bound; this is the default setting;
  - forceOn: force use at every node;
- roundingHeuristic on/off: use/turn off rounding heuristic;
- branchAndCut: solve the ILP by branch-and-cut;
- logLevel k: set the level of output to k;
- solution sol.txt: print the optimal solution in file sol.txt. To print on screen use stdout as file name;
- quit: quit the program.

Note that this command line interface is not a very robust code, but the problem is only with the interface, not with the underlying library. It is quite easy to make act in strange ways (for example, try to import and solve p0033.mps and then import and solve dcmulti.mps), but the problem is only with the interface, not with the underlying library. To run cbc with its default settings, use:

Coin: import dcmulti.mps

Coin: branchAndCut

To prevent cbc to use Gomory cuts, use:

Coin: import dcmulti.mps

Coin: gomory off

Coin: branchAndCut

Note that it is also possible to issue a single command collecting all the options that you want to set. For example the command

```
% \sim/Cbc-2.6.1/build/bin/cbc -import p0033.mps \ -gomory off -branchAnd -solution stdout
```

loads p0033.mps, turns off Gomory cuts generation, solve the problem and print the solution to the screen.

Do the following:

- 5. Write down the cpu time taken to solve dcmulti.mps with the default settings.
- 6. By changing the default settings for Gomory cuts, Mixed Integer Rounding cuts, Probing cuts, Rounding heuristic and strong branching what improvement in term of running time can you get when solving dcmulti.mps? Experiment with four or five settings.
- 7. Set the logLevel to value k for  $0 \le k \le 4$  and try to understand what is in the output in each case.

# 5 Compiling the Project Code

The files proj5.cpp, p5\_driver4.cpp and related code can be compiled by typing in the directory PROJ5:

#### 8. % make

If the compilation fails, you might have to modify some of the entries in PROJ5/makefile. Here are some modifications that might be needed:

1) If you placed the build directory somewhere else than in the recommended \$(HOME)/Cbc-2.6.1/build, replace in the makefile CBC = \$(HOME)/Cbc-2.6.1/build by the correct full path.

- 2) If you get an error message at run time saying that some shared COIN-OR library can not be loaded, you might need to add the path to the Cbc-2.6.1/build/lib/coin directory into the environment variable LD\_LIBRARY\_PATH.
- 3) If the configure script used in step 6 of Section 2 was able to find Lapack and Blas libraries on your machine you might need to define additional environment variables, as described in Section 4.1 of projl.pdf. To check if the configure script indeed found Lapack, use:

```
% grep lapack last_configure.txt
```

If Lapack was found, this should print a line resembling on of the following:

```
checking whether -llapack has LAPACK... yes checking whether user supplied LAPACKLIB="/usr/lib/liblapack.so.3" works... yes
```

The code can be run using:

## 9. % ./proj5

and enter, for example, p0033.mps when prompted for an input file. The code currently asks for the input file name and accepts either an LP file (the extension of the file name must be ".lp") or an MPS file (the extension of the file name must be ".mps"). It then reads the input file, solves the ILP, and prints the optimal solution. The code can be compiled with the flag -DTRACE (see file PROJ5/makefile, line starting with DEFS =) or without it. Removing it will remove most of the default output. Additional flags are -DPRIORITIES, -DPSEUDO , and -DPSEUDODYN whose use and meaning will be explained in Section 11. The code p5\_driver4 is an example of customization using many of the default setting of Cbc and is described in Section 12.

## 6 Class CbcModel

The class CbcModel is the central class of Cbc. A model holds the description of the problem, and, among others, the branching decision rules, the cut generators, and the heuristics to use during the solution process. It also gives access to the result of the optimization.

The simplest way to create a CbcModel object is to read an LP or MPS file in an OsiSolverInterface object and then to create the model, as done in PROJ5/proj5.cpp. It is of course possible to build the representation of the problem in the OsiSolverInterface object from memory instead of reading a file, similarly to what was done earlier in projects 2 and 3.

