Table of Contents

QUESTION 1:	
QUESTION 2:	
QUESTION 3:	
QUESTION 4:	
QUESTION 5:	
QUESTION 6:	
QUESTION 7:	
QUESTION 8:	
ALL FUNCTIONS SUPPORTING THIS CODE	10

clear;

QUESTION 1:

```
% Function is at the bottom in the supporting code section
% function out = f(theta)

% Testing theta = pi/4
f(pi/4)

% Testing theta = -pi/4
f(-pi/4)

% Both are close to 0, so we are good
```

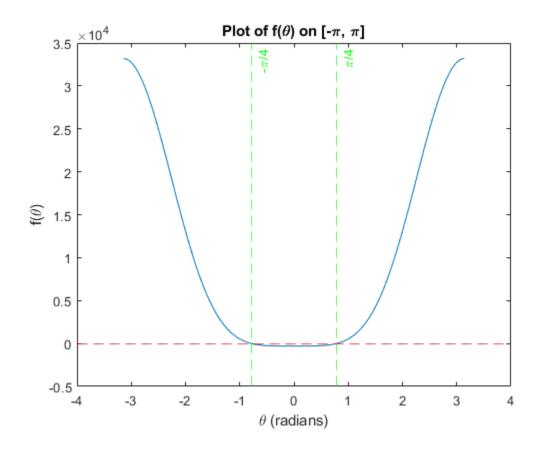
QUESTION 2:

```
% Plotting f(theta) on [-pi, pi]
theta_vals = -pi:0.01:pi;

f_vals = f(theta_vals);

figure(1)
plot(theta_vals, f_vals)
xlabel('\theta (radians)')
ylabel('f(\theta)')
title('Plot of f(\theta) on [-\pi, \pi]')
yline(0, '--r');
xline(pi/4, '--g', '\pi/4');
xline(-pi/4, '--g', '-\pi/4');
drawnow;

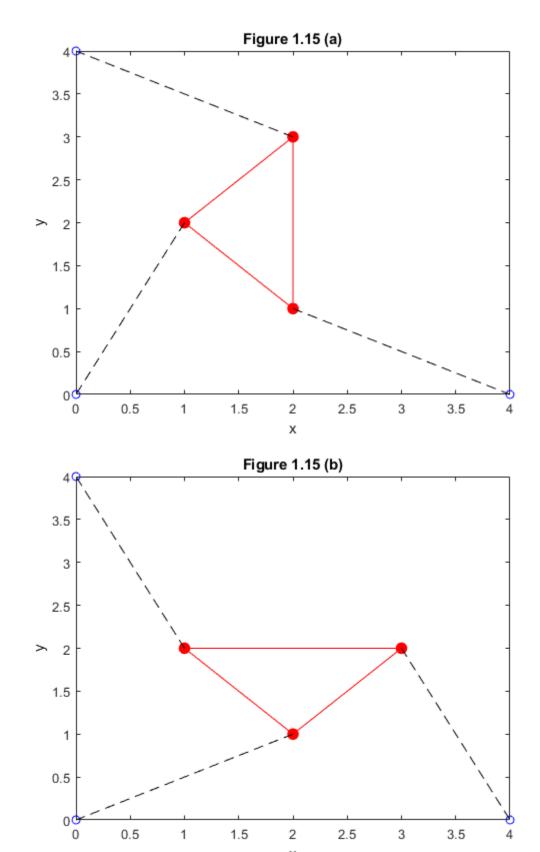
% Plot clearly shows that there are roots at +/- pi/4
```



