Satisfaction without provisos

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Presupposition

The empirical observation

We have linguistic devices that grammatically encode what we take for granted in making an utterance.

(1) Karlos brought his car.

 \sim Karlos has a car.

(presupposition)

Presupposition

The empirical observation

How do we identify presuppositions?

- Family-of-sentence tests (Chierchia and McConnell-Ginet, 1990)
- "hey, wait a minute!" test (von Fintel, 2004)

Major research question: what grammatical properties of an expression give rise to its presuppositions?

A **compositional** account answers two questions:

- How do we grammatically encode presuppositions in simple expressions (presupposition triggers)?
- How do presuppositions project in complex expressions?
 - The "projection problem" (Langendoen and Savin, 1971)

Today's talk

Outline:

- Investigate an influential compositional framework for studying presupposition projection: "satisfaction theory" (Geurts, 1996).
 - Heim 1983

 - · The "proviso problem"
- Build a satisfaction account on top an alternative-semantics for indefinites (Charlow, 2014, 2019a,b)
 - which allows presupposition triggers to take (exceptional) scope.
 - Same theory gives rise to exceptional scope for both indefinites and presupposition triggers.
 - Investigate the proviso problem in this setting.
- Suggest how presupposition accommodation might work.

Plan

The satisfaction theory

Rouch sketch of how it works The proviso problem

Alternative semantics and presupposition

Basic grammar for indefinites
Adding presupposition
The proviso problem?

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- Basic ideas come from Heim 1983.
- Sentences denote context change potentials.

$$\begin{split} & & \llbracket \Delta \ ; \ \textit{it's raining} \rrbracket \\ & = & \llbracket \Delta \rrbracket + \llbracket \textit{it's raining} \rrbracket \\ & \text{e.g.,} & = \{ w \in \mathcal{W} \mid \llbracket \Delta \rrbracket^w = \top \} \ \cap \ \{ w \in \mathcal{W} \mid \textit{rain } w \} \end{split}$$

- What is +? Depends on your (more specific) theory.
 - Might amount to set intersection (for sets of worlds, sets of assignments, etc.).

▶ What if the sentence updating Δ has a presupposition?

$$[\![\Delta]\!] + [\![Karlos\ brought\ his\ car]\!]$$

- Δ "admits" Karlos brought his car only if Δ entails that Karlos has a car.
 - "Stalnaker's bridge" (von Fintel, 2008)
- Foregoing assumptions are meant to provide a way of determining what a sentence's presuppositions are:
 - S_1 presupposes S_2 iff every context Δ , such that $[\![\Delta]\!] + [\![S_1]\!]$ is successful, entails S_2 .
 - Karlos brought his car → Karlos has a car

The satisfaction theory

Rouch sketch of how it works

- Explaining projection behavior: just a matter of using + in the right way.
- (2) Karlos has a car, and he brought his car.
 - c + [(2)] = (c + [K has a car]) + [K brought his car]
 - Update is successful iff each of the individual updates is successful.
 - ...iff c entails If Karlos has a car, then Karlos has a car.
 - \sim No presuppositions for (2).
 - The second sentence's presupposition is filtered.
- (3) If Karlos has a car, he brought his car.
 - c + [(3)]:
 - $c_1 := c + \llbracket K \text{ has } c \rrbracket$
 - $c_2 := (c + \llbracket K \text{ has } c \rrbracket) + \llbracket K \text{ brought } c \rrbracket$
 - $\bullet = c (c_1 c_2)$
 - Again, update is successful iff each of the individual updates is.
 → No presuppositions for (3).

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The proviso problem

- Geurts 1996: there's a big problem!
- (4) It's raining, and my car is too far away.
 - Update successful iff each of the individual updates is.
 - c + [it's raining, and my car is too far away]
 = (c + [it's raining]) + [my car is too far away]
 - ...iff the context entails if it's raining, I have a car.
 - (4) \sim if it's raining, I have a car \odot
- (5) If EWR is nearby, I can pick my sister up once she lands.
 - · Individual updates:
 - $c_1 := c + \llbracket EWR \text{ is nearby} \rrbracket$
 - $c_2 := (c + \llbracket EWR \text{ is nearby} \rrbracket) + \llbracket pick \text{ sister up} \rrbracket$
 - $\bullet = c (c_1 c_2)$
 - (5) \sim if EWR is nearby, I have a sister \odot

The satisfaction theory

The proviso problem

- ► According to the satisfaction theory, filtration is *automatic*.
- ▶ But sometimes it shouldn't happen.

