Overview of "Wage" Dataset from "ISLR" Package

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This document provides a brief overview of the Wage dataset in the ISLR R package.

```
##
         year
                         age
                                            sex
                                                                    maritl
##
           :2003
                           :18.00
                                     1. Male :3000
                                                       1. Never Married: 648
   Min.
                    Min.
   1st Qu.:2004
                    1st Qu.:33.75
                                     2. Female:
                                                      2. Married
##
                                                  0
                                                                        :2074
##
   Median:2006
                    Median :42.00
                                                       3. Widowed
                                                                           19
##
   Mean
           :2006
                    Mean
                           :42.41
                                                      4. Divorced
                                                                        : 204
##
    3rd Qu.:2008
                    3rd Qu.:51.00
                                                       5. Separated
                                                                           55
##
    Max.
           :2009
                    Max.
                           :80.00
##
##
                                   education
          race
                                                                  region
##
    1. White:2480
                    1. < HS Grad
                                        :268
                                               2. Middle Atlantic
                                                                     :3000
##
    2. Black: 293
                     2. HS Grad
                                        :971
                                               1. New England
##
    3. Asian: 190
                     3. Some College
                                        :650
                                               3. East North Central:
##
    4. Other: 37
                    4. College Grad
                                        :685
                                               4. West North Central:
                     5. Advanced Degree: 426
                                               5. South Atlantic
                                                                          0
##
                                               6. East South Central:
                                                                          0
##
##
                                               (Other)
                                                                          0
##
              jobclass
                                       health
                                                   health_ins
                                                                    logwage
    1. Industrial :1544
                                        : 858
                                                  1. Yes:2083
##
                           1. <=Good
                                                                 Min.
                                                                         :3.000
                           2. >=Very Good:2142
##
    2. Information:1456
                                                  2. No: 917
                                                                 1st Qu.:4.447
##
                                                                 Median : 4.653
##
                                                                 Mean
                                                                        :4.654
##
                                                                 3rd Qu.:4.857
##
                                                                 Max.
                                                                        :5.763
##
##
         wage
##
    Min.
           : 20.09
##
    1st Qu.: 85.38
   Median :104.92
##
   Mean
           :111.70
   3rd Qu.:128.68
```

```
## Max. :318.34 ##
```

From the summary, and the associated help (not shown), the following observations can be made:

The dataframe contains 3000 rows and 12 columns.

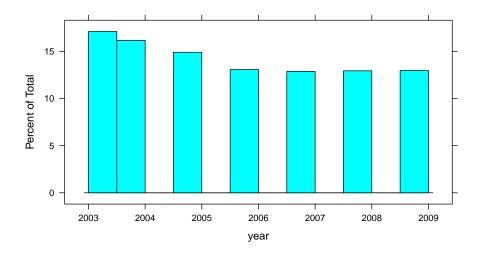


Figure 1: Histogram of the year variable

```
##
##
   Welch Two Sample t-test
##
## data: wage by jobclass
## t = -11.489, df = 2714.9, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -20.21940 -14.32378
##
## sample estimates:
   mean in group 1. Industrial mean in group 2. Information
##
##
                       103.3211
                                                     120.5927
##
##
##
   Welch Two Sample t-test
##
## data: wage by health
## t = -9.2265, df = 1934.3, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   -17.05452 -11.07524
## sample estimates:
##
        mean in group 1. <=Good mean in group 2. >=Very Good
##
                       101.6613
                                                     115.7262
##
##
```