QUESTION 3:

```
% Pose from Figure 1.15 (a)
% Connected to (0, 0) aka (x, y)
u1 = 1; v1 = 2;
% Connected to (x1, 0)
u2 = 2; v2 = 1;
% Connected to (x2, y2)
u3 = 2; v3 = 3;
x1 = 4; x2 = 0; y2 = 4;
figure(2)
plot([u1 u2 u3 u1], [v1 v2 v3 v1], 'r'); hold on
                                                        % Platform triangle
plot([0 x1 x2], [0 0 y2], 'bo')
                                                       % Base anchors
plot([u1 u2 u3], [v1 v2 v3], 'ro', 'MarkerSize', 8, 'MarkerFaceColor', 'r')
% Platform joints
plot([u1 0], [v1 0], 'k--') % p1
plot([u2 x1], [v2 0], 'k--') % p2
plot([u3 x2], [v3 y2], 'k--') % p3
title('Figure 1.15 (a)')
xlabel('x')
```

```
ylabel('y')
drawnow;
% Pose from Figure 1.15 (b)
% Connected to (0, 0) aka (x, y)
u1 = 2; v1 = 1;
% Connected to (x1, 0)
u2 = 3; v2 = 2;
% Connected to (x2, y2)
u3 = 1; v3 = 2;
x1 = 4; x2 = 0; y2 = 4;
figure(3)
plot([u1 u2 u3 u1], [v1 v2 v3 v1], 'r'); hold on
                                                   % Platform triangle
plot([0 x1 x2], [0 0 y2], 'bo')
                                                        % Base anchors
plot([u1 u2 u3], [v1 v2 v3], 'ro', 'MarkerSize', 8, 'MarkerFaceColor', 'r')
% Platform joints
plot([u1 0], [v1 0], 'k--') % p1
plot([u2 x1], [v2 0], 'k--') % p2
plot([u3 x2], [v3 y2], 'k--') % p3
title('Figure 1.15 (b)')
xlabel('x')
ylabel('y')
drawnow;
% Here, we're just reproducing Figure 1.15 (a) and (b)
```



2

Х

2.5

3

3.5

1.5

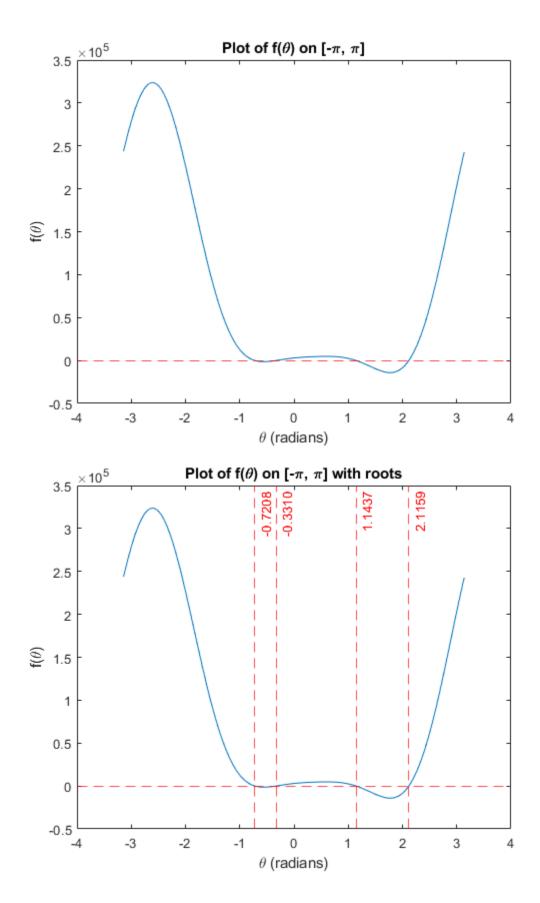
0.5

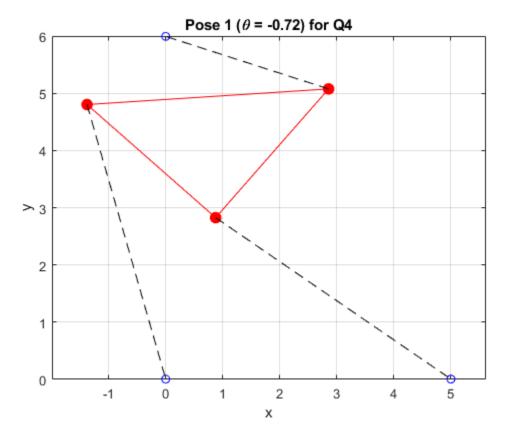
1

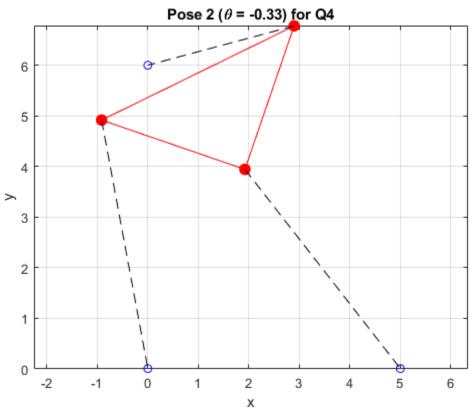
QUESTION 4:

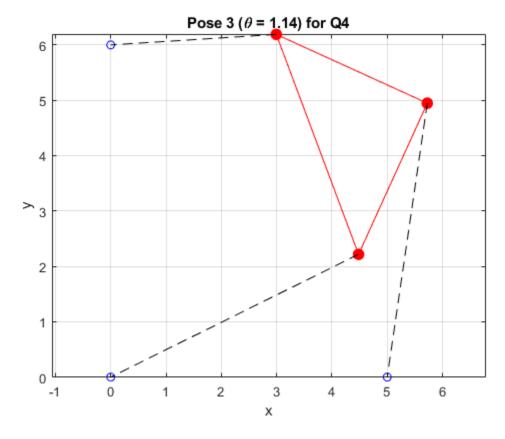
```
% Forward kinematics is when we compute (x, y) and theta for each given p1,
% p2, and p3
% The inverse kinematic problem is when we find p1, p2, p3, given x, y, and
% The new f(theta) function is in the supporting functions section at the
% bottom (f 4(theta))
% Plotting f 4(theta) on [-pi, pi]
theta vals = -pi:0.01:pi;
f \text{ vals} = f 4 \text{ (theta vals)};
figure(4)
plot(theta vals, f vals)
xlabel('\theta (radians)')
ylabel('f(\theta)')
title('Plot of f(\theta) on [-\pi, \pi]')
yline(0, '--r');
drawnow;
% Finding the four theta values (quesses are from eyeballing the graph)
theta1 = fzero(@f 4, -0.72);
theta2 = fzero(@f 4, -0.33);
theta3 = fzero(@f 4, 1.14);
theta4 = fzero(@f 4, 2.11);
thetas = [theta1 theta2 theta3 theta4];
% From the above it appears that our roots are at:
% theta = -0.7208, -0.3310, 1.1437, and 2.1159 radians
figure (5)
plot(theta vals, f vals)
xlabel('\theta (radians)')
ylabel('f(\theta)')
title('Plot of f(\theta) on [-\pi, \pi] with roots')
yline(0, '--r');
xline(theta1, '--r', '-0.7208');
xline(theta2, '--r', '-0.3310');
xline(theta3, '--r', '1.1437');
xline(theta4, '--r', '2.1159');
drawnow;
% Since we're asked to solve the forward kinematics problem, we need to
% solve for x and y now (we just solved for theta)
% Finding the x and y coordinates for the four poses
% Created a new function at the bottom called forward kinematics
[x 1 y 1] = forward kinematics(theta1);
[x 2 y 2] = forward kinematics(theta2);
[x 3 y 3] = forward kinematics(theta3);
```