Plan

The satisfaction theory

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Basic grammar for indefinites

- Let's build our satisfaction account by starting with a grammar in which indefinites systematically give rise to *alternatives*.
- Importing basic ideas from Charlow 2014.
- ► I'll add in a few extra things though:
 - intensionality (we want to compose contexts)
 - Quantifier Raising & Predicate Abstraction(Heim and Kratzer, 1998)
 - Just for expository purposes (see, e.g., Charlow, 2019a,b).
 - presupposition

Basic grammar for indefinites

- Basic ingredients:
 - $[a \ dolphin] = \{\langle w, x \rangle \mid dolphinwx\}$
 - Really, $(\lambda w, x.\mathbf{dolphin} wx)$.
 - Type $s \rightarrow e \rightarrow t$ (shorthand: S(e)).
 - $\llbracket swam \rrbracket = (\lambda y. \{\langle w, swam wy \rangle \mid w \in \mathcal{W}\})$
 - Really, $(\lambda y, w, t.t = \mathbf{swam} wy)$.
 - Type $e \rightarrow s \rightarrow t \rightarrow t$ (shorthand: $e \rightarrow \mathbf{S}(t)$).
- What we want:

$$\llbracket a \ dolphin \ swam \rrbracket = \{\langle w, swam \ wx \rangle \mid dolphin \ wx \}$$

- Type $S(t) = s \rightarrow t \rightarrow t$ (a "proposition").
- If we want to know if ϕ true at some world w, we just ask: "is $\langle w, \top \rangle \in \phi$?"

Basic grammar for indefinites

- ▶ To get there, we need to somehow compose something of type S(e) (*a dolphin*) with something of type $e \rightarrow S(t)$ (*swam*).
- ▶ It would be nice if we could turn *a dolphin* into something of type $(e \rightarrow \mathbf{S}(t)) \rightarrow \mathbf{S}(t)$.
 - A quantifier: takes scope over functions into propositions, to return a proposition.
- ► Following Charlow (2019a,b), let's use an operator (·) (bind') to do the trick.

$$(\cdot)^{\stackrel{S}{\Longrightarrow}} : \mathbf{S}(\alpha) \to (\alpha \to \mathbf{S}(\beta)) \to \mathbf{S}(\beta)$$

$$m^{\stackrel{S}{\Longrightarrow}} k = \{ \langle w, y \rangle \mid (\exists x. \langle w, x \rangle \in m \land \langle w, y \rangle \in kx) \}$$

$$\{ \langle w, x \rangle \mid \mathbf{dolphin} wx \}^{\stackrel{S}{\Longrightarrow}} k$$

$$= \{ \langle w, t \rangle \mid (\exists x. \mathbf{dolphin} wx \land \langle w, t \rangle \in kx) \}$$

Basic grammar for indefinites

► A dolphin swam:

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The proviso problem?

- So far, we've previewed a grammar for composing propositions of type $\mathbf{S}(t) = s \to t \to t$.
- Let's add in presupposition:
 - A new type, *t*_#, inhabitted by three truth values:
 - ⊤ : *t*[±] 'true'
 - ⊥ : t_# 'false'
 - #: t# 'undefined'
 - Keep old type t, too (\top : t and \bot : t, but # \not \not t).
- Next, some preliminaries: interpreting some useful constants (bear with me).

Adding presupposition

We need a new semantics for connectives!

- $(\phi \land \#) = (\# \land \phi) = \#$.
- $(\Phi \to \#) = (\# \to \Phi) = \#.$
- ¬# = #.
- Undefinedness automatically projects.

¹The "internal" logic of Bochvar 1939; a.k.a. "weak Kleene".

Adding presupposition

We also need a new semantics for the existential quantifier!