Useful methods<sup>1</sup>:

- branchAndBound(): Use branch-and-cut to optimize the problem contained in the model;
- setIntegerTolerance(): Set tolerance for deciding if a number is integer or not;
- setMaximumSeconds(): Set the time limit.
- setNumberStrong(): Set the number of candidates considered during strong branching;
- setLogLevel(): Set the level of the output.
- setPrintFrequency(): Set the frequency for printing the status line for the optimization;
- getObjValue(): Give the value of the best known feasible solution;
- bestSolution(): Give a pointer on the best known feasible solution;
- phase(): Get the phase number of the optimization;
- setBestSolution(): Set the best known solution and its value;
- setBestObjectiveValue(): Set the objective value to beat;
- addCutGenerator(): Add a Cgl cut generator (see Section 7);
- addHeuristic(): Add a heuristic (see Section 8);
- setNodeComparison(): Set the rule for selecting the next node to process (see Section 9);
- setBranchingMethod(): Set the rule used to select the best candidate during strong branching (see Section 10);

<sup>&</sup>lt;sup>1</sup>SrcCbc/CbcModel.hpp, cSrcCbc/CbcModel.cpp or DocCbc->CbcModel.

• addObjects(): Add to the model objects describing the integrality of the variables (see Section 11);

Do the following:

- 10. Find out how to set a limit on the number of cutting passes at the root node. Modify the file PROJ5/proj5.cpp to limit the number of such passes to 10.
- 11. Find out how to specify an upper bound on the optimal solution value (for a minimization problem). Modify the file PROJ5/proj5.cpp so that the user is prompted for giving such an upper bound at the beginning of the execution.

## 7 Pre-defined Cut Generators

The Cgl library contains a number of cut generators that can easily be added to the model. Assuming that the CbcModel object has name model, the key method is model.addCutGenerator(generator, mode, name); where

- generator is a pointer on a Cgl generator, such as CglGomory for Gomory cuts or CglKnapsack for knapsack covers (see DocCbc for the complete list of available generators);
- mode is an integer controlling how often the generator is called. If mode
  is set to k with
  - i) k = 0, 1: the generator is called at every node;
  - ii) k > 1: the generator is called every k nodes;
  - iii)  $-98 \le k < 0$ : the generator is called every (-k) nodes but it may be switched off by Cbc;
  - iv) k = -99: the generator is only called at the root node;
  - v) k < -99: the generator is not used.
- name is a string of characters that will be associated with the generator and used when output is written.

There are additional parameters to the method addCutGenerator() but the above ones are sufficient for most applications. The file PROJ5/proj5.cpp gives an example for using the Probing cut generator and the Gomory cut generator, including parameter setting for the generators.

Do the following:

12. Add a Mixed Integer Rounding cut<sup>2</sup> generator to the model defined in PROJ5/proj5.cpp. Set the maximum number of aggregations to 10. Make sure that the generator will be called every 10 nodes, leaving to Cbc the option to turn it off at any time. Don't forget to add the required include statements.

## 8 Heuristics

Some of the predefined heuristics are:

- Rounding: class CbcRounding<sup>3</sup>;
- Relaxation Induced Neighborhood Search (RINS): class CbcHeuristicRINS<sup>4</sup> (see [2]);
- Feasibility Pump: class CbcHeuristicFPump<sup>5</sup> (see [10]);
- Greedy: class CbcHeuristicGreedy<sup>6</sup>;
- Pivot and Fix: class CbcHeuristicPivotAndFix<sup>7</sup>;
- Diving: classes CbcHeuristicDiveCoefficient<sup>8</sup>, CbcHeuristicDiveFractional<sup>9</sup>, CbcHeuristicDiveGuided<sup>10</sup>, CbcHeuristicDiveVectorLength<sup>11</sup>,

 $<sup>^2 {\</sup>tt Cbc-2.6.1/Cgl/src/CglMixedIntegerRounding/CglMixedIntegerRounding.hpp,} \\ {\tt Cbc-2.6.1/Cgl/src/CglMixedIntegerRounding/CglMixedIntegerRounding.cpp} \ \, {\tt or} \ \, {\tt DocCbc->CglMixedIntegerRounding.} \\ \\ {\tt Cbc-2.6.1/Cgl/src/CglMixedIntegerRounding.cpp} \ \, {\tt or} \ \, {\tt DocCbc->CglMixedIntegerRounding.} \\ \\ {\tt Cbc-2.6.1/Cgl/src/CglMixedIntegerRounding.cpp} \ \, {\tt or} \ \, {$ 

<sup>&</sup>lt;sup>3</sup>SrcCbc/CbcHeuristic.hpp, SrcCbc/CbcHeuristic.cpp or DocCbc->CbcRounding.

<sup>&</sup>lt;sup>4</sup>SrcCbc/CbcHeuristicRINS.hpp, SrcCbc/CbcHeuristicRINS.cpp or DocCbc->CbcHeuristicRINS.