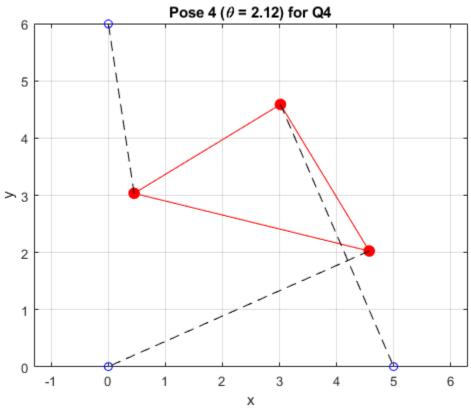
```
[x 4 y 4] = forward kinematics(theta4);
xs = [x 1 x 2 x 3 x 4];
ys = [y 1 y 2 y 3 y 4];
% It was found that
% (x_1, y_1) = (-1.3784, 4.8063)
% (x 2, y 2) = (-0.9147, 4.9156)
% (x_3, y_3) = (4.4818, 2.2167)
% (x 4, y 4) = (4.5718, 2.0244)
% Now we need to plot the four poses
\ensuremath{\$} Helper function is in the supporting functions section
gamma = pi/4;
x1 = 5; x2 = 0; y2 = 6;
for i = 1:4
    draw pose 4(5+i, xs(i), ys(i), thetas(i));
    drawnow;
    % Compute triangle corners again (same as inside draw pose 4)
    x = xs(i); y = ys(i); theta = thetas(i);
    % This one is connected to (0,0)
    u1 = x;
    v1 = y;
    % This one is connected to (x1, 0)
    u2 = x + 3*\cos(theta);
    v2 = y + 3*sin(theta);
    % This one is connected to (x2, y2)
    u3 = x + 3*sqrt(2)*cos(theta + gamma);
    v3 = y + 3*sqrt(2)*sin(theta + gamma);
    % Check strut lengths
    p1 = norm([u1 v1] - [0 0]);
    p2 = norm([u2 v2] - [x1 0]);
    p3 = norm([u3 v3] - [x2 y2]);
    fprintf("Pose %d: p1 = %.4f, p2 = %.4f, p3 = %.4f\n", i, p1, p2, p3);
end
% The strut lengths are correct!!!
Pose 1: p1 = 5.0000, p2 = 5.0000, p3 = 3.0000
Pose 2: p1 = 5.0000, p2 = 5.0000, p3 = 3.0000
Pose 3: p1 = 5.0000, p2 = 5.0000, p3 = 3.0000
Pose 4: p1 = 5.0000, p2 = 5.0000, p3 = 3.0000
```











