Quicksort

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Sorting

Input:

A sequence of *n* elements

$$\langle a_1, a_2, ..., a_n \rangle$$



Output:

A permutation of the input sequence

$$\langle a_1', a_2', ..., a_n' \rangle$$

do it efficiently.

such that
$$a_1' \leq a_2' \leq \ldots \leq a_n'$$

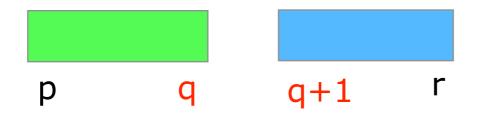
Quicksort

- Divide and conquer algorithm.
- Recursive
- Sorts in place (no extra arrays!).
- Popular: Top-10 algorithms 20th century (SIAM).

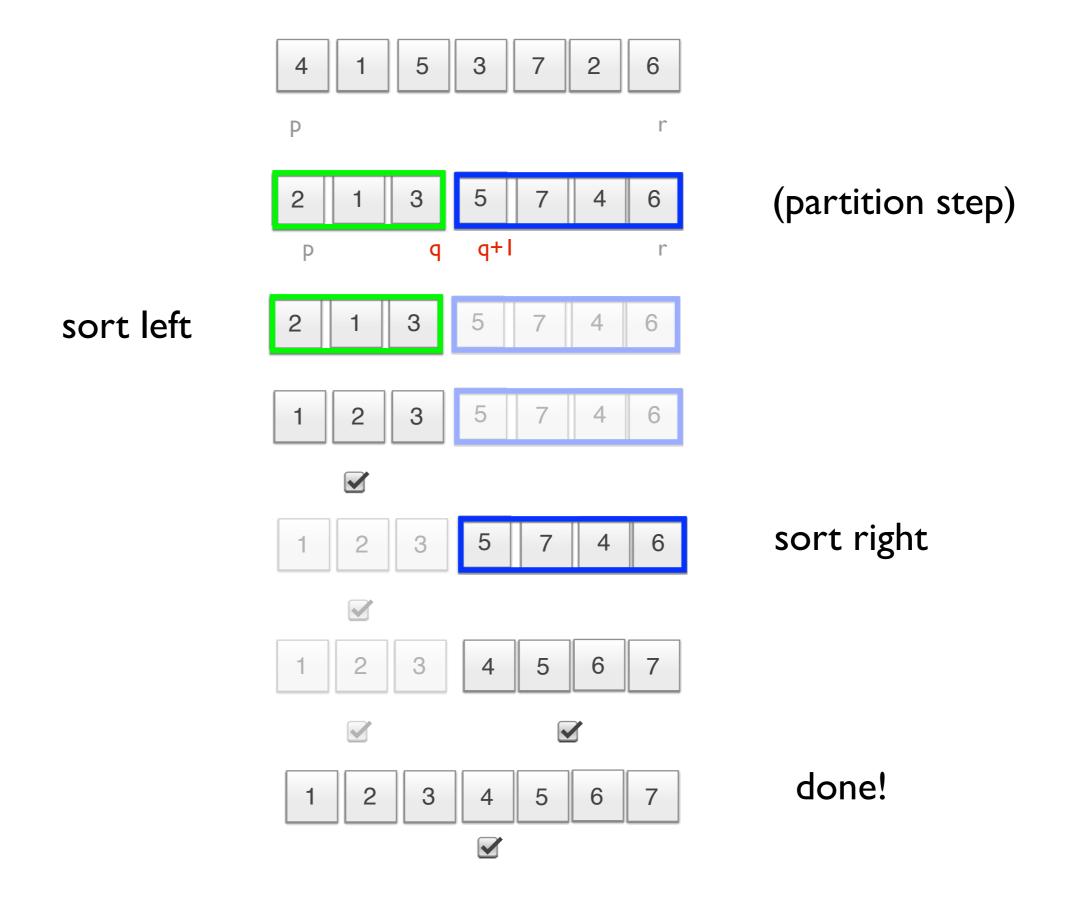
Quicksort strategy

<u>Input:</u> A: ______ m

Conquer: Recursively solve two smaller problems.



Combine: In-place! so we are done.



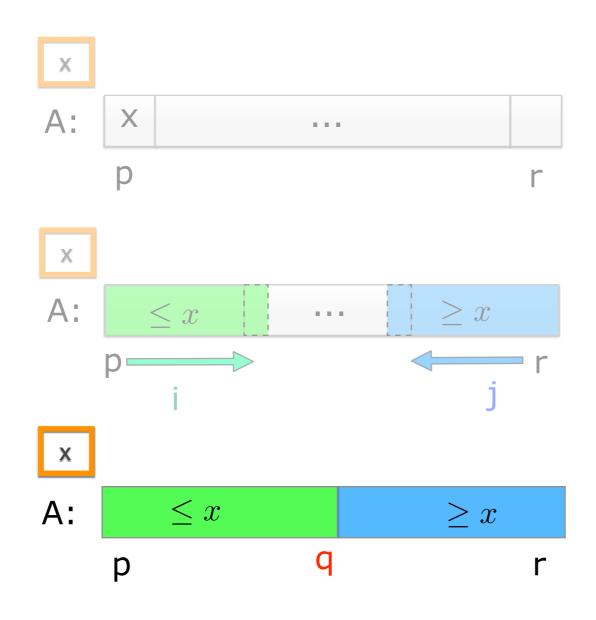
QUICKSORT
$$(A, p, r)$$
 [s it non-trivial?]