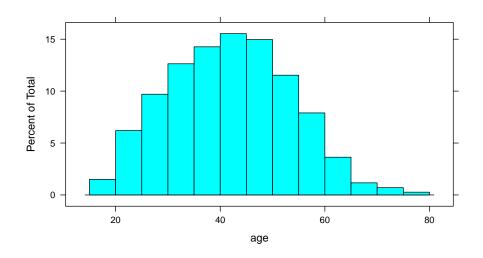


Figure 2: Histogram of the age variable

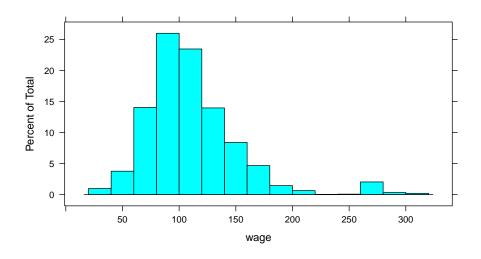


Figure 3: Histogram of the wage variable

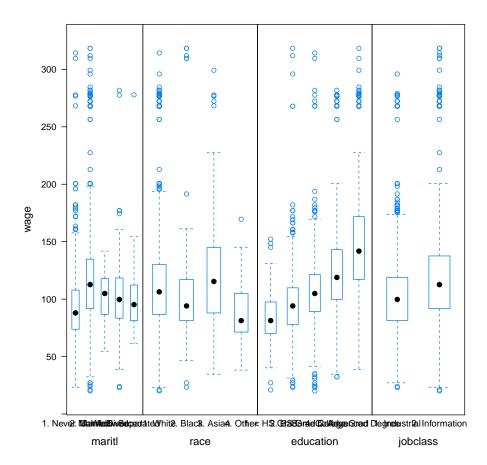


Figure 4: Boxplot of the dependent variable wage by each factor variable

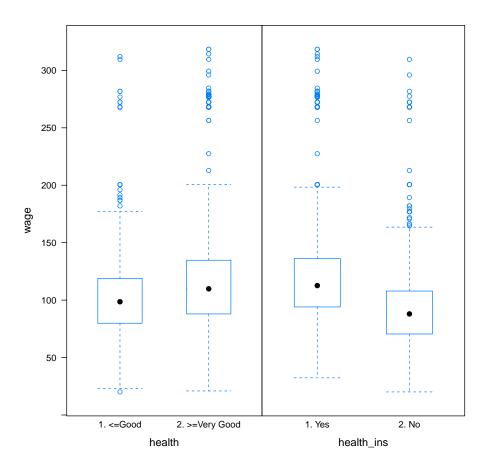
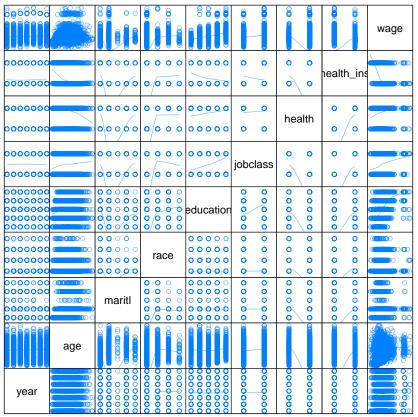


Figure 5: Boxplot of the dependent variable wage by each factor variable

Scatter Plot Matrix of Wage



Scatter Plot Matrix

Figure 6: multi-variate comparisons

Correlogram of Wage

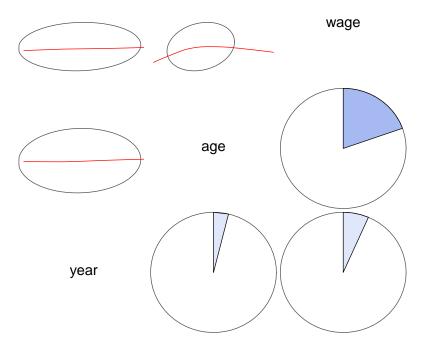


Figure 7: Correlogram

```
## Welch Two Sample t-test
##
## data: wage by health_ins
## t = 18.708, df = 1989.5, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 24.99464 30.84858
## sample estimates:
## mean in group 1. Yes mean in group 2. No
   120.2383
##
## Call:
## lm(formula = fmla1, data = df)
## Residuals:
##
            1Q Median
      Min
                           3Q
## -90.550 -26.606 -6.415 17.830 206.393
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## year
          1.3499
                         0.3753 3.597 0.000328 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 41.65 on 2998 degrees of freedom
## Multiple R-squared: 0.004296, Adjusted R-squared: 0.003964
## F-statistic: 12.94 on 1 and 2998 DF, p-value: 0.0003277
##
##
## Call:
## lm(formula = fmla1, data = df)
## Residuals:
##
     Min
             1Q Median
                               3Q
## -100.265 -25.115 -6.063 16.601 205.748
##
## Coefficients:
##
             Estimate Std. Error t value Pr(>|t|)
## (Intercept) 81.70474 2.84624
                                 28.71 <2e-16 ***
## age
            0.70728
                     0.06475
                               10.92 <2e-16 ***
```