QUESTION 5:

```
% Here we are changing p2 to 7 and resolving problem 4
% The new f(theta) function is in the supporting functions section at the
% bottom (f 5(theta))
% Plotting f 5(theta) on [-pi, pi]
theta vals = -pi:0.01:pi;
f \text{ vals} = f 5 \text{(theta vals)};
figure(10)
plot(theta vals, f vals)
xlabel('\theta (radians)')
ylabel('f(\theta)')
title('Plot of f(\theta) on [-\pi, \pi] for Question #5')
vline(0, '--r');
drawnow;
% The problem states that there are now six poses
% Finding the six theta values (quesses are from eyeballing the graph)
theta1 = fzero(@f 5, -0.68);
theta2 = fzero(@f 5, -0.36);
theta3 = fzero(@f 5, 0.03);
theta4 = fzero(@f 5, 0.44);
theta5 = fzero(@f 5, 0.97);
theta6 = fzero(@f 5, 2.5);
thetas = [theta1 theta2 theta3 theta4 theta5 theta6];
% From the above it appears that our roots are at:
% theta = -0.6732, -0.3547, 0.0378, 0.4589, 0.9777, and 2.5139 rad
figure (11)
plot(theta vals, f vals)
xlabel('\theta (radians)')
ylabel('f(\theta)')
title('Plot of f(\theta) on [-\pi, \pi] with roots')
yline(0, '--r');
xline(theta1, '--r', '-0.6732');
xline(theta2, '--r', '-0.3547');
xline(theta3, '--r', '0.0378');
xline(theta4, '--r', '0.4589');
xline(theta5, '--r', '0.9777');
xline(theta6, '--r', '2.5139');
drawnow;
% Since we're asked to solve the forward kinematics problem, we need to
% solve for x and y now (we just solved for theta)
% Finding the x and y coordinates for the four poses
% Created a new function at the bottom called forward kinematics 5
```

```
[x 1 y 1] = forward kinematics 5(theta1);
[x 2 y 2] = forward kinematics 5(theta2);
[x \ 3 \ y \ 3] = forward kinematics 5(theta3);
[x 4 y 4] = forward kinematics 5(theta4);
[x 5 y 5] = forward kinematics 5(theta5);
[x 6 y 6] = forward kinematics 5(theta6);
xs = [x 1 x 2 x 3 x 4 x 5 x 6];
ys = [y 1 y 2 y 3 y 4 y 5 y 6];
% It was found that
% (x 1, y 1) = (-4.3148, 2.5264)
% (x_2, y_2) = (-4.8049, 1.3831)
% (x 3, y 3) = (-4.9490, 0.7121)
% (x 4, y 4) = (-0.8198, 4.9323)
% (x 5, y 6) = (2.3036, 4.4378)
% (x_5, y_6) = (3.2157, 3.8287)
% Now we need to plot the four poses
% Helper function is in the supporting functions section
gamma = pi/4;
x1 = 5; x2 = 0; y2 = 6;
for i = 1:6
    % can use same function for drawing as last time
    draw pose 5(11+i, xs(i), ys(i), thetas(i));
    drawnow;
    % Compute triangle corners again (same as inside draw pose 4)
    x = xs(i); y = ys(i); theta = thetas(i);
    % This one is connected to (0,0)
    u1 = x;
    v1 = y;
    % This one is connected to (x1, 0)
    u2 = x + 3*\cos(theta);
    v2 = y + 3*sin(theta);
    % This one is connected to (x2, y2)
    u3 = x + 3*sqrt(2)*cos(theta + gamma);
    v3 = y + 3*sqrt(2)*sin(theta + gamma);
    % Check strut lengths
    p1 = norm([u1 v1] - [0 0]);
    p2 = norm([u2 v2] - [x1 0]);
    p3 = norm([u3 v3] - [x2 y2]);
    fprintf("Pose %d: p1 = %.4f, p2 = %.4f, p3 = %.4f\n", i, p1, p2, p3);
end
% The strut lengths are correct!!!
```

```
Pose 1: p1 = 5.0000, p2 = 7.0000, p3 = 3.0000

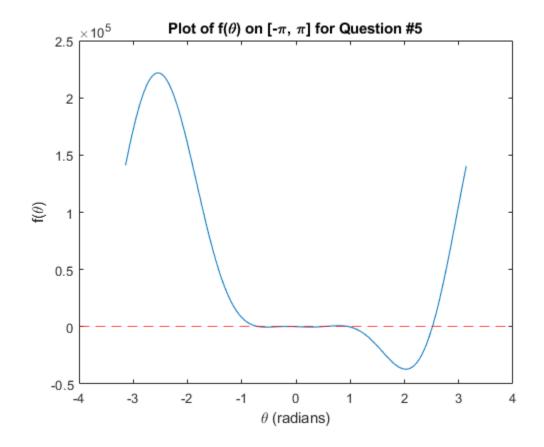
Pose 2: p1 = 5.0000, p2 = 7.0000, p3 = 3.0000

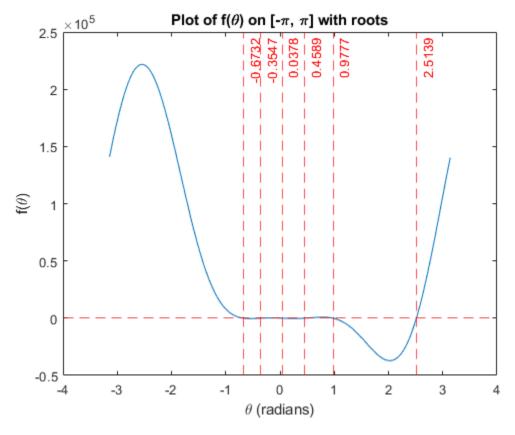
Pose 3: p1 = 5.0000, p2 = 7.0000, p3 = 3.0000

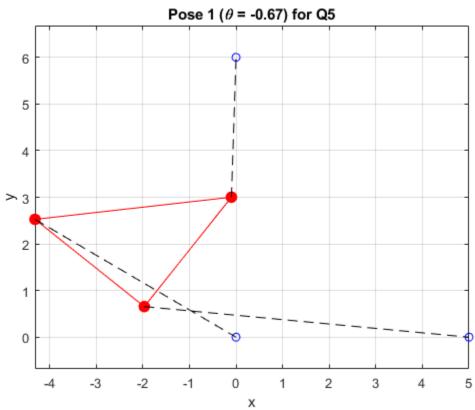
Pose 4: p1 = 5.0000, p2 = 7.0000, p3 = 3.0000

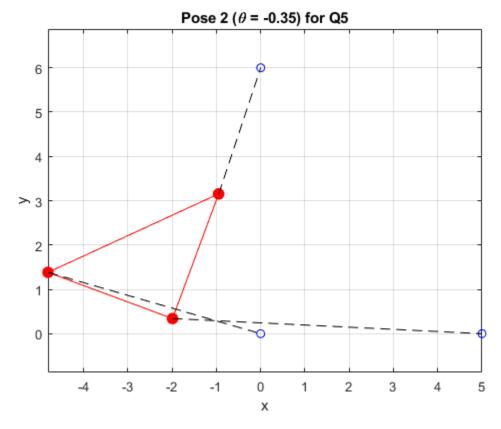
Pose 5: p1 = 5.0000, p2 = 7.0000, p3 = 3.0000

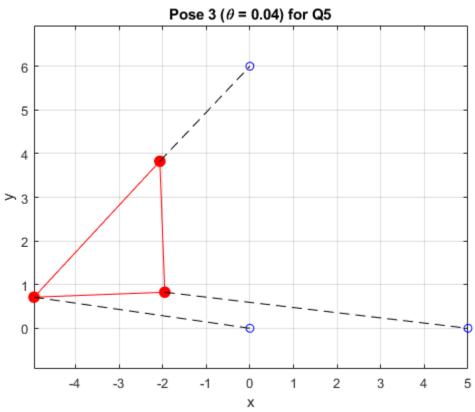
Pose 6: p1 = 5.0000, p2 = 7.0000, p3 = 3.0000
```