	$\{\llbracket \varphi \rrbracket_{\mathcal{M},g'} \mid g[x]g'\}$	$\llbracket \lceil (\exists x. \varphi) \rceil \rrbracket_{\mathcal{M},g}$
•	{⊤}	T
	$\{\bot\}$	
	{#}	#
	$\{\top, \bot\}$	Т
	$\{\top,\#\}$	Т
	$\{\bot,\#\}$	
	$\{\top, \bot, \#\}$	T

- Undefined only when the only potential witnesses lead to undefinedness.
- If there's any witness at all, make it true.
- If there are no witnesses, but some potential ones lead to falsity, make it false.
- · Undefinedness is a last resort.

- Last important piece: the δ-operator (Beaver, 1999, 2001;
 Beaver and Krahmer, 2001; Coppock and Beaver, 2015, i.a.).
 - · How it works:

$$\delta: t \to t_{\#}$$

 $\delta \top = \top$
 $\delta \bot = \#$

- Say you've got $\lceil \phi \wedge \delta \psi \rceil$:
 - true or false, depending on ϕ (assuming it's defined)
 - defined or undefined, depending on ψ
- Turns a truth condition into a definedness condition.

- Those are all the basic pieces we need.
- ▶ Before, our propositions were of type $S(t) (= s \rightarrow t \rightarrow t)$.
- Let's upgrade them to our new setting:

$$\{\langle w, \mathbf{swam} wx \rangle \mid \mathbf{dolphin} wx \} : \mathbf{P}(t)$$

$$= s \to t \to t_{\#}$$
Really, $(\lambda w, t.(\exists x.\mathbf{dolphin} wx \land t = \mathbf{swam} wx)) : \mathbf{P}(t)$

- For any $\phi : \mathbf{P}(t)$,
 - ϕ is *true* at w iff $\langle w, \top \rangle \in \phi$;
 - ϕ is *false* at w iff $\langle w, \top \rangle \notin \phi$;
 - ϕ is *undefined* at w iff it can't be said whether or not $\langle w, \top \rangle \in \phi$ (i.e., if $\phi w \top = \#$).
- Presuppositions of ϕ : set of worlds at which ϕ is defined.

- New basic ingredients:
 - $[a dolphin] = \{\langle w, x \rangle \mid dolphinwx\}$
 - Really, $(\lambda w, x.dolphinwx) : P(e)$.
 - $\llbracket swam \rrbracket = (\lambda y. \{\langle w, swam wy \rangle \mid w \in \mathcal{W}\})$
 - Really, $(\lambda y, w, t.t = \mathbf{swam} wy) : e \rightarrow \mathbf{P}(t)$.
 - [[the dolphin]] = { $\langle w, x \rangle \mid \delta(\mathbf{dolphin} wx)$ }
 - Really, $(\lambda w, x.\delta(\mathbf{dolphin} wx)) : \mathbf{P}(e)$.
- What we want:

$$[\![\textit{the dolphin swam}]\!] = \{ \langle w, \mathbf{swam} \, wx \rangle \mid \delta(\mathbf{dolphin} \, wx) \}$$
$$= (\lambda w, t. (\exists x. \delta(\mathbf{dolphin} \, wx) \land t = \mathbf{swam} \, wx))$$

- $\langle w, \top \rangle \in [\![the \ dolphin \ swam]\!]$ iff a dolphin swam in w.
- If no dolphin in w, then we can't check this (i.e., we get #).
- The worlds w in which $\langle w, \top \rangle$ can be checked for membership are all dolphin worlds... existence presupposition!

We'll invoke the type shift (·)^P to turn our presupposition trigger into a quantifier.

$$(\cdot)^{\stackrel{\mathbf{P}}{\Rightarrow}} : \mathbf{P}(\alpha) \to (\alpha \to \mathbf{P}(\beta)) \to \mathbf{P}(\beta)$$

$$m^{\stackrel{\mathbf{P}}{\Rightarrow}} k = \{ \langle w, y \rangle \mid (\exists x. \langle w, x \rangle \in m \land \langle w, y \rangle \in kx) \}$$

$$\{ \langle w, x \rangle \mid \delta(\mathbf{dolphin} wx) \}^{\stackrel{\mathbf{P}}{\Rightarrow}} k$$

$$= \{ \langle w, t \rangle \mid (\exists x. \delta(\mathbf{dolphin} wx) \land \langle w, t \rangle \in kx) \}$$

Once fed its scope, the presupposition trigger creates a proposition with presuppositions.