 $<sup>^5 {\</sup>tt SrcCbc/CbcHeuristicFPump.hpp}, {\tt SrcCbc/CbcHeuristicFPump.cpp}$  or DocCbc->CbcHeuristicFPump.

 $<sup>^6 {\</sup>tt SrcCbc/CbcHeuristicGreedy.hpp}, {\tt SrcCbc/CbcHeuristicGreedy.cpp}$  or DocCbc->CbcHeuristicGreedy.

<sup>&</sup>lt;sup>7</sup>SrcCbc/CbcHeuristicPivotAndFix.hpp, SrcCbc/CbcHeuristicPivotAndFix.cpp or DocCbc->CbcHeuristicPivotAndFix.

<sup>&</sup>lt;sup>8</sup>SrcCbc/CbcHeuristicDiveCoefficient.hpp,

SrcCbc/CbcHeuristicDiveCoefficient.cpp or DocCbc->CbcHeuristicDiveCoefficient.

<sup>9</sup>SrcCbc/CbcHeuristicDiveFractional.hpp,

SrcCbc/CbcHeuristicDiveFractional.cpp or DocCbc->CbcHeuristicDiveFractional.

<sup>&</sup>lt;sup>10</sup>SrcCbc/CbcHeuristicDiveGuided.hpp,

SrcCbc/CbcHeuristicDiveGuided.cpp or DocCbc->CbcHeuristicDiveGuided.

<sup>11</sup> SrcCbc/CbcHeuristicDiveVectorLength.hpp,

SrcCbc/CbcHeuristicDiveVectorLength.cpp or DocCbc->CbcHeuristicDiveVectorLength.

 ${\tt CbcHeuristicDivePseudoCost}^{12}, {\tt CbcHeuristicDiveLineSearch}^{13}.$ 

Assuming that the CbcModel object has name model, the key method to add an heuristic is model.addHeuristic(heur); where heur is a pointer on an object of one of the above classes or on an object of a user defined heuristic class.

To code a new heuristic, a new class has to be derived from the class CbcHeuristic defined in the same files as the Rounding heuristic mentioned above. As a simple example, the files PROJ5/p5\_HeuristicRound.hpp and PROJ5/p5\_HeuristicRound.cpp implement in class p5\_HeuristicRound the simplest rounding heuristic where each integer variable value is rounded to the nearest integer. Besides a number of constructor, destructor, clone, and assignment methods that must be implemented as they are virtual in the base class, the core of the heuristic is implemented in the method p5\_HeuristicRound::solution().

Do the following:

13. Add the Feasibility Pump heuristic available in Cbc to the model in PROJ5/proj5.cpp. Set the maximum number of passes to 10. Don't forget to add the required include statements.

## 9 Node Selection

Some of the predefined node selection rules  $^{14}$  are:

- Depth-First: class CbcCompareDepth<sup>15</sup>;
- Best-First: class CbcCompareObjective 16;
- Hybrid strategy: class CbcCompareDefault<sup>17</sup>. This is the default comparison rule of Cbc. It is based on the infeasibility of the nodes their depths and objective values. See the code for more details.
- Heuristic strategy: class CbcCompareEstimate<sup>18</sup>. Selection based on an estimation of the objective value of the subproblem.

 $<sup>^{12} {\</sup>tt SrcCbc/CbcHeuristicDivePseudoCost.hpp},$ 

SrcCbc/CbcHeuristicDivePseudoCost.cpp or DocCbc->CbcHeuristicDivePseudoCost.

 $<sup>^{13} {\</sup>tt SrcCbc/CbcHeuristicDiveLineSearch.hpp},$ 

SrcCbc/CbcHeuristicDiveLineSearch.cpp or DocCbc->CbcHeuristicDiveLineSearch.

 $<sup>^{14} {\</sup>tt SrcCbc/CbcCompareActual.hpp, SrcCbc/CbcCompareActual.cpp.}$ 

<sup>&</sup>lt;sup>15</sup>DocCbc->CbcCompareDepth.

<sup>16</sup>DocCbc->CbcCompareObjective.

<sup>17</sup>DocCbc->CbcCompareDefault.

<sup>&</sup>lt;sup>18</sup>DocCbc->CbcCompareEstimate.

Assuming that the CbcModel object has name model, the key method to set the comparison rule is model.setNodeComparison(compare); where compare is a pointer on an object of one of the above classes or on an object of a user defined comparison class.