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1

```
## Residual standard error: 40.93 on 2998 degrees of freedom
## Multiple R-squared: 0.03827, Adjusted R-squared: 0.03795
## F-statistic: 119.3 on 1 and 2998 DF, p-value: < 2.2e-16
##
##
## Call:
## lm(formula = fmla1, data = df)
##
## Residuals:
## Min
              1Q Median
                               3Q
## -98.775 -24.788 -4.754 15.845 221.595
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                      92.735
                              1.582 58.608 < 2e-16 ***
## maritl2. Married
                      26.126
                                  1.813 14.413 < 2e-16 ***
## maritl3. Widowed
                       6.804
                                          0.726 0.46804
                                  9.375
## maritl4. Divorced
                       10.425
                                   3.234
                                          3.224 0.00128 **
## maritl5. Separated 8.481
                                   5.657
                                         1.499 0.13392
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 40.28 on 2995 degrees of freedom
## Multiple R-squared: 0.06954, Adjusted R-squared: 0.0683
## F-statistic: 55.96 on 4 and 2995 DF, p-value: < 2.2e-16
##
##
## Call:
## lm(formula = fmla1, data = df)
##
## Residuals:
## Min
              1Q Median
                               3Q
## -92.478 -24.708 -6.251 17.283 216.741
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 112.5637
                          0.8333 135.088 < 2e-16 ***
## race2. Black -10.9625
                           2.5634 -4.276 1.96e-05 ***
                           3.1236
                                   2.473 0.01345 *
## race3. Asian 7.7246
                            6.8726 -3.287 0.00102 **
## race4. Other -22.5903
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 41.5 on 2996 degrees of freedom
## Multiple R-squared: 0.0121, Adjusted R-squared: 0.01112
```

```
## F-statistic: 12.24 on 3 and 2996 DF, p-value: 5.89e-08
##
##
## Call:
## lm(formula = fmla1, data = df)
##
## Residuals:
   Min 1Q Median
                              3Q
                                     Max
## -112.31 -19.94 -3.09 15.33 222.56
##
## Coefficients:
##
                             Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                           2.231 37.695 < 2e-16 ***
                               84.104
## education2. HS Grad
                                11.679
                                           2.520
                                                  4.634 3.74e-06 ***
                                           2.652 8.920 < 2e-16 ***
## education3. Some College
                               23.651
## education4. College Grad
                               40.323
                                           2.632 15.322 < 2e-16 ***
## education5. Advanced Degree
                                           2.848 23.462 < 2e-16 ***
                                66.813
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 36.53 on 2995 degrees of freedom
## Multiple R-squared: 0.2348, Adjusted R-squared: 0.2338
## F-statistic: 229.8 on 4 and 2995 DF, p-value: < 2.2e-16
##
##
## Call:
## lm(formula = fmla1, data = df)
##
## Residuals:
       Min
                 1Q
                     Median
                                  3Q
## -100.507 -25.362 -6.117
                             15.697 197.750
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
                                     1.039
                                            99.43 <2e-16 ***
## (Intercept)
                         103.321
## jobclass2. Information 17.272
                                     1.492
                                             11.58 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 40.83 on 2998 degrees of freedom
## Multiple R-squared: 0.04281, Adjusted R-squared: 0.04249
## F-statistic: 134.1 on 1 and 2998 DF, p-value: < 2.2e-16
##
##
## Call:
```

```
## lm(formula = fmla1, data = df)
##
## Residuals:
             1Q Median
                             3Q
## -94.792 -26.618 -5.892 17.223 210.273
##
## Coefficients:
                       Estimate Std. Error t value Pr(>|t|)
                                           72.19
## (Intercept)
                       101.661
                                    1.408
                                                   <2e-16 ***
## health2. >=Very Good 14.065
                                    1.667
                                             8.44
                                                   <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 41.25 on 2998 degrees of freedom
## Multiple R-squared: 0.02321, Adjusted R-squared: 0.02288
## F-statistic: 71.23 on 1 and 2998 DF, p-value: < 2.2e-16
##
##
## Call:
## lm(formula = fmla1, data = df)
##
## Residuals:
              1Q Median
                              3Q
## -87.872 -25.355 -5.763 15.919 217.255
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
##
                             0.8699 138.22 <2e-16 ***
## (Intercept)
                  120.2383
## health_ins2. No -27.9216
                             1.5734 -17.75
                                              <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 39.7 on 2998 degrees of freedom
## Multiple R-squared: 0.09505, Adjusted R-squared: 0.09475
## F-statistic: 314.9 on 1 and 2998 DF, p-value: < 2.2e-16
##
## Call:
## lm(formula = fmla, data = df)
##
## Residuals:
   Min 1Q Median
                            3Q
                                    Max
## -100.33 -18.70 -3.26
                          13.29 212.79
##
## Coefficients:
##
                               Estimate Std. Error t value Pr(>|t|)
```

```
## (Intercept)
                             -2.423e+03 6.165e+02 -3.931 8.67e-05 ***
## year
                              1.241e+00 3.074e-01
                                                   4.037 5.54e-05 ***
                              2.707e-01 6.223e-02 4.350 1.41e-05 ***
## age
## maritl2. Married
                             1.718e+01 1.720e+00 9.985 < 2e-16 ***
## maritl3. Widowed
                              2.052e+00 8.005e+00 0.256 0.79774
## maritl4. Divorced
                             3.967e+00 2.887e+00
                                                   1.374 0.16951
## maritl5. Separated
                             1.153e+01 4.844e+00
                                                   2.380 0.01736 *
## race2. Black
                             -5.096e+00 2.146e+00 -2.375 0.01760 *
## race3. Asian
                             -2.814e+00 2.603e+00 -1.081 0.27978
## race4. Other
                             -6.059e+00 5.666e+00 -1.069 0.28505
## education2. HS Grad
                             7.759e+00 2.369e+00
                                                   3.275 0.00107 **
## education3. Some College
                            1.834e+01 2.520e+00
                                                   7.278 4.32e-13 ***
                           3.124e+01 2.548e+00 12.259 < 2e-16 ***
## education4. College Grad
## education5. Advanced Degree 5.395e+01 2.811e+00 19.190 < 2e-16 ***
## jobclass2. Information
                           3.571e+00 1.324e+00
                                                   2.697 0.00704 **
## health2. >=Very Good
                             6.515e+00 1.421e+00
                                                   4.585 4.72e-06 ***
## health_ins2. No
                             -1.751e+01 1.403e+00 -12.479 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 34 on 2983 degrees of freedom
## Multiple R-squared: 0.3396, Adjusted R-squared: 0.3361
## F-statistic: 95.89 on 16 and 2983 DF, p-value: < 2.2e-16
```

Single vs Multivariate model parameters