Adding presupposition

► The dolphin swam:

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The proviso problem?

- (2) If Karlos has a car, he brought his car.
 - Basic pieces:
 - $[Karlos\ has\ a\ car] = \{\langle w, havewxk \rangle \mid carwx\}$
 - [Karlos brought his car] = $\{ \langle w, broughtwxk \rangle \mid \delta(carwx \wedge bavewxk) \}$

• *if* ...

- $(\bot \Rightarrow \#) = \top$
- Only checks definedness of the consequent if the antecedent is true.

$$\begin{split} \text{if}: \mathbf{P}(t) &\to \mathbf{P}(t) \to \mathbf{P}(t) \\ \text{if} \varphi \psi &\coloneqq \{\langle w, \top \rangle \mid \langle w, \top \rangle \in \varphi \Rightarrow \langle w, \top \rangle \in \psi\} \end{split}$$

The proviso problem?

If Karlos has a car, he brought his car:

```
\{\langle w,\top\rangle \mid (\exists x.\mathsf{car}wx \land \mathsf{have}wx\mathsf{k}) \Rightarrow (\exists x.\delta \, (\mathsf{car}wx \land \mathsf{have}wx\mathsf{k}) \land \mathsf{brought}wx\mathsf{k})\} (\lambda \psi.\{\langle w,\top\rangle \mid (\exists x.\mathsf{car}wx \land \mathsf{have}wx\mathsf{k}) \Rightarrow \langle w,\top\rangle \in \psi\}) \qquad \{\langle w,\mathsf{brought}wx\mathsf{k}\rangle \mid \delta \, (\mathsf{car}wx \land \mathsf{have}wx\mathsf{k})\} if \{\langle w,\mathsf{have}wx\mathsf{k}\rangle \mid \mathsf{car}wx\} if \{\langle w,\mathsf{have}wx\mathsf{k}\rangle \mid \mathsf{car}wx\} if K \, \mathsf{has} \, a \, \mathsf{car}
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- $\{\langle w, \top \rangle \mid (\exists x. \mathsf{car} wx \land \mathsf{have} wx \mathsf{k}) \Rightarrow (\exists x. \delta (\mathsf{car} wx \land \mathsf{have} wx \mathsf{k}) \land \mathsf{brought} wx \mathsf{k})\}$ = $\{\langle w, \top \rangle \mid (\exists x. \mathsf{car} wx \land \mathsf{have} wx \mathsf{k}) \Rightarrow (\exists x. \mathsf{car} wx \land \mathsf{have} wx \mathsf{k} \land \mathsf{brought} wx \mathsf{k})\}$
- ▶ $\langle w, \top \rangle$ is in this set iff Karlos brought a car he has in w, as long as he has a car in w.
- Definedness conditions are trivial: filtration!

The proviso problem?

► If EWR is nearby, I'll get my sister:

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\{\langle w, \top \rangle \mid \mathbf{nearby} \, w \Rightarrow (\exists x. \delta(\mathbf{sis} \, wx\mathbf{me}) \land \mathbf{get} \, wx\mathbf{me})\}
(\lambda \psi. \{\langle w, \top \rangle \mid \mathbf{nearby} \, w \Rightarrow \langle w, \top \rangle \in \psi\}) \qquad \{\langle w, \mathbf{get} \, wx\mathbf{me} \rangle \mid \delta(\mathbf{sis} \, wx\mathbf{me})\}
\text{if} \qquad \{\langle w, \mathbf{nearby} \, w \rangle \mid w \in \mathcal{W}\}
\text{if} \qquad ERW \, is \, nearby}
```

- ► $\{\langle w, \top \rangle \mid \text{nearby } w \Rightarrow (\exists x.\delta(\text{sis } wx\text{me}) \land \text{get } wx\text{me})\}$
- $\langle w, \top \rangle$ can be checked for membership in this set iff:
 - nearby $w \Rightarrow (\exists x. sis wxm)$
- ▶ Should presuppose *If EWR nearby, I have a sister.* ②

The proviso problem?

- Our framework's analog of the proviso problem:
 - Filtration is built into the semantics of the conditional (and it should be—look at (2)!).
 - But then the presupposition of (5) is filtered, which we don't want.