To code a new comparison rule, a new class has to be derived from the class CbcCompareBase<sup>19</sup>. For example, files PROJ5/p5\_CompareDFS\_BFS.hpp and PROJ5/p5\_CompareDFS\_BFS.cpp implement class p5\_CompareDFS\_BFS corresponding to the following selection rule: Start with Depth-First-Search (DFS) until either two feasible solutions have been found or one thousand nodes have been processed. Then, switch to Breadth-First-Search (BFS).

The class p5\_CompareDFS\_BFS has a data member called do\_DFS which indicates if DFS or BFS should be used. Besides a number of constructor, destructor, clone, and assignment methods that must be implemented as they are virtual in the base class, the core of the rule is implemented in the method p5\_CompareDFS\_BFS::test().

The method p5\_CompareDFS\_BFS::newSolution() is called each time a new feasible solution is found. It is used to switch to DFS as soon as two feasible solutions have been found.

The method p5\_CompareDFS\_BFS::every1000Nodes() is called every thousand nodes, starting from the root node. It is used to switch to DFS if one thousand nodes have been processed.

Do the following:

14. Try to understand the code for the default node selection of Cbc. Good luck.

## 10 Best Candidate Selection Rule

After strong branching on several candidate is done, a selection rule for the branching variable is required. Some of the predefined candidate selection rules are:

• Default selection: class CbcBranchDefaultDecision<sup>20</sup>. Selection is based on four different criteria. See the code for more details;

<sup>&</sup>lt;sup>19</sup>SrcCbc/CbcCompareBase.hpp, SrcCbc/CbcCompareBase.cpp or DocCbc->CbcCompareObjective.

<sup>&</sup>lt;sup>20</sup>SrcCbc/CbcBranchActual.hpp, SrcCbc/CbcBranchActual.cpp or DocCbc->CbcBranchDefaultDecision.

• Alternative selection: class CbcBranchDynamicDecision<sup>21</sup>. Selection is based on infeasibility until a feasible solution is found by search, then switch to selection based on change in objective value.

Assuming that the CbcModel object has name model, the key method to set the candidate selection rule is model.setBranchingDecision(bdec); where bdec is a pointer on an object of one of the above classes or on an object of a user defined candidate selection class.

To code a new selection rule, a new class has to be derived from the class CbcBranchBase<sup>22</sup>. As a simple example, the files PROJ5/p5\_Branch.hpp and PROJ5/p5\_Branch.cpp implement class p5\_Branch corresponding to the following candidate selection rule: Pick the candidate for which the minimum improvement in the value of the objective function in its two sons is maximum

Besides a number of constructor, destructor, clone, and assignment methods that must be implemented as they are virtual in the base class, the core of the rule is implemented in the method p5\_Branch::bestBranch().

Do the following:

15. Modify the files PROJ5/p5\_Branch2.hpp,cpp (the class defined in these files is identical to the class p5\_Branch) to implement a new class p5\_Branch2 for the selection rule of [1]: If branching on variable  $x_i$  gives an improvement of  $q_1$  in the first son and an improvement  $q_2$  in the second son, the score associated with branching on  $x_i$  is

$$\frac{5}{6}\min\{q_1,q_2\} + \frac{1}{6}\max\{q_1,q_2\} \ .$$

The index of the branching variable is chosen so that it maximizes the above value. Use your new class instead of p5\_Branch in the model defined in PROJ5/proj5.cpp.

# 11 Variable Selection for Strong Branching

Without going into too much details, it might be useful to understand how integrality conditions are used and stored in Cbc. For each integer vari-

<sup>&</sup>lt;sup>21</sup>SrcCbc/CbcBranchDynamic.hpp, SrcCbc/CbcBranchDynamic.cpp or DocCbc->CbcBranchDynamicDecision.

<sup>&</sup>lt;sup>22</sup>SrcCbc/CbcBranchBase.hpp, SrcCbc/CbcBranchBase.cpp or DocCbc->CbcBranchBase.

able, Cbc associates an object of class CbcObject<sup>23</sup>. An object has methods, among others, to check feasibility and generate branching objects. By default, Cbc associates an object of class CbcSimpleInteger<sup>24</sup> to each integer variable  $x_i$ , implementing the usual branching rule "either  $x_i \leq k$  or  $x_i \geq k + 1$ " for some integer k.

The simplest way to direct the choice of variables for performing strong branching in Cbc is to define priorities on the integer variables, i.e. to associate an integer  $p_i$  with each integer variable  $x_i$ . Then, when candidates for strong branching are selected, variable  $x_i$  will be preferred to variable  $x_j$  if  $p_i < p_j$ . To use priorities with the code, set the flag -DPRIORITIES on the line starting by "DEFS =" in PROJ5/makefile and recompile using make.