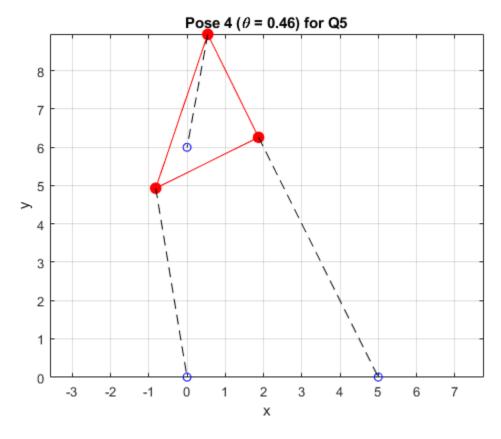


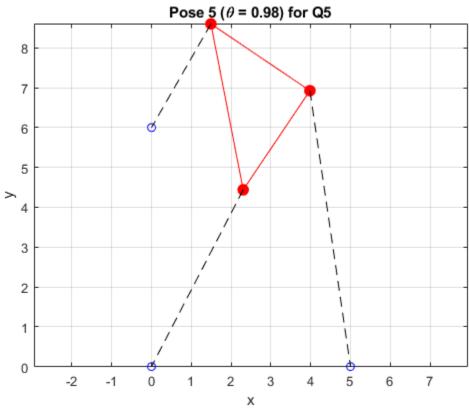


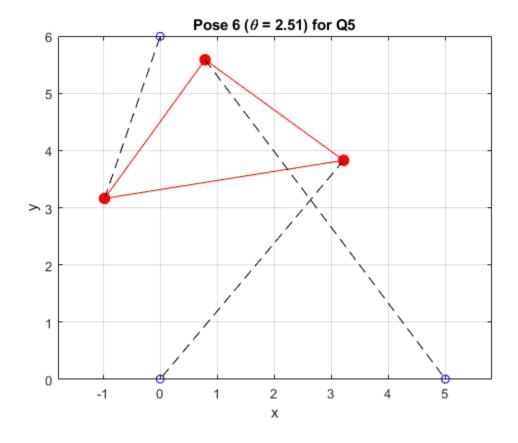












QUESTION 6:

QUESTION 7:

QUESTION 8:

ALL FUNCTIONS SUPPORTING THIS CODE

```
% First f(theta) function
function out = f(theta)

% Platform lengths
L1 = 2;
L2 = sqrt(2);
L3 = sqrt(2);

% Angle across from L1
gamma = pi / 2;

% Strut lengths
p1 = sqrt(5);
p2 = sqrt(5);
p3 = sqrt(5);
```

```
% Strut base positions
    % Got these from Figure 1.15
    x1 = 4;
    x2 = 0;
    y2 = 4;
   A2 = L3 * cos(theta) - x1;
    B2 = L3 * sin(theta);
    A3 = L2 * (cos(theta) * cos(gamma) - sin(theta) * sin(gamma)) - x2;
    B3 = L2 * (cos(theta) * sin(gamma) + sin(theta) * cos(gamma)) - y2;
   N1 = B3 .* (p2^2 - p1^2 - A2.^2 - B2.^2) - B2 .* (p3^2 - p1^2 - A3.^2 - B2.^2)
B3.^2);
    N2 = -A3 .* (p2^2 - p1^2 - A2.^2 - B2.^2) + A2 .* (p3^2 - p1^2 - A3.^2 - B2.^2)
B3.^2);
    D = 2 * (A2 .* B3 - B2 .* A3);
    out = N1.^2 + N2.^2 - p1.^2 * D.^2;
end
% f(theta) function for part 4
function out = f 4(theta)
    % Platform lengths
    L1 = 3;
    L2 = 3 * sqrt(2);
    L3 = 3;
    % Angle across from L1
    gamma = pi / 4;
    % Strut lengths
    p1 = 5;
   p2 = 5;
   p3 = 3;
    % Strut base positions
    x1 = 5;
    x2 = 0;
    y2 = 6;
   A2 = L3 * cos(theta) - x1;
    B2 = L3 * sin(theta);
    A3 = L2 * (cos(theta) * cos(gamma) - sin(theta) * sin(gamma)) - x2;
    B3 = L2 * (cos(theta) * sin(gamma) + sin(theta) * cos(gamma)) - y2;
   N1 = B3 .* (p2^2 - p1^2 - A2.^2 - B2.^2) - B2 .* (p3^2 - p1^2 - A3.^2 - B2.^2)
B3.^2);
   N2 = -A3 .* (p2^2 - p1^2 - A2.^2 - B2.^2) + A2 .* (p3^2 - p1^2 - A3.^2 - B2.^2)
B3.^2);
```

```
D = 2 * (A2 .* B3 - B2 .* A3);
    out = N1.^2 + N2.^2 - p1.^2 * D.^2;
end
% Forward kinematics problem solver for question #4
function [x y] = forward kinematics(theta)
    % Platform lengths
    L1 = 3;
    L2 = 3 * sqrt(2);
    L3 = 3;
    % Angle across from L1
    gamma = pi / 4;
    % Strut lengths
   p1 = 5;
   p2 = 5;
   p3 = 3;
    % Strut base positions
    x1 = 5;
    x2 = 0;
    y2 = 6;
    A2 = L3 * cos(theta) - x1;
    B2 = L3 * sin(theta);
    A3 = L2 * (cos(theta) * cos(gamma) - sin(theta) * sin(gamma)) - x2;
    B3 = L2 * (cos(theta) * sin(gamma) + sin(theta) * cos(gamma)) - y2;
    N1 = B3 .* (p2^2 - p1^2 - A2^2 - B2^2) - B2 .* (p3^2 - p1^2 - A3^2)
B3.^2);
    N2 = -A3 .* (p2^2 - p1^2 - A2.^2 - B2.^2) + A2 .* (p3^2 - p1^2 - A3.^2 - B2.^2)
B3.^2);
    D = 2 * (A2 .* B3 - B2 .* A3);
    x = N1 / D;
    y = N2 / D;
end
% Helper function to draw the poses for question four
function draw pose 4(fig num, x, y, theta)
    L2 = 3 * sqrt(2);
    L3 = 3;
    gamma = pi/4;
    % This one is connected to (0,0)
    u1 = x;
    v1 = y;
```

```
% This one is connected to (x1, 0)
   u2 = x + L3*cos(theta);
   v2 = y + L3*sin(theta);
    % This one is connected to (x2, y2)
   u3 = x + L2*cos(theta + gamma);
   v3 = y + L2*sin(theta + gamma);
   x1 = 5; x2 = 0; y2 = 6;
    % Create figure
    figure(fig num)
   plot([u1 u2 u3 u1], [v1 v2 v3 v1], 'r'); hold on
                                                              % Platform
triangle
   plot([0 x1 x2], [0 0 y2], 'bo')
                                                               % Base anchors
   plot([u1 u2 u3], [v1 v2 v3], 'ro', 'MarkerSize', 8, 'MarkerFaceColor',
'r') % Platform joints
   plot([u1 0], [v1 0], 'k--')
                                                               % p1
   plot([u2 x1], [v2 0], 'k--')