The proviso problem?

- Quick detour: indefinites.
- What do we know about indefinites?
 - They take exceptional scope!
 - If a friend of mine comes, I'll be happy (a friend > if)

 $\{\langle w, \top \rangle \mid (\exists x. friend wx \wedge (comewx \Rightarrow happyw))\}$ $\{\langle w, x \rangle \mid friend wx\}^{\frac{p}{2m}} \qquad (\lambda i. \{\langle w, \top \rangle \mid comewi \Rightarrow happyw \rangle\})$ $\{\langle w, x \rangle \mid friend wx\}$ a friend $if \{\langle w, comewi \rangle \mid w \in \mathcal{W}\}$ $if \{\langle w, comewi \rangle \mid w \in \mathcal{W}\}$ $if \{\langle w, comewi \rangle \mid w \in \mathcal{W}\}$ $if \{\langle w, comewi \rangle \mid w \in \mathcal{W}\}$

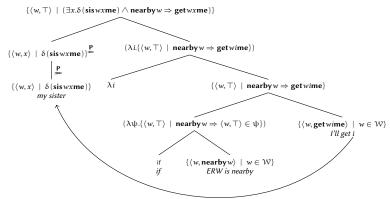
Somehow, our theory has to allow the indefinite to scope out of the conditional (see Charlow 2019a,b).

The proviso problem?

- But if the theory allows indefinites to do this... then it also allows presupposition triggers to do it!
- ► End of detour.

The proviso problem?

► If EWR is nearby, I'll get my sister (take 2):



- ► $\{\langle w, \top \rangle \mid (\exists x.\delta(siswxme) \land nearbyw \Rightarrow getwxme)\}$
- ▶ $\langle w, \top \rangle$ can be checked for membership in this set iff:
 - $(\exists x. sis wxme)$
- ▶ Should presuppose *I have a sister*. ©

The proviso problem?

- If we admit exceptional scope for indefinites, then we admit exceptional scope for presupposition triggers automatically.
- ▶ But once we do the latter, we may circumvent the proviso problem.

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- ► Lewis (1979) observes that presuppositions which are not satisfied by prior discourse are often *accommodated*.
- (6) I lost my gloves.
 - Heim (1983) further observes that examples in which presuppositions are cancelled might receive an analysis in terms of an interpretation strategy she calls "local accommodation".
- (7) The dolphin wasn't fast, because there is no dolphin!
 - No existence presupposition.
 - Basic idea: the presupposition is promoted to at-issue content, which is then targeted by the negation.

Presupposition accommodation

▶ To describe sentences like (7), we could introduce an operator, δ^{-1} , which promotes definedness conditions back to truth conditions.

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• \delta^{-1}\# = \bot
• \delta^{-1}\top = \top and \delta^{-1}\bot = \bot.
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▶ In terms of it, we may define a new type shift:

$$\begin{aligned} \operatorname{accom} : \mathbf{P}(\alpha) &\to \mathbf{P}(\alpha) \\ \operatorname{accom} m &\coloneqq (\lambda w, x.\delta^{-1}(mwx)) \\ &= \left\{ \langle w, x \rangle \mid \delta(\mathbf{dolphin}wx) \right\} \\ &= \left\{ \langle w, x \rangle \mid \delta^{-1}(\delta(\mathbf{dolphin}wx)) \right\} \\ &= \left\{ \langle w, x \rangle \mid \mathbf{dolphin}wx \right\} \end{aligned}$$

• From the meaning of a definite description, we get the meaning of the corresponding indefinite!

- ▶ If such a type shift could apply in (7), then (7) would be semantically equivalent to (8) (with the indefinite taking narrow scope).
- (8) A dolphin wasn't fast, because there is no dolphin!
 - If an analysis like this were viable, then it would allow us to view accommodation as simple model-theoretic operation.

Conclusion

- We should really try to hold onto the satisfaction account of presuppositin projection because it allows us to describe presupposition projection using nothing more than the tools semanticists are used to (and need anyway).
 - Truth conditions (sets of worlds)
 - · Compositional view of the syntax-semantics interface
- It has been hindered by the proviso problem, but...
 - the problem is overcome if we state the account in terms Charlow's independently motivated theory of indefinites.

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