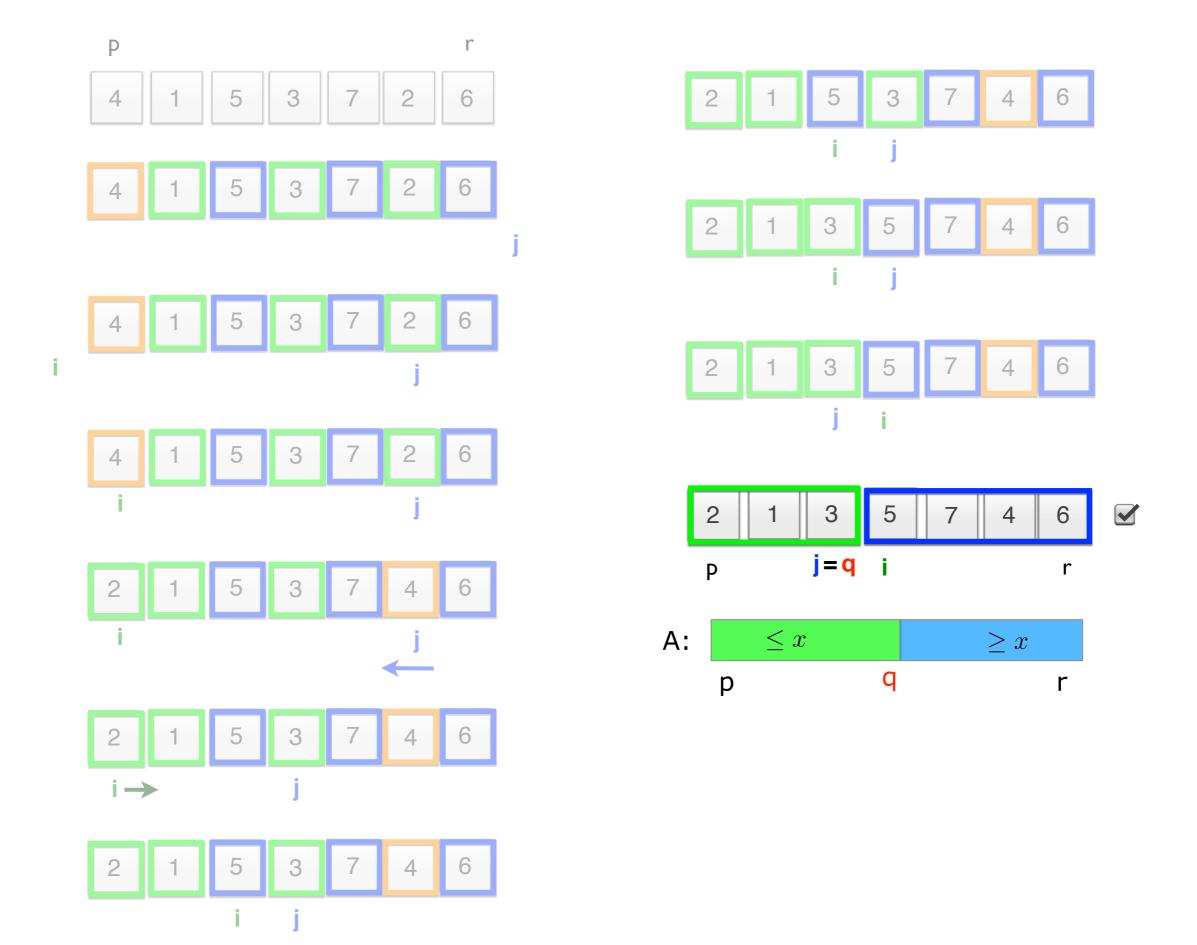
1 if $p < r$

2 $q = \text{PARTITION}(A, p, r)$ \Rightarrow A: $extit{A} = extit{A} = exti$

partition really does all the work!

Partition(A, p, r)





```
Partition(A, p, r)
 1 x = A[p] -----
 2 \quad i = p - 1 \longrightarrow
 3 \quad j = r + 1 \longleftarrow
 4 while TRUE
 5
         repeat
 6
            j = j - 1
         until A[j] \leq x
                                    A:
 8
         repeat
 9
            i = i + 1
         until A[j] \ge x
10
         if i < j
11
              exchange A[i] with A[j]
12
         else return j ..... A:
                                                \leq x
13
```

Key points

- Several ways to do the partition (check lecture handout, experiment)
- Number of comparisons depends on the choice of the pivot, i.e., data.
 - Best case: we partition in halves all along
 - Worst case: ordered list (partition sizes: I, n-I)
- The best case is to be expected.
 On average quicksort is very efficient.

Summing up

- Divide and conquer
 - <u>Divide</u>: Partition in-place
 - Conquer: Order each partition recursively
- Partition algorithms <u>vary</u>, and affect the process dramatically
- Efficient on average

Thank you.

More info: lecture handout

Literature:

- Leiserson, Charles E., Ronald L. Rivest, and Clifford Stein.
 Introduction to algorithms. Edited by Thomas H. Cormen.
 The MIT press, 2001.
- Sedgewick, Robert. and Wayne, Kevin. *Algorithms*. Pearson Education, 2011.

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