Another way to direct the choice of variables for performing strong branching is to define pseudo-costs associated with each integer variables. Although dynamic pseudo-costs (i.e. pseudo-costs that are updated during the search) are more powerful, the example in PROJ5/proj5.cpp just sets static pseudo-costs: For integer variable  $x_i$  with objective coefficient  $c_i$ , its pseudo-cost for branching up or down is set to the absolute value of  $c_i$ .

The predefined class CbcSimpleIntegerPseudoCost<sup>25</sup> is convenient to use pseudo-costs. We just need to construct an object of this class for each integer variable, collect these objects in an array and use the method model.addObjects() to add them to the model.

If we add an object of class CbcSimpleIntegerPseudoCost associated with variable  $x_i$ , Cbc recognizes that this is an object of a class derived from CbcSimpleInteger and will replace the existing object by the new one.

To use pseudo-costs with the code, set the flag -DPSEUDO on the line starting by "DEFS =" in PROJ5/makefile and recompile proj5 using make in PROJ5. Note that using both flags -DPRIORITIES and -DPSEUDO is identical to using only the second one, as the priorities are passed to the model before the objects used for pseudo-costs are passed to the model. It is possible to define both priorities and pseudo-costs and the candidate selection will use both in a non trivial way (see method CbcNode::chooseBranch()<sup>26</sup>).

Do the following:

 $<sup>^{23} {\</sup>tt SrcCbc/CbcBranchBase.hpp}, {\tt SrcCbc/CbcBranchBase.cpp} \ {\tt or} \ {\tt DocCbc->CbcObject}.$ 

 $<sup>^{24} {\</sup>tt SrcCbc/CbcBranchActual.hpp}, {\tt SrcCbc/CbcBranchActual.cpp} \ {\tt or} \ {\tt DocCbc->CbcSimpleInteger}.$ 

 $<sup>^{25} {\</sup>tt SrcCbc/CbcBranchActual.hpp}, {\tt SrcCbc/CbcBranchActual.cpp} \ {\tt or} \ {\tt DocCbc->CbcSimpleIntegerPseudoCost}.$ 

<sup>&</sup>lt;sup>26</sup>SrcCbc/CbcNode.cpp or DocCbc->CbcNode.

16. Use the class CbcSimpleIntegerDynamicPseudoCost<sup>27</sup> which implements the dynamic pseudo-costs of [1] instead of the pseudo-costs used in PROJ5/proj5.cpp. Just defining objects of that class for each integer variable and adding them to the model is enough. Add your code between

```
#ifdef PSEUDODYN
...
#endif
```

add the flag PSEUDODYN (removing -DPRIORITIES and -DPSEUDO if present) on the line starting with "DEFS ="," in the makefile and recompile using make. Don't forget to add the required include statements.

## 12 Customizing the default Cbc code

In this section, we use a combination of the command line options (see Section 4) and the customization covered in the subsequent sections to add customization to the default Cbc settings. The code is based on the example driver4 that can be found in Cbc-2.6.1/Cbc/examples. The main part of the code is in file p5\_driver4.cpp. The code expects the name of the input file (either an LP or MPS file) followed by the Cbc command line options that should be passed to Cbc, in the same format as seen in Section 4.

For example, you can use:

```
% ./p5_driver4 p0033.mps -logLevel 2 -branchA
```

The code in p5\_driver4.cpp reads the input file, asks for an upper bound value that will be passed to Cbc, creates a CbcModel, adds to it an event handler, and call CbcMain1() with the command line options given to p5\_driver4. Finally, it prints the best known solution in file f\_sol.xxx. Customization is done in two ways: Using the event handler and callback. These two options are described in more detail in the next two sections.

The files p5\_miscMeth.hpp and p5\_miscMeth.cpp contain several simple methods: printFileName() to print the name of the input file and upper bound, printInfoLine() to print the best known solution value, the current LP relaxation bound, the cpu time, node number, final Cbc status

 $<sup>^{27} {\</sup>tt SrcCbc/CbcBranchDynamic.hpp}, {\tt SrcCbc/CbcBranchDynamic.cpp} \ {\tt or} \ {\tt DocCbc->CbcSimpleIntegerDynamicPseudoCost}.$ 

and secondary status<sup>28</sup>, printSol() to print the best known solution and getSolverPtr() to get a pointer on the solver of a CbcModel. These method are useful to perform the tasks listed below.