                                                               % p2
   plot([u3 x2], [v3 y2], 'k--')
                                                               % p3
   new num = fig num - 5;
   title(sprintf('Pose %d (\\theta = %.2f) for Q4', new num, theta))
   xlabel('x')
   ylabel('y')
    axis equal
    grid on
end
% f(theta) function for part 5
function out = f = 5 (theta)
    % Platform lengths
   L1 = 3;
   L2 = 3 * sqrt(2);
   L3 = 3;
    % Angle across from L1
   gamma = pi / 4;
    % Strut lengths
   p1 = 5;
   p2 = 7; % Update it to p2=7 for part 5
   p3 = 3;
   % Strut base positions
   x1 = 5;
   x2 = 0;
   y2 = 6;
   A2 = L3 * cos(theta) - x1;
   B2 = L3 * sin(theta);
   A3 = L2 * (cos(theta) * cos(gamma) - sin(theta) * sin(gamma)) - x2;
```

```
B3 = L2 * (cos(theta) * sin(gamma) + sin(theta) * cos(gamma)) - y2;
    N1 = B3 .* (p2^2 - p1^2 - A2.^2 - B2.^2) - B2 .* (p3^2 - p1^2 - A3.^2 - B3.^2)
B3.^2);
    N2 = -A3 .* (p2^2 - p1^2 - A2.^2 - B2.^2) + A2 .* (p3^2 - p1^2 - A3.^2 - B2.^2)
B3.^2);
    D = 2 * (A2 .* B3 - B2 .* A3);
    out = N1.^2 + N2.^2 - p1.^2 * D.^2;
end
% Forward kinematics problem solver for question #5
function [x y] = forward kinematics 5(theta)
    % Platform lengths
    L1 = 3;
    L2 = 3 * sqrt(2);
    L3 = 3;
    % Angle across from L1
    gamma = pi / 4;
   % Strut lengths
    p1 = 5;
   p2 = 7;
    p3 = 3;
    % Strut base positions
    x1 = 5;
    x2 = 0;
    y2 = 6;
    A2 = L3 * cos(theta) - x1;
    B2 = L3 * sin(theta);
    A3 = L2 * (cos(theta) * cos(gamma) - sin(theta) * sin(gamma)) - x2;
    B3 = L2 * (cos(theta) * sin(gamma) + sin(theta) * cos(gamma)) - y2;
    N1 = B3 .* (p2^2 - p1^2 - A2^2 - B2^2) - B2 .* (p3^2 - p1^2 - A3^2)
B3.^2);
    N2 = -A3 .* (p2^2 - p1^2 - A2.^2 - B2.^2) + A2 .* (p3^2 - p1^2 - A3.^2 - B2.^2)
B3.^2);
    D = 2 * (A2 .* B3 - B2 .* A3);
    x = N1 / D;
    y = N2 / D;
% Helper function to draw the poses for question five
function draw pose 5(fig num, x, y, theta)
```

```
L2 = 3 * sqrt(2);
    L3 = 3;
    gamma = pi/4;
    % This one is connected to (0,0)
    u1 = x;
   v1 = y;
    % This one is connected to (x1, 0)
    u2 = x + L3*cos(theta);
    v2 = y + L3*sin(theta);
    % This one is connected to (x2, y2)
    u3 = x + L2*cos(theta + gamma);
    v3 = y + L2*sin(theta + gamma);
    x1 = 5; x2 = 0; y2 = 6;
    % Create figure
    figure(fig num)
    plot([u1 u2 u3 u1], [v1 v2 v3 v1], 'r'); hold on
                                                              % Platform
triangle
    plot([0 x1 x2], [0 0 y2], 'bo')
                                                               % Base anchors
    plot([u1 u2 u3], [v1 v2 v3], 'ro', 'MarkerSize', 8, 'MarkerFaceColor',
'r') % Platform joints
    plot([u1 0], [v1 0], 'k--')
                                                               % p1
    plot([u2 x1], [v2 0], 'k--')
                                                               % p2
   plot([u3 x2], [v3 y2], 'k--')
                                                               % p3
    new num = fig num - 11;
    title(sprintf('Pose %d (\\theta = %.2f) for Q5', new num, theta))
    xlabel('x')
    ylabel('y')
    axis equal
    grid on
end
ans =
  -4.5475e-13
ans =
  -4.5475e-13
```

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