### 12.1 Class p5\_CbcEventHandler

The class p5\_CbcEventHandler<sup>29</sup> is derived from class CbcEventHandler<sup>30</sup> and the only non trivial method is p5\_EventHandler::event(). That function is called from Cbc each time some predefined CbcEvent<sup>31</sup> occurs. The events we are interested here are node, solution, and heuristicSolution. A node event occurs at the end of the processing of a node, a solution event when a feasible solution is found by the LP relaxation, and a heuristicSolution event when a feasible solution is found by one of the heuristics. By adding code in p5\_EventHandler::event(), one can direct Cbc to perform operations each time one of these events occur. The method should return a CbcAction<sup>32</sup> and can be either noAction (i.e. continue regular operations), stop, restart, or restartRoot which are self-explanatory.

As an illustration, try to implement the following:

- 17. Print a line info in file f\_res.xxx (using a call to printInfoLine()) and print on the screen the current best known solution value of the preprocessed problem each time a feasible solution is found.
- 18. Print the number of integer variables with fractional value in the solution of the final LP relaxation at each node of the tree.

#### 12.2 Callback

It is possible to pass a callback method to Cbc. An example of such a method is callback()<sup>33</sup> which has a parameter whereFrom that can have any value between 1 and 5 with the following meaning:

- 1: After solving the initial LP relaxation;
- 2: After preprocessing;

<sup>&</sup>lt;sup>28</sup>See SrcCbc/CbcModel.hpp or DocCbc->CbcModel for a description of status and secondary status

<sup>&</sup>lt;sup>29</sup>See files p5\_EventHandler.hpp, p5\_EventHandler.cpp.

<sup>&</sup>lt;sup>30</sup>SrcCbc/CbcEventHandler.hpp, SrcCbc/CbcEventHandler.cpp or DocCbc->CbcEventHandler.

<sup>&</sup>lt;sup>31</sup>SrcCbc/CbcEventHandler.hpp, DocCbc->CbcEventHandler.

<sup>&</sup>lt;sup>32</sup>SrcCbc/CbcEventHandler.hpp or DocCbc->CbcEventHandler.

<sup>&</sup>lt;sup>33</sup>See files p5\_callback.hpp and p5\_callback.cpp.

- 3: Just before starting the branch-and-cut;
- 4: Just after finishing the branch-and-cut (before post processing);
- 5: After post processing.

The method callback() is called by Cbc at each of these steps, with the corresponding value for whereFrom. It is thus possible to direct Cbc to perform operations depending on that value.

As an example, try to implement the following:

- 19. Direct Cbc to use the node comparison rule p5\_CompareDFS\_BFS, to use the Feasibility Pump heuristic at every node of the tree with a maximum of 10 passes, to use the CbcHeuristicDiveFractional heuristic at every node of the tree with a maximum time of 5 minutes, no limit on iteration number, fixing all integer variables with current integer value, and a maximum of 5000 nodes, as well as the simple rounding heuristic p5\_HeuristicRound at every node of the tree. All this can be implemented in the method setMySelection()<sup>34</sup> that is called by callback() just before the start of the branch-and-cut.
- 20. Make a call to printLineInfo() to print the final information line at the end of the solution process.

## References

- [1] T. Achterberg, T. Koch, A. Martin, "Branching Rules Revisited", Operations Research Letters 33 (2005), 42–54.
- [2] Danna E., Rothberg E., Le Pape C., "Exploring Relaxation Induced Neighborhoods to Improve MIP Solutions", *Mathematical Programming* 102 (2005), 71–90.
- [3] http://www.coin-or.org/projects/Cbc.xml
- [4] https://projects.coin-or.org/Cbc
- [5] http://www.coin-or.org/download/source
- [6] https://projects.coin-or.org/CoinHelp
- [7] https://projects.coin-or.org/CoinHelp/wiki/user-troubleshooting
- [8] J. Forrest, R. Lougee-Heimer, "CBC User Guide", http://www.coin-or.org/Cbc/cbcuserguide.html

<sup>&</sup>lt;sup>34</sup>See file p5\_callback.cpp.

- $[9] \ \mathtt{http://www.stack.nl/}{\sim} \mathtt{dimitri/doxygen/}$
- [10] M. Fischetti, F. Glover, A. Lodi, "The feasibility pump" *Mathematical Programming* 104 (2004), 91–104.
- [11] http://subversion.tigris.org/